

Effects of acid dissociation and ionic solutions on the aggregation of 2-pyrone-4,6-dicarboxylic acid

Jianping Li^{*,1,2} and Reid C. Van Lehn^{*,1,2}

¹*Department of Chemical and Biological Engineering, University of Wisconsin-Madison, Madison, WI 53705, USA*

²*DOE Great Lakes Bioenergy Research Center, USA*

E-mail: jianping.li@anl.gov; vanlehn@wisc.edu

Abstract

The conversion of lignin can produce biomass-derived aromatic compounds such as 2-pyrone-4,6-dicarboxylic acid (PDC), which is a potential sustainable precursor of bioplastics. PDC is a pseudoaromatic dicarboxylic acid that can aggregate in aqueous solution. Aggregation depends upon PDC-PDC, PDC-water, and PDC-ion interactions that are representative of interactions in similar charged, aromatic compounds. These interactions both dictate PDC aggregation and the likelihood that PDC aggregates exhibit parallel stacking configurations that may promote PDC crystallization, which can be leveraged to separate PDC from solution. However, the interplay of interactions that drive aggregation and structure formation, and how these depend upon the charge of PDC and ionic species present in solution, remains unclear. In this work, we investigate PDC aggregation in diverse ionic solutions using all-atom molecular dynamics simulations and molecular clustering analysis. We consider ion-induced dipole interactions by using a modified Lennard-Jones non-bonded model for divalent ions in solutions. From molecular clustering analysis, we derive characteristic parameters to quantify aggregate sizes and parallel stacking configurations. We show

that acid dissociation facilitates PDC aggregation in ionic solutions via ion-mediated interactions, and different ionic solutions influence both the likelihood of aggregation and the formation of parallel aggregates. In particular, we find that parallel stacking is primarily found in solutions with monovalent ions, whereas divalent ions promote larger, but less structured, aggregates. These results provide molecular-scale insight into the effects of specific ions on the aggregation of like-charged PDC molecules to inform understanding of related separation processes.

1 Introduction

Lignocellulosic biomass is an abundant renewable feedstock which can potentially be used for the sustainable production of fuels and high-value chemicals, thereby reducing dependence upon petroleum and contributing to decarbonization.^{1,2} A pathway for biomass valorization is through the conversion of lignin, one of the three primary components of biomass, to diverse bioproducts with rich functional groups.³ One product that can be obtained from the microbial conversion of lignin is 2-pyrone-4,6-dicarboxylic acid (PDC), a pseudoaromatic dicarboxylic acid.⁴ PDC shows promise as a precursor for the production of bioplastics and epoxy adhesives.^{5,6} However, the production of PDC requires its separation from the aqueous fermentation broth utilized in microbial conversion processes. A common separation method for obtaining high-purity PDC is crystallization, which is mediated by added salt such as sodium chloride.⁷ The resulting crystal structure of $\text{Na}(\text{PDC})_2$ has PDC molecules oriented with their pyran rings packed against each other and sodium ions bridging between carboxylic acid groups. This structure suggests the importance of ion-mediated interactions in promoting PDC crystallization; such interactions will depend upon the identity of the salt added to induce crystallization. Given the complex composition of fermentation broth, including the presence of multiple different ionic species, further improving separation

*Correspondence should be addressed to Reid C. Van Lehn at vanlehn@wisc.edu or Jianping Li at jianping.li@anl.gov.

processes of PDC or related molecules via crystallization requires insight into the effect of solution pH and ion identity on intermolecular interactions with PDC.

In general, crystallization involves the (1) nucleation of a crystal after the aggregation of molecules into a stable cluster and (2) growth of the crystal through packing of molecules on its surface.⁸ The initial aggregation of molecules into clusters is thus a critical step in the crystallization process.^{9,10} More broadly, molecular aggregation is relevant to numerous industrial applications in pharmaceuticals, solar cells, sensing, detergents, coatings, and food.^{11–13} Aggregation is usually driven by non-covalent interactions that are sufficiently attractive to overcome the unfavorable entropy change associated with spontaneous aggregation.^{14–16} Non-covalent interactions can include electrostatic interactions, hydrogen bonding, dipole-dipole interactions, and van der Waals interactions. The solvent environment can also influence the magnitude of these interactions. For example, cosolvents can strengthen the hydrogen-bond network of water to modulate the function and stability of aggregated structures,¹⁷ solvent-mediated hydrophobic interactions can mediate the assembly of nonpolar aggregates,¹⁸ and pH and ionic strength can alter the formation and properties of molecular aggregates.^{19,20} Understanding the balance of the interactions that contribute to the thermodynamic stability of aggregated structures can provide insight into conditions that facilitate molecular aggregation as a precursor to crystallization.^{21,22}

Based on the PDC crystal structure,^{23,24} two less common interactions may influence PDC aggregation: stacking interactions and ion-mediated interactions. In molecules with planar, aromatic or pseudoaromatic rings, stacking interactions promote the formation of structures with rings attractively packed in close contact,²⁵ which we refer to as “parallel molecular stacking” due to the alignment of rings. Ion-mediated interactions can counterintuitively promote the aggregation of like-charged molecules, in contrast to conventional expectations from Debye-Hückel theory,²⁶ by increasing the charge density in the spatial region between charged molecules.^{27,28} For instance, Lavagna et al.²⁹ and Petretto et al.³⁰ found that ion-mediated interactions drive the aggregation of like-charge nanoparticles on lipid membranes

or in aqueous salt solution through ion bridges. Moreover, the identity and concentration of ions influence ion-mediated interactions' strength. In particular, metal cations lead to ion-mediated interactions by providing an interaction center with a large attractive interaction energy that can promote specific orientations of the interacting species.³¹ Lee et al. showed that a high concentration of metal ions promotes the formation of oligomers for amyloid β aggregates, and zinc ions can more effectively destabilize fibril structures for amyloid β aggregates than copper ions.³² Ions with smaller radii can also lead to higher aggregation numbers, as has been shown for charged polymers.³³ Thus, a competition between stacking interactions, ion-mediated interactions, and other non-covalent interactions can determine PDC aggregation and the resulting structure of PDC aggregates. The fundamental open question is as follows: How do the charge of PDC and the identity of other ions in solution influence this competition between molecular interactions?

A challenge in studying the PDC aggregation process is resolving molecular-scale details of aggregate structure. Although experiments have revealed the precipitation of PDC in solutions containing alkali metal ions,²⁴ limited work has studied the aggregation of PDC, or similar pseudoaromatic carboxylic acid molecules, to reveal the influence of ion identity on PDC aggregation. Doing so requires methods to accurately resolve the effect of varying ions on ion-mediated interactions and to quantitatively characterize differences in aggregate structures. As an alternative to experimental characterization of molecular aggregates, computational modeling can provide insight into aggregation mechanisms³⁴⁻³⁶ and reveal parameters influencing aggregate structures.^{37,38} One commonly used method to study molecular-scale aggregation in ionic solutions is classical molecular dynamics (MD) simulation.³⁹ For instance, MD simulations have been used to investigate how ion-mediated interactions influence protein stabilization on nanoparticle surfaces.⁴⁰ Dai et al. used MD simulations to investigate ion-mediated attractive interactions between DNA molecules and rationalized this attractive force through the formation of ion bridges.⁴¹ Lewis et al. leveraged MD simulations to investigate the role of ionic interactions in aqueous lithium

bistriflimide solutions as a function of concentration and found that highly interconnected ion-rich network forms in the super-concentrated regime.⁴² Petretto et al. found that the aggregation of weakly charged hydrophilic polyelectrolytes with biguanide groups in water or in monovalent ionic solutions is driven by the like-charged pairing of the biguanide units and is favored by increasing salt concentration.⁴³ These studies indicate that MD simulations are suitable for analyzing the factors contributing to PDC aggregation as a precursor to crystallization.

In this work, we perform all-atom MD simulations to study factors that influence PDC aggregation. In particular, we seek to understand how the pH and specific ionic species present in solution influence the competition of stacking interactions, ion-mediated interactions, and non-covalent interactions between PDC and water to dictate the structure of the resulting aggregates. Specifically, we focus on determining conditions that lead to aggregates with parallel molecular stacking, which are consistent with the PDC crystal structure. To do so, we systematically model PDC molecules with different degrees of acid dissociation (to investigate the role of pH) and in the presence of various metal ions. We develop a method to identify PDC aggregates and compute two order parameters that characterize aggregates in terms of concentration and degree to which PDC molecules pack pyran rings against each other. Our results show that the dissociation of PDC molecules and addition of Na^+ , K^+ , Rb^+ , Cs^+ , Be^{2+} , Mg^{2+} , and Ca^{2+} ions facilitate PDC aggregation. These results provide insight into how adjustment to solution pH and selection of appropriate ionic species can promote PDC aggregation into highly ordered structures with parallel molecular stacking.

2 Methods

2.1 Molecular Dynamics Simulations

Classical molecular dynamics (MD) simulations were performed to analyze PDC aggregation in water or in various ionic solutions. All MD simulations were performed in the isothermal-isobaric (*NPT*) ensemble using Gromacs 2018.⁴⁴ Figure 1 shows the PDC chemical structure and an example snapshot of a simulation system. As shown in Figure 1a, PDC is a planar, pseudoaromatic compound with two carboxylic acid groups of varying pKa:⁴⁵ (1) the carboxylic acid group in the green box dissociates first when the pH is lowered (pKa = 1.13), and (2) the carboxylic acid group in the red box dissociates second when the pH is further lowered (pKa = 2.52). Each simulation system contained 100 PDC molecules (of varying net charge; *vide infra*) and 6191 water molecules. Either 50, 100, or 200 metal ions were added to neutralize the system depending upon the charge of the PDC molecules and added metal ions. As shown in Figure 1, a number of monovalent and divalent metal ions were considered. For comparison, we also considered a system consisting of 100 neutral PDC molecules and 6246 water molecules without additional ions. All systems were initiated in a cubic simulation box with dimensions of 6 nm in all directions. The resulting PDC concentration was approximately 0.77 mol/L, which is considered to be low concentration.^{7,46,47}

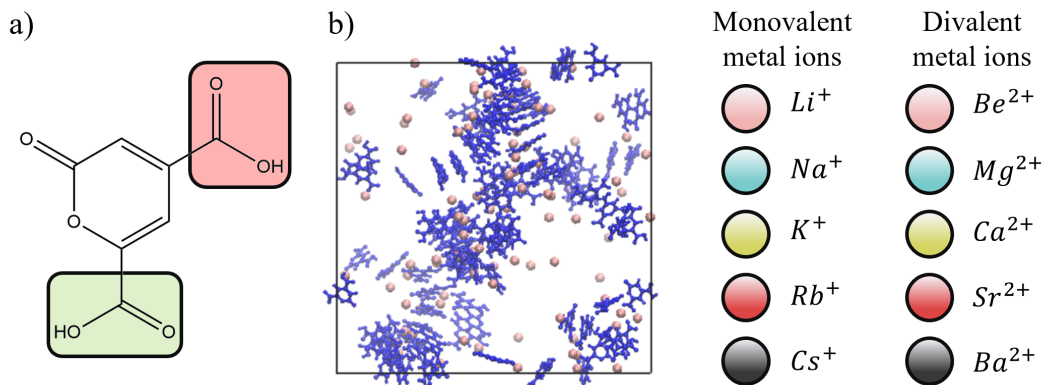


Figure 1: Simulation systems used to investigate PDC aggregation in various ionic solutions. a) PDC chemical structure with two carboxylic acid groups indicated. The group in green dissociates first and the group in red dissociates second when the pH is lowered to acidic conditions. b) Snapshot of 100 PDC⁺ ions in a solution with Li⁺ counterions. PDC⁺ ions are in blue, metal ions are in pink and water is not shown for visual clarity. The images at right illustrate the range of monovalent and divalent metal ions studied in this work.

PDC molecules were parameterized using the Generalized AMBER force field.⁴⁸ Water molecules were modeled using the SPC/E model. To more accurately capture interactions with divalent metal cations, referred to as M(II) ions, the functional form of the standard Lennard-Jones (LJ) potential was modified following the approach by Li and coworkers:⁴⁹

$$U_{i,i'} = \epsilon_{i,i'} \left[\left(\frac{R_{i,i'}^{min}}{r_{i,i'}} \right)^{12} - 2 \left(\frac{R_{i,i'}^{min}}{r_{i,i'}} \right)^6 - 2\kappa (R_{i,i'}^{min})^2 \left(\frac{R_{i,i'}^{min}}{r_{i,i'}} \right)^4 \right] \quad (1)$$

Here, $R_{i,i'}^{min}$ is the distance between two atoms corresponding to the minimum value of the LJ potential and $\epsilon_{i,i'}$ is the depth of the LJ minimum. $2\kappa(R_{i,i'}^{min})^2 \left(\frac{R_{i,i'}^{min}}{r_{i,i'}} \right)^4$ is an additional term that represents ion-induced dipole interactions when M(II) ions are present in the system, with $\kappa = 0$ if only monovalent M(I) ions are present in the system. If M(II) ions are present in the system, we took the value of $\epsilon_{i,i'}$, $R_{i,i'}^{min}$, and κ from Ref.⁴⁹ Equation (1) was implemented using tabulated potentials in Gromacs 2018. In constructing the parameter matrix for the nonbonded LJ parameters, we used Lorentz-Berthelot combining rules.⁴⁸

Each simulation system was equilibrated for 2 ns at 293.15 K (based on experimental conditions²⁴) and 1 bar using the velocity-rescale thermostat and Berendsen barostat. A

100-ns simulation was then performed at the same temperature and pressure using the Nose-Hoover thermostat and Parrinello-Rahman barostat. Simulations were performed using the leap-frog algorithm with a 2-fs time step for most simulations and a 1-fs time step for simulations that exhibited numerical instabilities. Van der Waals interactions were modeled with a shifted LJ potential and Verlet cutoff scheme that was smoothly shifted to zero at 1.2 nm. Electrostatic interactions were calculated using the smooth particle mesh Ewald method with a short-range cutoff of 1.2 nm, a grid spacing of 0.14 nm, and fourth-order interpolation. Bonds were constrained using the LINCS algorithm. All thermostats used a 2.0 ps time constant, and all barostats used a 2.0 ps time constant with $4.5 \times 10^{-5} \text{ bar}^{-1}$ as the isothermal compressibility.

2.2 Identification of PDC Aggregates and Parallel Clusters

We developed and implemented a clustering method to identify PDC molecular aggregates and the degree to which PDC molecules stack in parallel configurations within these aggregates. We calculated two quantities to determine PDC aggregates: (1) the minimum pairwise molecular distance between molecules, $D_{j,j'}$, and (2) the dihedral angle between pairs of molecules, $A_{j,j'}$. We use $j \in \mathbf{J}$ to denote a PDC molecule (neutral or charged) and $t \in \mathbf{T}$ to denote an atom in molecule j . $D_{j,j'}$ is determined as follows:

$$D_{j,j'} = \min_{t,t'} \sqrt{X_{j,j',t,t'}^2 + Y_{j,j',t,t'}^2 + Z_{j,j',t,t'}^2} \quad (2)$$

Here, $X_{j,j',t,t'}$, $Y_{j,j',t,t'}$, and $Z_{j,j',t,t'}$ are pairwise distances between atom t (in molecule j) and t' (in molecule j') projected onto the x-axis, y-axis, and z-axis, respectively.

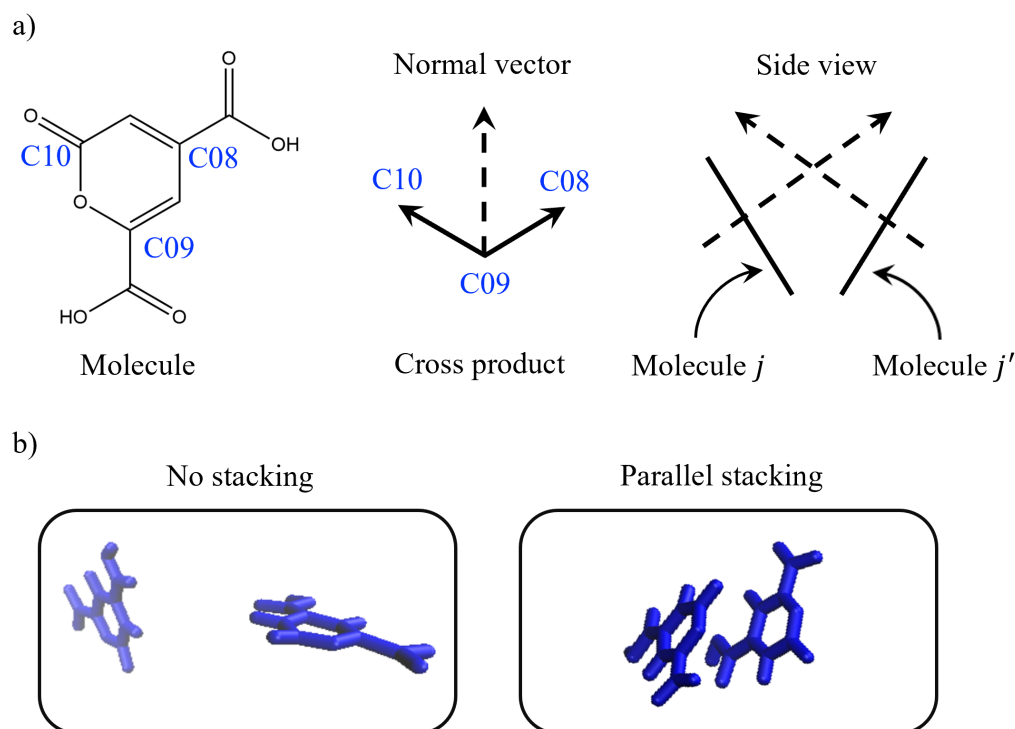


Figure 2: Geometries and stacking structures between two PDC molecules. a) Geometries and computation of dihedral angle between two PDC molecules. The molecular plane is determined using carbon atoms C08, C09, C10, and the cross-product of vectors between C09-C08 and C09-C10 define the normal vector to the the molecular plane. The dot product of a pair of normal vectors for different PDC molecules determines the dihedral angle between them. b) Snapshot of stacking structures of two PDC⁺ ions in a solution with Li⁺ counterions. PDC⁺ ions are in blue while other components are not shown. PDC⁺ ions that satisfy Equation 4 but do not exhibit parallel stacking are shown at left, whereas PDC⁺ ions that satisfy both Equation 4 and 5 and exhibit parallel stacking are shown at right.

$A_{j,j'}$ is determined as follows:

$$\cos A_{j,j'} = \frac{|\mathbf{n}_j \cdot \mathbf{n}_{j'}|}{|\mathbf{n}_j| |\mathbf{n}_{j'}|} \quad (3)$$

The vector \mathbf{n}_j is the normal vector to the plane of molecule j . The molecular plane is defined by two vectors, which are computed based on the positions of carbon atoms C08, C09, C10; see Figure 2. The cross-product of these two vectors determines the normal vector \mathbf{n}_j (shown in Figure 2). $D_{j,j'}$ and $A_{j,j'}$ were computed using MDTraj.⁵⁰

We identified aggregates by using a clustering algorithm detailed in Section S2 of the Supporting Information. Briefly, the method involves determining $D_{j,j'}$ and $A_{j,j'}$ for each pair of PDC molecules in each simulation configuration. PDC molecules were assigned to aggregates based on the following two equations:

$$D_{j,j'} \leq D_0 \quad (4)$$

$$A_{j,j'} \leq A_0 \quad (5)$$

Pairs of PDC molecules that satisfy Equation 4 were assigned to the same aggregate. Pairs of PDC molecules within the same aggregate that further satisfy Equation 5 were considered to be in a parallel stacking configuration and were defined as being within the same parallel cluster; each aggregate could contain multiple parallel clusters. The cutoff value A_0 was set to 20° . The cutoff value D_0 was set to 0.31 nm based on sensitivity analysis of several potential cutoff values (Figure S1 of Supporting Information). Because the clustering algorithm was performed separately for different simulation configurations, the number and distribution of both aggregates and parallel clusters fluctuate throughout the simulation trajectory.

2.3 Aggregate Order Parameters

We defined two order parameters to compare the tendency of PDC to assemble into aggregates that exhibit parallel molecular stacking. The first order parameter, R_c , quantifies the degree of parallel molecular stacking for parallel clusters. To compute R_c , we first implemented the clustering method (Algorithm 1 of Supporting Information) described in the prior section by applying Equation 4 and not Equation 5 to determine a set of aggregates (i.e., PDC molecules were assigned to aggregates without considering parallel molecular stacking). For each aggregate p in this set, we define the aggregation number L_p as the total number of molecules within the aggregate. The number of PDC molecules

in parallel stacking configurations was counted by further applying Equation 5 to pairs of PDC molecules, thereby generating a set of parallel clusters. We note that multiple distinct parallel clusters are possible per aggregate. We define N_c as the number of PDC molecules within parallel cluster c that are contained in aggregate p ; hence, $c \in p$. Finally, we define R_c as:

$$R_c = \frac{N_c}{L_p} \quad (6)$$

Thus, R_c is the ratio of the number of PDC molecules in parallel cluster c to the total number of PDC molecules within aggregate p that contains parallel cluster c . R_c is a continuous parameter with a value between 0 and 1: $R_c = 0$ indicates that no molecules in aggregate p are in parallel stacking configurations whereas $R_c = 1$ indicates that all molecules in aggregate p are in parallel stacking configurations.

The second order parameter, M_c , quantifies the total number of PDC molecules in parallel clusters. For the set of parallel clusters defined by applying Equations 4 and 5 to all pairs of PDC molecules, N_c was defined as the number of PDC molecules within parallel cluster c and $F(N_c)$ was defined as the number of parallel clusters with a given value of N_c . Since each aggregate defined using Equation 4, can contain zero, one, or multiple parallel clusters, $F(N_c)$ is not necessarily equal to the number of aggregates in the system. We then define M_c as follows:

$$M_c = N_c \times F(N_c) \quad (7)$$

Hence, M_c counts the total number of PDC molecules in parallel clusters containing N_c molecules. Note that $M_c = M_{c'}$ for two different parallel clusters c and c' if $N_c = N_{c'}$. Larger values of M_c indicate an overall increased propensity for PDC molecules to exhibit parallel molecular stacking regardless of whether the PDC molecules are in a large number of small parallel clusters (i.e., small N_c , large $F(N_c)$) or a small number of large parallel clusters (i.e., large N_c , small $F(N_c)$), whereas reporting the distribution of N_c alone may lead to peaks at small values of N_c without revealing the overall extent of parallel stacking with the system.

An illustrative example of determining R_c and M_c for the PDC-water- Li^+ system is given in Section S4 of Supporting Information.

2.4 Spatial Distribution Function

The spatial distribution function (SDF) describes the probability of finding a molecule at a certain position in the 3D space around a given reference molecule. Each SDF is stored in a gaussian cube file, which consists of a reference molecule structure (a .xyz coordinate file) and an isosurface depicting the probability of the observed atom or molecule. We used the Gromacs tool *gmx spatial* to determine SDFs and generate gaussian cube files, then Visual Molecular Dynamics (VMD) was used for visualisation.⁵¹ We selected the reference PDC molecule as the molecule that was found in a parallel cluster with the highest frequency across all simulation configurations. Reference molecules for all simulation systems are shown in Section S6 of the Supporting Information. When visualising SDFs, a different isovalue was selected for each molecule (80 for PDC, 8 for water, and 100 for ions), which is based on the amount of information expected to be shown.

3 Results and Discussion

This section presents results and analysis of PDC aggregation in water and various ionic solutions. Additional data quantifying aggregation from the simulation trajectories for each system are provided in the Section S5 of the Supporting Information. We discuss the effects of acid dissociation, monovalent metal ions, and divalent metal ions on PDC aggregation.

3.1 Neutral PDC-Water System

We first simulated a neutral PDC-water system. Although this system would correspond physically to a low pH in which both carboxylic acid groups are protonated, the primary goal of these simulations is to serve as a comparison to other PDC-water-ion systems in subsequent

sections. PDC molecules rapidly aggregate within 20 ns (Figure S3) to form aggregates that remain stable for the duration of the simulation. Figure 3a shows a snapshot of the final simulation configuration after 100 ns in which a single large aggregate structure (spanning the periodic boundaries) is present along with several smaller isolated PDC molecules; parallel stacking between aggregated PDC molecules is not clearly observed in the snapshot. Figure 3b shows the SDF to more clearly quantify preferred configurations of molecular aggregates. The regions of highest PDC density (indicated by the blue surface in Figure 3b) encircle the PDC molecule, indicating that surrounding PDC molecules can interact with the reference PDC molecule at positions on or below the surface of the pyran ring. This suggests that stacking interactions are not the dominant interaction driving the aggregation of neutral PDC molecules since parallel molecular stacking is not the only configuration observed. Moreover, water molecules preferentially occupy spatial regions (indicated by the green surfaces) near the (protonated) carboxylic acid groups, indicating the formation of strong PDC-water hydrogen bonds.

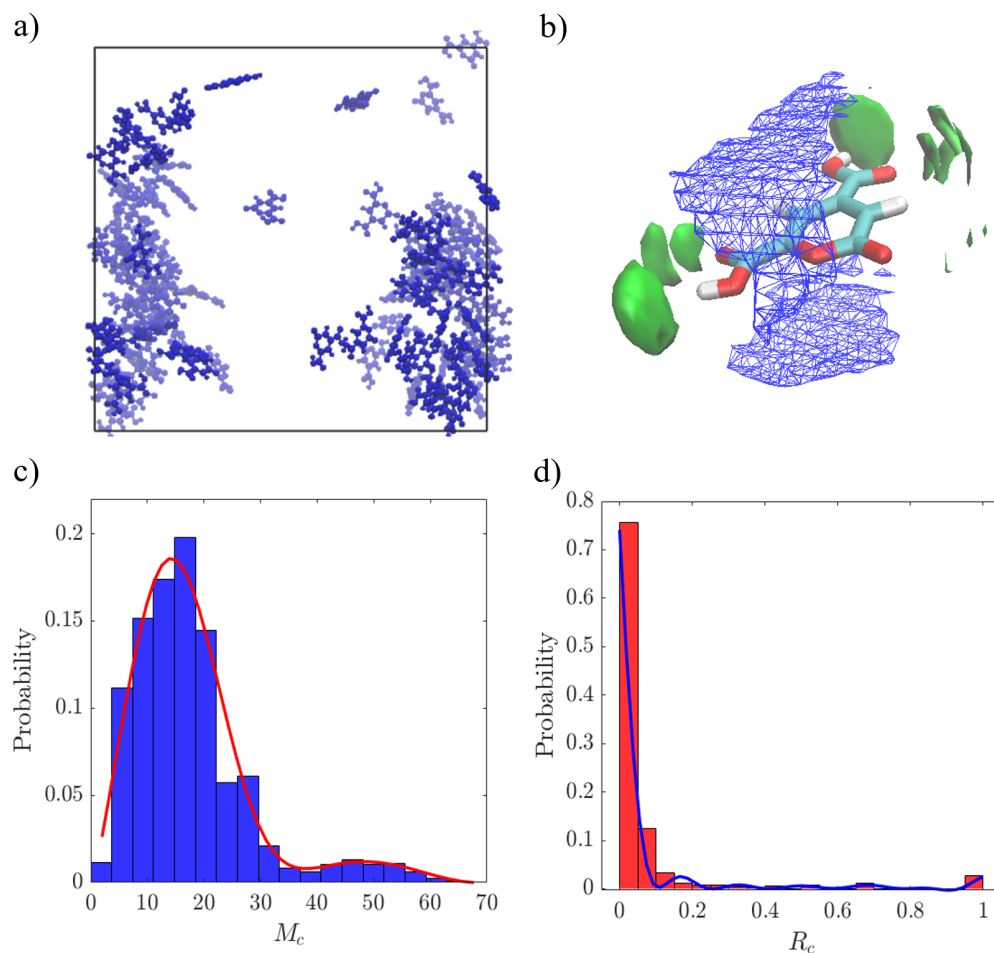


Figure 3: Aggregation of neutral PDC molecules in water. a) Snapshot of the PDC-water system after 100 ns. PDC molecules are drawn in blue and water molecules are not shown. The lines indicate periodic boundaries. b) Spatial distribution function (SDF) centered on a reference PDC molecule. For the reference model, carbon, oxygen, and hydrogen atoms are in cyan, red, and white, respectively. The isosurface in blue indicates PDC molecular density and the isosurface in green indicates water molecular density. c) Concentration indicator of aggregated PDC (M_c). d) Degree of parallel stacking for PDC (R_c). Red and blue curves in Figure 3c and 3d are gaussian process regression fits of the probability distribution.

Figure 3c and 3d show probability distributions for M_c and R_c computed from the simulation trajectory to quantify the propensity for PDC aggregation into parallel stacking configurations. To better visualize trends, we fit the probability distributions using Gaussian process regression implemented with the MATLAB function `fitrgp` (fits are shown as red and blue curves in Figure 3c and 3d). As shown in Figure 3c, the probability distribution for M_c is peaked near 17 with a small value near 0 and a long tail for larger values of M_c . Figure 3d

further shows that the probability distribution for R_c is strongly peaked near zero, indicating that PDC aggregates in pure water lack a high degree of parallel molecular stacking, which is consistent with the simulation snapshot in Figure 3a and the SDF in Figure 3b. Since larger values of M_c indicate either a large number of small clusters with parallel stacking or a small number of large clusters with parallel stacking, with Figure 3c and 3d, the distribution of M_c suggests a strong propensity for neutral PDC molecules to aggregate in pure water without a high degree of parallel stacking despite the strong PDC-water hydrogen bonding. Together, these data indicate that the interactions of neutral PDC molecules in water are sufficiently favorable that aggregation ($M_c > 1$) is preferred, which we can attribute to the generally hydrophobic nature of PDC in its neutral form. However, aggregation is not driven by PDC-PDC stacking interactions and PDC molecules maintain strong hydrogen bonds with water. These factors lead to disordered, randomly packed structures that are unlikely to be precursors to PDC crystals due to the lack of parallel molecular stacking.

3.2 Effect of Acid Dissociation on PDC Aggregation in Li^+ Solution

The formation of randomly packed structures by neutral PDC molecules suggests a role for ion-mediated interactions in promoting parallel stacking. To investigate the effect of such interactions, we next investigated how the addition of Li^+ ions to solution would influence the aggregation of PDC ions. Li^+ is a common metal ion with a small radius compared with other metal ions. We performed simulations for both PDC^- and PDC^{2-} , reflecting both possible protonation states of the carboxylic acids and hence effects of pH on the competition between stacking interactions, Li^+ -mediated PDC interactions, and hydrogen bonding interactions between PDC and water. Simulation snapshots of these systems are presented in the Section S6 of Supporting Information.

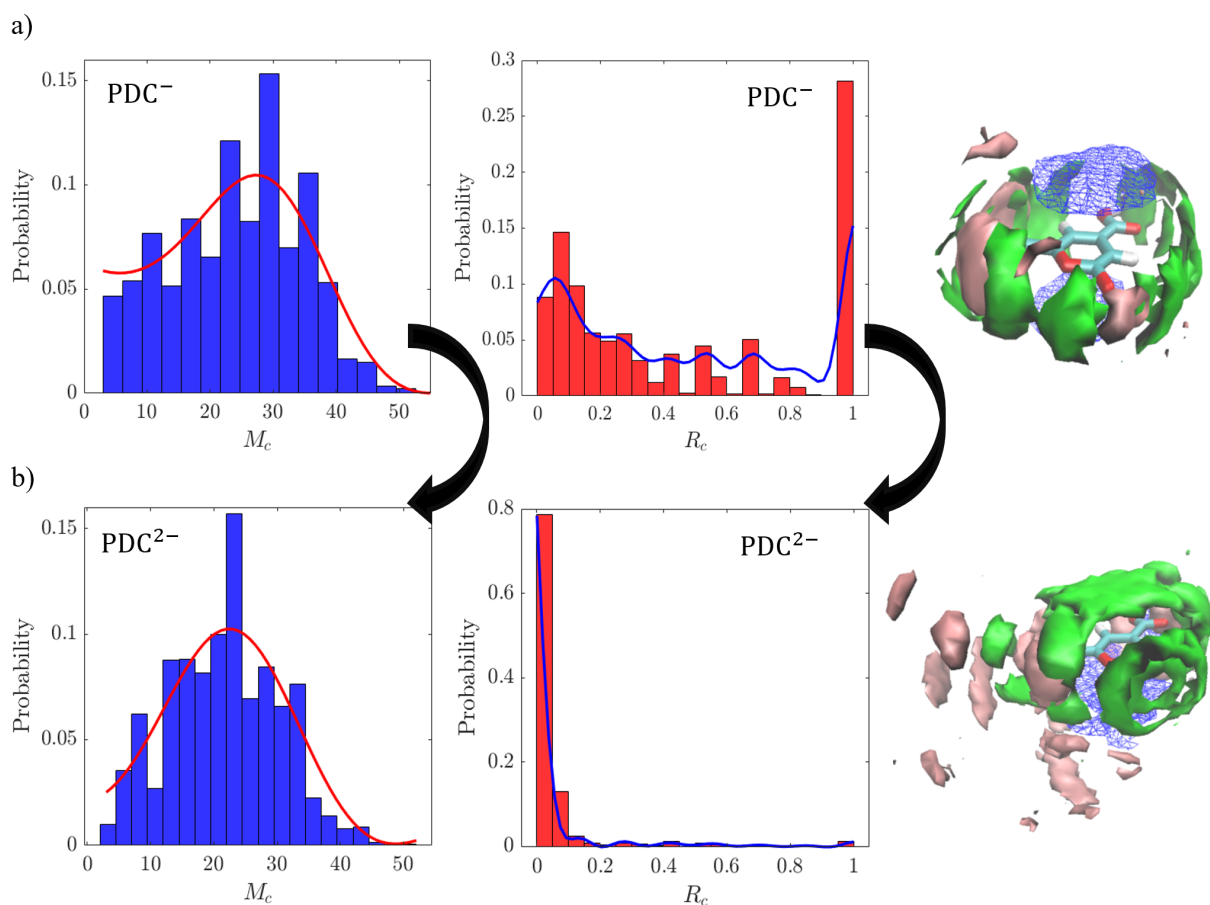


Figure 4: Effect of acid dissociation on PDC aggregation in Li^+ solution. a) At the first degree of acid dissociation, b) at the second degree of acid dissociation. Left: concentration indicator of aggregated PDC molecules (M_c). Middle: degree of parallel stacking for PDC (R_c). Right: SDFs (The isosurfaces in blue, green, and pink indicate PDC molecular density, water molecular density, and Li^+ density, respectively). For the reference model, carbon atoms are in cyan, oxygen atoms in red, and hydrogen atoms in white. Red and blue curves in Figure 4a and 4b are gaussian process regression fits of probability distribution.

For PDC^- in the presence of Li^+ ions, the probability distribution for M_c is peaked near 30 (Figure 4a). Compared to the prior system of neutral PDC molecules, the shift of M_c to larger values indicates a stronger tendency of PDC^- to aggregate into structures that exhibit parallel molecular stacking (specifically, a small number of large parallel clusters). Similarly, the distribution of R_c also indicates a high probability of $R_c = 1$, which indicates that parallel stacking is favorable. Given that charged PDC ions might be expected to repel each other and be more strongly solvated by water, this result instead suggests that

Li^+ ions promote favorable PDC-PDC interactions. The SDF in Figure 4a indicates that there is significant Li^+ density located near the carboxylic acid group, indicating that Li^+ ions outcompete water molecules when comparing to Figure 3b. The PDC density located immediately above and below the pyran ring is due to the stacking interactions, and water molecules instead occupy only a region around the periphery of the ring. Together, these results indicate that the Li^+ ions are able to promote favorable PDC-PDC interactions by occupying regions in between negatively charged carboxylic acid groups while permitting pyran rings to pack against each other in parallel stacking configurations.

For PDC^{2-} in the presence of Li^+ ions, the probability distribution for M_c is peaked near 24 (Figure 4b), representing a reduced peak compared to PDC^- , and the distribution of R_c also indicates a high probability of $R_c = 0$. Together, these quantities indicate that the second degree of acid dissociation and the corresponding increase in PDC charge disrupts the parallel stacking of PDC ions. Comparison of the SDFs in Figure 4a and 4b indicates that the increase of PDC's charge through acid dissociation attracts more water around the reference molecule. These water molecules occupy the space that initially accommodated Li^+ and PDC ions (Figure 4a Right), which disrupts the parallel stacking of PDC ions. We attribute this to the strong solvation of the charged ions (PDC and Li) by water outcompeting the stacking interactions between pyran rings. Compared to the case of neutral PDC, the analysis of PDC^- and PDC^{2-} indicates that parallel stacking is only observed for PDC^- due to the combination of Li^+ -mediated attraction and stacking interactions; for neutral PDC, the absence of ion-mediated interactions disrupt parallel stacking, whereas for PDC^{2-} , the strong solvation of ions disrupts parallel stacking.

3.3 Effect of Monovalent Metal Ions on PDC Aggregation

To extend the analysis of PDC aggregation in Li^+ solutions, we further compare and analyze the effects of different monovalent metal ions on aggregation behavior for PDC^- and PDC^{2-} . Figure 5 summarizes aggregation trends in all studied monovalent metal ionic solutions.

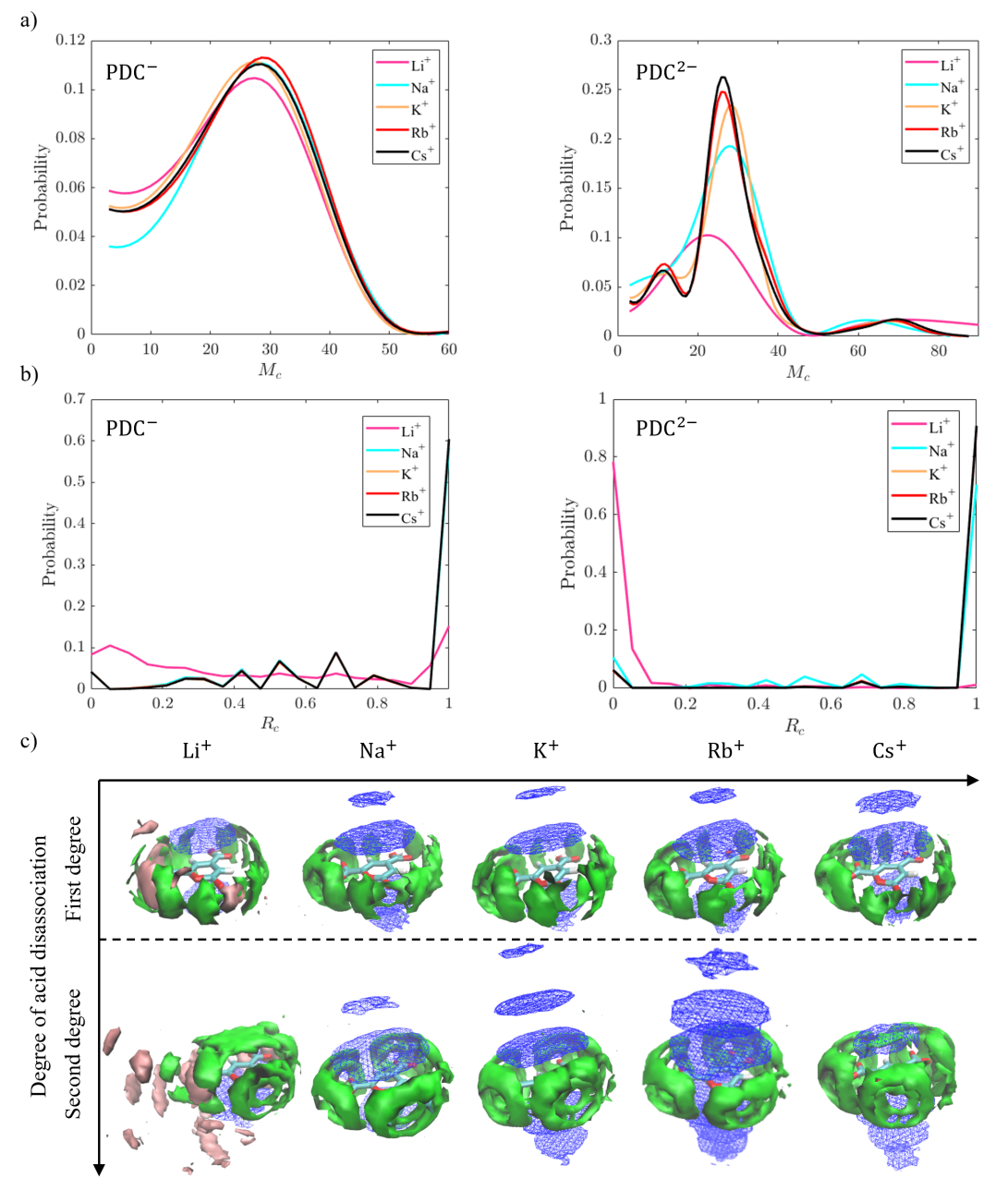


Figure 5: Effect of monovalent metal ions on PDC aggregation. a) Concentration indicator of aggregated PDC (M_c), and b) degree of parallel stacking (R_c), and c) Spatial distribution functions (SDFs) for PDC-water-ion systems. The isosurfaces in blue, green, and pink indicate the PDC molecular density, water molecular density, and Li^+ density, respectively. The isosurfaces for other ionic densities are negligible when using the isovalue of 100. In Figure 5a and 5b, left and right figures are for PDC^- and PDC^{2-} , respectively. Solid curves or lines in Figure 5a and 5b are gaussian process regression fits of probability distribution.

For PDC^- , all solutions promote the formation of PDC aggregates and the probability

distribution of M_c is peaked near 30 (Figure 5a, left). Moreover, all solutions strongly favor the parallel stacking of aggregated PDC ions (Figure 5b, left) as shown by the peaks in R_c near 1. The outlier is Li^+ ; compared with the other ions, Li^+ leads to more PDC aggregates with a high concentration and a low degree of parallel stacking. Since Na^+ is typically used to crystallize PDC,⁷ the preference for monovalent ions to promote parallel stacking as a presumed precursor to crystallization is consistent with experimental observations.

For PDC^{2-} , the Li^+ solution leads to different PDC stacking behavior compared with other M(I) ionic solutions by not facilitating PDC aggregation (Figure 5a Right) or promoting a high degree of parallel stacking (Figure 5b Right). Hence, at the second degree of acid dissociation, the Li^+ solution leads to PDC aggregates with disordered and randomly packed structures, which are unlikely to be the precursors to PDC crystals. All other solutions facilitate the formation of PDC aggregates that exhibit more parallel stacked structures (with R_c near 1) and the probability distribution of M_c value is more sharply near 30 compared to PDC^- and has a longer tail to the distribution with M_c as high as 80 (Figure 5a Right). The Na^+ , K^+ , Rb^+ , and Cs^+ ions show the strongest effects in facilitating PDC aggregation (the peaked probability value of M_c probability distribution in Figure 5a Left is near 0.1 – 0.11 while the peaked probability value of M_c probability distribution in Figure 5a Right is higher than 0.18). Furthermore, all other solutions (except Li^+ solution) facilitate the parallel stacking of PDC ions (Figure 5b Right).

Figure 5c compares the M(I) ions' influence on the SDFs of PDC-water-ion systems for PDC^- and PDC^{2-} . For all solutions (except Li^+ solutions), the counterintuitive observation is that more PDC ions aggregate around the reference molecule at the second degree of acid even though the increased charge on PDC ions should increase like-charge repulsion. The resulting SDFs have clear layers of PDC density consistent with parallel stacking. This result is consistent with the observation that the second degree of acid dissociation facilitates the PDC^{2-} aggregation as shown in Figure 5a Right (the peaked probability value of M_c probability distribution for PDC^{2-} is higher than for PDC^-). Furthermore,

Figure 5c elucidates the competition among various intermolecular interactions. For all solutions (except Li^+ solutions), near the edge of PDC's pyran ring, the hydrogen bonding interactions between PDC ions and water are stronger than ion-mediated interactions and stacking interactions between pairs of PDC ions, leading to enriched water density. Above and below PDC's pyran ring, the stacking interactions between pairs of PDC ions are stronger than the ion-mediated interactions and hydrogen bonding interactions between PDC ions and water. This analysis indicates that increasing pH in the solutions of monovalent metal ions (except the Li^+ solution) to facilitate dissociation can lead to PDC aggregates with large aggregation numbers and parallel stacking, which can serve as precursors of PDC crystals.

3.4 Effect of Divalent Metal Ions on PDC Aggregation

As discussed in the previous section, we observe diverse PDC aggregation patterns within the solutions of monovalent metal ions, with an increase in aggregation and parallel stacking observed for the higher charge density PDC^{2-} ions. These observations further motivate the investigation of how divalent metal ions affect PDC aggregation, as shown in Figure 6.

For PDC^- , solutions of Be^{2+} , Ca^{2+} , Sr^{2+} , and Ba^{2+} facilitate the formation of aggregated PDC ions with the probability distribution of M_c peaked near 25 – 30 (Figure 6a Left), which is similar to observations for monovalent ions. Be^{2+} and Ca^{2+} solutions facilitate parallel stacking of PDC ions while the rest of the solutions do not (Figure 6b Left). For PDC^{2-} , all solutions facilitate PDC aggregation with the M_c probability distribution peaked near 30 – 35 (Figure 6a Right). Notably, the Ba^{2+} solution leads to aggregated PDC with the probability distribution M_c peaked near 35 and with a higher peaked probability value than any other metal ion. Moreover, the Mg^{2+} solution leads to a high degree of parallel stacking of PDC ions (the probability distribution of R_c is peaked near one in Figure 6b Right). This indicates that the Mg^{2+} solution leads to aggregated PDC ions with a higher degree of parallel stacking compared with the rest of ionic solutions. These two results indicate that divalent ionic solutions containing Mg^{2+} could be ideal for crystallizing PDC at a pH

that promotes dissociation of both carboxylic acid groups, but other divalent metal ions may preferentially form large, disordered aggregates that are less likely to lead to crystallization.

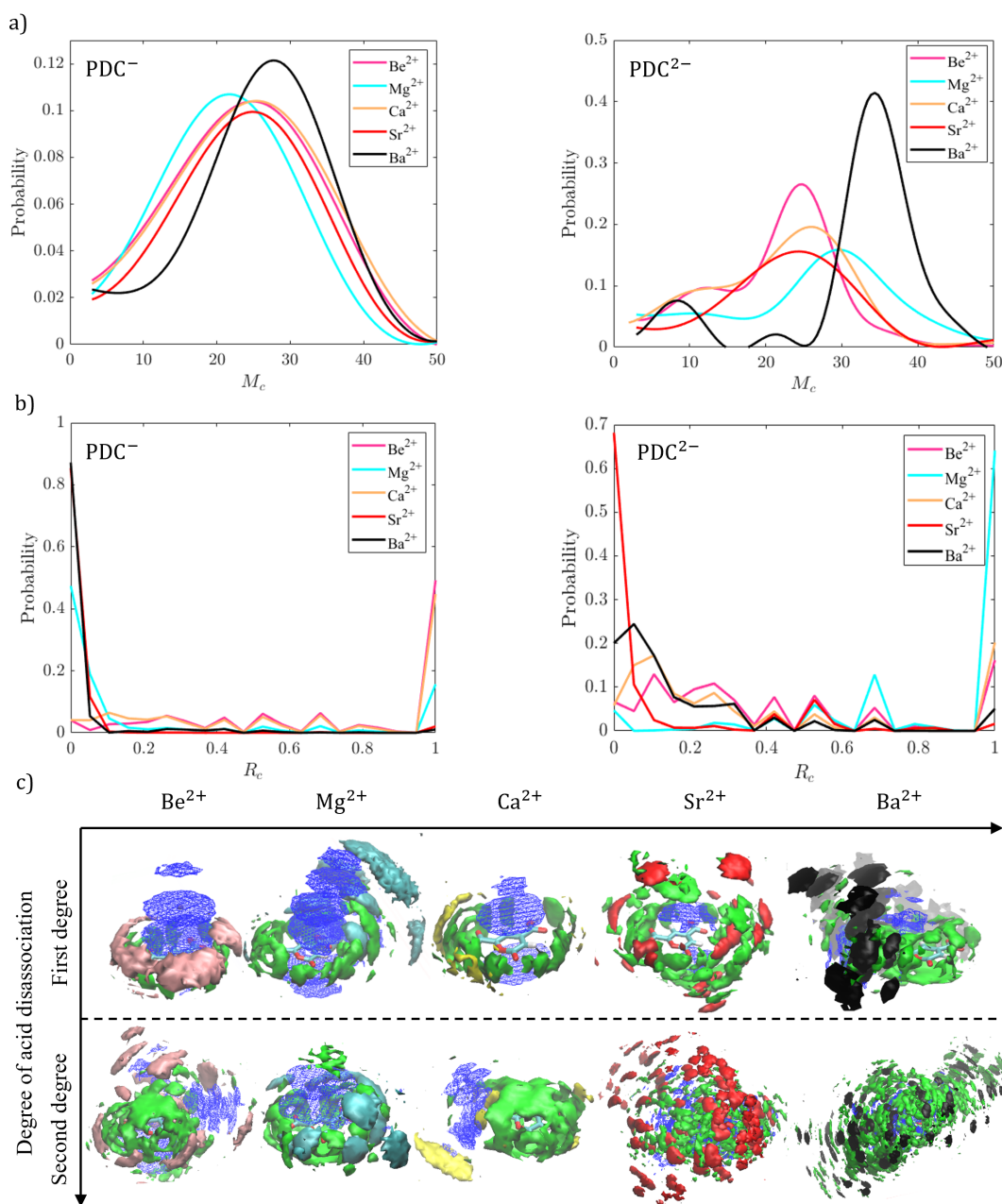


Figure 6: Effect of divalent metal ions on the PDC aggregation. a) Order parameters to quantify PDC aggregation (M_c), and b) degree of parallel stacking (R_c), and c) Spatial distribution functions (SDFs) for PDC-water-ion systems. The isosurfaces in blue and green indicate the PDC molecular density and water molecular density, respectively. In Figure 6a and 6b, left figures are for PDC^- and right figures are for PDC^{2-} . Solid curves or lines in Figure 6a and 6b are gaussian process regression fits of probability distribution.

The SDFs in Figure 6c further indicate behaviors related to the probability distribution of M_c and R_c . For PDC^- , the Be^{2+} , Mg^{2+} , and Ca^{2+} solutions lead to more aggregated PDC ions and metal ions than aggregated water molecules around the reference molecule, with the plots again similar to monovalent ions. For PDC^{2-} , all solutions of divalent metal ions (except Mg^{2+}), lead to more aggregated water molecules than aggregated PDC ions and metal ions around the reference PDC ion. This result suggests that the strong electrostatic interactions between the PDC^{2-} and metal ions and hydration of metal ions by water disrupts parallel stacking. This also indicates that for these solutions of metal ions, the hydrogen bonding interactions between PDC ions and water are stronger than the stacking interactions between pairs of PDC ions and ion-mediated interactions between PDC ions and metal ions.

For Sr^{2+} and Ba^{2+} solutions, water molecules and metal ions disrupt the parallel stacking of PDC ions around the reference PDC ion. This indicates that for Sr^{2+} and Ba^{2+} solutions at all degrees of acid dissociation, the hydrogen bonding interactions between PDC ions and water, and ion-mediated interactions between PDC ions and metal ions are stronger than the stacking interactions between pairs of PDC ions. However, for the ionic solution of Mg^{2+} , around the reference molecule, there are more aggregated Mg^{2+} ions at the second degree of acid dissociation than aggregated Mg^{2+} ions at the first degree of acid dissociation. This disrupts the aggregation of water molecules and hence allows more space for PDC aggregation around the reference PDC ion. This also indicates that for the ionic solution of Mg^{2+} , at the second degree of acid dissociation, stacking interactions between pairs of PDC ions and ion-mediated interactions between PDC ions and Mg^{2+} are stronger than the hydrogen bonding interactions between PDC ions and water.

Compared to solutions with monovalent metal ions (Figure 5), the peaked value for the probability distribution of R_c for PDC ions in solutions with divalent metal ions tends to be lower for both PDC^- and PDC^{2-} . This result is due to enhanced hydrogen bonding interactions between PDC ions and water, and ion-mediated interactions between PDC ions and divalent metal ions, compared with the stacking interactions between pairs of

PDC ions. This attracts more water or metal ions around the reference PDC ion, which disrupts the parallel stacking of PDC ions. In summary, we show solutions with Be^{2+} and Ca^{2+} facilitate PDC^- aggregation with large aggregation numbers but without parallel stacking while Mg^{2+} facilitates PDC^{2-} aggregation with large aggregation numbers and parallel stacking structures.

4 Conclusions

Understanding molecular aggregation is critical for designing crystallization processes for PDC separation. In this work, we investigate PDC aggregation in solutions containing monovalent or divalent metal ions to determine ions that promote the aggregation of PDC into structures with parallel stacking, which is expected to lead to favorable crystallization. First, we perform atomistic molecular dynamics simulations of PDC at different degrees of acid dissociation and in various metal ion solutions. We then implement molecular clustering analysis based on the minimum distance and the dihedral angle between pairs of PDC molecules. From molecular clustering analysis, we compute order parameters for PDC aggregation to indicate the concentration of PDC aggregates and their preference for parallel stacking structures. The results show that the dissociation of PDC can contribute to PDC aggregation in the solutions of metal ion despite apparent like-charge repulsion. For both PDC^- and PDC^{2-} , solutions of Na^+ , K^+ , Rb^+ , and Cs^+ facilitate the formation of PDC aggregates with large aggregation numbers and parallel stacking structures, which is consistent with the experimental utilization of Na^+ to promote PDC crystallization. For divalent metal ions, Be^{2+} and Ca^{2+} solutions facilitate the aggregation the formation of PDC^- aggregates with large aggregation numbers and parallel stacking, while only Mg^{2+} solutions facilitate the formation of PDC^{2-} with large aggregation numbers and parallel stacking. These results indicate that the choice of ion in solution can impact the relative interplay of PDC-PDC stacking interactions, PDC-water hydrogen bonding interactions, and

electrostatic interactions that influences aggregate structures. The results also indicate that future separation processes should consider the addition of divalent cations, and particularly Mg^{2+} , to further promote PDC crystallization.

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Supporting Information Available

Supporting information includes nomenclature, determination of distance cutoff value and aggregate order parameters, implementation and molecular simulation trajectories, simulation snapshots and index of the reference molecule.

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