

1 Pharmaceutical Digital Design: From Chemical
2 Structure through Crystal Polymorph to Conceptual
3 Crystallization Process

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17 Synopsis: This work considers the theoretical basis of crystal structure prediction (CSP), free
18 energy, solubility, morphology and growth rate prediction, and the current state of nucleation
19 simulation to provide the conceptual process design for industrial crystallizations of
20 pharmaceutical compounds. This is illustrated by applying the modeling techniques to real
21 examples, olanzapine and succinic acid. We describe and demonstrate the promise of using *ab*
22 *initio* computer modeling for solid form selection and process design in pharmaceutical
23 development from only a molecular structure.

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69 ABSTRACT: A workflow for the digital design of crystallization processes starting from the
70 chemical structure of the active pharmaceutical ingredient (API) is a multi-step, multi-disciplinary
71 process. A simple version would be to first predict the API crystal structure and from it the
72 corresponding properties of solubility, morphology, and growth rates, assume that the nucleation
73 would be controlled by seeding, and then use these parameters to design the crystallization process.
74 This is usually an over-simplification as most APIs are polymorphic, and the most stable crystal
75 of the API alone may not have the required properties for development into a drug product. This
76 perspective, from the experience of a Lilly Digital Design project, considers the fundamental
77 theoretical basis of crystal structure prediction (CSP), free energy, solubility, morphology and
78 growth rate prediction, and the current state of nucleation simulation. This is illustrated by
79 applying the modeling techniques to real examples, olanzapine and succinic acid. We demonstrate
80 the promise of using *ab initio* computer modeling for solid form selection and process design in
81 pharmaceutical development. We also identify open problems in the application of current
82 computational modeling and achieving the accuracy required for immediate implementation that
83 are currently limiting the applicability of the approach.

84 1 Introduction

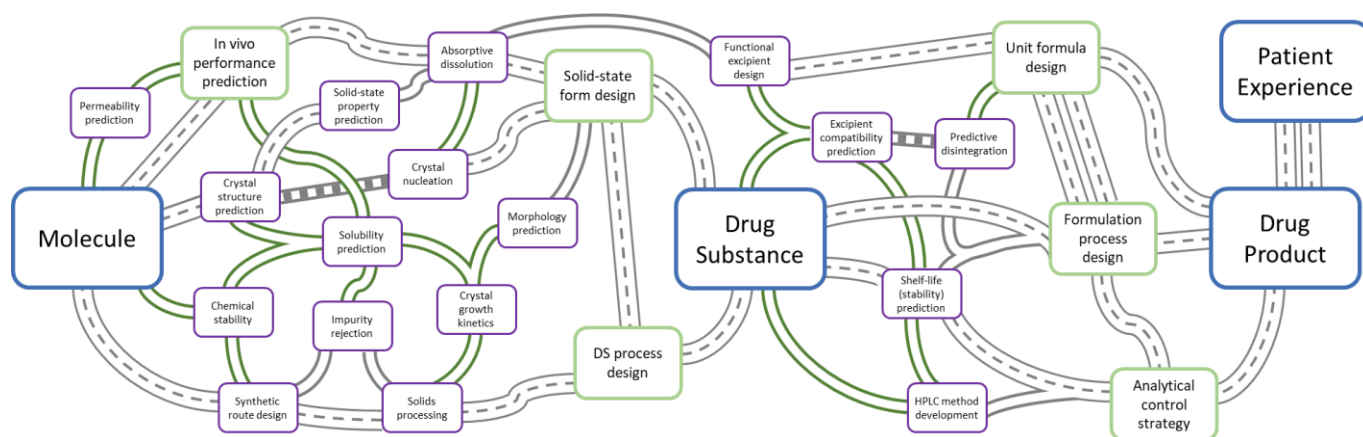
85 The development of a new pharmaceutical product begins with a hypothesis that a new molecule
86 will either promote or interrupt a biochemical pathway to affect a disease state. The target
87 molecule is tested in clinical trials for safety (Phase I) and efficacy (Phase II and III) and ultimately
88 progresses to the commercialization of a new medicine if successful. The journey for a molecule
89 to become a medicine is long, usually fraught with many obstacles, and very expensive. The
90 average cost to develop a new drug has been estimated to be between \$2.3 billion (reported in
91 2023^{1, 2}) and \$3 billion (reported in 2013³), with the probability that a Phase I compound will
92 successfully progress to product approval at just under 12%.³

93 Innovative pharmaceutical companies have long been utilizing computational tools to improve
94 the success rate of identifying prospective drug candidates to validate *in vivo*. Computational tools
95 are regularly used in the initial phase of drug discovery, e.g. to predict medicinal chemistry targets
96 and pathways,⁴⁻⁶ to identify candidate molecules, to compute binding affinity,^{7, 8} to forecast the
97 metabolism of a drug⁹ and to anticipate toxicological issues.^{10, 11} These computational efforts
98 increasingly drive the subsequent experimental efforts by identifying promising candidates prior
99 to synthesis and *in vivo* testing.

100 Simulation tools hold similar potential to shorten the time and lower the cost of product design
101 and development, but *ab initio* simulations have not been used to the same extent in the commercial
102 phase of product and process development. Except for perhaps the use of pharmacokinetic and
103 pharmacodynamic (PK-PD) models to predict drug absorption for solid oral dosage forms¹²⁻¹⁵ and
104 retrosynthetic techniques for route selection,¹⁶⁻¹⁹ development has remained mostly empirically
105 and experimentally driven, with computational approaches taking a supporting role as a drug enters
106 the product formulation and commercial process design stage.

107 The paths envisaged to digitally design a drug product, i.e., to progress a drug through clinical
 108 trials and develop it into a commercial drug product, are depicted in Figure 1. Overall, the process
 109 is not linear and there are many opportunities for iteration. However, many key milestones cannot
 110 be achieved until a precursor activity is completed – and for solid oral dosage forms, nothing is
 111 more critical than identifying the crystal form of the drug to carry into commercial development.
 112 Should the selection of the crystal form change, much of the product development process must
 113 be repeated, including clinical trials to demonstrate the equivalence of the new form to that
 114 previously tested in humans.

115



116

117 Figure 1. Roadmap illustrating the major (in bold) elements and associated work streams
 118 necessary for developing a new molecular entity into a solid oral drug product. (DS is drug
 119 substance).

120 The concept of digital design and utilization of computer modeling to complement the
 121 experimental input required for the design of solid forms and the crystallization processes to make
 122 them has emerged over the past two decades,²⁰⁻²² and is the subject of a recent review.²³ There has
 123 been much work assessing progress in each step, from the series of blind tests of crystal structure
 124 prediction organized by the Cambridge Crystallographic Data Centre (CCDC)²⁴ and the aqueous

125 solubility prediction challenges,²⁵ to Faraday Discussion meetings on crystallization,²⁶ as well the
126 output of the crystallization working group of the Enabling Technologies Consortium.^{22, 27}
127 Considerable progress is also being made with the use of informatics, for example, the extensive
128 range of tools in the CCDC's suite of programs, to complement experimental and computational
129 chemistry efforts.²⁸

130 This contribution evaluates how current computational tools can be combined in a workflow to
131 design crystallization processes from the molecular structure of the API. It is not intended as a
132 review of the different steps, but rather a **demonstration** of the use of *ab initio* computational tools
133 in the development cycle of a pharmaceutical product through the **integration** of the current state
134 of the art in selecting the desired solid state form of the API, through calculation of the requisite
135 physical properties necessary for optimal bioavailability and downstream processability. This
136 paper seeks to outline the fundamental physical basis of predicting each property and illustrate
137 these calculations on two systems, olanzapine, an atypical antipsychotic agent originally marketed
138 by Lilly as Zyprexa[®],²⁹ and succinic acid. Both are relatively small molecules compared with
139 current small molecule APIs under development. Consideration is given to both pure computation
140 of absolute or relative properties and where the input of some experimental data into the simulation
141 can provide a wide range of data of the required accuracy.

142 Inevitably, the practical computational models are more suited to certain types of molecules than
143 others, and the range of molecules to which they have been applied successfully with the accuracy
144 necessary for digital design varies. This leads to an outline of the open problems, both for each
145 step and overall, towards developing digital design strategies that could be deployed for the
146 crystallization of a wide range of pharmaceuticals, including multicomponent systems.

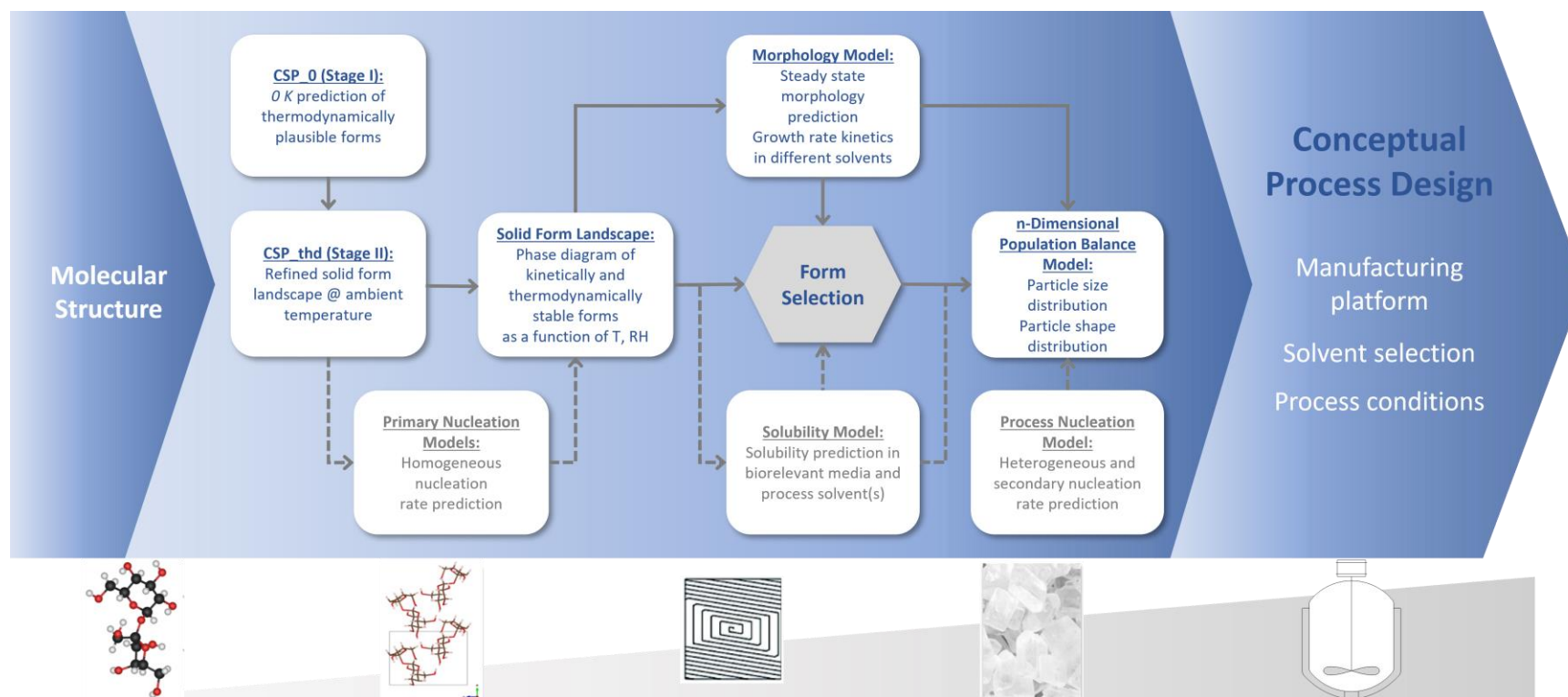
147 2 The Vision of *Ab Initio* Crystallization Process Design

148 Most drugs are developed as solid dosage forms, such as tablets or capsules,³⁰ due to patient
149 preference for orally administered drugs. *In silico* modeling should, in principle, provide a forward
150 look at the effort needed to develop an API into a new solid oral dosage form. Such methods
151 should not only help to design a product that will reliably deliver the drug to its target, but also
152 help to estimate and manage complexity, direct the experimental effort in an efficient and material
153 sparing way, optimize resources, and minimize the risk of downstream failures. Herein, we share
154 our vision for how *ab initio* methods will continue to evolve towards enabling crystallization
155 process design.

156 Development generally progresses along two streams, one to produce the drug substance from
157 commercially available starting materials and the other to produce the final dosage form with the
158 desired attributes (size, dose, shape, etc.). The two streams are not mutually exclusive given that
159 the process to make the drug product must be able to accommodate the physical properties (bulk
160 density, powder flowability, etc.) of the drug substance.³¹ Moreover, a coordinated effort may be
161 required to optimize the drug substance alongside the formulation to achieve the desired *in vivo*
162 performance of the solid oral dosage form.

163 For either situation, the choice of a suitable crystalline form of the API is one that meets the
164 needs of both drug substance and drug product development. This means that in practice,
165 concurrent with selecting a commercially viable synthetic route and before other key activities can
166 commence, the desired solid form of the drug substance is identified. Thus, the proposed digital
167 first workflow depicted in Figure 2 starts from the molecular structure with the prediction of the
168 static crystal structure landscape (CSP₀) to identify low energy structures that are plausible
169 polymorphs. These structures are then refined through the determination of the free energy at
170 room temperature to allow for prediction of phase diagrams (as a function of temperature, relative

171 humidity (RH), and sometimes pressure) as well as modeling and prediction of key properties
172 (solubility, etc.) to support the selection of the solid form.



173

174 Figure 2. Schematic digital workflow to define a conceptual crystallization process, starting from molecular structure on the left, and

175 proceeding to the crystallizer on the right. *Ab initio* models demonstrated in this paper are depicted in blue; those for which first-

176 principles models are not yet sufficiently accurate (currently determined experimentally) are colored gray.

177 Once the desired crystal form is selected, the design of an API crystallization process typically
178 commences by considering multiple objectives: purification/chemical purity, physical properties,
179 product yield, robustness, and productivity. Some models already exist to design crystallization
180 processes conceptually, helping to identify feasible operating conditions, guide economic
181 assessments, and in conjunction with control strategies, achieve target particle sizes and crystal
182 morphologies prior to the start of an experimental development program. Current models,
183 however, require existing experimental data (solubility, growth rates, nucleation rates) as inputs.
184 For example, the fate and purge of impurities after crystallization can be estimated based on the
185 impurity partition coefficient between the solvent and crystalline drug substance, and solubility of
186 the crystalline drug and impurity,³² although a computational impurity rejection model based on
187 impurities forming solid solutions has been recently proposed.³³

188 In our proposed digital workflow, polymorph-specific and facet-specific growth rates, together
189 with their dependence on solvent composition, and product solubility, are computed for putative
190 polymorphs (thermodynamically competitive crystal structures), then used in process models to
191 predict the crystal shape and to provide insight to the process design. We employ state-of-the-art
192 multi-dimensional population balance modeling to predict particle size and shape distributions,
193 but for these to be predicted by growth rates alone, we consider only seeded batch processes,
194 operating under conditions such that primary and secondary nucleation are minimized. While
195 reliable empirical models for secondary nucleation do exist, they require a few material- and
196 crystallizer-specific parameters, which must be experimentally determined. Thus, without a means
197 to predict secondary nucleation kinetics from a first-principles approach (see Section 6), the fully
198 *ab initio* conceptual design of a continuous crystallization process³⁴ is not yet possible.

199 The main components of the proposed digital workflow in Figure 2 (blue boxes) can, in
200 principle, be applied to any small molecule to design and ultimately deliver a drug substance with
201 desirable physical properties. However, situations may arise where additional models (not shown)
202 are needed to inform the crystallization process design. For example, content uniformity models³⁵⁻
203 ³⁷ may be required for high potency, low dose drugs and bioavailability models^{13, 14} are necessary
204 for BCS class II/IV molecules to establish the upper limit of the crystal size distribution that the
205 process must achieve. Whether the individual models are foundational (broadly applicable to small
206 molecules) or situational, they must be compatible for the overall workflow to succeed. That is,
207 the accuracy of the outputs must be sufficiently high to be useful as inputs to subsequent models.
208 To this end, we draw attention herein to three key areas (gray boxes in Figure 2) where accurate
209 first-principles models are needed for the vision of conceptual (batch or continuous) crystallization
210 process design to be realized: primary nucleation (for polymorph discovery), biorelevant
211 solubility, and secondary nucleation.

212

213 3 Crystal Polymorph Selection

214 Following the expensive and very public recall of Norvir® from the market due to the sudden
215 appearance of a more stable, less soluble polymorph of the API, ritonavir, in the drug product,³⁸⁻
216 ⁴¹ all large pharmaceutical companies have made major investments in solid form and salt
217 screening programs to mitigate the risk of late-appearing forms. The selection of the solid form
218 usually starts with screening studies to identify viable solid compositions from potentially many
219 salts (if ionizable), cocrystals, or the parent compound itself. This is followed by the screening
220 and ultimately selection of the desired crystal polymorph (neat form or hydrate) among the
221 crystalline ‘hits’. Theoretically, these exercises are best done holistically, but in reality, the

222 process of selecting a solid form is iterative, limited by the supply of the drug substance and the
223 time allotted for form screening.

224 Getting form selection right is non-negotiable as it affects downstream operations, as well as *in*
225 *vivo* performance. However, while industry has adopted a number of ‘best practices’ over the years
226 to rapidly screen diverse crystallization conditions, the path to a commercially-viable crystal form
227 remains very unpredictable and molecule-dependent; there is no one-size-fits-all recipe to
228 crystallize a molecule for the first time, let alone in a solid form that is suitable for a commercial
229 drug product. Furthermore, form selection is often conducted at a time in development when the
230 certainty of the compound moving forward into commercialization or even further into Phase II or
231 Phase III clinical trials is extremely low.⁴² Therein lies the conundrum; how much investment is
232 required to determine that a suitable composition (parent compound, salt, cocrystal) and the
233 preferred, most stable polymorph have been identified, when the commercial success rate is so low
234 and when speed to the clinic is critical? The need to get the crystal form right, preferably the first
235 time to minimize rework, must be balanced with the cost of screening a potentially large portfolio
236 of molecules, most of which will never progress further in development. This is where the *in silico*
237 design of solid forms, starting with the prediction of the crystal structure, has the potential to
238 change the game for solid oral dosage form development.

239

240 3.1 Crystal Structure Prediction

241 The pharmaceutical industry is interested in crystal structure prediction (CSP) from the desire to
242 right-size the search for the possible crystal forms (i.e. the polymorphs of the neat API⁴³ and at
243 least its hydrates⁴⁴). The main risk to avoid is the late appearance of a form more stable than the
244 one under development, as this may lead to its “disappearance”³⁹ or a sudden need to change the

245 form, the manufacturing process or storage conditions. As a complement to the experimental
246 screening and characterization of solid forms,⁴⁵ a CSP study can provide confidence that the most
247 stable form is known, and, in favorable cases, aid the design of an appropriate experimental search
248 for that form, as well as identify metastable forms to design around during process development.

249 The ideal CSP computational code would predict all the polymorphs that could be
250 experimentally realized and give a recipe for obtaining the first sample of each polymorph. This is
251 indeed the ultimate aim,⁴⁶ but the series of blind tests of CSP organized by the CCDC²⁴ show that
252 this is still an aspiration in this rapidly developing area. Currently, the first stage in the type of
253 CSP that is most commonly applied in industry,⁴⁷ referred to as CSP_0, is the search for structures
254 that are the most stable minima in the lattice energy. This is the energy required to separate a
255 (hypothetical) static infinite perfect crystal into infinitely separated molecules in their lowest
256 energy conformation, approximating the relative stability at 0 K. Since the relative stability of
257 polymorphs often changes with temperature and pressure, we need to develop the calculation of a
258 crystal energy landscape at processing and storage conditions (CSP_thd). Other thermodynamic
259 factors, such as the balance of bulk and surface energies, reflecting particle size should be taken
260 into account⁴⁸ as this can affect the relative stability of polymorphs, and can lead to the observation
261 of new polymorphs in confined crystallization experiments.⁴⁹ Environmental factors, such as
262 water activity (or relative humidity), must also be considered, such that the crystal structures of
263 anhydrates and hydrates of different stoichiometries can be directly compared on the same energy
264 landscape.⁵⁰

265 A major limitation of CSP_0 is that it usually generates significantly more crystal structures
266 within the likely energy range of polymorphism than are found experimentally.^{51,52} Although some
267 structures may appear as disorder components in observed polymorphs, many of these structures

268 may be artifacts of the neglect of the temperature-dependent molecular motions within the crystals.
269 Other structures identified as putative polymorphs could be kinetically forbidden, because of the
270 kinetics of nucleation and growth relative to the ability to transform to a more stable form. Despite
271 the advances in modeling nucleation and growth kinetics at the atomic scale,⁵³ our current
272 understanding of the kinetic competition involved in apparent polymorph stability is not yet
273 sufficiently mature to be encapsulated into a CSP workflow.

274 3.1.1 Lattice energy CSP

275 Current CSP₀ methods search for the possible crystal structures corresponding to a given
276 molecular diagram, i.e. covalent connectivity. Hence, typical CSP₀ searches will not include
277 crystal structures containing different tautomers, or allow a cocrystal to convert to a salt, even
278 when these are more stable. CSP studies consider a fixed stoichiometry of multi-component forms,
279 such as cocrystals, solvates and salts. The relative energies from CSP studies with different
280 tautomers or compositions can be compared, but the current success of CSP₀ comes from the
281 cancellation of errors in relative lattice energies, and the introduction of different types of
282 molecules and additional types of intermolecular interactions means that direct comparison is more
283 prone to error. The searches are generally limited to a specified number of crystallographically
284 independent molecules (often just $Z'=1$) and range of space groups. This is often leveraged to
285 concentrate the computational search into specific, chemically relevant, regions of the crystal
286 packing space. For example, a search can be restricted to the chiral space groups if the API is
287 chiral, and the other enantiomer cannot appear in the crystal structure.

288 A CSP search must also consider the range of conformations that could plausibly be of
289 sufficiently low energy to appear in a crystal structure. Typically many tens of thousands, even
290 millions of structures are generated for a pharmaceutical API with only one molecule in the

291 asymmetric unit cell ($Z'=1$). Searches with two or more independent molecules in the unit cell are
292 required for multicomponent systems and when there is experimental evidence that the API has
293 crystallized with two or more conformations or packing environments, and these CSP studies
294 generate many more structures than a ($Z'=1$) search. This number of crystal structures practically
295 necessitates a hierarchical ranking process to find the most stable distinct crystal structures, using
296 increasingly accurate and expensive methods of optimizing the structures to the nearest minimum
297 in the lattice energy, while progressively eliminating structures that are too high in energy to be
298 plausible polymorphs or are duplicates. The cost of a worthwhile CSP_0 strongly depends on the
299 molecule: the diversity of functional groups determines the range of possible intermolecular
300 interactions that dictate the crystallization process, and the conformational flexibility determines
301 how much the molecule can be distorted from the isolated molecule conformation by the packing
302 forces. It also depends on the range of crystal structures covered in the structure generation stage.
303 Hence, it is difficult to estimate in advance how many low energy crystal structures the CSP_0
304 will generate within the energy window being considered for possible polymorphism, and how
305 accurate the relative energies need to be to give a reliable order of stability. This ranges from
306 clearly monomorphic molecules, where there is only one way to pack the molecules densely in all
307 three dimensions, to molecules that have many closely related structures generated by CSP_0 that
308 contribute to the disordered crystal structures often observed in experiments.^{51, 54}

309 An efficient ranking of crystal structures necessitates computationally inexpensive methods for
310 the initial calculation of lattice energies. Traditional point-charge classical force fields that have
311 been extensively developed for liquid state and biomolecular simulations are rarely sufficiently
312 accurate for the final stages of CSP_0, as shown by the early blind tests of CSP. Molecule-specific
313 force fields can be generated by purpose-developed applications (e.g. GRACE⁵⁵) for use in the

314 structure generation stage, but these differ from traditional force fields by dispensing with the
315 assumption that the same atomic types and parameters can be used for intermolecular and
316 intramolecular forces. An approach that recognizes that the molecule is very similar in its crystal
317 structures uses the definition $E_{latt} = U_{inter} + \Delta E_{intra}$, where U_{inter} is the sum over all the
318 intermolecular interactions within the crystal as calculated with an anisotropic atom-atom force
319 field, and ΔE_{intra} is the penalty for conformational change. This approach is denoted Ψ_{mol} , as it
320 only requires electronic structure calculations on the isolated molecule.⁵⁶ The molecular electronic
321 structures calculations provide the molecular structure within the crystal, the conformational
322 energy penalty ΔE_{intra} for changes from the most stable isolated molecule conformation, and the
323 atomic multipole moments required to model the electrostatic contribution to U_{inter} . Many
324 worthwhile CSP_0 studies combine this anisotropic atom-atom electrostatic model with an
325 empirical *exp-6* repulsion dispersion potential,^{57, 58} and are very inexpensive for small rigid
326 molecules, where only one molecular wavefunction needs to be calculated. The success of this
327 approach can be attributed to the atomic dipoles and quadrupoles modeling the anisotropic
328 electrostatic effects of the lone pairs and π electron density, hence capturing the directionality of
329 hydrogen-bonding, $\pi \cdots \pi$ stacking and other dominant intermolecular interactions.^{59, 60} The theory
330 of intermolecular forces allows the development of increasingly realistic models for the
331 intermolecular interactions from the molecular charge distribution, and the generation of non-
332 empirical models.⁶¹ It has recently been shown that improving the quality of the *ab initio* method
333 used to describe the intramolecular energies (ΔE_{intra}) can significantly increase the accuracy of the
334 Ψ_{mol} approach.⁶² However, because the charge distribution of the molecule changes with
335 conformation, the cost of this approach scales with the number of conformations that have to be
336 considered, although various interpolation and database methods mean that this approach can be

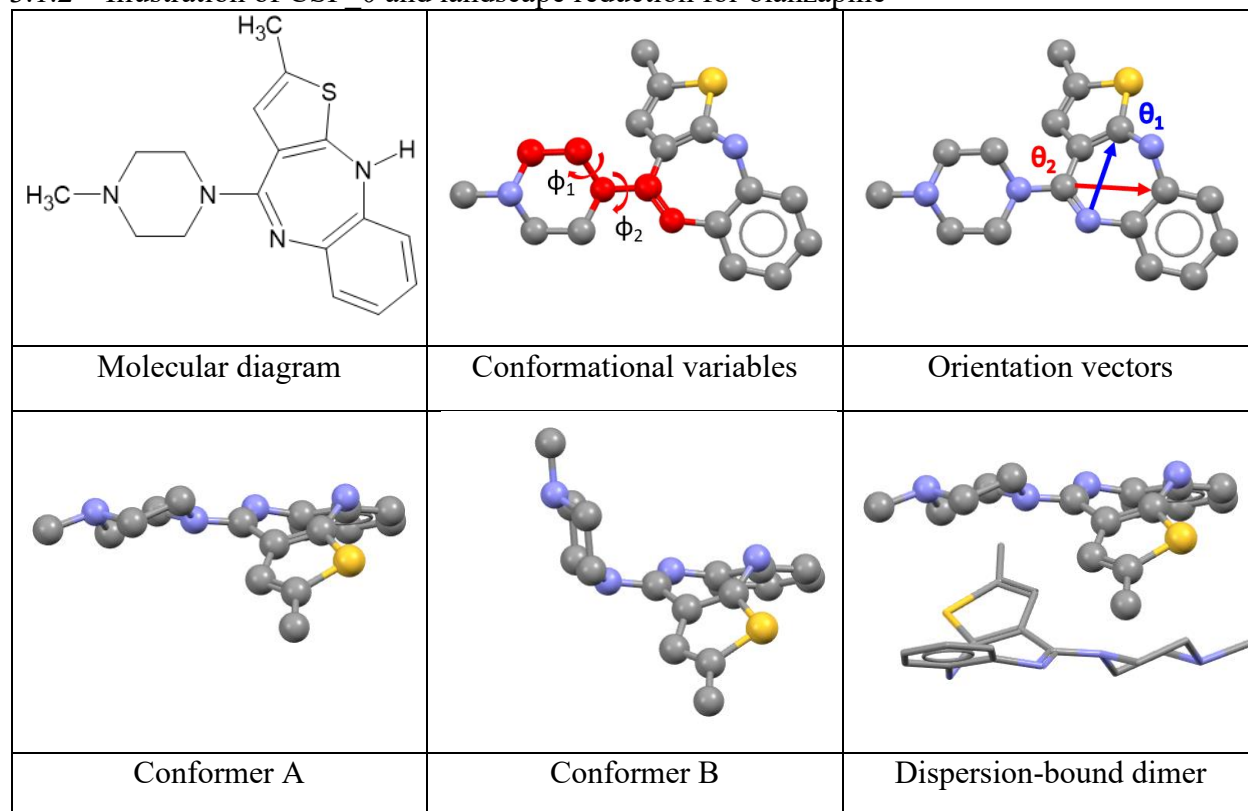
337 applied to pharmaceuticals.⁶³ A disadvantage of this method is that it is difficult to accurately
338 calculate the additional stabilization of the lattice by changes in the molecular charge distribution
339 (i.e. polarization) induced by the surrounding molecules.⁵⁸ This can be approximated in a structure-
340 independent fashion by calculating the molecular charge density (and hence ΔE_{intra} and the atomic
341 multipoles) in a polarizable continuum model (PCM) with a dielectric constant typical for organic
342 crystals.⁶⁴

343 A conceptually easier approach is to calculate the relative lattice energies of a set of crystal
344 structures directly from periodic electronic structure methods, denoted Ψ_{crys} . The cost of this final
345 stage in a CSP_0 scales with the number of crystal structures, as well as the number of atoms and
346 electrons in the unit cell. Practically, a Ψ_{crys} calculation must use an electronic structure theory
347 that is far inferior to that which can be used for a Ψ_{mol} CSP_0. Indeed, the use of Ψ_{crys} for organic
348 crystals only became worthwhile when periodic density functional calculations could be corrected
349 for the missing electron correlation terms that generate the universally attractive dispersion energy
350 (DFT-D methods).

351 CSP_0 has provided a strong impetus for the development of diverse methods of evaluating the
352 relative lattice energies of organic crystals.⁶⁵⁻⁶⁷ However, the computational effort required to
353 calculate the relative lattice energies of large numbers of CSP_0 structures can be wasted because
354 some of the static lattice energy minima are artifacts of the neglect of molecular motion. The
355 barriers between different minima can be lower than the zero-point energy of the molecular
356 vibrations,⁶⁸ and many lattice energy minima are not stable and may melt or merge to the same
357 free energy minimum.⁶⁹ To reduce the extent of over prediction associated with these features of
358 the lattice energy landscape, we have recently devised a workflow that leverages Molecular
359 Dynamics (MD) simulations and enhanced sampling methods to reduce a CSP_0 landscape to

360 those structures that are (computationally) distinct at ambient temperatures^{70, 71} or rationalize that
361 only an amorphous phase is likely to form.⁷²

362 3.1.2 Illustration of CSP₀ and landscape reduction for olanzapine

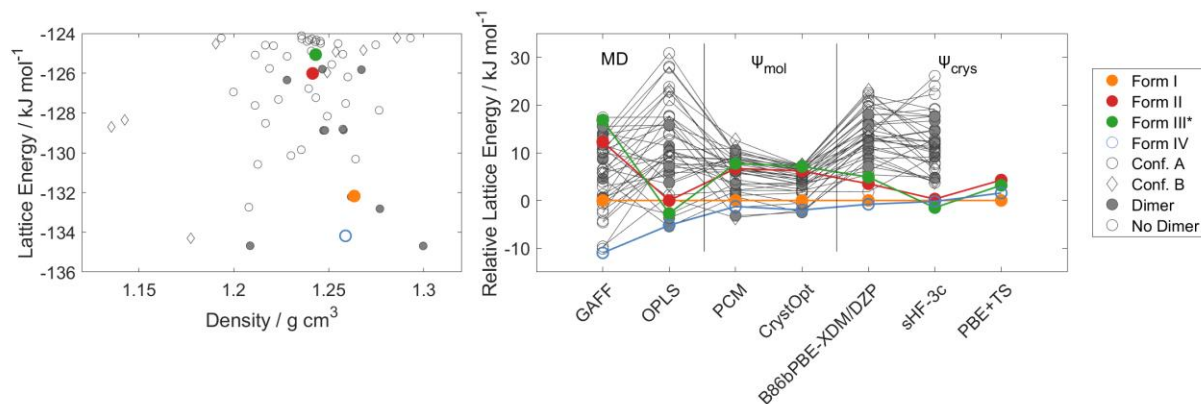


363 Figure 3. Top row: Molecular diagram of olanzapine, the conformational variables (ϕ_1 and ϕ_2)
364 used in the CSP₀ search and structural fingerprints, and the vectors (θ_1 and θ_2) used to define the
365 relative orientation of molecules in the structural fingerprints. Bottom row: The two types of
366 conformer, and the van der Waals bound dimer of conformer A found in most observed crystal
367 structures containing neutral olanzapine (the notable exception is form IV).

368 Olanzapine (Figure 3) is a good illustration of how CSP and molecular modeling can be used as
369 a complementary technique in understanding the experimental solid form landscape of a drug. The
370 extensive work at Lilly, who developed olanzapine as a solid oral dosage form, established²⁹ that
371 the marketed form I is the most thermodynamically stable form, and that the metastable forms II

372 and III are always found concomitantly, in varying proportions, in microcrystalline samples
373 obtained by desolvating solvates. An academic joint CSP and experimental screening program⁷³
374 characterized 56 solvates, and was able to solve the structure of form II from a suitable single
375 crystal grown by sublimation along with form III. This enabled the contribution of form II to the
376 diffraction of polycrystalline samples to be (computationally) removed to provide a powder X-ray
377 diffraction (pXRD) pattern for form III. The CSP study proposed a model for form III (denoted
378 III*), which was based on the same sheets as form II but stacked in a different fashion. The
379 existence of such similar CSP-generated structures helped rationalize the concomitancy of
380 olanzapine II and III, and for other molecules suggests the possibility of disorder⁷⁴ or polymorphic
381 domains.⁷⁵

382 The CSP_0 landscape (Figure 4) showed that there were thermodynamically competitive crystal
383 structures that did not contain olanzapine in the dispersion bound dimer (Figure 3), despite this
384 motif being observed in all previously characterized crystal structures. Only recently have studies
385 of the growth of an olanzapine solvate from solution shown why the dimers appear to be the growth
386 unit as often assumed.⁷⁶⁻⁷⁸ Decades after Zyprexa was developed, a new pXRD pattern was
387 observed for olanzapine produced by heat-induced crystallization from an amorphous
388 polyvinylpyrrolidone (PVP) based molecular dispersion.⁷⁹ The comparison of the pXRD pattern
389 with those simulated from the CSP_0 landscape lead to the structural characterization of form IV,
390 which did not contain the usual dimer. This is an example of the late-appearance of a polymorph
391 from heterogeneous nucleation, either through novel crystallization experiments such as attempted
392 crystallization or through changes in impurity profiles.



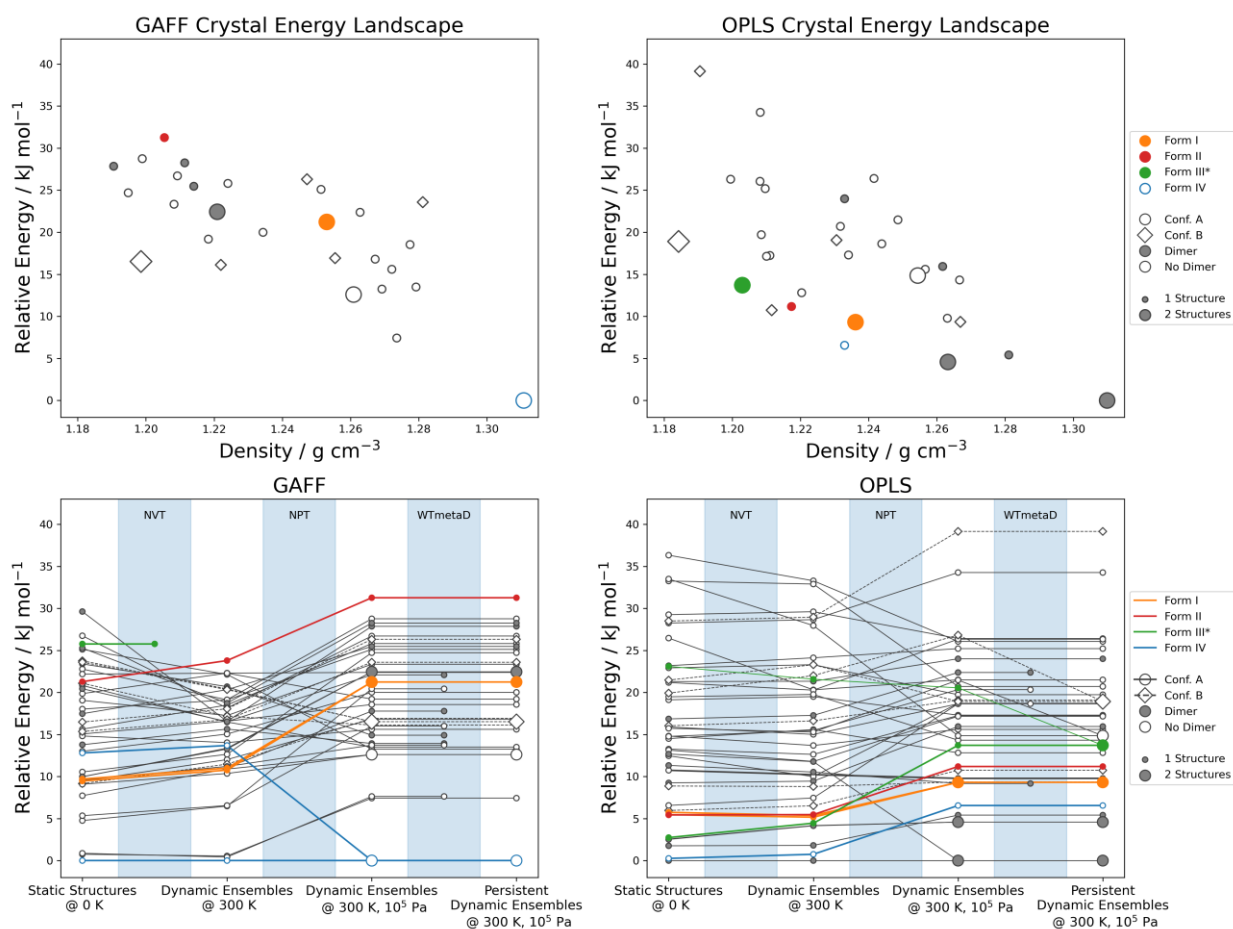
393
 394 Figure 4. Left: the lattice energy landscape obtained with a Ψ_{mol} CSP study of olanzapine using
 395 CrystalOptimizer (CrystOpt) for the final lattice energy refinement, with each point representing
 396 the lattice energy and density of a mechanically stable CSP₀-generated structure. Points are
 397 classified by packing motif and those that match forms I, II and IV and the proposed model form
 398 III* given in color. Right: the comparison of lattice energies obtained from different methods. The
 399 central Ψ_{mol} contrasts the CrystOpt energies shown in the lefthand landscape with those
 400 recalculated with the intramolecular energy penalty and distributed multipoles calculated in a PCM
 401 with a dielectric constant $\epsilon=3$ typical of organic crystals, as published in ref ⁷³. The Ψ_{crys} methods
 402 for all structures are from ref ⁸⁰, and can be compared with the PBE-TS results for the experimental
 403 forms. The two MD force fields, the General Amber Force Field (GAFF) and the Optimized
 404 Potentials for Liquid Simulations (OPLS), are those used in the landscape reduction (Section
 405 3.1.2). Conformers and the dimer are shown in Figure 3

406 The relative lattice energies of known and CSP-generated structures of olanzapine are typically
 407 sensitive to the computational model used (Figure 4). Reranking⁸⁰ these CSP₀ structures by
 408 single point plane-wave B86bPBE-XDM Ψ_{crys} calculations resulted in the four known polymorphs
 409 being the most stable structures, all within 5 kJ mol⁻¹ of the most stable form I, and with form III*
 410 the least stable. A similar stability order is given by optimization of the Ψ_{mol} minima with periodic

411 PBE-TS, a Ψ_{crys} model often used in CSP_0, confirming that forms I and IV remain, within the
412 margin of error, comparable in lattice energy and more stable than forms II and III* (Figure 4).
413 Experimentally, form I appears to be the most stable form, but the relationship between the
414 metastable forms is complex,⁸¹ with the free energy differences depending on temperature (see
415 3.2.1).

416 The CSP_0 lattice energy landscape of olanzapine has been reduced using our workflow⁷¹ to
417 those structures that appear stable at ambient conditions (300 K, 10^5 Pa). The structural fingerprints
418 used to compare the different dynamic structures in supercells containing between 216 and 360
419 molecules required consideration of two torsion angles and the relative intermolecular orientation
420 of the vectors shown in Figure 3, as well as the center of mass distances. In MD simulations of
421 large supercells it is impractical and computationally demanding to use the same intermolecular
422 force field used in the ranking of CSP_0 structures. As such, a typical choice is to employ small-
423 molecule point charge classical force fields such as GAFF or OPLS. For olanzapine, the choice
424 of GAFF or OPLS makes a significant difference to the relative lattice energies of the structures
425 (Figure 4), with the latter conserving all the known polymorph structures after reduction (Figure
426 5), and providing a better agreement of their lattice energy ranking with the more accurate lattice
427 energy models used in CSP_0 (Figure 4). The very high relative energy for form III* and
428 difference from form II with GAFF may explain why it melts in the GAFF simulation but does not
429 melt when simulated with OPLS (Figure 5). There is some clustering of the structures, but not a
430 drastic reduction (45 CSP_0 structures give 35 clusters with GAFF and 38 with OPLS). However,
431 using well-tempered metadynamics (WTmetaD) to enhance crystal cell fluctuations removes
432 significantly more structures, (28 retained with GAFF, 32 with OPLS). At this stage, we observe

433 a higher proportion of the dimer-based structures than the non-dimeric structures transforming to
434 more stable or disordered structures.



435
436 Figure 5. Top: The reduced energy landscapes of olanzapine: calculated with (left) GAFF and
437 (right) OPLS, with the size of the symbol representing the number of CSP₀ structures that have
438 merged to that form (the relative energy is the average potential energy of the structure in the MD
439 simulation at 300 K as distinct from the lattice energy (Figure 4) and so has a different energy
440 ordering). Bottom: the loss of structures (e.g. form III* through melting during the MD step)
441 resulting from the use of (left) GAFF and (right) OPLS, through the clustering and WTmetaD
442 steps. Here, relative energy of the static structures at 0 K indicates the relative lattice energy
443 computed after energy minimization, while at 300 K it is the relative potential energy averaged

444 over the last 200 ps. In the cases where relative energy at 300 K changes between the MD and
445 WTmetaD steps the initial crystal structure has transitioned to a different configuration.

446 Thus, the reduction of the energy landscape for olanzapine is not as extensive as for urea,
447 succinic acid⁷¹ or ibuprofen.⁷⁰ While noting that the reduction extent can indeed be system-
448 dependent, we also note that in this case we had pre-selected a subset of low-energy structures that
449 seemed likely to be long lived. Most dimeric and non-dimeric structures are stable, and so the
450 explanation for non-dimeric form IV being so elusive, despite its apparent stability in lattice
451 energy, is presumably that dimers form early in the crystallization process without the presence of
452 polymer. However, the short timescale of the MD simulations in the reduction workflow means
453 that this cannot be used to estimate the free energies of the surviving structures corresponding to
454 the force field.

455 A CSP was performed on succinic acid, following the serendipitous discovery of the γ
456 polymorph, which adopts a bent conformation that is dominant in solution.⁸² This structure was
457 readily predicted by a Ψ_{mol} CSP_0 search as intermediate in stability between the low temperature
458 stable β form and the high temperature α form, both of which have a planar molecular
459 conformation. The relative lattice energy is sensitive to the Ψ_{crys} dispersion correction and exact
460 crystal structure used, but all calculations with the PBE functional have the γ form as more stable
461 in lattice energy than β . Hence a polymorph that has only been observed once, despite efforts to
462 recreate the necessary crystallization conditions, would have been predicted as the most stable
463 form by a PBE-D Ψ_{crys} CSP_0 study.

464 The workflow for CSP_0 landscape reduction was developed using succinic acid as the example
465 with conformational flexibility.⁷¹ With GAFF, a set of over 100 CSP_0 structures was reduced to

466 27 low energy, persistent crystal structures, and identified the types of disorder and stacking faults
467 that probably occur in real crystal structures, particularly the high temperature α form.

468 The reduction of a CSP_0 landscape, using the observation that the number of CSP structures is
469 reduced by an MD shake-up⁸³ and that hypothetical structures will melt,⁸⁴ is a major step forward
470 to reduce the number of structures that need to be considered for more accurate calculations. Other
471 methods are emerging that can use an estimate of the energy barriers between the different forms.⁸⁵

472 3.2 Free energies of polymorphs

473 The relative stability of many polymorphs can change with temperature. In fact, a rigid-
474 molecule harmonic estimate of the free energy differences between 475 pairs of polymorphs
475 indicated the possibility of an enantiotropic phase transition in 21% of the studied systems.⁸⁶
476 Hence it is important to go beyond 0 K lattice energies and calculate relative free energies
477 (CSD_thd). These calculations can have a considerable cancellation of errors, particularly between
478 structures with similar types of intermolecular interactions and density. However, even at 0 K the
479 zero-point motions of the atoms within the crystal can differ between polymorphs. Polymorph
480 free energies deviate from the 0 K energy differences because of different vibrational modes and
481 frequencies and different degrees of vibrational anharmonicity. These differences are apparent in
482 the IR, Raman, and terahertz spectra. In particular, the higher frequencies associated with
483 hydrogen bonding often differ between polymorphs, and there is considerable mixing of the
484 intermolecular and intramolecular modes for all but the most rigid molecules.⁸⁷ Some polymorphs
485 may even accommodate a degree of dynamic disorder under ambient conditions, e.g. torsion
486 modes may become hindered rotors for some functional groups.

487 3.2.1 *Ab initio* free energies in the harmonic approximation and beyond

488 The harmonic approximation can be used in periodic density functional codes with an increasing
489 range of density functionals and dispersion interactions⁸⁸ to determine the phonons and hence free
490 energies. As different polymorphs usually have very different unit cells, care has to be taken to
491 use a sufficiently large supercell for the comparisons (i.e. converge the Brillouin zone). The choice
492 of supercell was straightforward for the single crystal to single crystal transformations in
493 desloratadine, as the unit cells were closely related, and the harmonic phonons gave a reasonable
494 estimate of the transitions.⁸⁹ For succinic acid, calculating the Helmholtz free energy using
495 harmonic phonons stabilizes β such that β is more stable than γ at ambient temperatures, although
496 the energy differences are very small.⁸² Coronene is another example where a harmonic phonon
497 calculation has been sufficient to show that the global minimum structure in a CSP_0 is actually
498 metastable at ambient temperature.⁹⁰

499 Recently, a limited CSP_thd study of olanzapine, using embedded fragment quantum
500 mechanical methods,⁹¹ compared the calculated frequencies of the two most stable structures (form
501 I and II) with experiment and confirmed that form I was monotropically more stable than form II,
502 with a Gibbs free energy difference that increased with temperature. An alternative electrical
503 embedding method using both DFT and single point MP2 calculations⁹² gave the same stability
504 order for lattice energies as the PBE-TS calculations in Figure 4, but showed that forms IV and III
505 swapped stability order around 200 K.

506 Fundamentally, the harmonic approximation is valid only at low temperatures. It neglects
507 thermal expansion and the effects of zero-point motion on the cell parameters. Quasi-harmonic
508 calculations on carbamazepine form III⁹³ estimate that this introduces an error of 1-2 kJ mol⁻¹ into
509 the enthalpy and entropy at ambient, but these contributions largely cancel. Hierarchical schemes
510 may allow the quasi-harmonic approximation to be applied more affordably and accurately to

511 organic crystals.⁹⁴ Several authors have included anharmonic effects and the contribution of
512 entropy at elevated temperatures for accurate estimation of free energies.^{95, 96}

513 A recently demonstrated framework for the thermodynamics of polymorphs⁹⁷ uses rigorous *ab*
514 *initio* Gibbs free energy calculations, based on the streamlined development of machine-learning
515 potentials to accurately reproduce *ab initio* (PBE0-MBD) potential energy surfaces and their
516 integration with path integral methods, accounting for the quantum statistical mechanics of the
517 nuclei. The quantum nuclei corrections contribute about 1 kJ mol⁻¹ to the free energy difference
518 between α and β succinic acid, correctly predicting that α is the high temperature form.⁹⁷

519 3.2.2 Free energies from biased Molecular Dynamics

520 Molecular Dynamics (MD) when combined with techniques from statistical mechanics, can also
521 compute free energies of crystal structures. The free energy in the canonical ensemble is:⁹⁸

522 Eq. 1
$$A = -k_B T \ln(Q)$$

523 where A is the Helmholtz free energy of the system, k_B is the Boltzmann constant, T is the
524 absolute temperature, and Q is the partition function, *i.e.* the Boltzmann-weighted sum over all
525 possible configurations of the system. Although force fields continue to limit accuracy, there are
526 now several methods that can compute relative free energy differences for large fully flexible
527 molecules and fully anharmonic crystals with extremely high precision, *i.e.* with minimal statistical
528 sampling errors. We discuss some of these methods in the following subsections.

529 From the definition of the canonical free energy as a function of the partition function, Q , it
530 follows that the free energy difference between two putative polymorphs, can be directly computed
531 from the ratio of their configurational integrals. In turn, the ratio of configurational integrals can
532 be estimated from an MD trajectory sampling the interconversion between putative polymorphs,
533 in the ergodic limit.

534 In practice, however, ergodic sampling of polymorph transitions cannot be obtained from
535 standard MD within computationally accessible timescales. As such, the calculation of free energy
536 differences between polymorphs *via* MD requires augmentation by suitable enhanced sampling
537 methods.^{99, 100} A class of enhanced sampling methods that has been often used to estimate the
538 relative finite-temperature thermodynamic stability of crystal polymorphs is based on the
539 introduction of a perturbation to the Hamiltonian of the system in the form of a bias potential to
540 overcome high free energy barriers and estimate free energy differences between long-lived
541 metastable states. Methods belonging to this family include static biasing approaches, such as
542 Umbrella Sampling (US),^{101, 102} as well as history-dependent biasing methods, such as
543 Metadynamics (MetaD).¹⁰³⁻¹⁰⁵ Both static and history-dependent biasing methods are based on the
544 ability to sample reversibly a pathway between different crystal forms, and on the ability to
545 represent such a pathway in a low-dimensional set of collective variables (CVs). Typically, static
546 approaches, such as US, require some *a priori* knowledge of the transformation pathway between
547 crystal forms. In US, the perturbative bias introduced is harmonic in CV space, and aims to achieve
548 an exhaustive sampling of the ensemble of configurations that are projected in CV space near the
549 center of the “umbrella”-like biasing potential. Appropriately combining series of independently
550 biased simulations that partly overlap in CV space and connect the polymorphic metastable states
551 of interest, enables the calculation of global free energy surfaces and, in turn, free energy
552 differences.^{101, 102, 106, 107} Unlike static approaches, history-dependent methods, such as MetaD,
553 can explore low dimensional CV spaces to autonomously identify transition pathways. In MetaD,
554 the bias potential is instead constructed adaptively as a sum of repulsive Gaussians, a function of
555 the system’s position in CV space. Such a potential discourages the visitation of configurations
556 that have already been sampled, leading to an autonomous exploration of unseen configurations

557 and to the discovery of transition pathways connecting metastable states. In this case, given the
558 total bias adaptively constructed as a simulation progresses, the unbiased probability, and thus the
559 free energy of relevant metastable states, can be computed.¹⁰⁸⁻¹¹²

560 Another approach to enhancing the sampling of polymorphic transformation *via* direct MD
561 sampling builds on the Adiabatic Free Energy Dynamics (AFED) methods developed by Rosso
562 and Tuckerman.¹¹³ The method implemented most recently, named crystal-AFED,¹¹⁴ is a variant
563 of the driven-AFED algorithm,¹¹⁵⁻¹¹⁷ where CVs, such as the supercell parameters or order
564 parameters capturing the local arrangement of molecules in the crystal, are adiabatically decoupled
565 from fast degrees of freedom and sampled at an artificial high temperature. In this case the bias
566 introduced by the sampling algorithm can be rigorously removed by applying appropriate
567 reweighing techniques.¹¹²

568 In all methods discussed, the sampling efficiency and the accuracy of the free energy estimates
569 depend on the ability of CVs to resolve degeneracies between metastable states of interest and to
570 capture the slow transition modes associated with a polymorphic phase transformation. As such,
571 for most molecular systems, the calculation of free energy differences between crystal forms
572 requires the identification or the development of *ad hoc* CVs, and the ability to efficiently compute
573 such CVs on-the-fly as a dynamic simulation progresses.¹¹⁸⁻¹²⁴ These aspects become increasingly
574 problematic with the complexity of the growth units considered,¹²⁵ and this directly impacts the
575 applicability of MD-based sampling approaches to large scale CSP_{thd} studies, where relative free
576 energy differences between hundreds of crystal forms, often exhibiting radically different local
577 structure, must be computed. As such, while direct sampling methods can yield a rich insight into
578 the mechanism of phase transitions and can in principle be used to investigate nucleation of

579 competing polymorphs in realistic environments, their application to CSP_thd is still somewhat
580 limited.

581 3.2.3 Free energies by Einstein Crystal

582 To circumvent the need to directly sample phase transformations, a common strategy is that of
583 taking advantage of thermodynamic cycles connecting the metastable state to a suitably defined
584 reference state. There are many literature examples where a reference state is chosen for which
585 free energy can be computed analytically or numerically.¹²⁶⁻¹²⁸ In the case of fluid phases, the most
586 suitable reference state is an ideal gas, and for the solid phases, the appropriate reference state will
587 be an Einstein crystal, introduced in 1984 by Frenkel and Ladd. This is a rigorous method to
588 compute the absolute free energy of solids.¹²⁶ An Einstein crystal is structurally identical to the
589 crystal of interest, with no interparticular/intermolecular interactions.¹²⁶ Each atom in the Einstein
590 crystal is attached to its lattice site *via* harmonic springs. Once the reference state's free energy is
591 known, the reference state is connected to the system of interest *via* a reversible path. Free energy
592 differences are computed along the reversible path as a ratio of partition functions.¹²⁹ The most
593 common methods to compute free energy differences are the free energy perturbation (FEP)
594 method and thermodynamic integration (TI).¹³⁰ The integration path should be free from phase
595 transitions.

596 Vega proposed a variant of the Einstein crystal method known as the Einstein molecule
597 method.¹²⁷ The key difference between these two methods lies in the implementation. In the
598 Einstein crystal method, the system's center of mass is held constant to avoid divergence at low
599 spring strength. In the Einstein molecule method, one of the atoms in the simulation box is held
600 constant to achieve the same.¹²⁷ These methods start from an Einstein crystal/molecule, then turn
601 on the interparticular/intermolecular interactions using the perturbation method. Finally, harmonic

602 springs attached to the lattice sites are removed to recover the solid of interest using TI. The
603 methods based on Einstein crystal and Einstein molecule references are often collectively called
604 “Frenkel-Ladd” methods, and they have been extensively used to compute the free energy of
605 atomic solids and molecular solids. Versions of these methods have also been implemented in
606 MD packages.¹³¹⁻¹³⁴

607 The Frenkel-Ladd methods obtain polymorph free energy differences by subtracting the absolute
608 free energies evaluated for two different polymorphs. Typically, the free energy difference is small
609 (a few kJ mol^{-1}) compared to the absolute values. Hence to obtain a meaningful small free energy
610 difference, two large free energy differences (from Einstein reference to each polymorph) must be
611 computed with high precision. The lattice switch methods provide a more direct polymorph-to-
612 polymorph pathway. Lattice Switch Monte Carlo (LSMC)¹³⁵ uses an energy gap order parameter.
613 The energy gap is obtained for any configuration by one-to-one mapping the thermal
614 displacements from the 0 K structure of one polymorph onto the 0 K structure of the other
615 polymorph. Umbrella sampling or other strategies can then drive the energy gap from negative
616 values through gateway states, where the energy gap is zero, to positive values for a reversible
617 pathway from one polymorph to the other. The recipe, in principle, works for arbitrarily complex
618 crystal structures, although LSMC itself has mainly been used in high accuracy calculations for
619 atomic solids.¹³⁵⁻¹³⁷ A diabatic free energy variant of LSMC makes further use of the exact Zwanzig-
620 Bennet relationship^{138, 139} between free energy diabats.¹⁴⁰ This new method shows promising
621 precision and efficiency for polymorphs of atomic systems,¹⁴¹ as well as molecular systems¹⁴²
622 (requiring only two unbiased MD simulations in some cases). Our application to carbamazepine
623 demonstrated precision at a level $\pm 0.01 \text{ kcal mol}^{-1}$ ($\pm 0.04 \text{ kJ mol}^{-1}$) in computed free energy
624 differences with just 5 ns of computing time per polymorph pair.¹⁴²

625 3.3 Open problems in CSP and free energy calculations

626 There are many open problems in the study of polymorphism.¹⁴³ The ideal polymorphs are those
627 that are predicted to be the most stable under any condition of temperature, pressure, or relative
628 humidity to which the drug product could be exposed. However, this is not generally the case for
629 many systems and the experimental observation of phase transformations, particularly in the solid
630 state, can be difficult.¹⁴⁴ Indeed, the prediction of free energies is particularly critical when there
631 is a major kinetic barrier to the transformation between structures, such that the transformation is
632 not readily or easily observed experimentally.

633 The possibility of a change in stability order of polymorphs is restricted to cases where the lattice
634 energy difference is comparable to the relative thermal contributions to free energy. However, as
635 shown clearly in Figure 4, the error in the relative lattice energies is still substantial, particularly
636 with the potential energy surfaces (force fields) that can be used to simulate anharmonic effects,
637 i.e., realistic molecular movement, including thermal expansion.

638 In choosing a method for computing polymorph free energies, several factors must be
639 considered. These include issues of both accuracy and precision. Accuracy pertains to the model
640 chemistry, e.g. an *ab initio* description or an empirical force field both of which include numerous
641 options with varying accuracy. Precision pertains to the ability to sample completely and
642 efficiently without assuming harmonic vibrations or other approximations beyond those inherent
643 to the model chemistry. Considerations of accuracy and precision are typically interrelated. For
644 example, high level electronic structure calculations offer better accuracy than most force fields,
645 but they are limited to harmonic approximations. In contrast, force fields enable calculations at
646 the 0.01 kJ mol⁻¹ level of precision, but the predictions are often hampered by questions about
647 force field accuracy.

648 The comparison of a CSP output with the known crystal forms usually poses the question as to
649 which of the unknown structures could be observed as relevant polymorphs. This is where CSP
650 can play a significant role as a complement to solid form screening.⁴⁵ There are often “predicted”
651 structures that are competitive with, or even more stable than the known forms,¹⁴⁵ raising the
652 question as to whether knowing the crystal structure of the targeted form can suggest an experiment
653 to produce the first sample. When the targeted polymorph is denser than the observed polymorphs,
654 further calculations of the lattice enthalpy as a function of the applied pressure may suggest that
655 crystallization under pressure would favor the targeted form.^{146, 147} The calculation of energy-
656 structure-function maps,¹⁴⁸ where the properties for each CSP-generated structure are
657 calculated,¹⁴⁹ has been powerful in the search for novel functional materials. It can also be used
658 for testing whether changes in experimental conditions are likely to be useful in polymorph
659 discovery, for example, the calculation of the anisotropy of the diamagnetic susceptibility tensor
660 of different polymorphs can indicate whether the polymorphic outcome may change if the
661 crystallization occurs within a magnetic field.⁹⁰ The most direct method to target a specific crystal
662 structure is when there is another molecule which adopts the desired crystal structure and can be
663 used as a template in a crystallization experiment.¹⁵⁰ For example, the first catemeric polymorph
664 of carbamazepine (form V) and form III of cyheptamide were found¹⁵¹ by sublimation onto a
665 crystal of dihydrocarbamazepine form II, and tolfenamic acid forms VI and VII were discovered
666 by sublimation onto mefenamic acid form I and a tolfenamic acid:flufenamic solid solution,
667 respectively.¹⁵²

668 4 Solubility Determination

669 Critical to the development of a crystallization process is the determination of the equilibrium
670 solubility of the given compound in the process solvent(s). Solubility is the concentration limit of

671 a chemical compound where the chemical potentials of the solid and solution phases are equal.
672 Supersaturation, the concentration of the solute above the saturation concentration of the specific
673 form, provides the driving force for crystallization. While it is generally straightforward to measure
674 the solubility of a stable polymorph, metastable polymorphs, which by definition create
675 supersaturated solutions, tend to transform in solution during the experiment into a more stable
676 form.¹⁵³ Computational methods to predict phase equilibria and free energy differences between
677 solid and fluid phases are therefore critical for studies of polymorph-specific crystal nucleation
678 and growth, and have great potential to aid solubility estimation tasks during crystallization
679 process development of API molecules. Solubility can either be calculated from considering the
680 coexistence of the two phases (Section 4.1) or by a thermodynamic cycle (Section 4.2).

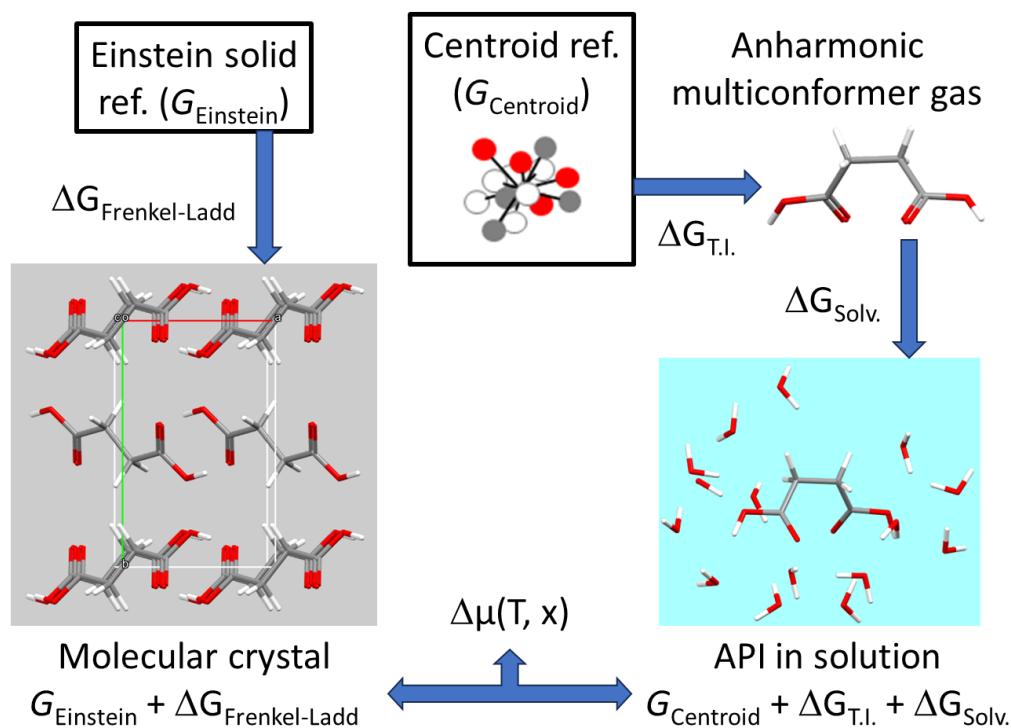
681 4.1 Methods based on coexistence

682 Direct coexistence simulations bypass the need for free energy calculations and directly provide
683 an estimate of the solubility limit. Basically, a long simulation with the crystalline material and
684 the solution in contact (usually at isobaric and isothermal conditions) allows the two phases to
685 reach equilibrium with each other. Direct coexistence simulations are simple and useful for initial
686 solubility estimates, but they have two important limitations.^{154, 155} These simulations are prone
687 to errors arising from long time scale, activated processes, such as attachment and detachment at
688 kinks,^{156, 157} 1D nucleation of kinks,¹⁵⁸⁻¹⁶⁰ and 2D island or pit nucleation.^{154, 161-165} Simulations
689 with special “everkinked” crystal orientations can eliminate the row/kink and island/pit nucleation
690 phenomena,^{162, 166} but the attachment and detachment rates at kink sites still set a fundamental limit
691 on the efficiency of direct coexistence results. These limitations can be effectively mitigated by
692 using enhanced sampling methods to facilitate an exhaustive sampling of the attachment and
693 detachment processes to and from kink sites, as recently demonstrated by Bjelobrk et al. for

694 organic molecules¹⁶⁷ and salts in solvent-antisolvent mixtures.¹⁶⁸ However, direct coexistence
695 simulations can only estimate equilibrium concentrations, e.g., the equilibrium solubility limit, the
696 melting temperature, or the partial pressure for evaporation. They cannot estimate the chemical
697 potential differences at non-equilibrium supersaturated conditions that drive crystallization.

698 4.2 Methods based on thermodynamic integration

699 An alternative route is to compute the dissolution free energy in stages *via* a thermodynamic
700 cycle of subliming the crystal into the gas phase and then solvating the molecule, an approach
701 shown adapted to thermodynamic integration (TI) in Figure 6. We have already seen (Section
702 3.2.3) how Frenkel-Ladd methods (TI for solids) starting from the Einstein crystal or Einstein
703 molecule can compute free energies of solid phases.^{169, 170} Starting from a suitable reference model
704 for the gas phase molecule, TI methods can also provide the free energy of molecules in solution
705 as a function of temperature, solute concentration, and pressure. The typical gas phase reference
706 for small and relatively rigid molecules is the free energy with harmonic vibrations. Figure 6
707 shows the alternative centroid reference of Khanna *et al.*¹⁶⁹ The centroid is comprised of all atoms
708 in the solute molecule, tethered *via* springs to their collective center of mass. It has the same mass
709 and the same number of vibrational and rotational modes as the final molecule. The centroid is
710 converted to a fully anharmonic molecule by a TI that turns on all intramolecular interactions such
711 as bonds, angles, dihedrals and pairwise interactions within the molecule, e.g. Lennard-Jones and
712 coulombic interactions.¹⁶⁹ This one extra step, the centroid-to-molecule transformation, provides
713 the absolute free energy for fully anharmonic and multiconformer gas phase molecules. The next
714 step, whether starting from a harmonic reference or centroid reference, is to compute the free
715 energy of solvation. Note that the solute free energy in the gas phase is a function of its partial
716 pressure, and that in the solution phase it is a function of its mole fraction.



717

718 Figure 6. Thermodynamic integration starting from two reference models to obtain the free energy
 719 of the crystal and that for the molecules in solution. The calculations are illustrated for the β form
 720 of succinic acid, which has a planar conformation in the crystal but the dominant gas and solution
 721 phase conformation is bent.⁸²

722 The solubility can be computed by equating the chemical potential of the compound in the crystal
 723 phase with that in the solution phase, i.e. $\mu_{\text{crystal}}(T) = \mu_{\text{solution}}(T, x)$ where x is the mole fraction of
 724 solute in solution. The equality of chemical potentials is satisfied for the special composition x_{sat} ,
 725 i.e. the solubility limit.

726 4.2.1 Heat of sublimation

727 The heat of sublimation, the energy difference between the crystal and gas phases, is usually the
 728 best experimental test of the energy scale of the intermolecular interactions within the crystal and
 729 hence the lattice energy. Computationally, we can estimate the heat of sublimation from the slope

730 of Clausius-Clapeyron plots, which require vapor pressure data at various temperatures.¹⁷⁰ Vapor
731 pressures at each temperature are computed by equating the chemical potential of the crystal phase
732 with that of the gas phase.¹⁷⁰ Crystal and gas phase free energies are computed using the methods
733 mentioned in Sections 3.2.3 and 4.2.

734 4.2.2 Solvation energies

735 For the solution phase, we add the solvation free energies to the molecule's intramolecular and
736 translational free energy. Solvation free energy refers to the work required to insert one solute
737 molecule into the given solvent. Like Widom's method,¹⁷¹ direct insertion of solute molecules with
738 complex molecular structures into the highly dense solvent phase will be difficult. Alternatively,
739 several authors have come up with new strategies based on Monte Carlo methods to address this
740 problem. For example, methods like Configuration Bias Monte Carlo methods¹⁷² (CBMC) and
741 Continuous Fractional Monte Carlo methods¹⁷³ (CFMC) will improve the statistics for the
742 insertion of solute molecules in the solvent.

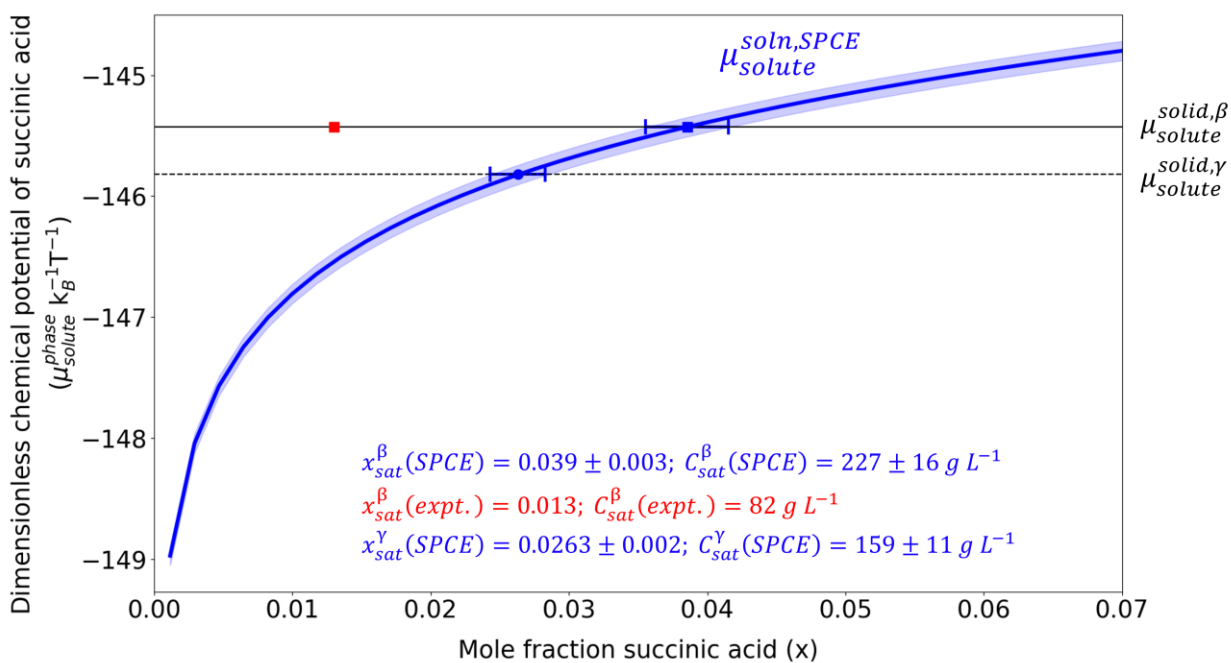
743 Other methods combine MD simulations along with FEP or TI to compute solvation free energy.
744 Most of these methods use an external repulsive potential (Weeks-Chandler-Anderson (WCA)
745 potential¹⁷⁴ or Born potential) to create a cavity for solute insertion. Shivakumar *et al.* developed
746 a method that uses MD with an FEP scheme to compute absolute solvation free energies of small
747 neutral molecules in various solvents.¹⁷⁵ Mobley and Guthrie computed the free energy of
748 hydration for nearly 650 molecules and constructed a database of solvation free energies for
749 explicit and implicit solvent models.¹⁷⁶ They report an rms error of 6.3 ± 0.3 kJ mol⁻¹ between the
750 computed and experimental hydration free energies using GAFF. Li *et al.* proposed a TI based
751 scheme with MD simulations to compute the solvation free energies of sparingly soluble solutes
752 in different solvents. The strategy involves three main steps. First, the solvent is evacuated from

753 a cavity with an external repulsive potential, then the solute molecule is inserted into the cavity,
754 and finally the external potential is removed to recover the state of interest.

755 Recently, Khanna *et al.* proposed a decoupling approach to compute the solvation-free energies
756 of solutes in each solvent.¹⁷⁷ In this method, the authors invoke a shorter thermodynamic cycle by
757 decoupling the solute-solvent interactions in the solution phase. Then they gradually turn on the
758 Lennard-Jones and coulombic interactions in two steps to compute the solvation free energy in
759 each solvent. The added advantage with the recent two methods is that these methods are
760 compatible with popular open-source MD engines such as LAMMPS and GROMACS.

761 4.2.3 Pilot Compound Results – succinic acid

762 The approach reported in references¹⁷⁷ and¹⁶⁹ has been used to predict the solid-vapor and solid-
763 solution equilibria of β - and γ -succinic acid at various temperatures, along with the driving forces
764 (chemical potential difference for solute in solution phase and crystalline phase) for crystallization.
765 Shown in Figure 7 is the chemical potential computed for succinic acid as a function of solution
766 phase mole fraction at 300 K, along with the computed chemical potentials for the β and γ
767 polymorphs. The vapor pressures and solubility predictions for succinic acid when plotted against
768 inverse temperature give rise to the Clausius-Clapeyron (Figure 8) and van't Hoff (Figure 9) plots,
769 respectively.



770

771 Figure 7. Chemical potential as a function of solubility mole fraction in aqueous solution at 300 K

772 and 1 atm pressure (adapted from Figure 9 in Khanna *et al.*¹⁷⁰, reprinted by permission of the

773 publisher (Taylor & Francis Ltd, <http://www.tandfonline.com>)), along with computed chemical

774 potentials of the β and γ succinic acid polymorphs. The force field model used for succinic acid

775 is GAFF, and that used for water is SPCE.¹⁷⁸ The computed saturation solubility, x_{sat} , of each

776 polymorph lies at $\mu_{crystal}(T) = \mu_{solution}(T, x)$, where the chemical potential of the compound in the

777 crystal phase and that in the solution phase intersect. The width of the curve represents plus and

778 minus one standard deviation in the predicted chemical potential, i.e., the "error bar." The error

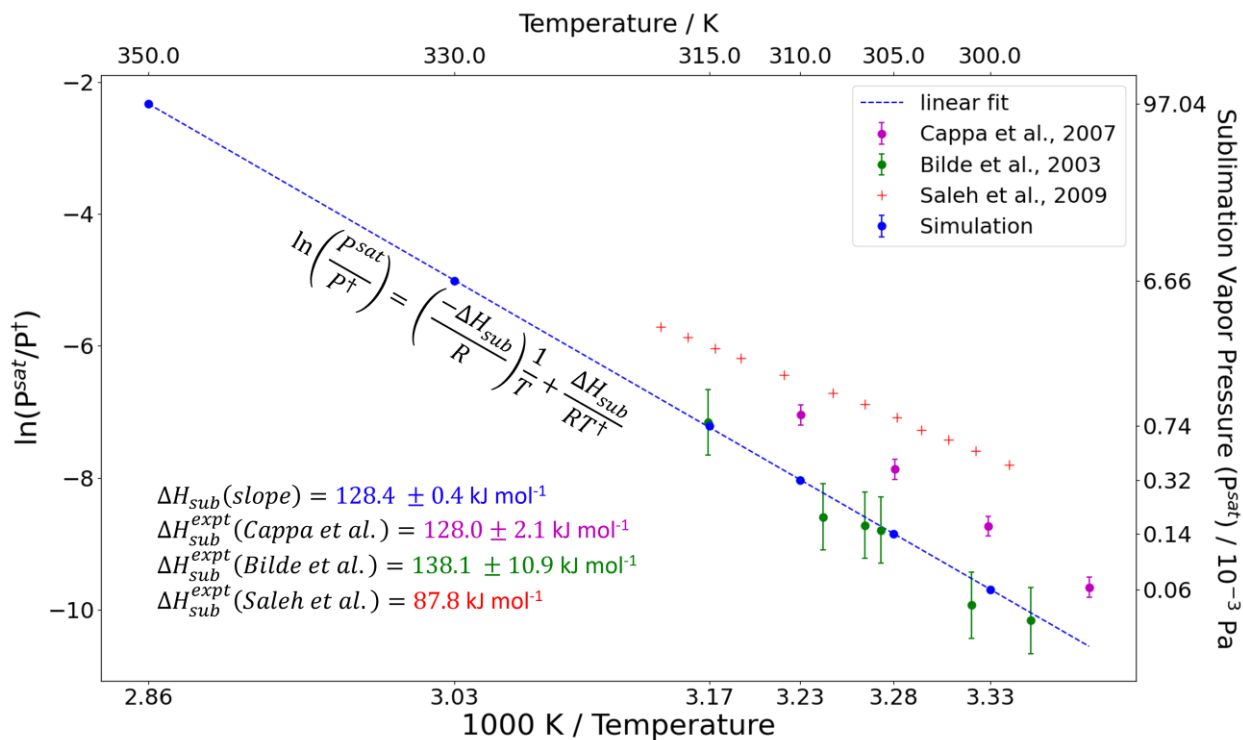
779 bars reflect statistical uncertainty (i.e. precision) in the calculations, as opposed to bias errors from

780 force field inaccuracy which are the main reason for the discrepancy with experiment. In

781 conversion of mole fractions to C_{sat} , we assumed negligible volume of mixing, i.e. that the volume

782 of the solution was equal to the volume of water at 300 K plus the volume of solid succinic acid at

783 298 K.



784

785 Figure 8. Clausius-Clapeyron plot of β succinic acid sublimation vapor pressure and temperature,

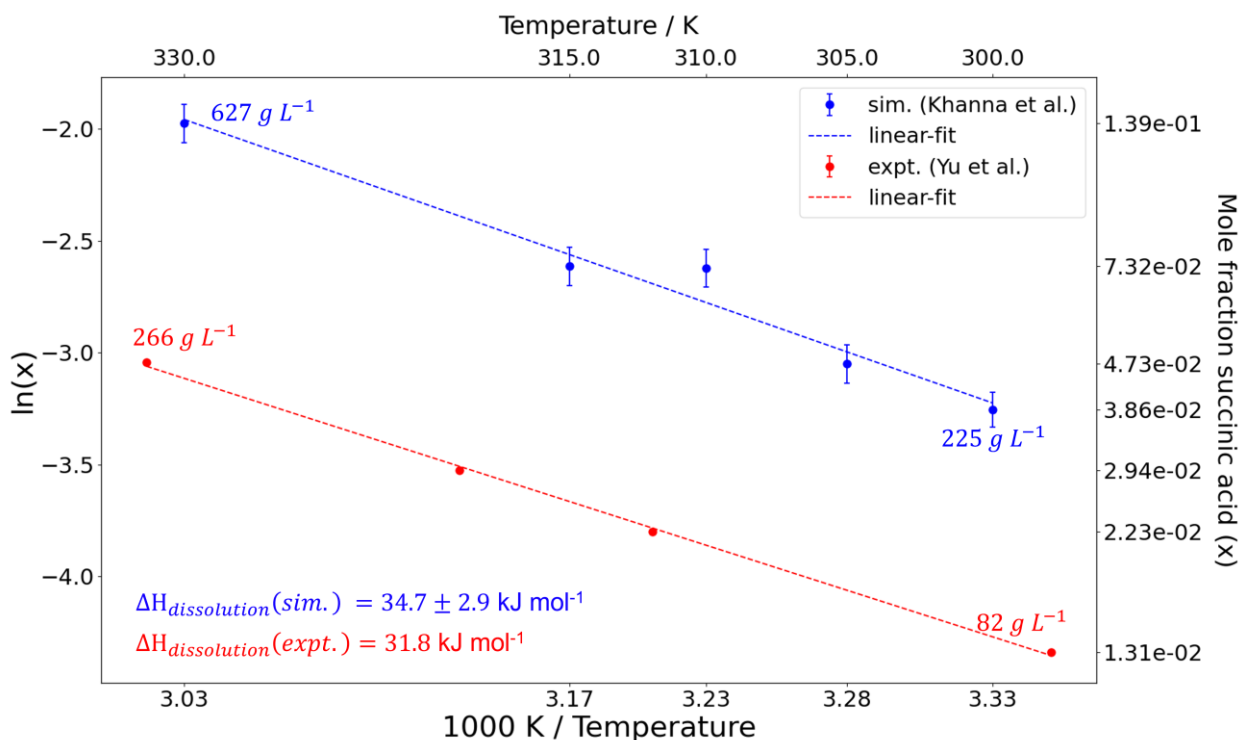
786 where $P^\ddagger = 1 \text{ Pa}$, and T^\ddagger is the corresponding sublimation temperature. The tick marks on the

787 secondary ordinate axis on the right-hand side of the figure correspond to the simulation data

788 points. Adapted from Figure 6 in Khanna *et al.*,¹⁷⁰ reprinted by permission of the publisher (Taylor

789 & Francis Ltd, <http://www.tandfonline.com>), including experimental data from Cappa *et al.*,¹⁷⁹

790 Bilde *et al.*,^{180, 181} and Saleh *et al.*¹⁸²



791

792 Figure 9. Van't Hoff solubility plot for β succinic acid in aqueous solution at atmospheric pressure.

793 The tick marks on the secondary ordinate axis on the right hand side of the figure correspond to

794 the experimental (taken from Yu *et al.*¹⁸³) and simulation data points (taken from Khanna *et al.*¹⁷⁰),

795 with tick marks for overlapping points not shown for clarity. Adapted from Figure 11 in Khanna

796 *et al.*,¹⁷⁰ reprinted by permission of the publisher (Taylor & Francis Ltd,

797 <http://www.tandfonline.com>). In conversion of mole fractions to C_{sat} , we assumed negligible

798 volume of mixing, i.e. that the volume of the solution was equal to the volume of water at the

799 appropriate temperature plus the volume of solid succinic acid at 298 K.

800 On the Clausius-Clapeyron plot (Figure 8) the simulation points lie almost perfectly on a straight

801 line although no such requirement is imposed on the simulation algorithm (of course the

802 experimental data are equally unaware that they are expected to follow the same trend). The slope

803 of the line gives the sublimation enthalpy, which is in reasonable agreement with the range of

804 experimental values. At the current time it is not possible to say anything general about vapor
805 pressure predictions since Figure 8 is the first vapor pressure prediction for organics that we know
806 of in the literature. Nevertheless, we can conclude that the estimation of sublimation vapor
807 pressure is now possible for organic molecules and may be a useful addition to workflows for
808 digital drug product design.

809 One word of caution is worth mentioning. Vapor pressure predictions exponentially magnify
810 small errors in the chemical potential calculations (regardless of whether these errors arise from
811 simulation methodology errors or force field inaccuracies), as explained by Khanna *et al.*¹⁶⁹ in
812 connection with eq. 16b in that paper. In their calculations, an error of 0.05% in absolute chemical
813 potential for succinic acid becomes a 10% error in vapor pressure prediction.

814 The computed slope (enthalpy of solution) tends to be in close agreement with experiments, but
815 predictions for the intercept (related to entropy of solution and the absolute solubility) are less
816 reliable as seen in Figure 9.¹⁸⁴⁻¹⁸⁶ One reason is that Van't Hoff plots for solubility-temperature
817 relationship exhibit non-linearities over a wide temperature range.¹⁸⁷ The nonlinear 1/T
818 dependence emerges because enthalpy and entropy of solvation are not truly temperature
819 independent quantities. Moreover, as seen in Figure 7, the absolute solubility (related to the
820 intercept in the Van't Hoff plot) is highly sensitive to the computed chemical potential. If the
821 curve of chemical potential of the solute in solution, $\mu_{solute}^{solution}$, is shifted up by approximately 1
822 $k_B T$ or if the chemical potential of the pure solid solute is shifted down by approximately 1 $k_B T$ the
823 predictions would align with experiments. This difference is less than 1% of the free energies
824 being computed (1 part in ~ 145), which demonstrates the level of accuracy required to correctly
825 predict absolute solubility. This is unlikely to be achieved very often with the current generation

826 of classical force fields, but with just one experimental data point, the simulated line can be fixed
827 in the correct position to follow the remaining experimental data.

828 Polymorph stability is demonstrated in Figure 7 where the chemical potential of the γ crystalline
829 form of succinic acid is also plotted. The resulting chemical potential for the γ form is lower than
830 for the β form (more negative), leading to a lower solubility in solution, indicating a more stable
831 solid form at 300 K and 1 atm pressure. However, the two forms differ in their chemical potential
832 by only $\sim 0.4 k_B T$ molecule⁻¹, which is small indeed compared to the absolute scale of $\sim -145 k_B T$
833 molecule⁻¹. It seems reasonable to conclude that the two forms are close in stability, so close in
834 fact that it may be difficult to discriminate between them, as also shown by the relative lattice
835 (Section 3.1.2) and free energies (3.2.1). However, to do this experimentally will first require an
836 experimental protocol for producing and isolating the γ form which has only been observed once
837 in the lab as a concomitant solid with the commonly observed β form.⁸²

838 Another method of calculating absolute solubility by the thermodynamic cycle is based on using
839 the Ψ_{mol} estimate of lattice energies (section 3.1.1) and the harmonic phonons (3.2.1) to evaluate
840 the heat of sublimation, along with either implicit or explicit solvation models for the heat of
841 solvation. This has been shown to rival the accuracy of informatics models for calculating absolute
842 solubility.¹⁸⁸ In the case of succinic acid, computing hydration free energies from atomistic MD
843 simulations using FEP methods and GAFF combined with the water SPCE force field gave a
844 hydration energy of $-57.47 \text{ kJ mol}^{-1}$, in somewhat better agreement with experiment (-61.08 kJ
845 mol^{-1})¹⁸⁹ than various implicit solvation models. A Ψ_{mol} estimate of the lattice energies, and Ψ_{crys}
846 estimate of thermal corrections from harmonic phonon calculations gave a heat of sublimation of
847 $121.04 \text{ kJ mol}^{-1}$ (Fowles et al.¹⁸⁸ used an experimental value¹⁹⁰ of $123.2 \text{ kJ mol}^{-1}$ which can be
848 compared with the values on Figure 8). Combining these estimates gave an aqueous solubility of

849 0.447 mol L⁻¹, equivalent to 52.75 g L⁻¹, which is within reasonable agreement with experimental
850 determinations ranging from 70 to 82 g L⁻¹. This was more accurate than the best machine learning
851 estimate, yet the agreement with experiment is very dependent on the quality of electronic structure
852 method and choice of empirical force field used.¹⁸⁸

853 4.3 Open problems in the calculation of solubility

854 Solubility prediction is an ongoing challenge for “first principles” methods that do not require
855 any experimental input. The simplest strategy accounts for solvation through an implicit solvation
856 model, often based on Poisson-Boltzmann equations¹⁹¹ or polarizable continuous medium
857 models¹⁹² in combination with density functional theory calculations. A related strategy, used
858 extensively in crystallization, is the conductor-like screening model (COSMO). This uses *ab initio*
859 calculations to obtain “sigma profiles” (surface charge density profiles) specific to each solute and
860 solvent molecule. Solvation free energies are estimated *via* a thermodynamic cycle of melting and
861 mixing with the solvent sigma profiles. This method is a conductor-like screening model based on
862 the use of solvation thermodynamics and can use the growing open-source database of “sigma
863 profiles” for different solvents.¹⁹³ Although the COSMO approach offers a route to varying both
864 single solvents and mixed solvents (especially, solvent-antisolvent mixtures) into crystal growth
865 and morphology modeling, there is the limitation of the requirement of experimental melting data
866 for the drug crystals that may not be obtainable when there is thermal degradation.

867 Moving to explicit solute-solvent simulation methods, direct coexistence simulations are
868 susceptible to undetected errors, and they cannot provide thermodynamic driving forces beyond
869 the solubility limit. Methods based on harmonic approximations can be implemented with
870 electronic structure theories that remain accurate across solutes and solvents, but harmonic
871 approximations and continuum solvent approximations become inaccurate for large molecules

872 (especially in fluid phases). Methods based on thermodynamic cycles require precise free energy
873 calculations for the crystal phase, the gas phase, and the solvation free energies. All three free
874 energy calculations can now be done precisely, but accuracy remains limited even for the best
875 available force fields. Given the difficulty in experimentally determining the thermodynamic
876 differences between polymorphs, or even their melting points and heats of fusion, further progress
877 in the calculation of solubilities is both necessary and expected. Efforts to predict solubility may
878 benefit from machine learning methods, which require large experimental datasets for training.¹⁸⁸
879 An open challenge in solubility prediction is to combine machine learning with physical principles,
880 in ways that can guide the rational selection of solvents.¹⁹⁴

881 5 Crystal Growth and Morphology Prediction

882 Crystal morphology (by which we mean the particular faces exposed on the crystal surface
883 together with their relative areas) plays a significant role in pharmaceutical manufacturing.
884 Needle-like and plate-like crystals are to be avoided because they are difficult to process in both
885 upstream (crystallizer-filter-dryer) and downstream (formulation and tableting) operations.
886 However, due to the large number of crystalline products in development, coupled with the vast
887 choice of growth conditions, including choice of solvent (and possibly solvent mixture and/or
888 choice of antisolvent), temperature, supersaturation, pH, and impurities/additives, it is a great
889 challenge to obtain specific crystals which have a particular product functionality and morphology
890 in an acceptable process development timescale. *In silico* methods hold promise of providing
891 useful tools to guide experiment and pre-screen the desired crystals more cheaply and efficiently

892 In many instances the goal is to produce well-faceted prism-like crystals of the desired
893 polymorph in the size range 30 – 80 μm .¹⁹⁵ Such crystals are generally formed in a layer-by-layer
894 fashion. The usual transport picture is that solute molecules diffuse from the bulk solution across

895 a boundary layer to the crystal-solution interface (3D diffusion), where they adsorb on the crystal
896 terraces, then diffuse across the terraces (2D diffusion) and incorporate into vacant sites (called
897 kink sites) on the steps, thereby causing the steps to “flow across the surface” to create the
898 layers.^{196, 197} At low supersaturation, the steps are generated by screw dislocations on the crystal
899 surface leading to the famous spiral growth mechanism of Burton, Cabrera and Frank,¹⁹⁸ or at high
900 supersaturation they correspond to the faceted edges of a 2D nucleus that has formed on the crystal
901 face.¹⁹⁹⁻²⁰³ Under such a layer-by-layer mechanism the growth rate, G_{hkl} (in units of nm s^{-1}), of
902 each face (hkl) is given by

903 Eq. 2
$$G_{hkl} = \frac{h_{hkl}}{\tau_{hkl}}$$

904 where h_{hkl} is the step height (nm), and τ_{hkl} is the time taken (s) to lay down a layer. Under normal
905 conditions for API molecules G_{hkl} is in the range 5-100 nm s^{-1} (or about 5-100 unit cells per
906 second).

907 In many industrial crystallizations, the slowest process in this picture is solute incorporation at
908 kink sites.^{198, 200, 204} Mechanistic models based on this assumption are widely used in the literature.
909 The step height is a simple multiple (typically $\frac{1}{2}$ or 1) of the interplanar spacing, d_{hkl} , and for spiral
910 growth τ_{hkl} is the rotation time of the spiral, which involves the step velocity, v_i^{step} , for each of the
911 i steps on the spiral, and critical length of each spiral side.²⁰⁵ The critical length can be reliably
912 calculated using the Gibbs-Thomson equation²⁰⁶ (also see Fig. 3 and eq. 23 in ref²⁰²). Step
913 velocity, however, is more challenging. The normal assumption is that the step remains stationary
914 until it has reached its critical length, whereupon it travels at constant velocity across the surface
915 of the face (this is the Voronkov assumption;²⁰⁷ see Teng *et al.*²⁰⁶ for an assessment of this model).
916 For the special cases of Kossel growth units (cubic “molecules” with six identical faces each
917 exposing identical “broken bonds” with neighboring molecules) and centrosymmetric growth units

918 (molecules with an inversion center such as planar succinic acid and naphthalene) step velocity is
919 calculated using

920 Eq. 3
$$v_i^{step} = a_{p,i} \rho_i u$$

921 where $a_{p,i}$ is the distance that edge i propagates with the addition of a single row of growth units,
922 ρ_i is the density of kink sites along the edge; and u is the kink rate, which represents the net
923 incorporation rate of growth units into the kink site (rate of attachment minus rate of detachment).
924 The propagation distance is determined from the size of the growth unit and crystallographic
925 considerations. At low levels of supersaturation such as often occur in cooling crystallization, the
926 kink density is taken to be constant (independent of supersaturation) and equal to its value for
927 single-height kinks at saturation conditions, given by the Boltzmann distribution²⁰⁸

928 Eq. 4
$$\rho_i = \frac{2}{2 + e^{\beta \phi_i^{kink}}}$$

929 where ϕ_i^{kink} is the “kink energy” of edge i , and β takes its usual meaning of $1/k_B T$. The kink energy
930 is half the strength of total interaction energy between neighboring growth units in the kink
931 direction – it is taken to be half the total bond energy between neighboring molecules in the kink
932 direction so that each molecule has the same “broken bond” energy – and is a key parameter in the
933 theory of crystal growth.

934 For vapor (sublimation) growth, ϕ_i^{kink} is the solid state bond energy (calculated using an atom-
935 atom force field such as GAFF) in the kink direction between neighboring growth units on the
936 edge. For solution growth, this kink energy must be “solvent-modified.” This is often
937 accomplished using the classical Dupre interface model in which the interfacial energy between
938 crystal and solvent at the kink site is given by the cohesive energy minus the adhesive energy.²⁰⁹
939 Solubility parameter methods are often used to capture the adhesive energy between the solvent

940 and crystal surface.²¹⁰⁻²¹² Different solvents modify the kink energy by different amounts, which
941 is how the “solvent effect” is captured in the model.

942 For centrosymmetric growth units, the kink rate is given by

943 Eq. 5
$$u = j^+ - j^-$$

944 where the attachment rate, j^+ , and detachment rate, j^- , are given by the following rate
945 expressions.^{157, 213}

946 Eq. 6
$$j^+ = k^+x = k^+x_{sat}S$$

947 Eq. 7
$$j^- = k^-$$

948 The attachment rate is first order with respect to the solute mole fraction in solution, x (which is
949 related to supersaturation, $S=x/x_{sat}$), and the detachment rate is zeroth order. The attachment rate
950 constant, k^+ , is normally assumed to be site-independent (i.e., depends only on solvent, but not the
951 specific surface site). This is assuming that the complexities of attachment that affect absolute
952 growth rates (Section 5.3) are the same for all surfaces and so cancel for morphologies. The
953 detachment rate constant, k^- , depends on the bonding structure of the site (in addition to the
954 solvent). It follows that¹⁵⁷

955 Eq. 8
$$k^- = k^+ \exp\left(-\frac{\Delta W}{k_B T}\right)$$

956 where ΔW is the energy penalty for detaching a growth unit from a kink site to the solution or
957 vapor (the total work of detachment from a kink site). For both Kossel growth units and
958 centrosymmetric molecules ΔW is the same for every site (although the kink, edge and terrace
959 energies are different for different edges²¹⁴). This explains why u is not edge-dependent for such
960 crystal systems, and leads to a linear relationship for u as a function of relative supersaturation ($S-$
961 1)²¹⁵

962 Eq. 9
$$u = k^+x_{sat}(S - 1)$$

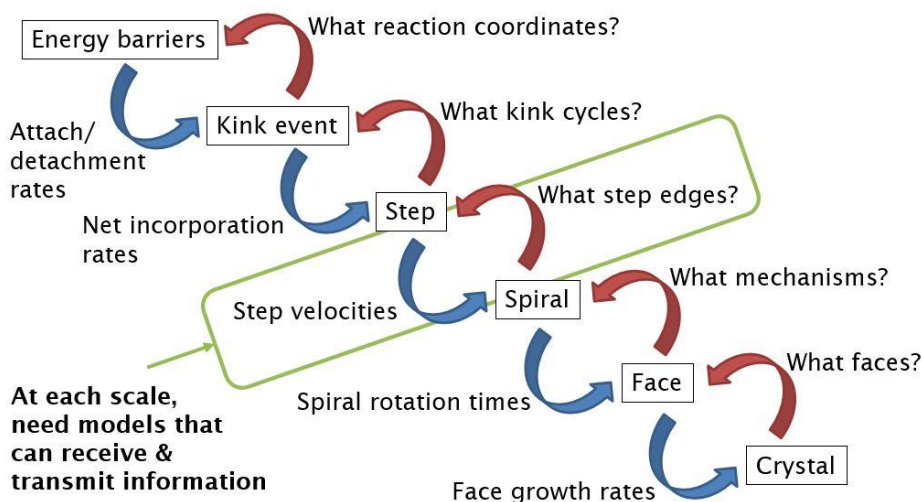
963 and also a linear relationship for step velocity

964 Eq. 10
$$v_i^{step} = a_{p,i} \rho_i k^+ x_{sat} (S - 1)$$

965 This linear step velocity relationship has been validated by experiment.²¹⁶⁻²¹⁸

966 This mechanistic modeling framework is completed once the step edges are identified on each
967 candidate crystal face. This is done using the concept of Periodic Bond Chains (PBCs).²¹⁹⁻²²¹
968 These correspond to the directions of the strongly bonded growth units throughout the 3D solid
969 structure. Faces that have two or more PBCs generally grow by either the spiral mechanism or the
970 2D nucleation mechanism where the edges of the spirals or 2D nuclei correspond to the PBC
971 directions.²⁰³ Such faces grow slowly relative to other faces (which have only one or zero PBCs²¹⁹⁻
972 ²²¹) and therefore dominate the surface structure of the crystal, as first stated by Gibbs in 1875²²²
973 (footnote on pp. 325-326).

974 The overall mechanistic approach is depicted schematically in Figure 10.

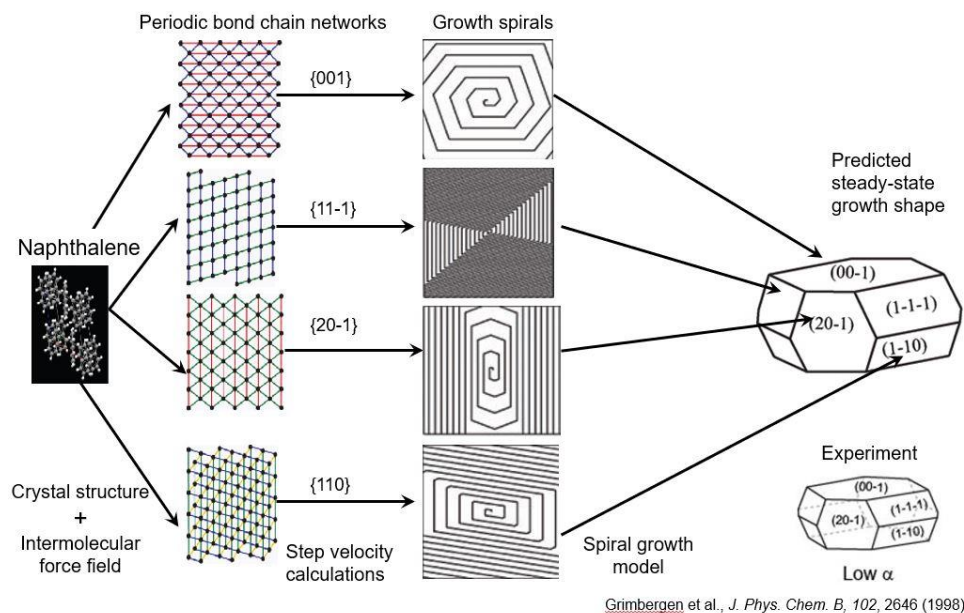


975
976 Figure 10. Schematic representation of the mechanistic growth model for calculating absolute
977 growth rates of crystal faces. The red arrows indicate the questions asked during assembly of the
978 growth model; the blue arrows indicate the type of calculations required to execute the growth
979 model.

980 If absolute growth rates are desired, then this mechanistic modeling approach requires that we
981 calculate values for x_{sat} and k^+ . Saturation composition can be calculated by the methods described
982 in Section 4 and the attachment rate constant as discussed in Section 5.3. However, morphology
983 prediction depends only on the relative growth rates of the crystal faces, R_f , (where the index f
984 refers to a specific crystal facet among a set on the crystal surface) where it is conventional to use
985 the slowest growing face (let's say face 1) that dominates the morphology as the reference, $R_f = G_f$
986 / G_1 . For centrosymmetric molecules the quantities x_{sat} and k^+ cancel from the relative growth
987 rates and thus do not need to be known. The steady-state growth shape of the crystal is determined
988 from the Frank-Chernov construction^{223, 224}

989 Eq. 11
$$\frac{R_1}{x_1} = \frac{R_2}{x_2} = \dots = \frac{R_f}{x_f} = 1$$

990 where x_f now represents the relative perpendicular distance of face f to an origin at the center of
991 the crystal (relative to the absolute perpendicular distance of face 1 to the same origin). A dynamic
992 evolution model can also be computed for faceted crystals starting from an arbitrary initial faceted
993 shape containing all the likely low index crystal faces (such as, e.g., a “disco ball”) which
994 ultimately leads to Eq. 11 at steady-state.^{225, 226} The overall mechanistic approach for predicting
995 morphology is depicted schematically in Figure 11 and reviewed by Li *et al.*²²⁷



996
 997 Figure 11. Schematic representation of the mechanistic growth model for predicting crystal
 998 morphology, applied to the growth of naphthalene from ethanol solution.^{203, 228} Adapted from
 999 Figure 5.1 in Li *et al.*,²²⁷ with permission from Elsevier.

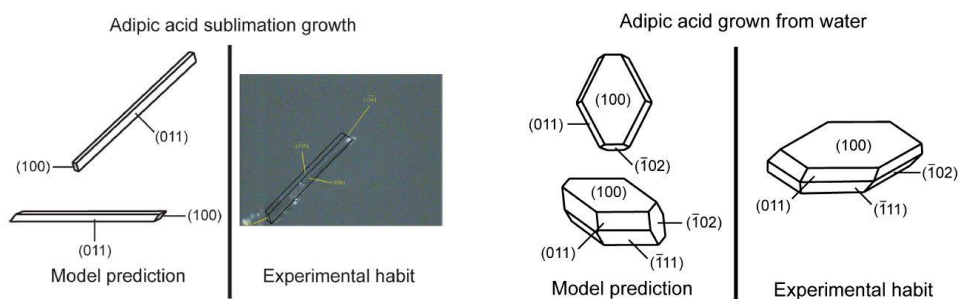
1000 It is best to start morphology studies by measuring and predicting the sublimation enthalpy and
 1001 the morphology for sublimation-grown crystals. This eliminates all solvent effects and allows for:

- 1002 1. a fidelity test of the chosen classical force field to represent the solid state. If there is a big
 1003 difference between the predicted and measured sublimation enthalpy, then it is highly likely
 1004 that the kink energy (and other bond energies) in the solid are in error. In such a case it is
 1005 unlikely that the morphology predictions will be good. As an example, GAFF predicts a
 1006 sublimation enthalpy for adipic acid of approx. -170 kJ mol^{-1} whereas the measured value is
 1007 approx. -130 kJ mol^{-1} . The resulting morphology predictions are poor.
- 1008 2. comparison of the morphologies calculated with different solvents to the “reference”
 1009 sublimation shape, and hence a qualitative assessment of the solvent effect, i.e., how

1010 different functional groups on the solvents interact with various functional groups exposed
1011 on the different crystal faces.

1012 5.1 Examples for centrosymmetric molecules

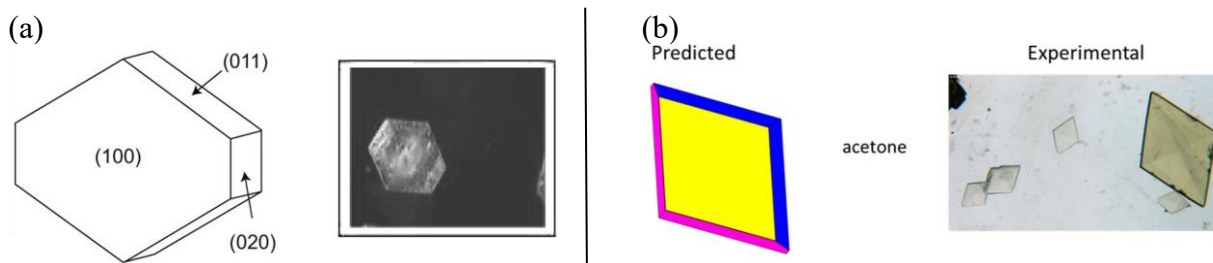
1013 Tilbury *et al.*²¹² report just such a study for four centrosymmetric crystal systems, namely,
1014 experimental and predicted morphologies for both sublimation-grown crystals and solution-grown
1015 crystals for biphenyl, adipic acid, pentaerythritol and naphthalene. In each case the solute
1016 molecule is unusually symmetric with an inversion center. The Gavezzotti Coulomb-London-
1017 Pauli (CLP)²²⁹ force field was used for the solid state energy calculations and the van Oss,
1018 Chaudhury and Good (vOCG)²³⁰ interface model to capture the solvent effect. In each case the
1019 predicted morphology is in good agreement with the experimental morphology, and in each case
1020 there is a significant shape change between sublimation-growth and solution-growth. For
1021 example, adipic acid grows as a rod from the vapor but as a hexagonal plate from aqueous solution
1022 (Figure 12).



1023
1024 Figure 12. Adipic acid crystals. (a) two views of the predicted morphology for sublimation growth
1025 (left) and the experimentally grown sublimation shape (right), (b) two views of the predicted
1026 morphology for growth from aqueous solution (left) and a rendering of the experimental shape
1027 from aqueous solution (right).²³¹ Adapted from Figure 6 and Figure 7 in Tilbury *et al.*,²¹²

1028 In Figure 12, it is highly noticeable that the (100) face is the smallest face on the sublimation
1029 shape but the largest on the solution-grown shape. Thus, the presence of water transforms the
1030 (100) from the fastest growing to the slowest growing face. This face exposes acid groups, and in
1031 particular O-H groups which form hydrogen bonds with water. Thus, the face becomes strongly
1032 solvated with water molecules which increases the solvation activation barrier for detachment of
1033 water molecules from kink sites (or equivalently, attachment of adipic acid growth units to kink
1034 sites) on the (100) surface (see section on absolute growth rates 5.3). The result is a significant
1035 reduction of the face growth rate relative to sublimation growth. Davey *et al.*²³¹ described the
1036 process being modeled as “adipic acid molecules approaching the (100) face do not experience the
1037 expected H-bonded interaction with molecules in the surface. One reason for this could be that
1038 the surface is covered by a layer of water molecules occupying the H-bonding sites such that
1039 growth of this surface is controlled by desorption of water molecules rather than attachment of
1040 adipic acid molecules.”

1041 Two other notable examples of morphology prediction for centrosymmetric growth units are
1042 shown in Figure 13, for succinic acid grown from aqueous solution, and for olanzapine grown
1043 from acetone. Olanzapine molecules are not centrosymmetric, but it has been established that the
1044 building block of most known forms of olanzapine (3.1.2) incorporate into the crystal lattice as
1045 centrosymmetric molecular dimers – thus the growth unit is centrosymmetric.^{78, 232-235}



1046

1047 Figure 13. (a) Succinic acid crystals (β form) grown from aqueous solution; left – predicted
1048 morphology, right – experimental shape, adapted from Figure 7 in Snyder *et al.*,²²⁶ with permission
1049 from Wiley, Copyright © 2007 American Institute of Chemical Engineers (AIChE), and (b)
1050 olanzapine crystals (Form I) grown from acetone; left - predicted morphology (yellow=(100),
1051 blue=(11-1), magenta=(011)), right – experimental shape, adapted from Figure 7 in Sun *et al.*²¹⁵

1052 5.2 Growth and morphology for non-centrosymmetric molecules and high supersaturations

1053 Crystal morphology prediction for simple centrosymmetric molecules is well in hand and quite
1054 reliable for a wide selection of crystal systems, especially at low levels of supersaturation.
1055 Extending the methods to high supersaturation (typical of antisolvent crystallization) and to non-
1056 centrosymmetric growth units (e.g., most API molecules and all ionic crystals) remain areas of
1057 current research. Good progress has been made on both these topics, but the theory is incomplete
1058 for crystals under high supersaturation with non-centrosymmetric growth units, e.g., antisolvent
1059 crystallization of API molecules.

1060 It is known from kinetic Monte Carlo (kMC) simulations of Kossel crystals that kink density
1061 increases rapidly as supersaturation increases, thus the Boltzmann treatment for this quantity
1062 becomes invalid.^{236, 237} To establish the correct supersaturation dependence of kink density, a
1063 master equation model is constructed that balances the rate of kink-forming events with the rates
1064 of kink-destroying events. In the context of a Kossel crystal model, the “gold standard” work on
1065 this topic was published twenty years ago by Cuppen *et al.*²³⁶ where they derived the non-
1066 equilibrium kink density model for kinks of all heights and showed that it agrees perfectly with
1067 kMC simulations over a wide range of supersaturations, and moreover agrees analytically with the
1068 Boltzmann equilibrium kink density expression (also derived in the paper) for kinks of all heights.
1069 They also showed that the step velocity model resulting from the new kink density model agrees

1070 perfectly with kMC simulations and is nonlinear over a wide range of supersaturations. Thus,
1071 crystal growth and morphology models for simple centrosymmetric molecules are well in hand
1072 even at high supersaturations, although we do not know of any direct tests with experimental
1073 morphologies for crystallizations at high supersaturation.

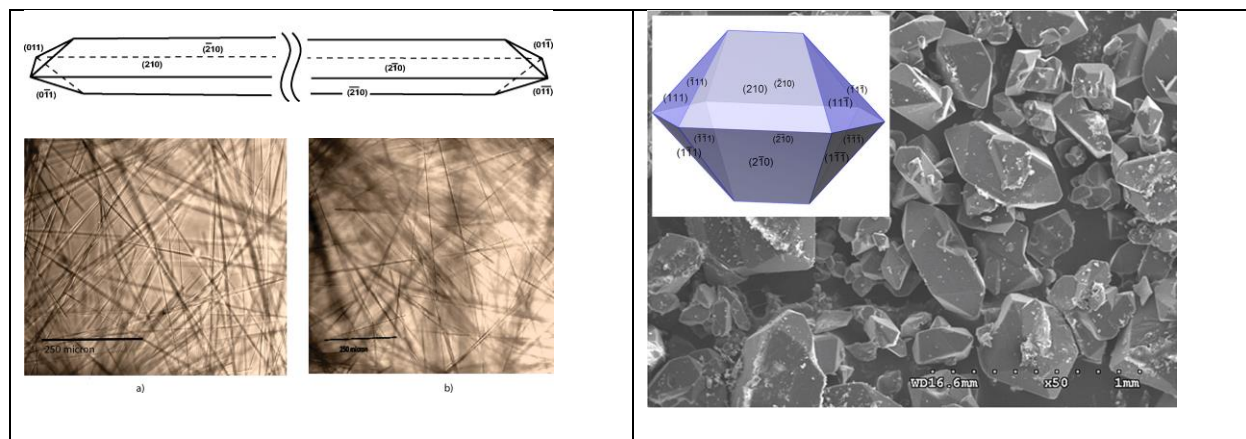
1074 This leaves growth and morphology modeling for non-centrosymmetric molecules (at both low
1075 and high supersaturation) as the key targets of current research. Kink rate models have been
1076 developed for two growth units²³⁸ and for any number of growth units.^{214, 239} One of the new
1077 phenomena that arises when there are multiple growth units in the unit cell is the pattern of growth
1078 units in the rows of steps. Take the case of two growth units, A and B, in the unit cell, where A
1079 and B may stand for two ions (e.g., Na⁺ and Cl⁻), or two non-centrosymmetric molecules which
1080 are arranged in different orientations in the unit cell (e.g., in a herringbone pattern). In some
1081 crystallographic directions the steps have a row of AAAAAA growth units followed by a row of
1082 BBBBBB, then repeating; while in other crystallographic directions the pattern is ABABAB along
1083 every row (other patterns also occur). There is no such behavior for Kossel or centrosymmetric
1084 growth units. Among the consequences of this are:

- 1085 1. steps in different crystallographic directions on the same face (i.e., different edges of the
1086 same spiral or 2D nucleus) grow by different kink rate mechanisms that lead to different step
1087 velocity models.
- 1088 2. steps that have different rows of growth units (e.g., AAAAAA followed by BBBBBB) have
1089 different edge energies for the different rows. As a result of anisotropic interactions, one of
1090 the rows can become unstable (thermodynamically unfavorable to elongate) and this
1091 behavior must be taken into account in the growth modeling.^{214, 239-241}

1092 These concepts have been generalized to any number of growth units in the unit cell, leading to
 1093 the concept of kink cycles (and corresponding kink rate formulae) that capture the various
 1094 patterns.^{214, 239} However, the link between step velocity and kink rate/kink cycle for crystals with
 1095 multiple growth units is still not settled and multiple relationships have been proposed.^{214, 239, 240}
 1096 When these methods are put in the hands of experts, good results for predicted crystal morphology
 1097 may be obtained for a wide range of complex crystals with non-centrosymmetric growth units.
 1098 Especially notable are the papers by Shim and Koo.²⁴²⁻²⁴⁴ Nevertheless, it remains a challenge to
 1099 convert physics-based expert knowledge to a general-purpose digital design aid for morphology
 1100 prediction that is robust enough to use in API workflows. The two most advanced digital aids at
 1101 the present time are ADDICT²⁴⁵ and CrystalGrower.²⁴⁶

1102 Two successful examples of morphology predictions for crystals with non-centrosymmetric
 1103 growth units are shown in Figure 14.

1104



1105 Figure 14. Left: lovastatin crystals grown from alcohol solutions; top – predicted morphology,
 1106 bottom – experimental shape grown from isopropanol (left) and methanol (right), adapted from
 1107 Figures 26 and 27 in Kuvadia *et al.*²³⁹ Right: the explosive RDX grown from acetone with
 1108 predicted morphology inset, adapted from Figures 6 and 8 in Shim *et al.*²⁴²

1109 Improved methods for estimating solvent effects may lead to better morphology predictions. A
1110 new approach that uses a “thermodynamic path” to obtain an expression for the solvent-modified
1111 bond energy between two neighboring growth units C & D on a crystal step edge is given by the
1112 equation:

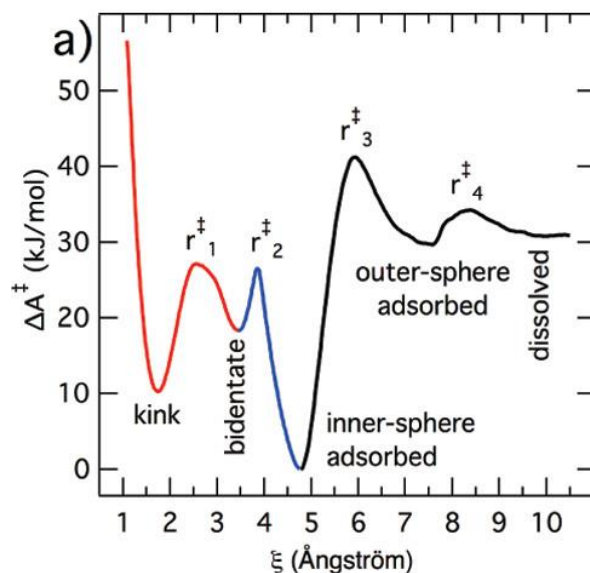
$$1113 \quad \Phi_{CD}^{solv.modif.}(liq) = \Phi_{CD}^{vapor}(solid\ state) + \Delta G_{monomer}^{solv} - \Delta G_{BP}^{solv} / 2$$

1114 where $\Phi_{CD}^{solv.modif.}(liq)$ is the solvent-modified bond energy between growth units C & D in
1115 presence of a solvent, $\Phi_{CD}^{vapor}(solid\ state)$ is the bond energy between growth units C & D in a
1116 vapor environment (i.e., without solvent present, and is calculated directly from the atom-atom
1117 force field in the solid state), $\Delta G_{monomer}^{solv}$ is the solvation free energy for the monomer growth unit
1118 when immersed in the solvent, and ΔG_{BP}^{solv} is the solvation free energy for the bonded pair of
1119 growth units C & D when immersed in the solvent. These solvation free energies may be estimated
1120 using molecular simulation or COSMO-based methods.

1121 5.3 Absolute growth rates

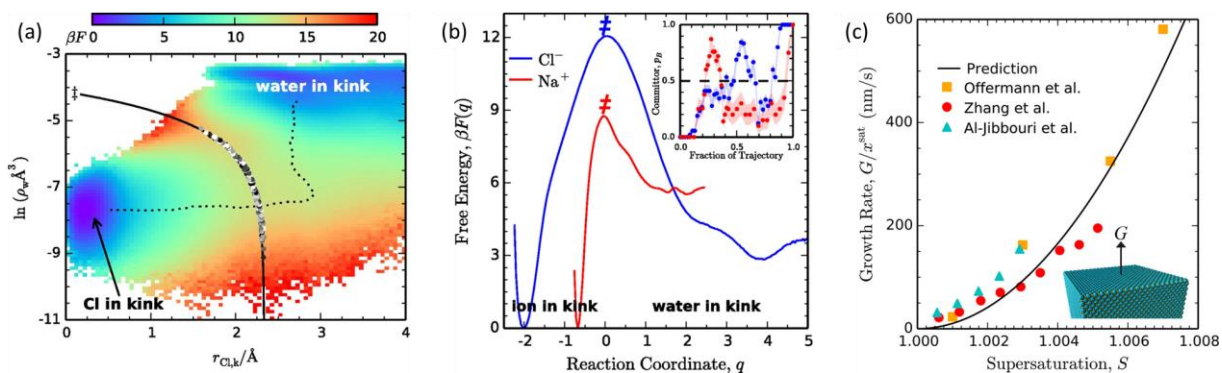
1122 We now return to the matter of predicting absolute growth rates of crystal faces. The key
1123 quantity needed is k^+ , the attachment rate constant for growth units into kink sites. This is
1124 calculated using molecular simulation to generate the free energy landscape at a given temperature
1125 and pressure for the undocked and docked growth unit in the kink site (i.e., kink site occupied by
1126 solvent and solute, respectively). The transition path through this surface (locus of minimum free
1127 energy) is determined and the activation energy barrier is calculated. Transition state theory is
1128 then used to obtain a value for k^+ . A major success using this approach was reported²⁴⁷ for barite
1129 (barium sulfate) grown from aqueous solution. The calculated free energy profile as a function of
1130 reaction coordinate is shown in Figure 15, where there are four separate transition states (peaks in
1131 the graph) between five energetically distinct states (valleys). Repeating the calculations at various

1132 temperatures allows for the calculation of the rate-limiting attachment and detachment rate
 1133 constants as a function of temperature, which yield a straight line on an Arrhenius plot (see Fig. 4
 1134 in ref²⁴⁷). The resulting activation energies for attachment and detachment are in good agreement
 1135 with experimental estimates of the activation energies for step growth and dissolution,
 1136 respectively.



1137
 1138 Figure 15. Calculated free energy profile for barium ions as a function of reaction coordinate for
 1139 barite grown from aqueous solution, reproduced from Figure 2 in Stack *et al.*²⁴⁷

1140 Joswiak *et al.*¹⁶⁶ performed a similar study for the simpler system of sodium chloride
 1141 crystallization from aqueous solution (Figure 16). The simplicity of this system permitted a
 1142 prediction of absolute crystal growth rate as a function of supersaturation (Figure 16c).²⁴⁸ All the
 1143 major crystal faces of sodium chloride ((001), (010), (001)) are identical, as are the steps on each
 1144 face, thus limiting the number of calculations required to perform the growth rate calculation.
 1145 Once a value for k^+ was calculated it was inserted into their equation for calculating the crystal
 1146 face growth rates to obtain Figure 16c.²⁴⁸ The resulting predictions are in good agreement with
 1147 experiment.



1148
 1149 Figure 16. (a) Free energy landscape for chloride kink site on a sodium chloride step. The CVs
 1150 are the distance of the chloride ion from the kink site and the local water density in the kink site.
 1151 The minimum free energy path (dotted) indicates that the chloride attachment process is two-step;
 1152 first water molecules leave the kink site (the site desolvates) then the chloride ion docks in the
 1153 cavity created. (b) Free energy profile as a function of reaction coordinate. Reproduced from
 1154 Figures 3 and 4 in Joswiak *et al.*¹⁶⁶ (c) Comparison between predicted NaCl crystal growth rate
 1155 (solid black curve) and experimental measurements (colored symbols), reproduced from Figure 4
 1156 in Joswiak *et al.*²⁴⁸

1157 Recent molecular simulation studies on solvation effects and activation barriers in crystal growth
 1158 from solution include glutamic acid crystallization from aqueous solution, and concluded that
 1159 solvent fluctuations in the solvation shell are among the factors determining the activation barrier
 1160 for crystal growth rates.²⁴⁹

1161 One useful byproduct is that these state-of-the-art modeling techniques enable the prediction of
 1162 absolute face growth rates from the predicted relative growth rates plus one absolute growth rate
 1163 (for the reference face) from either experiment or molecular simulation. This enables a big
 1164 reduction in experimental effort to obtain such growth rates. The resulting growth rates can then
 1165 be used, for example, in multidimensional population balance models, as noted by Kuvadia and
 1166 Doherty.²⁵⁰

1167 5.4 Open problems for morphology and growth rate

1168 Despite these successes, modeling methods are not quite ready for application to the everyday
1169 workflow in API research and development (but they are much closer than they were ten years
1170 ago). Open problems include:

- 1171 • developing non-equilibrium kink density models (at high supersaturation) for crystals with
1172 many (> 2) non-centrosymmetric growth units in the unit cell.
- 1173 • developing step velocity models for such systems.
- 1174 • improving methods for estimating solvent-modified bond energies, particularly for solvent
1175 mixtures, and especially mixtures of solvent and antisolvent.
- 1176 • prediction methods for attachment rate constants for API-like solutes with multiple
1177 “floppy” functional groups. It has been shown that conformational equilibria as well as
1178 conformational transition mechanisms can become the kinetic bottleneck in crystal
1179 growth,²⁵¹ and that the presence of slow conformational equilibria can affect overall
1180 crystal growth rates at process scale.¹⁹⁰ How to identify molecular systems that are subject
1181 to these conformational limitations and how to generalize growth rate estimates in such
1182 cases remains an open challenge.

1183 6 Nucleation

1184 Nucleation is the initial irreversible step in the formation of a new crystal, so it has an unremitting
1185 influence on later stages of crystallization. Nucleation is a notoriously rare event. The fastest
1186 measurable rates of solute precipitate nucleation, ca. $10^{10} \text{ cm}^{-3} \text{ s}^{-1}$, are still excruciatingly slow
1187 compared to accessible simulation time scales. To see even one nucleation event at realistic
1188 conditions in a typical simulation box of size ca. 100 nm^3 , one would need to simulate a staggering
1189 10^9 s of dynamics. Real simulations are (at present) limited to the microsecond time scale, so

1190 direct simulations cannot access realistic nucleation rates. But a systematic use of direct
1191 simulations can reveal important trends in the nucleation rate as a function of solute
1192 supersaturation,^{161, 252, 253} solvent composition,²⁵⁴⁻²⁵⁶ surfactants/additives,²⁵⁶⁻²⁵⁹ and
1193 characteristics of heterogeneous nucleation sites and surfaces.²⁶⁰

1194 The key reason for concern about nucleation is in polymorph discovery. Late appearing
1195 polymorphs are clearly those whose nucleation has usually been out-competed by other
1196 polymorphs. The cases of disappearing polymorphs are likely to arise when the more stable form
1197 has a very slow nucleation rate but fast growth rate (Table 1 in Section 8.3). In this context,
1198 atomistic simulations, while hardly able to provide estimates of absolute nucleation rates, could
1199 help in ranking the relative nucleation kinetics of different forms, at least in the absence of
1200 impurities, and thus provide approaches beyond thermodynamics to refine CSP-generated crystal
1201 energy landscapes and identify long-lived putative polymorphs. An ability to model nucleation
1202 could allow the assessment that there is little risk of a computationally more stable crystal structure,
1203 that has not been observed in extensive screening, disrupting the manufacture of a metastable but
1204 kinetically favored form.

1205 Rare events methods^{101, 261, 262} made it possible to compute single-component nucleation rates at
1206 realistic conditions, even for extremely slow nucleation processes.²⁶³⁻²⁶⁶ However, formidable
1207 challenges remain, especially for solute precipitate nucleation²⁶⁷ and heterogeneous nucleation.²⁶⁸
1208 The challenges originate from multiple factors.

- 1209 • Unlike predictions of structure and stability which only require bulk solid properties,
1210 understanding nucleation requires a quantitative understanding of the solvent properties,^{254,}
1211 ^{256, 269} interfaces,^{270, 271} and perhaps also interactions with other surfaces, impurities,
1212 surfactants, etc.^{272, 273}

- 1213 • Nucleation rates are highly sensitive to supersaturation. Except in highly coincidental
1214 cases where the force field exactly predicts the solubility limit, a simulation is not being
1215 performed at the experimental supersaturation concentration. For quantitative comparisons
1216 and predictions, experimental and simulated supersaturations should match. Therefore,
1217 precise solubility and driving force calculations are important (and non-trivial) first
1218 steps.^{154, 274, 275}
- 1219 • Nucleation is an intrinsically irreversible non-equilibrium process, and (for solute
1220 precipitate nucleation) the solid invariably has a different composition from the starting
1221 solution.^{267, 276} The transformation from a solution with one composition to a solid with
1222 another poses tremendous difficulties for simulations.
- 1223 • Most theoretical analyses and simulations focus on well-defined but improbable
1224 homogeneous primary nucleation processes.²⁷⁷ However, most nucleation processes occur
1225 by heterogeneous nucleation^{269, 272, 278, 279} or secondary nucleation.^{280, 281} This daunting
1226 challenge motivates much of the discussion below.

1227 Theory and molecular simulations have overcome numerous hurdles, but accurate predictions
1228 remain elusive for all but the simplest of systems. The following sections highlight key
1229 developments in primary homogeneous nucleation, primary heterogeneous nucleation, and
1230 secondary nucleation models as related to pharmaceutical crystallization and polymorph screening.

1231 6.1 Homogeneous nucleation

1232 Homogeneous nucleation, in the context of API crystallization, is the spontaneous emergence of
1233 a stable crystallite or amorphous precursor from the pure metastable solution, with no assistance
1234 from templating surfaces or particulates. In experiments, homogeneous nucleation tends to be the
1235 most difficult pathway to observe, because heterogenous (Section 6.3) or secondary nucleation

1236 (Section 6.2) pathways usually intercede. For simulations, understanding homogeneous
1237 nucleation is often the first goal because it occurs in a well-defined pristine solution. Nevertheless,
1238 even homogeneous nucleation poses serious difficulties. In particular, nucleation studies require
1239 efficient advanced sampling schemes to overcome the rare events problem,¹⁶¹ precise solubility
1240 calculations to match simulated and experimental supersaturations,^{154, 162, 274, 282-284} accurate order
1241 parameters for cluster size calculations,^{254, 255} surface free energy-corrected nucleation rate
1242 estimates,^{285, 286} and methods to predict the impact of surfactant adsorption.^{257, 258, 287} There is a
1243 significant problem in controlling the supersaturation during a simulation of solute precipitate
1244 nucleation, because of the difficulty of keeping the chemical potential difference constant in a
1245 small box with constant number of molecules.²⁸⁸ Putting a small nucleus to seed the simulation
1246 can estimate rates without artifacts from supersaturation depletion, but this requires *a priori*
1247 assumptions about nucleus structure.^{274, 275, 289, 290} Osmotic ensemble methods can control
1248 supersaturation with no assumptions about nucleus structure,²⁹¹ which may prove particularly
1249 useful in studies of two-step homogeneous nucleation.^{271, 292, 293}

1250 6.2 Secondary nucleation

1251 Secondary nucleation, in multiple ways, is the opposite of homogeneous nucleation. While
1252 homogeneous nucleation involves molecular-scale spontaneous assembly from solution with no
1253 crystals, secondary nucleation occurs by mechanical breakage of existing macroscopic crystals
1254 into pre-formed viable crystallites.^{267, 294, 295} Homogeneous nucleation rarely (if ever) occurs in an
1255 industrial crystallizer, while secondary nucleation is thought to be the dominant mechanism.^{280, 296-}
1256 ²⁹⁸ Quantitative models have been developed for secondary nucleation, assuming that crystals can
1257 fracture on collision, accounting for crystal-crystal collisions, impeller-crystal collisions, and other
1258 mechanisms.^{267, 294, 295, 299} The solute morphology and mechanical properties³⁰⁰ are important in

1259 determining the ease of fracture, but this is not explicit in current models, in which fracture enters
1260 through an experimental parameter. Secondary nucleation models are extremely useful for
1261 industrial crystallization,³⁰¹ but not for polymorph screening, where the main targets are low
1262 energy solid forms that are predicted to be kinetically stable, but are yet-to-be experimentally realized
1263 (Section 3.3).

1264 6.3 Heterogeneous nucleation

1265 Heterogeneous nucleation can occur where the solution contacts a bubble, an oil droplet, or an
1266 atomically smooth solid surface.^{267, 273, 302} Like homogeneous nucleation, these special cases of
1267 heterogeneous nucleation are amenable to theoretical modeling and molecular simulations. We
1268 have gained tremendous insight from these studies, e.g. how solid-crystal, solid-solution, and
1269 crystal-solution interfaces modulate nucleation barriers^{272, 273, 279} and how barriers for
1270 heterogeneous nucleation relate to barriers for homogeneous nucleation.^{279, 303} Theory and
1271 simulation have also explained how barriers are influenced by additional factors like line
1272 tension,^{304, 305} lattice mismatch/elasticity,^{306, 307} curvature,^{308, 309} hydrophobicity,^{310, 311}
1273 electrostatics,^{312, 313} and adsorbates.^{309, 314-316}

1274 6.3.1 Heterogeneous nucleation for polymorph discovery

1275 In a few impressive cases, instead of using CSP output to select an isomorphous crystal (as in
1276 Section 3.3), special epitaxially matching surfaces have been identified and prepared to promote
1277 heterogeneous nucleation of a desired form.^{151, 152, 317-320} Since this is a surface phenomenon, the
1278 use of natural ledges³²¹ or even engineered surfaces³²² can be worth trying.³²³ Both the shape and
1279 the nature of the exposed functional groups appear to be important in designing surfaces for
1280 polymorph discovery or control.^{324, 325} However, there are many situations, such as the discovery
1281 of the γ form of succinic acid in a failed purification by co-crystallization experiment,⁸² or the

1282 stabilization of a form of progesterone by impurities,³²⁶ where it has been impossible to identify
1283 the specific impurities or templates involved. Because identifying and preparing ordered structure-
1284 selective templates is not trivial,³¹⁹ template discovery and fabrication will probably be pursued
1285 only for otherwise elusive targets of the highest priority.

1286 6.3.2 Heterogeneous nucleation on disordered nucleants

1287 Heterogeneous nucleation is not limited to perfect surfaces. It can also occur in pores, pits, and
1288 other defect sites.³²⁷ Theory and simulation have also provided important and generalizable
1289 insights about heterogeneous nucleation in these environments, e.g. the effects of pore size³²⁸ and
1290 wedge angles³²⁵ on nucleation rates. Again, the pore environments and geometries in these studies
1291 are somewhat idealized. The story of heterogeneous nucleation will be far more complicated for
1292 real scratches, cracks, fissures, and defects.^{327, 329}

1293 In addition, experiments^{49, 265, 330} and calculations^{48, 331, 332} show that nanopore confinement can
1294 reverse the relative stabilities of polymorphs and hydrates because the small size of the crystallites
1295 makes the surface energy important. Because different pore sizes and geometries can favor
1296 different polymorphs, porous disordered media are extremely useful for polymorph screening.
1297 “Naomi’s nucleants”³³³ are porous bioglass materials that promote nucleation of protein crystals.
1298 Polymers are also used, with porous polymer films being successful in numerous polymorph
1299 selection efforts,³³⁴⁻³³⁸ and polymer dispersions producing olanzapine form IV.⁷⁹

1300 To understand the advantages of disordered media for promoting nucleation, one must remember
1301 that nucleation is irreversible once the particle is large enough. In a small sample, the first event
1302 spurs the formation of a growing crystal that then consumes the supersaturation and suppresses
1303 subsequent nucleation events. Accordingly, the induction time and the resulting polymorph are
1304 the result of extreme value statistics. The most potent nucleation sites among thousands in the

1305 disordered media will determine the outcome. This is true for each droplet in a nucleation assay,
1306 but the most potent nucleants differ from droplet to droplet³³⁹ which make these assays useful in
1307 solid form screening. Once the first crystal of a new polymorph has been found, then it can be used
1308 to seed more conventional crystallization experiments, provided the growth and transformation
1309 kinetics are favorable.

1310 6.4 Open problems in nucleation

1311 There is some debate about the extent to which nucleation is a problem for pharmaceutical
1312 manufacturing. In most industrial crystallizers, nucleation can be practically avoided by seeding,
1313 and the collision-induced mechanism of secondary nucleation mainly eliminates the need for
1314 molecular level understanding of primary nucleation processes. However, at the polymorph
1315 screening and solid form discovery phase, nucleation is critical. In academic studies aimed at
1316 fundamental molecular scale understanding of nucleation, the diversity of heterogeneous
1317 nucleation sites and mechanisms is a frustrating nuisance. In contrast, polymorph screening and
1318 solid form discovery efforts could potentially exploit the number of sites that can promote
1319 heterogeneous nucleation³⁴⁰ and their promotion of different forms to different degrees. Thus,
1320 there is a need for empirical statistical analyses that can help design better polymorph screening
1321 assays, along with research aimed at understanding molecular level nucleation mechanisms.

1322 A key issue will be the extent to which the simulation methods and analysis tools for simple
1323 systems translate to API molecules. The dominant mechanisms for conformational transformation
1324 can differ significantly between the solution phase and as the molecule becomes incorporated into
1325 the crystal, even for molecules as small as ibuprofen.²⁵¹ An early systematic study aimed at
1326 quantifying the impact of molecular flexibility on the nucleation kinetics of four para substituted
1327 benzoic acids suggests that conformational change is only one of the many activated processes that

1328 contribute to and control the kinetics of crystallization. Its relative weight in the whole process
1329 will change depending on the system.³⁴¹

1330 7 Process Design

1331 The digital design of crystallization processes requires translating the insight obtained by
1332 studying crystallization at the atomistic scale into process-level information. This is achieved by
1333 developing population and material balance models of crystallizers. Morphology, growth rates,
1334 solubility and often nucleation rates are used in population balance models which predict the
1335 evolution of the particle size distribution (PSD) and, in the case of multidimensional population
1336 balance models, the evolution of the crystal shape distributions of the crystalline product. These
1337 outputs are essential for the design of crystallization processes. For example, the predicted PSD
1338 may be compared with the desired target PSD to determine whether wet milling, dry milling, or
1339 wet granulation operations should be included in the process. We construct a mixed suspension
1340 mixed product removal (MSMPR) crystallizer model, applicable for batch, semi- or fed-batch and
1341 continuous processes. This model assumes that the crystallizer provides perfect mixing with no
1342 gradients in solute concentration, crystalline suspension, temperature or anti-solvent. The
1343 population balance for an MSMPR assumes the crystallizer has an inlet stream(s) that supplies a
1344 fresh solution, a stirred tank containing a suspension of crystals in solution, and an exit stream that
1345 carries the suspension out of the vessel. In its most general form, the population balance model for
1346 such a system is given by:

1347 Eq. 12
$$\frac{\partial(nV)}{\partial t} + \frac{\partial}{\partial \mathbf{L}}(\mathbf{G}nV) = V(B - D) - qn + q_{in}n_{in}$$

1348 where $n(\mathbf{L},t)$, is the population density of particles per unit volume of suspension, \mathbf{L} is a vector of
1349 characteristic crystal dimensions in the different crystallographic directions derived from the
1350 crystallographic (hkl) values of the morphologically-relevant faces, t is time, V is the suspension

1351 volume, q is the volumetric flowrate of the inlet (subscript *in*) or outlet (no subscript) streams, \mathbf{G}
 1352 $= d\mathbf{L}/dt$ is the vector of absolute growth rates for each face (from Section 5), and B and D are the
 1353 birth and death rates of crystals per unit volume of suspension, e.g. by breakage, aggregation or
 1354 agglomeration. In this formulation, the crystallizer volume and the inlet and outlet volumetric
 1355 flow rates are allowed to vary with time to accommodate such processes as fed batch, co-addition,
 1356 antisolvent or other time variant crystallization processes. Nucleation kinetics, including
 1357 secondary nucleation, are expressed *via* a nucleation rate \mathbf{J} which enters the population balance
 1358 model *via* the boundary condition at $\mathbf{L} = 0$ discussed below (see Eq. 16).

1359 The solute concentration, C (mass/volume), is determined from a mass balance:

1360 Eq. 13
$$\frac{d}{dt}(C(V - V_S) - V_S \rho_s) = q_{in}C_{in} - q\left(1 - \frac{V_S}{V}\right)C - q\frac{V_S}{V}\rho_s$$

1361 where ρ_s is the density of the solid, V_S is the volume of solids in the crystallizer, and V_S/V (or ε)
 1362 is the solids volume fraction in the crystallizer:

1363 Eq. 14
$$\frac{V_S}{V} = \int d\mathbf{L} n(\mathbf{L}, t) v_{crystal}(\mathbf{L})$$

1364 where $v_{crystal}(\mathbf{L})$ is the volume of a single crystal with dimensions \mathbf{L} .

1365 Often the growth rate used in the population balance (Eq. 12) is modeled with a power law in
 1366 the degree of saturation³⁴²⁻³⁴⁴ or the relative supersaturation:³⁴⁵⁻³⁴⁷

1367 Eq. 15
$$G_j = k_g^j \exp\left(\frac{-E_{A,g}^j}{RT}\right) (S - 1)^{g_j}$$

1368 where the relative supersaturation is defined as $S = C/C_{sat}$, and j refers to the specific crystal face.

1369 To fully characterize the operation of an MSMPR crystallizer the system composed of the
 1370 coupled material and population balances (Eq. 12 to Eq. 15) need to be solved, together with initial
 1371 conditions and boundary conditions. The initial conditions are:

1372 Eq. 16
$$n(\mathbf{L}, t = 0) = n_{seed}$$

1373 Eq. 17
$$C(t = 0) = C_0$$

1374 where n_{seed} is the PSD of seed crystals inside the crystallizer at $t=0$, and C_0 is the initial
1375 concentration of clear liquid inside the crystallizer at $t = 0$.

1376 A boundary condition is also required to account for nucleation of particles of microscopic size.
1377 For the mono-dimensional population balance case, when particles can be characterized by a single
1378 length, and vector \mathbf{L} reduces to a scalar, L , the nucleation boundary condition at $L=0^+$ is:³⁴⁸

1379 Eq. 18
$$n(0^+, t) = \frac{J}{G}$$

1380 where 0^+ indicates that nuclei have a finite albeit extremely small size. This size is irrelevant to
1381 the process-design models, and instead of defining these microscopic sizes, one normally simply
1382 approximates them to zero, an approximation that has no significant effect on the shape of the
1383 distribution near the origin.

1384 A proper boundary condition in the multidimensional case requires delta functions or
1385 regularization approximations. It is worth noting here that this boundary condition holds
1386 irrespective of the dominant nucleation mechanism, and either primary or secondary nucleation
1387 can be introduced into crystallizer models following this approach. However, for primary
1388 nucleation, the boundary condition must be modified to account for the fact that \mathbf{J} represents the
1389 number of nuclei born per unit volume of clear liquid per unit time, rather than per unit volume of
1390 suspension per unit time.³⁴⁸ Most continuous crystallization processes rely on secondary
1391 nucleation to generate new particles, e.g., the birth of new particles by attrition from existing
1392 crystals due to collisions with walls, impellers, or other crystals.^{34, 349-352} For these cases, the *ab*
1393 *initio* conceptual design of a continuous crystallization process or a seeded batch crystallization
1394 process is not possible since secondary nucleation models cannot be predicted *ab initio*. There are
1395 reliable empirical models for secondary nucleation with just a few material- and crystallizer-

1396 specific parameters. The secondary nucleation rate also depends on the stirring rate and/or power
1397 input, the supersaturation, and the solid volume fraction in the crystallizer. For example, a
1398 commonly used model for the secondary nucleation rate³⁰¹ is

1399 Eq. 19
$$J = k_N \Omega^2 (V_S/V)(S - 1)^i$$

1400 where Ω is the stirrer speed. i and k_N are empirical reactor- and substance-dependent parameters
1401 that must be determined through prior experimentation. These two parameters cannot yet be
1402 predicted from first principles, but identifying the factors that influence secondary nucleation rates
1403 may open doors to fruitful data driven models in the future.^{280, 295, 353}

1404 Some continuous crystallization processes use continuous seeding or seed generation,³⁵⁴ where
1405 the size of the seeds fed to the cascade of crystallizers defines the final shape and crystal size
1406 distribution. These processes can also be modeled using the population balance framework.

1407 Eq. 12 can also be simplified to obtain a model for seeded batch crystallization processes. For
1408 a seeded batch process that operates under conditions where primary and secondary nucleation are
1409 avoided, particle size and shape may be predicted by:

1410 Eq. 20
$$\frac{\partial(nV)}{\partial t} + \frac{\partial}{\partial L}(GnV) = 0$$

1411 together with the solute balance and the initial conditions in Eq. 16 and Eq. 17.

1412 The seeded, batch crystallizer case is relevant for the majority of drug substance crystallization
1413 processes, and for this class, it is possible to consider the *ab initio* conceptual design of the batch
1414 process, provided that solubility can be predicted. This problem was first considered by Mullin
1415 and Nyvlt³⁵⁵ and later by Ward et al.^{356, 357}

1416 7.1 Open Problems in Conceptual Process Design

1417 A major bottleneck in *ab initio* crystallizer design is the current inability to predict secondary
1418 nucleation from first principles. Until this problem is solved there can be no further progress in *ab*

1419 *initio* crystallizer design. Related difficulties include the need for first principles models for
1420 agglomeration and attrition.

1421 While there has been some success at predicting homogeneous nucleation rates and critical
1422 nucleus size using a modified classical nucleation approach (employing the Tolman correction to
1423 account for the size dependence of surface energy at the nanometer size scale) this has no impact
1424 on crystallizer design since homogeneous nucleation is normally irrelevant in industrial practice.
1425 This is by design, not by accident. Induction times for homogeneous nucleation are usually so
1426 long that they are avoided by seeding crystallizers, whereupon secondary nucleation is the
1427 dominant mechanism for producing nuclei. Seeding is desired for control of PSD and crystal form.

1428 Multidimensional population balances have the potential to predict not only the particle size
1429 distribution but also the morphology/shape (habit) distribution. However, they are not used widely
1430 because a separate growth rate model is needed for each individual facet on the crystal surface
1431 (including facets that may ultimately grow off the crystal surface at long time and thus never appear
1432 at steady-state). Measured growth rates of individual facets of the same crystal are available for
1433 only a handful of systems, and this is unlikely to change in the foreseeable future due to the
1434 difficulty of making such measurements. As noted earlier in section 5, one way to overcome these
1435 difficulties is to reformulate the multidimensional PBE in terms of a single absolute growth rate
1436 for one of the crystal faces along with relative growth rates for all of the others [ref 249 in current
1437 version, Kuvadia and Doherty]. *Ab initio* growth models may then be used to estimate all the
1438 required growth terms in the PBE. Such an approach has never been tested so we can only
1439 speculate about its fidelity and utility in the process design workflow. The approach is ripe for
1440 further research.

1441 As the conceptual design gets closer to industrial deployment the influence of impurities in the
1442 solution cannot be ignored. These are usually present as a result of unwanted byproducts formed
1443 during the reaction steps that lead to the API. Some impurities are not recognized by the crystal
1444 surfaces (i.e., they do not adsorb) and are inert to the growth mechanism(s). Impurities that do
1445 adsorb on crystal surfaces are capable of having a significant effect on growth even at the ppm
1446 level (the classic paper by Botsaris et al.³⁵⁸ provides impressive experimental data for the drastic
1447 effect of lead chloride on the growth rate of potassium chloride crystals grown from aqueous
1448 solution). Impurities normally reduce growth rates of selected planes thereby modifying the
1449 crystal morphology in addition to slowing down the growth process, although instances are known
1450 of impurities that accelerate growth.³⁵⁹⁻³⁶¹ There is now a large literature on the effect of impurities
1451 and additives on crystal growth; selected papers include those reporting experimental methods and
1452 data^{218, 231, 362-364} and molecular models.^{32, 365-368}

1453 A related issue is impurity sequestration in the crystals, which is also undesired. For
1454 pharmaceuticals, where the impurities may be structurally related to the API, but with very
1455 different biological effects, it is imperative to avoid their incorporation.³⁶⁹⁻³⁷¹ The usual approach
1456 to solving problems caused by impurities is to stage the crystallization by first crystallizing from
1457 the crude solution followed by recrystallization from a pure solvent. However, this is not practical
1458 for every step along the process route (i.e., for each solid-form intermediate) and there is a push to
1459 better understand the effects of impurities with a view to having better control in a single operation.

1460 Higher fidelity crystallizer models that take into account imperfect mixing and other transport
1461 effects *via* the use of computational fluid dynamics are available.³⁷²⁻³⁷⁵ However, they are subject
1462 to the same limitations mentioned above with respect to secondary nucleation and impurity effects.

1463 8 Discussion

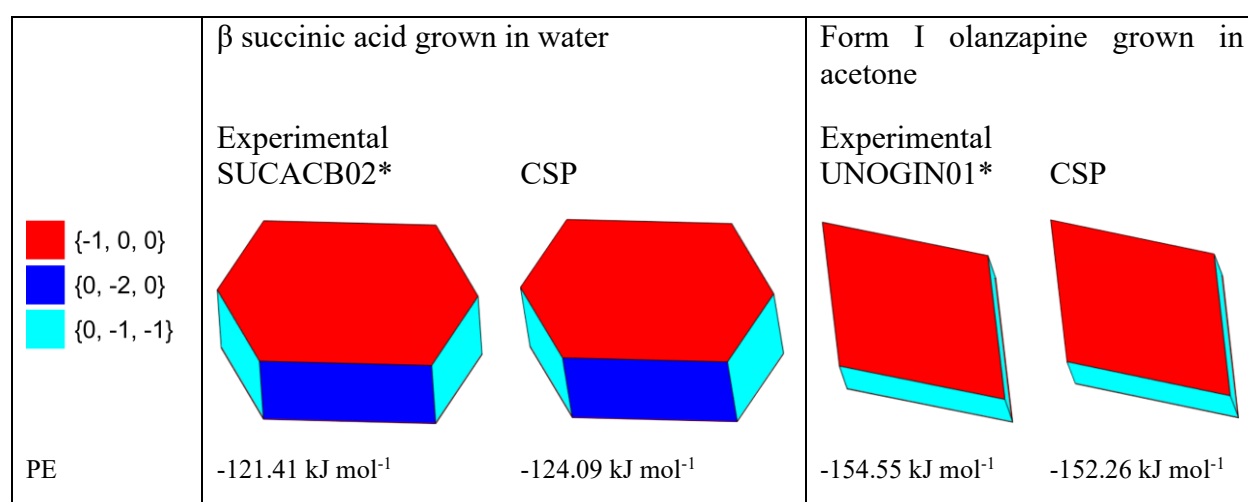
1464 We have shown how the components of a digital design workflow, going from the molecular
1465 structure through to the process design (Figure 2), are in an active state of development and
1466 producing worthwhile results. The time will come when this workflow can be integrated into drug
1467 discovery, allowing the discovery team to consider not only the medicinal chemistry in selecting
1468 candidates to carry forward into *in vivo* studies, but also product and process design and expected
1469 bioavailability of the candidate. **This integration will be a game changer.**

1470 This study has illustrated that it is not fully possible for quantitatively reliable simulations to be
1471 performed prior to the synthesis of the molecule. The main barrier is the inability to use the same
1472 force field to predict the crystal structures and subsequently all the relevant properties and get good
1473 enough results. Useful results can be obtained for some properties. Figure 17 shows that the
1474 predicted morphologies of succinic acid and olanzapine show little qualitative difference whether
1475 the CSP-generated structure or an experimental crystal structure is used, thus demonstrating that
1476 morphology can be predicted from the chemical structure. Zhang *et al* demonstrated similar results
1477 for ibuprofen grown from several solvents.³⁷⁶ However, the absolute growth rates do differ, and
1478 morphologies can be very sensitive to force field. Similarly, useful guidance on relative stabilities
1479 and solubilities for different polymorphs can be achieved, whereas the absolute values are not
1480 reliable. This is still extremely valuable information as knowledge of the potential form landscape
1481 provides an understanding of the complexity expected in the development of the solid state and
1482 oral dosage form. Likewise, a rank order of solubility in different solvents is also extremely useful
1483 in guiding solubility screens and solvent selection. From a product development perspective,
1484 knowing the expected morphology of a new API provides insight in the complexity expected for
1485 drug product development and can help to guide product development towards a continuous direct

1486 compression process for equant morphologies, or a granulation process for needlelike particles.
1487 This is very useful in resource allocation and early phase process planning.

1488 Solubilities, morphologies, and growth rates can be predicted at different temperatures and for
1489 different solvents once the desired form has been produced and some experimental data is available
1490 for that polymorph. The most important limitations on the absolute and relative values of the
1491 properties from computation that have been illustrated by this review are discussed below.

1492



1493 Figure 17. Comparison of morphology predictions using the CSP generated structure and an
1494 experimental structure. The morphologies were calculated with the CLP force field and vOCG
1495 solvent model, and can be compared with other calculations and the experimental morphologies
1496 in Figure 13. The packing energies (PE) calculated with the CLP force field approximate the
1497 lattice energy if conformational changes are neglected and can be compared with other estimates
1498 of the lattice energy for olanzapine in Figure 4 and Figure 5 and with the heat of sublimation of β -
1499 succinic acid in Figure 8 if temperature effects are also neglected. *The experimental structures
1500 had the positions of the hydrogen atoms corrected for the systematic error in X-ray determinations.
1501 Neither structure was optimized with the force field used for the morphologies.

1502 8.1 General problems identified

1503 8.1.1 Crystal structure and temperature effects

1504 In addition to the limitations of the ability of CSP to predict the observed polymorphs, there are
1505 limitations on how well a static perfect crystal structure produced by lattice energy minimization
1506 represents the ambient crystal structure. The effects of thermal expansion are neglected: this can
1507 be very anisotropic, depending on the polymorph and the extent to which there are different
1508 intermolecular forces defining the different cell dimensions. A review of over four thousand
1509 organic crystals shows that the anisotropy of the thermal expansion has a very broad distribution,
1510 with crystallographic evidence suggesting that a third may have at least one orthogonal axis with
1511 negative thermal expansion.³⁷⁷ Experimentally, the anisotropy shows in the changing appearance
1512 of the pXRD pattern with temperature, with the different peak shifts often changing the peak
1513 overlaps. Computationally, if comparing polymorphs where one has hydrogen bonding in all three
1514 dimensions, and another has hydrogen bonded layers only held together by dispersion interactions
1515 between the layers, the quality of the computational modeling of the structures may be very
1516 different.

1517 In specific cases, the inability of a crystallographic information file to capture the dynamic
1518 structure may limit the accuracy of the calculated thermodynamic and kinetic properties. Dynamic
1519 disorder of even part of the molecule in one polymorph can have a significant effect, but MD
1520 simulations will at least allow diagnosis of whether such effects are likely to be present. Other
1521 limitations include the implicit neglect of defects and unit cell disorder on the properties.

1522 However, it is the curse of the exponential dependence of many properties on temperature that
1523 is the most common limitation in the accuracy of the predicted values. The exponential dependence

1524 is a function of the ratio of the energy differences to temperature, and hence makes computer
1525 modeling very sensitive to the underlying potential energy surface (force field).

1526 8.1.2 Force field availability and accuracy

1527 A major limitation of the digital design of pharmaceutical products is the availability of
1528 sufficiently accurate force fields for pharmaceutical molecules to enable the CSP, landscape
1529 reduction, free energies, morphologies, and other properties to all be calculated to the accuracy
1530 required.

1531 The sensitivity of the pharmaceutical solid state to the underlying potential energy surfaces has
1532 given considerable impetus to academia to develop more accurate energy models for
1533 pharmaceutical crystals.³⁷⁸ There is a huge effort in the theory, computer codes and testing for both
1534 atomistic force fields³⁷⁹ (e.g. non-empirical anisotropic atom-atom intermolecular potentials⁶¹
1535 combined with separated intramolecular force fields³⁸⁰), electronic structure calculations^{65, 381} and
1536 fragment-based methods.⁶⁷ Many of these emerging methods were benchmarked in the 7th Blind
1537 Test of Crystal Structure Prediction.^{382, 383} However, there are many issues, ranging from choice
1538 of functional form to selection of experimental or theoretical data for validation, that means that
1539 choice of force field will be a major factor in determining the accuracy of the simulations.

1540 We have noted that the limitations of force field accuracy can to some degree be circumvented
1541 by approaches which use certain properties (e.g. the supersaturation driving force) calculated from
1542 the force field as input to simulations of more complex properties (e.g. absolute and relative growth
1543 rates in Section 5.3).

1544

1545 8.1.3 Computational resources

1546 Many methods described here have only been applied to small molecules, and they have different
1547 scaling of computational cost with the size of molecule, its flexibility and the largest unit cell that
1548 needs to be considered. The traditional force fields that are used for MD simulations, morphology
1549 calculations and some free energy calculations have a functional form that is generally too
1550 restrictive for them to be capable of accurately describing pharmaceutical molecules adequately
1551 for CSP. Thus, the computational resources required for progress in this field include the
1552 optimization of codes that can use more advanced models for the potential energy surfaces. The
1553 realism of the implicit assumptions in the traditional force fields, such as using the same parameters
1554 for intermolecular and intramolecular terms, assuming isotropic atoms including atomic charges,
1555 and ignoring the change in charge density with conformation, will depend on the specific
1556 molecules and crystal structures being studied. Commonly available simulation packages can use
1557 the same force field for CSP and morphology prediction and give “good enough” results for some
1558 molecules for some purposes.⁶¹ Hence, the need for more advanced codes and force fields is
1559 molecule dependent. There are hopes that machine-learning of potential energy surfaces may be
1560 a route forward,³⁸⁴ once there is an electronic structure method that can provide an accurate enough
1561 potential energy surface for training (c.f. Figure 4). However, the machine-learned force fields also
1562 cannot yet be directly used in the highly optimized codes that make long-timescale, large system
1563 MD simulations feasible. Thus, a simulation method using a traditional force field that gives high
1564 accuracy for benzene may not work well for a flexible API, even if infinite CPU hours could be
1565 used.

1566 8.2 Polymorphism and multicomponent systems

1567 The challenges of digital design of crystallization processes are very specific to the API
1568 concerned. The kinetic competition between polymorphs is very dependent on the molecule’s

1569 structure. What a medicinal chemist would consider minor differences in the molecular structure,
1570 such as introducing a methyl group or changing a hydrogen to a fluorine atom, will change the
1571 crystal structure and the propensity for polymorphism. A recent survey of 232 simply substituted
1572 chalcones ((*2E*)-1,3-diphenylprop-2-en-1-ones)³⁸⁵ had 170 different crystal packings, with the
1573 largest isomorphous group containing 15 compounds. Conversely, the digital design process could
1574 be used to foresee whether a given API was likely to be problematic to develop, and whether a
1575 multi-component form, or medically similar API should be considered.

1576 8.3 Utilization in Process Design

1577 Aspects of the vision of the digital design of crystallization processes are currently in use for
1578 drug development. CSP is used to understand the potential form landscape and inform the
1579 experimental form selection process. Morphology predictions are used to understand the effect
1580 solvent selection can have on the resultant crystal morphology, once a crystal form has been
1581 selected. However, both applications are employed in conjunction with experimental data to
1582 validate whether the potential energy surface and method are realistic enough – neither are used in
1583 the absence of experimental data, when only a molecular structure is available.

1584 Both tools could be used today *ab initio* to better understand and predict the risks associated
1585 with the development of a new API due to the complexity of the predicted solid form landscape
1586 and the expected crystal morphology landscape of each possible polymorph. The current state of
1587 the art of CSP, while limited by the accuracy of the potential energy surface and modeling of
1588 temperature effects, does usually identify the observed and stable polymorphs amongst other
1589 energetically competitive forms, as illustrated for both succinic acid⁸² and for olanzapine (Figure
1590 5 and refs ⁷³ and ⁷⁹). For olanzapine, as Figure 5 reveals, several forms that have not been observed
1591 experimentally are calculated to be more stable at ambient than those observed experimentally.

1592 However, Figure 4 shows that either force field used to model the molecular motions gives a very
1593 different lattice energy from the most advanced electronic structure methods, where the four
1594 known forms are the most stable. The general observation that CSP usually generates more
1595 thermodynamically plausible polymorphs than are found, even in state-of-the-art industrial
1596 screening (e.g. galunisertib³⁸⁶) and after landscape reduction (see Section 3.1.2), exemplifies the
1597 need for better primary nucleation models. It is conceivable that the rates of nucleation for the
1598 experimentally observed forms are faster than for the apparently thermodynamically competitive
1599 predicted yet not observed forms in all practically possible conditions.

1600 Table 1 illustrates the competition of the kinetics of nucleation and growth versus
1601 thermodynamics in predicting the form most likely to be observed when the free energy differences
1602 between competing forms are “small”. In those cases when the more stable form exhibits faster
1603 kinetics for both nucleation and growth, the thermodynamic form should be experimentally
1604 observed. Similarly, when both the nucleation and growth kinetics of the thermodynamically
1605 stable form are much slower than the unstable form, the unstable form is more likely to be
1606 observed. It is not obvious which form would be expected when either the growth rate or the
1607 nucleation rate of the thermodynamically stable form is slow relative to the unstable form. For
1608 digital design to be able to predict the most likely form, better models are needed for nucleation to
1609 support the design of experiments to alter the nucleation rates and find the first sample of the new
1610 form (Section 3.3) or conclude that the putative structure was so kinetically hindered that it could
1611 never be crystallized. There are cases where the most stable form has eventually been found despite
1612 being slower to nucleate and grow than the apparently stable metastable form.^{387, 388} However,
1613 once the solid form has been selected on the basis of experimental solid form screening with the

1614 aid of CSP, then the design of the crystallization process can proceed by ignoring the primary
1615 nucleation rate through seeding.

1616 Table 1: Experimentally expected form when the nucleation or growth rates of the stable form is
1617 fast/slow relative to the unstable forms.

Stable Form Nucleation Rate	Stable Form Growth Rate	Expected Form Observed
Fast	Slow	Unknown
Slow	Slow	Unstable Form
Fast	Fast	Stable Form
Slow	Fast	Unknown

1618

1619 More reasonable expectations of state-of-the-art molecular simulation at the present time or in
1620 the near future are to be able to:

- 1621 1. Approximate the stability order of a set of polymorphic forms as a function of
1622 temperature.
- 1623 2. Assess the risk of hydrate formation under real-world temperature and relative humidity
1624 conditions.
- 1625 3. Suggest the potential for further energetically competitive polymorphs and provide their
1626 structures, which may suggest an experimental route to their discovery.
- 1627 4. Predict the relative solubility of a given solute in different solvents.
- 1628 5. Predict the change in solubility with respect to temperature of a given solute in a given
1629 solvent (i.e., the slope of the van't Hoff plot (Figure 9)).
- 1630 6. Predict the morphology and the growth rates of the major facets for a set of polymorphic
1631 forms in a range of solvents.

1632 These are all important pieces of information needed during the development of a robust
1633 crystallization process. The methods we have described in this paper, based on the molecular
1634 mechanisms, using advanced MD sampling, etc are not yet commercially available.

1635 The inability to predict the most likely crystal form poses a conundrum for utilization of the
1636 digital design workflow as the predicted thermodynamically stable form may not be the form most
1637 likely to be observed and may not be the right basis to then use for *ab initio* conceptual process
1638 design. This suggests an alternative workflow for how the current state of the art in digital design
1639 can be used for conceptual crystallization process design – to carry forward all putative
1640 polymorphs within a reasonable free energy and hence solubility range (allowing for the errors in
1641 the simulation) and assess the crystal morphology landscape associated with each CSP-generated
1642 form. This workflow allows for a prediction of all crystal shapes possible and allows for resource
1643 and risk estimations to be made based on the complexity associated with the development of the
1644 crystallization process. As an example, if only equant crystal morphologies are predicted for all
1645 plausible polymorphs, then it can be anticipated that a smaller effort would be required to develop
1646 a crystallization process to provide a freely flowing powder. Conversely, if only needlelike
1647 crystals are predicted across all putative crystal forms, then it can be expected that more resources
1648 will be required to develop the crystalline API process to improve upon the crystal morphology
1649 through application of particle engineering techniques such as thermocycling.³⁸⁹ For batch
1650 crystallization processes, it is possible to consider conceptual process design provided that
1651 solubility can be predicted. As this paper shows, *in silico* models provide a forward look at the
1652 effort needed to develop a new product, as the model predictions can provide an estimate of the
1653 complexity (undesired morphology, poor aqueous solubility, multiple polymorphs of similar free

1654 energies, poor organic solubility in acceptable process solvents) the solid form of the API might
1655 exhibit, and thus the impact (time and resource needs) on developing a solid oral dosage form.

1656 While it is not currently possible to fully realize the *ab initio* vision of digital design, it is possible
1657 to benefit from the workflow provided that small amounts of experimental data are available. For
1658 example, solubility in the full range of solvents can be broadly predicted from a small set of
1659 solubility measurements, and the absolute growth rate can be estimated from knowledge of a single
1660 absolute growth rate for only one face. Both examples represent an enormous reduction in effort
1661 compared with the experimental determination of the absolute growth rates of every face on the
1662 crystal surface (something which is rarely done, even in academic labs) or measurement of
1663 solubility in thousands of solvents or solvent mixtures.

1664 9 Conclusions

1665 An industrial perspective on the engineering of pharmaceutical materials in 2007²⁰ saw
1666 computational prediction as a future step in the route from active molecule to finished product. We
1667 have demonstrated through examples the use of simulation as part of the support to experimental
1668 techniques foreseen in a 2015 review of the future of pharmaceutical manufacturing sciences,²¹
1669 and illustrated much progress in some of the opportunities identified by the crystallization working
1670 group of the Enabling Technologies Consortium.²²

1671 Computational methods are available to design a crystallization process from the chemical
1672 diagram (i.e. *a priori* without any experimental data) for all the main steps, apart from nucleation
1673 rates which are more important for polymorph discovery. However, which type and level of theory
1674 is accurate enough and practically affordable is very dependent on the specific molecule, its size,
1675 conformational flexibility, functional groups and particularly the nature of the competing
1676 polymorphs and hydrates that can affect the manufacture and stability of the product. Future efforts

1677 for utilizing CSP to aid polymorph discovery and minimizing the risks of the late emergence of
1678 more stable forms should focus on primary nucleation rates. A key requirement to the
1679 implementation of the digital design workflow is *a priori* solubility predictions but the exponential
1680 dependence of solubility on temperature and the free energy of solution (which can be greatly
1681 affected by anharmonic motions within the specific crystal) make this a particularly challenging
1682 property to compute. Morphologies can be computed, although this is more straightforward for
1683 centrosymmetric molecules or growth units, but absolute growth rates involve similar challenges
1684 to absolute solubilities.

1685 This paper shows that physics-based simulation methods are being actively developed for
1686 pharmaceuticals and are qualitatively and semi-quantitatively realistic enough to be useful. The
1687 ideal of using the accurate potential energy surfaces for CSP and all properties and a simulation
1688 method that is realistic for the dynamics, nucleation, and growth of pharmaceutical crystals, will
1689 eventually produce more reliable quantitative multi-scale modeling in the design of crystallization
1690 processes. In the meantime, such methods can considerably aid the design process when used
1691 either in conjunction with experimental data or for giving relative properties or key parameters in
1692 approximate models. The time is near when consideration of solid state properties for new
1693 chemical medicinal targets will be integrated into computational chemistry approaches for the
1694 identification of new drugs.

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1701

1702 11 References

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