

# Cooperativity and Frustration Effects (or Lack Thereof) in Polarizable and Non-Polarizable Force Fields

Jorge Nochebuena,<sup>†</sup> Jean-Philip Piquemal,<sup>‡</sup> Shubin Liu,<sup>¶,§</sup> and G. Andrés Cisneros<sup>\*,†,||</sup>

<sup>†</sup>*Department of Physics, University of Texas at Dallas, Richardson, TX, USA*

<sup>‡</sup>*Laboratoire de Chimie Théorique, Sorbonne Université, UMR 7616 CNRS, Paris, France*

<sup>¶</sup>*Research Computing Center, University of North Carolina, Chapel Hill, NC, USA*

<sup>§</sup>*Department of Chemistry, University of North Carolina, Chapel Hill, NC, USA*

<sup>||</sup>*Department of Chemistry and Biochemistry, University of Texas at Dallas, Richardson, TX, USA*

E-mail: andres@utdallas.edu

## Abstract

Understanding cooperativity and frustration is crucial for studying biological processes, such as molecular recognition and protein aggregation. Force fields have been extensively utilized to explore cooperativity in the formation of protein secondary structures and self-assembled systems. Multiple studies have demonstrated that polarizable force fields provide more accurate descriptions of this phenomenon compared to fixed-charge pairwise non-polarizable force fields, thanks to the incorporation of polarization effects. In this study, we assess the performance of the AMOEBA polarizable force field and the AMBER and OPLS non-polarizable pairwise force fields in capturing

positive and negative cooperativity recently explored in neutral and charged molecular clusters using Density Functional Theory. Our findings show that polarizable and non-polarizable force fields qualitatively reproduce the relative cooperativity observed in electron structure calculations. However, AMBER and OPLS fail in describing absolute cooperativity. In contrast, AMOEBA accounts for absolute cooperativity by considering interactions beyond pairwise interactions. According to the energy decomposition analysis, it is observed that the electrostatic interactions calculated with the AMBER and OPLS force fields seems to play an important and counter-intuitive role in reproducing the adiabatic interaction energies calculated with Density Functional Theory. However, it is important to note that these force fields, due to their nature, do not explicitly incorporate many-body effects, which limits their ability to accurately describe cooperativity. On the other hand, frustration in polarizable and non-polarizable force fields is caused by changes in bond stretching and angle bending terms of the building blocks when they are forming a complex.

## Introduction

Cooperativity plays a crucial role in understanding various biological processes, including molecular recognition, homochirality, protein folding and self-assembly.<sup>1-11</sup> Cooperativity refers to the non-additive and synergistic effects that arise when multiple components interact, leading to enhanced stability or activity. One of the most well-known examples of cooperativity is the binding of O<sub>2</sub> to hemoglobin. When one the four binding sites of hemoglobine binds an oxygen molecule, it triggers a conformational change that makes it easier for the other sites to bind oxygen as well.

Positive (negative) cooperativity occurs when the interactions between components of a system favor(disfavor) each other. By contrast, no cooperativity is observed when the interactions of the entire system can be represented by the individual interactions of its components. Conversely, frustration refers to the situation in which the optimal geometric

arrangement of a set of isolated molecules changes upon forming a new molecular system. This change in geometry can result from the intermolecular interactions and bonding between the molecules, which can lead to a deviation of individual molecular geometries from the optimized individual gas phase structure. This sub-optimal arrangement is referred to as frustration, as it deviates from the ideal or expected geometric arrangement. Cooperativity and frustration are two interconnected concepts, each emphasizing different aspects. Cooperativity primarily examines the behavior of systems as a whole, while frustration delves into the characteristics of individual components.<sup>12</sup>

Force fields have been used as a tool for investigating cooperative effects involved in the formation of protein secondary structures and self-assembled systems.<sup>13–15</sup> Notably, a growing body of evidence supports the superiority of polarizable force fields over fixed-charge force fields in providing more accurate descriptions of cooperativity due to the (partial) incorporation of terms that are explicitly involved in many-body effects.<sup>16–19</sup> By explicitly incorporating the concept of polarization effects, polarizable force fields can simulate for the dynamic electronic redistribution that occurs within molecular systems.<sup>20,21</sup> In contrast, fixed-charge force fields neglect the dynamic nature of charge distributions that arise from polarization and charge transfer interactions.<sup>22</sup>

In this work, we focus on studying cooperativity and frustration using molecular mechanics to evaluate the capability of force fields to reproduce these effects. We used three representatives:  $\text{NH}_3(\text{H}_2\text{O})_n$ ,  $\text{Li}^+(\text{H}_2\text{O})_n$ , and  $\text{F}^-(\text{H}_2\text{O})_n$  for neutral and charged systems. The previous systems have been studied using Density Functional Theory<sup>23–26</sup> Positive cooperative effects were observed in neutral systems and negative cooperativity was observed in charged systems. On the other hand, it was shown that the frustration effect is smaller than cooperativity, and can be positive or negative. Previously some of us have shown that the cooperativity of hydrogen bonds in infinite linear chains can be modeled using point dipoles.<sup>27</sup> Therefore, it is of interest to investigate whether force fields are capable of reproducing these effects in molecular clusters.

## Theoretical framework

We used molecular systems of the form  $AB_n$ , where B is the building block,  $n$  the number of building blocks, and A is the accessory component to quantify both cooperativity and frustrativity. In this work, water molecules are the building blocks and  $\text{NH}_3$ ,  $\text{Li}^+$  and  $\text{F}^-$  are the accessory components.

To calculate cooperativity and frustrativity we need to calculate the adiabatic and vertical interaction energies. The adiabatic interaction energy is defined as:

$$E_{\text{int}}^{\text{adiab}} = E(\text{AB}_n) - nE_{\text{B}}(\text{R}_{0\text{B}}) - E_{\text{A}}(\text{R}_{0\text{A}}), \quad (1)$$

where  $n$  is the number of building blocks included in the system,  $E$  is the total energy of the whole system,  $E_{\text{B}}$  is the total energy of the building block with the optimized structure  $\text{R}_{0\text{B}}$ , and  $E_{\text{A}}$  is the total energy of the accessory component with the optimized structure  $\text{R}_{0\text{A}}$ .

The cooperativity index  $k$  is defined as the negative change of adiabatic interaction energy per building block change, that is:

$$k = -(\partial E_n / \partial n), \quad (2)$$

where  $E_n$  is the interaction energy per building block obtained by dividing the adiabatic interaction energy by the number of building blocks, that is,

$$E_n = E_{\text{int}}^{\text{adiab}} / n \quad (3)$$

The parameter  $k$  can have three possible scenarios. If  $k$  is positive, the cooperativity is positive and it means that adding an additional building block makes the interactions stronger. If  $k$  is negative, then cooperativity is negative and it means that adding a building block weakens the interactions. Otherwise, if  $k$  is zero, there is no cooperativity and it means that adding an additional building block has no impact on the interactions.

The vertical interaction energy is defined as:

$$E_{\text{int}}^{\text{vert}} = E(\text{AB}_n) - \sum_{\text{B}=1}^n E_{\text{B}}(\text{R}_{\text{B}}) - E_{\text{A}}(\text{R}_{\text{A}}), \quad (4)$$

where  $E_{\text{B}}$  is the total energy of each building block with structure  $\text{R}_{\text{B}}$ , and  $E_{\text{A}}$  is the total energy of the accessory component with the structure  $\text{R}_{\text{A}}$ .

Note that the difference between equations (1) and (4) depends on which molecular geometry is used in each case. In equation (1) the optimized geometries of the individual molecules are used, while in equation (4) the geometries of the molecules forming the system are used. Because molecules outside of their optimized gas-phase geometry will always have a higher energy than their corresponding equilibrium structures, the vertical interaction energy will always be more stabilizing than the adiabatic interaction energy.

Then, the total frustration energy can be defined as the difference between the adiabatic interaction energy and the vertical interaction energy, that is,

$$E_{\text{frust}} = \sum_{\text{B}=1}^n E_{\text{B}}(\text{R}_{\text{B}}) + E_{\text{A}}(\text{R}_{\text{A}}) - nE_{\text{B}}(\text{R}_{0\text{B}}) - E_{\text{A}}(\text{R}_{0\text{A}}) \quad (5)$$

In a similar way to cooperativity, the frustration per building block can be defined as:

$$E_{0n} = E_{\text{frust}}/n \quad (6)$$

and frustrativity as:

$$\zeta = \partial E_{0n} / \partial n \quad (7)$$

If  $\zeta$  is positive, frustrativity is positive and means that adding an additional building block increases the difference in geometry of the individual molecules when they are part of the system. If  $\zeta$  is negative, frustrativity is negative and means that adding a new building block reduces the geometric difference between the individual molecules and forming the system. If  $\zeta$  is zero, frustrativity is zero and it means that adding a new building block does

not affect the geometry of the individual molecules.

We refer to the previous form of measuring of cooperativity as relative cooperativity because estimating the value of cooperativity for a given number of building blocks,  $n$ , requires knowing the interaction energy of a smaller cluster ( $n - 1$ ) and a larger cluster ( $n + 1$ ).

In addition, we are also interested in investigating how force fields reproduce absolute cooperativity. As described above, cooperativity is due exclusively to many-body effects. Therefore, an important question is how force fields are able to model some cooperativity effects. In particular, it is known that by construction, pair-wise non-polarizable potentials do not explicitly include many-body effects. One possibility is to determine if the following condition is satisfied:

$$E_{\text{int}}^{\text{vert}} = \sum_{B=1}^n [E_{\text{AB}} - E_B - E_A] + \sum_{B=1}^{n-1} \sum_{C=B+1}^n [E_{\text{BC}} - E_B - E_C] \quad (8)$$

where AB is a dimer formed by the accessory component, A, and a building block, B, and BC is a dimer formed by the building blocks B and C. If equation 8 is satisfied, it means that the vertical interaction energy can be represented through individual interactions, and therefore there is no cooperativity. On the other hand, if the vertical interaction energy is more stabilizing than the right-hand side of equation 8, it means there is an energy gain and thus positive absolute cooperativity. Conversely, if the vertical interaction energy is less stabilizing than the right-hand side of equation 8, it means there is an energy loss due to the formation of the complex, and therefore negative absolute cooperativity.

## Computational details

In this work we calculated the relative cooperativity, equation ((2)), and the frustrativity, equation ((7)), in three representative molecular systems: an ammonia molecule in water,  $\text{NH}_3(\text{H}_2\text{O})_n$ , a lithium cation in water,  $\text{Li}^+(\text{H}_2\text{O})_n$ , and a fluorine anion in water,  $\text{F}^-(\text{H}_2\text{O})_n$ .

The first of these systems is a neutral system, while the last two are negatively and positively charged systems, respectively. In all cases, systems including from 1 to 20 building blocks were considered.

The optimized DFT molecular geometries were taken from the work of Liu and Rong.<sup>26</sup> Each system is the global minimum for each number of building blocks. We optimized a water molecule as a building block and the accessory components with density functional theory using Gaussian16.<sup>28</sup> The exchange-correlation functionals and basis sets correspond to those used by Liu and Rong,<sup>26</sup> namely  $\omega$ B97X-D/aug-cc-pVDZ for  $\text{NH}_3(\text{H}_2\text{O})_n$ ,<sup>29-32</sup> M06-2X/6-311+G(d,p) for  $\text{Li}^+(\text{H}_2\text{O})_n$ ,<sup>33-37</sup> and B3LYP/aug-cc-pVDZ for  $\text{F}^-(\text{H}_2\text{O})_n$ .<sup>31,38,39</sup> AMOEBA was used for all polarizable force fields calculations, and for the non-polarizable calculations OPLS was used for the ammonia and fluoride systems, and AMBER was used for the lithium systems.<sup>22,33-37,40-44</sup>

To evaluate the performance of force fields in reproducing previously reported results with DFT, we considered two scenarios: In the first scenario, we performed single-point calculations on each of the systems optimized with DFT. In the second scenario, we carried out optimization of the systems with force fields using Tinker8 to calculate the adiabatic and vertical interaction energies.<sup>45</sup> Water molecules are described with the AMOEBA and TIP3P parameters by using polarizable and non-polarizable force fields, respectively.<sup>41,46</sup>

To evaluate whether equation (8) was satisfied, we computed vertical interaction energies for each possible dimer within the first four clusters ( $1 \leq n \leq 4$ ) for each of the systems studied here. We then performed single-point calculations using the same levels of theory described earlier, using the Psi4 code, and compared them to the equivalent systems calculated with force fields. In addition, we utilized the Symmetry-Adapted Perturbation Theory within Density Functional Theory, SAPT(DFT), implemented in Psi4 to analyze the noncovalent interaction components in these systems.

# Results and discussion

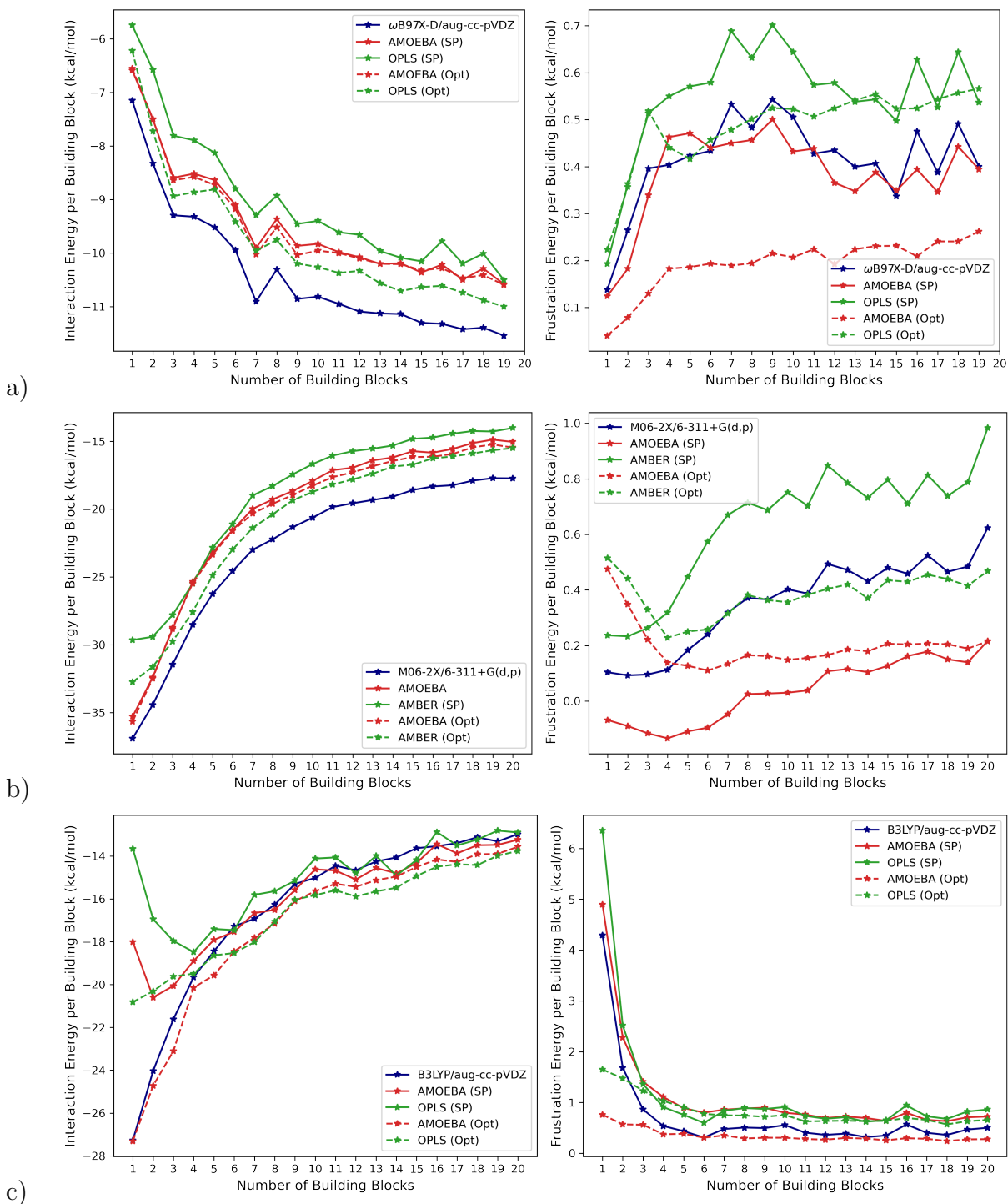


Figure 1: Relative cooperativity (left) and frustrativity (right) for a)  $\text{NH}_3(\text{H}_2\text{O})_n$ , b)  $\text{Li}^+(\text{H}_2\text{O})_n$ , and c)  $\text{F}^-(\text{H}_2\text{O})_n$  systems. Solid lines are single-point values calculated from optimized DFT structures while dashed lines are calculated in optimized FF structures.



We evaluated relative cooperativity and frustrativity in three representative neutral and charged systems:  $\text{NH}_3(\text{H}_2\text{O})_n$ ,  $\text{Li}^+(\text{H}_2\text{O})_n$ , and  $\text{F}^-(\text{H}_2\text{O})_n$ . We selected these systems because the parameters of the force fields already existed to describe each molecule of the systems. As previously mentioned, cooperativity is a phenomenon that cannot be captured by pairwise contributions alone because it involves complex many-body interactions. Knowing that force fields such as AMBER and OPLS lack many-body interactions, we examine the capability of force fields to reproduce the adiabatic interaction energies using clusters of varying sizes. Tables S1 to S6 show the total adiabatic and vertical interaction energies for each of the systems studied in this work. Tables S1, S3, and S5 show the interaction energies calculated via a single point on the structures optimized with DFT. Conversely, tables S2, S4, and S6 show the interaction energies using the structures optimized with their respective force fields. Each row indicates the interaction energy for each number of building blocks calculated with density functional theory and polarizable and non-polarizable force fields.

As expected, the vertical interaction energies are more negative than the adiabatic interaction energies for almost all cases due to the effect of considering the total energy of each molecule in its optimized gas-phase configuration or not. For the systems corresponding to the optimized DFT structures (Table S3) to calculate the interaction energies of the  $\text{Li}^+(\text{H}_2\text{O})_n$  system with AMOEBA, the first seven values exhibit an opposite trend, that is, the adiabatic interaction energy is more stabilizing than the vertical interaction energy. This can be explained because we are not allowing the geometry to be optimized for the force field used. That is, the optimizations made with density functional theory do not necessarily coincide with the optimized structure for the force field. For example, the optimal H–O–H angle in a water molecule calculated with AMOEBA is  $108.5^\circ$  but the same angle calculated using any of previous exchange-correlation functionals ranges between  $104.8$  and  $105.2^\circ$ . However, when we allow the system to relax (Table S4), the expected behavior is obtained.

We also note that for the  $\text{NH}_3(\text{H}_2\text{O})_n$  and  $\text{Li}^+(\text{H}_2\text{O})_n$  systems the interaction energies

obtained with the exchange-correlation functionals show more negative values than the force fields. On the other hand, for the  $F^-(H_2O)_n$  system, the lowest interaction energies were obtained with the force fields. This could be due to the different types of functionals and force fields used in each case. However, in all cases we can see that the force fields reproduce the same trends obtained with Density Functional Theory

Figure 1 shows the cooperativity and frustrativity profiles for the systems studied in this work. It shows the values obtained for the force fields using optimized DFT geometries and the values obtained for the force fields with their respective optimized structures. The values shown correspond to the energies of interaction and frustration for each building block. As previously reported, the  $NH_3(H_2O)_n$  (neutral) system shows positive cooperativity in that as the number of building blocks increases, the interaction energy per building block also increases, either using DFT or force fields. We can see that the largest building block interaction energies were obtained with DFT. However, both the OPLS polarizable and the AMOEBA non-polarizable force field reproduce the behavior of DFT, although the interaction energies are lower. Frustrativity is positive whether using DFT or force fields. That is, in all cases the cooperativity and frustrativity are positive. In Figure 1a we can see that the optimization of the structures improves the description of the interaction energy especially with the OPLS force field. However, the frustration energy undergoes several changes, increasing the difference with the results reported with DFT.

As previously reported,  $Li^+(H_2O)_n$  and  $F^-(H_2O)_n$  (charged systems) show negative cooperativity since, as the size of the system increases, the interaction energy per building block decreases. Considering the structures not optimized by force fields (Figure 1b), the polarizable and non-polarizable force fields reproduce quite well the cooperativity obtained by DFT for the  $Li^+(H_2O)_n$  system, with the performance for the AMOEBA polarizable force showing slight better agreement, especially for the first two structures. However, the frustration calculated with AMOEBA shows an interesting behavior since for the first structures the frustration energy has negative values. This means that the molecules forming

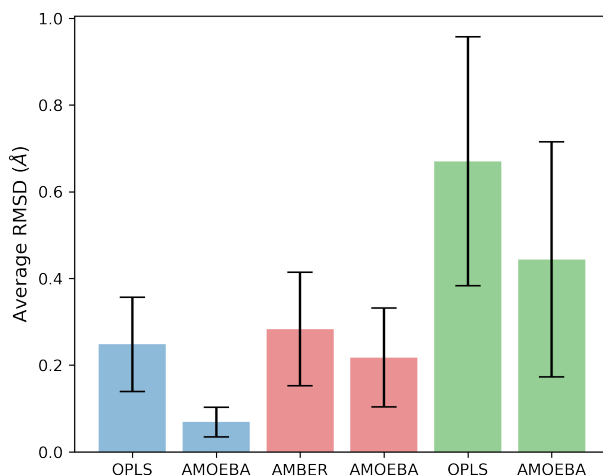
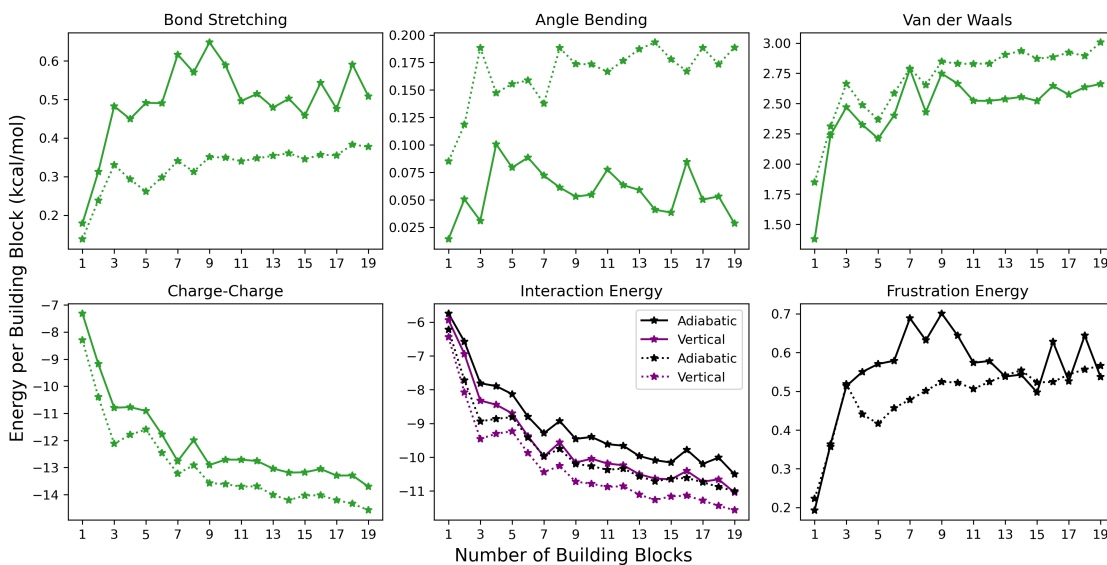


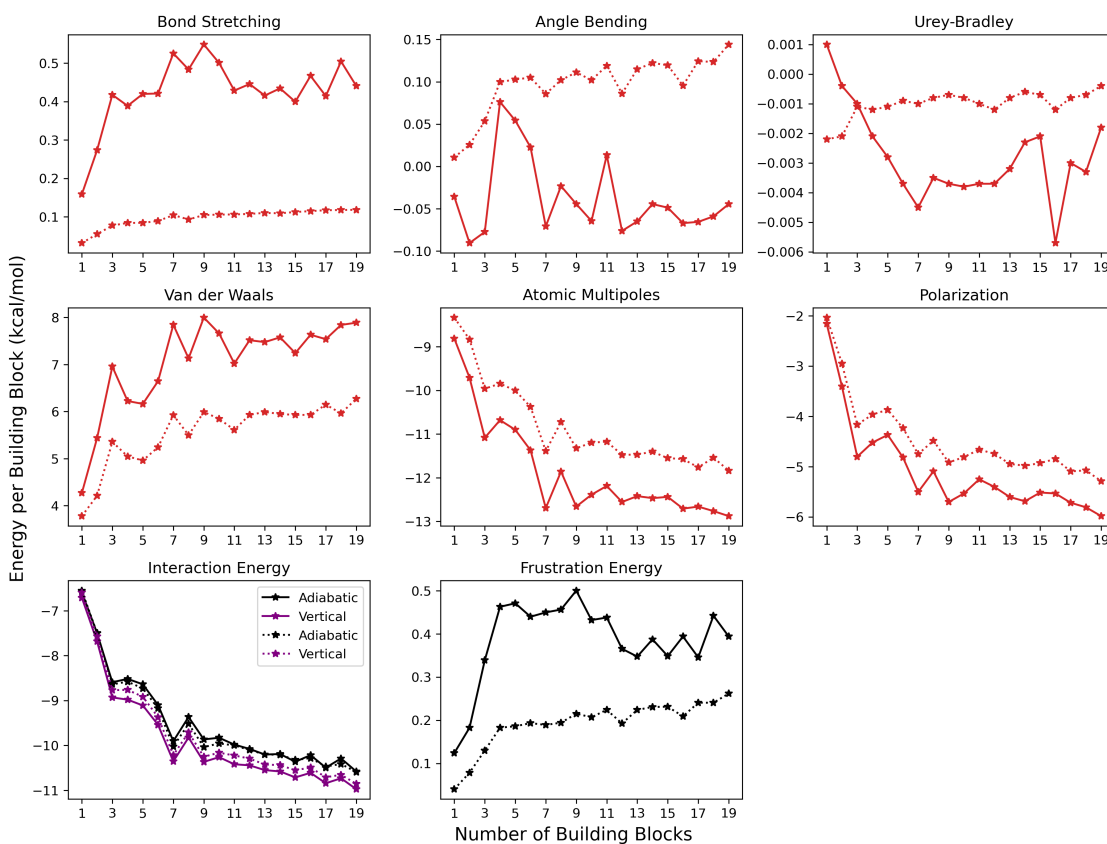
Figure 2: Average root-mean-square deviation (RMSD) between DFT and force field coordinates for the for a)  $\text{NH}_3(\text{H}_2\text{O})_n$ , b)  $\text{Li}^+(\text{H}_2\text{O})_n$ , and c)  $\text{F}^-(\text{H}_2\text{O})_n$  systems shown in blue, red and green bars, respectively. Errors bars indicate the standard deviation.

the system have a lower energy than the isolated molecules. As already discussed above, the reason for this behavior is because the optimized structure of the individual molecules obtained with DFT is different than the optimized structures of AMOEBA. On the other hand, the AMBER non-polarizable force field better reproduces the frustration, although it is far from the values obtained with DFT. If the optimized structures with the force fields are used (Figure 1b), it can be observed that the interaction energies are in much better agreement with respect to the reference. On the other hand, although frustration shows positive values for both force fields, the results show significant changes that are far from the results obtained with DFT.

For the  $\text{F}^-(\text{H}_2\text{O})_n$  system we note that both AMOEBA and the OLSAA non-polarizable force field quite accurately reproduce the frustration calculated with B3LYP when structures not optimized by force fields are used (Figure 1c). However, cooperativity shows interesting behavior. For the first systems, the cooperativity calculated with the force fields shows decreasing values for the first structures, indicating a negative cooperativity. But after the system reaches a certain size, the cooperativity is positive. Here the OPLS force field is the one that shows the largest deviations from the reference. When using the geometries opti-



a)



b)

Figure 3: Energy decomposition analysis for the  $\text{NH}_3(\text{H}_2\text{O})_n$  system. a) OPLS, b) AMOEBA. Solid lines represent single point values calculated from optimized DFT structures, while the dotted lines values were calculated using optimized FF structures.

Table 1: Correlation coefficients between each of the contributions and the adiabatic interaction energy (AIE), vertical interaction energy (VIE) and frustration energy (FE) for the  $\text{NH}_3(\text{H}_2\text{O})_n$  system.

		AIE		VIE		FE	
		DFT <sup>1</sup>	FF <sup>2</sup>	DFT <sup>1</sup>	FF <sup>2</sup>	DFT <sup>1</sup>	FF <sup>2</sup>
OPLS	Bonds	-0.722	-0.965	-0.762	-0.969	0.984	0.985
	Angles	-0.113	-0.843	-0.151	-0.851	0.526	0.933
	vdW	-0.821	-0.980	-0.845	-0.982	0.861	0.975
	Charges	0.989	0.999	0.995	0.999	-0.768	-0.966
AMOEBA	Bonds	-0.769	-0.993	-0.802	-0.994	0.875	0.961
	Angles	0.232	-0.874	0.185	-0.881	0.419	0.983
	UB <sup>3</sup>	0.702	-0.872	0.728	-0.877	-0.741	0.926
	vdW	-0.938	-0.983	-0.945	-0.982	0.667	0.913
	PE <sup>4</sup>	0.984	0.995	0.987	0.994	-0.631	-0.926
	Pol. <sup>5</sup>	0.971	0.986	0.979	0.987	-0.689	-0.947

<sup>1</sup> Single point values calculated over optimized DFT structures;

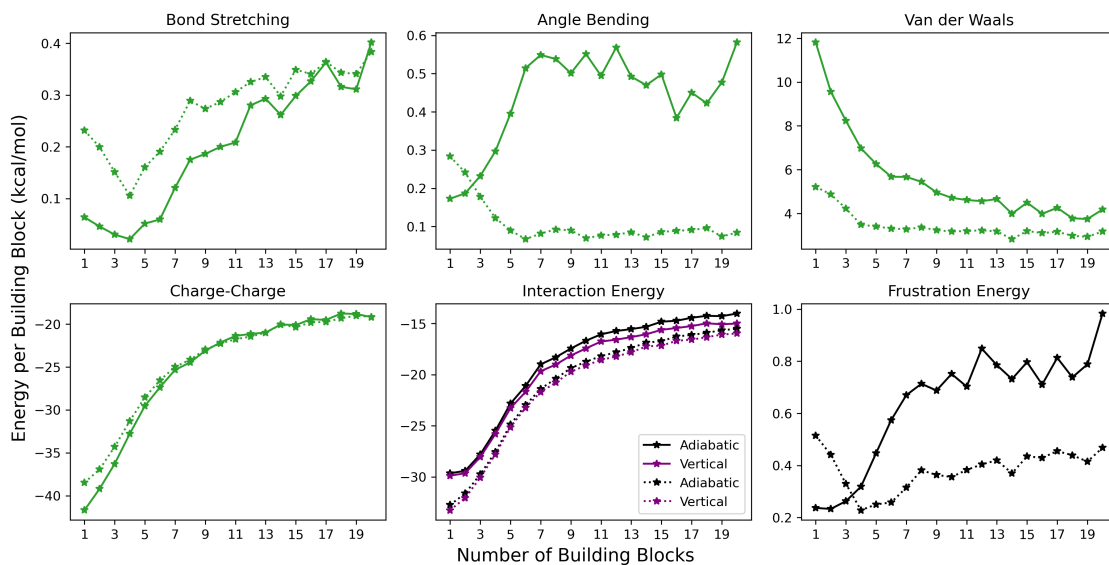
<sup>2</sup> Values calculated over optimized FF structures; <sup>3</sup> Urey-Bradley term;

<sup>4</sup> Permanent electrostatic; <sup>5</sup> Polarization.

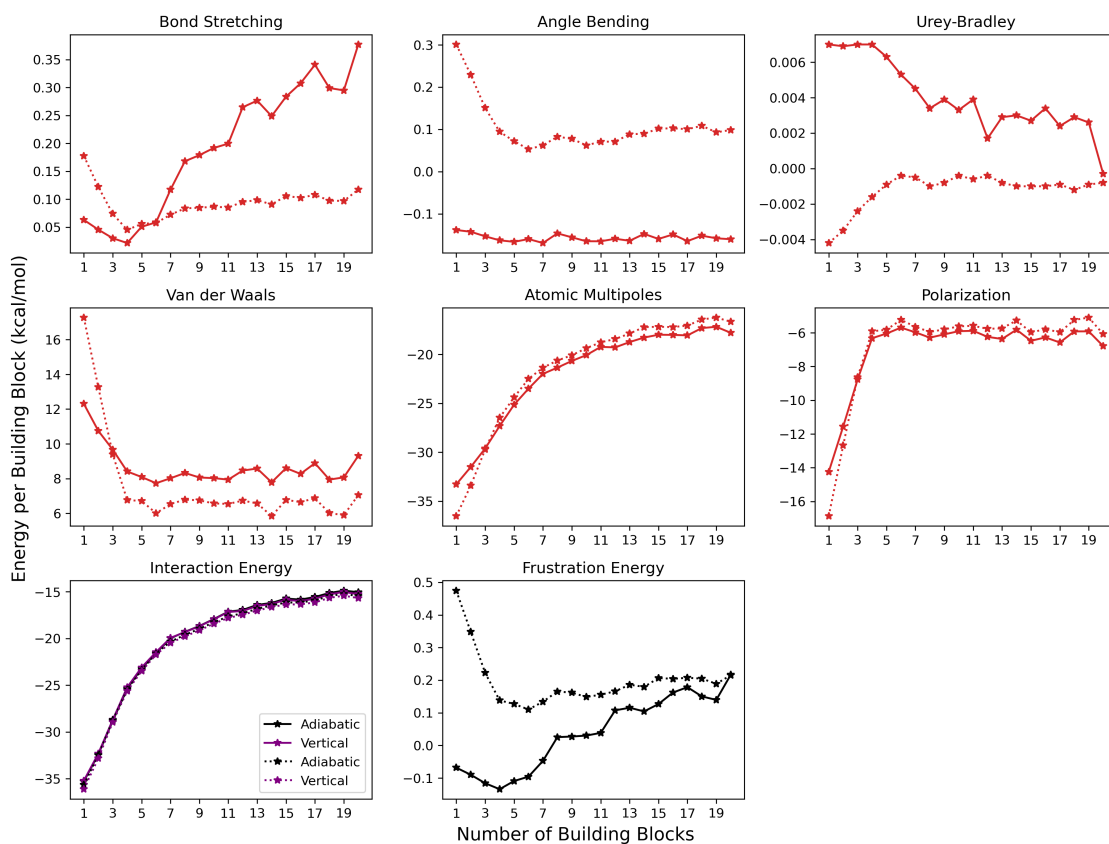
mized by force fields (Figure 1c), the interaction energies closely approximate the reference values. However, frustration becomes more prominent, particularly in smaller systems.

As can be seen in Figure 2, Figures S1-S6 and Table S7, the largest differences in geometric coordinates for the structures optimized with the force fields occur with the non-polarizable force fields. The  $\text{NH}_3(\text{H}_2\text{O})_n$  system shows the smallest errors whether using polarizable or non-polarizable force fields. For this system, the largest RMSD is 0.2 Å when using the AMOEBA force field and 0.45 Å when using the OPLS force field. The  $\text{Li}^+(\text{H}_2\text{O})_n$  system shows a maximum RMSD of 0.4 Å with AMOEBA and a maximum RMSD of 0.65 Å with the AMBER force field. Finally, the  $\text{F}^-(\text{H}_2\text{O})_n$  system shows the largest deviations, with an RMSD of 0.98 Å for AMOEBA and 1.24 Å for the OPLS force field.

We conducted an energy decomposition analysis of the total potential energy to discern the sources of relative cooperativity and frustrativity obtained using the force fields. Understanding how force fields such as AMBER and OPLS can simulate this phenomenon is truly intriguing, particularly considering that cooperativity, as calculated using density functional



a)



b)

Figure 4: Energy decomposition analysis for the  $\text{Li}^+(\text{H}_2\text{O})_n$  system. a) AMBER, b) AMOEBA. Solid lines represent single point values calculated from optimized DFT structures, while the dotted lines values were calculated using optimized FF structures.

Table 2: Correlation coefficients between each of the contributions and the adiabatic interaction energy (AIE), vertical interaction energy (VIE) and frustration energy (FE) for the  $\text{Li}^+(\text{H}_2\text{O})_n$  system.

		AIE		VIE		FE	
		DFT <sup>1</sup>	FF <sup>2</sup>	DFT <sup>1</sup>	FF <sup>2</sup>	DFT <sup>1</sup>	FF <sup>2</sup>
AMBER	Bonds	0.892	0.838	0.890	0.831	0.887	0.718
	Angles	0.823	-0.836	0.819	-0.843	0.889	0.327
	vdW	-0.949	-0.895	-0.950	-0.901	-0.888	0.215
	Charges	0.995	0.998	0.996	0.999	0.950	0.177
AMOEBA	Bonds	0.834	-0.252	0.828	-0.262	0.997	0.887
	Angles	-0.472	-0.780	-0.478	-0.786	-0.062	0.974
	UB <sup>3</sup>	-0.867	0.867	-0.862	0.872	-0.919	-0.899
	vdW	-0.768	-0.860	-0.775	-0.865	-0.255	0.930
	PE <sup>4</sup>	0.995	1.000	0.994	1.000	0.843	-0.641
	Pol. <sup>5</sup>	0.842	0.860	0.848	0.866	0.370	-0.933

<sup>1</sup> Single point values calculated over optimized DFT structures;

<sup>2</sup> Values calculated over optimized FF structures; <sup>3</sup> Urey-Bradley term;

<sup>4</sup> Permanent electrostatic; <sup>5</sup> Polarization.

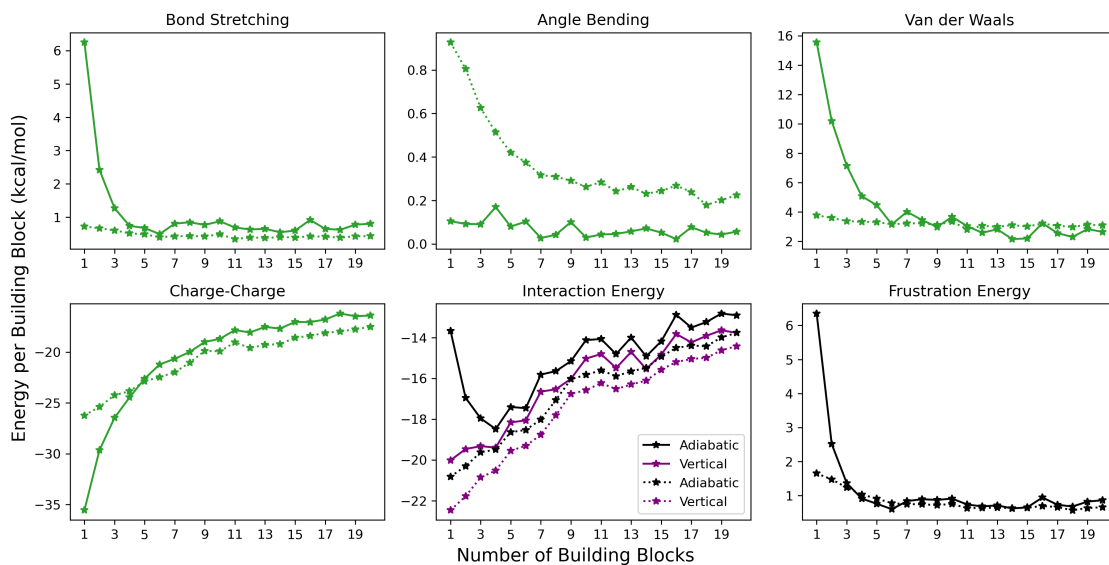
Table 3: Correlation coefficients between each of the contributions and the adiabatic interaction energy (AIE), vertical interaction energy (VIE) and frustration energy (FE) for the  $\text{F}^-(\text{H}_2\text{O})_n$  system.

		AIE		VIE		FE	
		DFT <sup>1</sup>	FF <sup>2</sup>	DFT <sup>1</sup>	FF <sup>2</sup>	DFT <sup>1</sup>	FF <sup>2</sup>
OPLS	Bonds	0.073	-0.774	-0.536	-0.809	1.000	0.972
	Angles	-0.632	-0.886	-0.704	-0.912	0.296	0.993
	vdW	-0.220	-0.778	-0.747	-0.805	0.942	0.908
	Charges	0.482	0.995	0.904	0.999	-0.839	-0.905
AMOEBA	Bonds	-0.406	-0.758	-0.653	-0.763	0.992	0.878
	Angles	-0.892	-0.930	-0.873	-0.931	0.509	0.911
	UB <sup>3</sup>	0.241	0.870	0.189	0.869	0.004	-0.800
	vdW	-0.588	-0.661	-0.793	-0.667	0.982	0.812
	PE <sup>4</sup>	0.831	0.996	0.955	0.995	-0.897	-0.925
	Pol. <sup>5</sup>	0.592	0.886	0.792	0.890	-0.971	-0.963

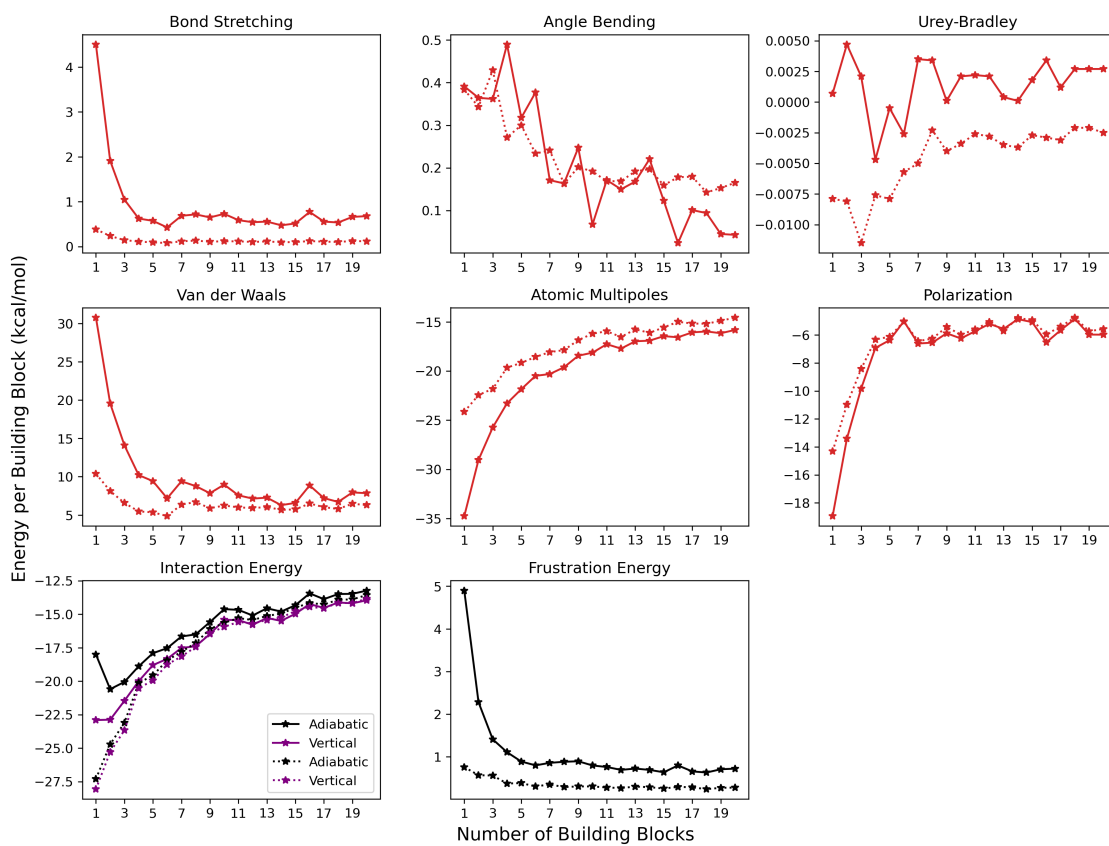
<sup>1</sup> Single point values calculated over optimized DFT structures;

<sup>2</sup> Values calculated over optimized FF structures; <sup>3</sup> Urey-Bradley term;

<sup>4</sup> Permanent electrostatic; <sup>5</sup> Polarization.



a)



b)

Figure 5: Energy decomposition analysis for the  $F^-(H_2O)_n$  system. a) OPLS, b) AMOEBA. Solid lines represent single point values calculated from optimized DFT structures, while the dotted lines values were calculated using optimized FF structures.



theory, incorporates contributions from many-body interactions. We did not repeat the analysis for the energies obtained with DFT since it has already been reported previously.<sup>25</sup> For the OPLS and AMBER non-polarizable force fields the decomposition results in four terms that correspond to bond stretching, angle bending, van der Waals interactions, and charge-charge interactions. For the AMOEBA polarizable force fields, the individual terms correspond to bond stretching, angle bending, Urey-Bradley interaction, van der waals interactions, permanent electrostatic interaction, and polarization. In both cases we have included the adiabatic and vertical interaction energies, and frustration energy interaction energy per building block for easy comparison. Solid lines show the values calculated with the optimized structures obtained from the exchange-correlation functionals, and dotted lines show the values obtained using the optimized structures with the force fields used.

Figure 3 shows the energy decomposition analysis for the  $\text{NH}_3(\text{H}_2\text{O})_n$  system calculated with the OPLS and AMOEBA force fields. The results show that the relative cooperativity comes mainly from intermolecular non-bonded electrostatic interactions, that is, from the charge-charge interaction with the OPLS force field and from the polarization and atomic multipoles with the AMOEBA force field, with the permanent electrostatics exhibiting the largest contribution. We can see from Table 1 that the highest correlation between the adiabatic and vertical interaction energy occurs for the electrostatic interaction when using the OPLS force field. Similarly, for the AMOEBA force field, the largest correlation is obtained between permanent electrostatics and polarization. In both cases, similar values are observed in the structures optimized either by the exchange-correlation functional or by the force field. The van der Waals contribution increases as the number of building blocks increases, with the AMOEBA polarizable force field showing a Van der Waals energy more than two times larger than the same term calculated with the OPLS non-polarizable force field.

From the same Table 1, we can see that the largest correlation for frustration occurs with respect to the bond stretching term for the structures optimized by the exchange-correlation

functional. This can be observed from the shape of the graph, which is very similar to the frustration energy per building block. Furthermore, the energy range of the bond stretching term is larger by almost an order of magnitude compared with the energy range of the angle bending term. On the other hand, for the structures optimized with the force field significant correlation is observed between the bond stretching and the angle bending terms, for both the non-polarizable and polarizable force fields. In both cases the optimization decreases the contribution of bond stretching term but increases the contribution of angle bending term. The Urey-Bradley contribution when using the polarizable force field does not have a significant contribution for this system.

In Figure 4, we observe that in the case of  $\text{Li}^+(\text{H}_2\text{O})_n$  system, the negative relative cooperativity also comes from the charge-charge interactions with the AMBER force field and from the polarization and permanent electrostatic with AMOEBA, the latter being the one that contributes the most.

From Table 2 we can see that the main correlation between the adiabatic and vertical interaction energy is obtained with the charge-charge interactions with the AMBER force field and with permanent electrostatics with AMOEBA, either before or after the force field optimization. The van der Waals contributions for the two force fields used are similar for the smaller complexes but decrease in a different way as the number of building blocks increases. In addition, geometry optimization has a different impact for each force field used. The contribution increases with the AMBER force field, while it decreases with AMOEBA, possibly reflecting the difference in the functional form between the two force fields. In AMOEBA, the 14-7 buffered Halgren potential is utilized to describe the van der Waals (vdW) interactions,<sup>47</sup> whereas, OPLS and AMBER use the 6-12 Lennard-Jones (LJ) potential.<sup>48-50</sup>

From the same Table 2 we can see that the best correlation for frustration with the AMBER force field is obtained with the charge-charge interactions using the structures not optimized by the force field. However this is a fortuitous result, since by definition the frustration must come from intra-molecular changes. On the other hand, it can be seen

that both the bond stretching and angle bending terms show similar correlation coefficients for the AMBER force field before optimization with the force field. After the optimization, the bulk of the correlation is obtained from the bond stretching term. For AMOEBA, the major contributor to the correlation is obtained from the bond stretching term when the DFT-optimized structures are used. Here the angle bending term shows negative results regardless of the number of building blocks. This result shows that the negative values of frustration previously observed in this system come from the difference of the optimal values of the H–O–H angles between the M06-2X exchange correlation functional and AMOEBA. However, during the optimization process, this behavior is corrected, resulting in positive values for all building blocks. In fact, the primary correlation with frustration is observed in the angle bending term, with the bond stretching term following closely behind. Again the Urey-Bradley term practically does not contribute to the total energy.

In Figure 5, we can see that once again the negative relative cooperativity in the  $F^-(H_2O)_n$  system comes from the charge-charge interaction with the OPLS force field and from the permanent electrostatics with AMOEBA for the optimized systems. However, when single point calculations are calculated using the optimized DFT structures, we obtain low correlation coefficients for the adiabatic interaction energy (see Table 3). This can be explained because, by contrast to the previous two systems, here we note a significant discrepancy between the adiabatic and vertical interaction energies in systems with few building blocks, when using either the OPLS non-polarizable force field or the AMOEBA polarizable force field. The structural differences between the complex-forming molecules and the isolated molecules are the primary cause of this disparity. Therefore, if the correlation coefficients are calculated using the vertical interaction energy, better results are obtained for the OPLS and AMOEBA force field (see Table 3).

Like the previous system, the van der Waals contribution is smaller as the number of building blocks increases. We note that optimization of the structures strongly reduces the contribution of van der Waals forces, especially for systems with the fewest number of building

blocks. The results demonstrate that bond stretching term is the primary cause of the observed frustration compared to the systems calculated with the optimized DFT structures. In systems optimized by force fields, similar correlation coefficients can be observed for both bond stretching and angle bending terms.

To explore whether force fields can replicate absolute cooperativity, which arises from many-body interactions, we calculated the vertical interaction energies in dimers for the first four clusters of each studied system. This analysis aimed to determine whether the force fields adhere to the equation (8) or not. For  $n = 1$ , only one dimer is possible. As  $n$  increases, the number of possible dimers also grows. Specifically, for  $n = 2$ , three dimers are possible; for  $n = 3$ , there are six possible dimers; and for  $n = 4$ , there are ten possible dimers. The results of these vertical interaction energies per dimer are presented in Tables 4-6. In each table, we provided the energy for each formed dimer calculated using exchange-correlation functionals, the AMOEBA polarizable force field, and the OPLS and AMBER non-polarizable force fields, as appropriate. We then compared the sum of these individual contributions to the total vertical interaction energy for each of the studied systems.

In Table 4, we show that the total interaction energy in the  $\text{NH}_3(\text{H}_2\text{O})_2$  cluster is -17.18 kcal/mol, while the sum of pairwise interactions is -14.74 kcal/mol using the  $\omega\text{B97X-D/aug-cc-pVDZ}$  level of theory, resulting in an absolute cooperativity of -2.44 kcal/mol. Interestingly, using the AMOEBA force field, a cooperativity of -2.51 kcal/mol is observed. Similarly, for the  $\text{NH}_3(\text{H}_2\text{O})_3$  cluster, we calculated an absolute cooperativity of -6.52 kcal/mol and -6.9 kcal/mol using the  $\omega\text{B97X-D/aug-cc-pVDZ}$  level of theory and the AMOEBA force field, respectively. For  $\text{NH}_3(\text{H}_2\text{O})_4$ , the calculated absolute cooperativity was -8.38 kcal/mol and -8.33 kcal/mol using the  $\omega\text{B97X-D/aug-cc-pVDZ}$  level of theory and the AMOEBA force field, respectively. Conversely, as expected, the OPLS force field showed no difference between the total interaction energy and the sum of individual interactions.

Table 4: Vertical interaction energies and energy decomposition analysis for the  $\text{NH}_3(\text{H}_2\text{O})_2$  system (energies in kcal/mol).

	Vertical Interaction Energy		Energy Decomposition Analysis									
			SAPT(DFT)			AMOEBA			OPLS			
	$\omega$ B97X-D	AMOEBA	Total <sup>1</sup>	Elect <sup>2</sup>	E+I+D <sup>3</sup>	Mult <sup>4</sup>	vdW <sup>5</sup>	Pol <sup>6</sup>	vdW+Pol <sup>7</sup>	q-q <sup>8</sup>	vdW <sup>9</sup>	
<i>(n = 1)</i>												
$\text{NH}_3\text{-H}_2\text{O}$	-7.28	-6.71	-5.86	-11.77	5.91	-8.81	4.27	-2.16	2.10	-7.32	1.38	
<i>(n = 2)</i>												
$\text{NH}_3(\text{H}_2\text{O})_2$	-17.18	-15.37	---	---	---	-19.42	10.87	-6.82	-5.82	-18.36	4.48	
$\text{NH}_3\text{-H}_2\text{O}^{\text{A}}$	-3.01	-2.61	-2.64	-4.68	2.04	-3.12	1.00	-0.48	0.52	-3.30	0.56	
$\text{NH}_3\text{-H}_2\text{O}^{\text{B}}$	-6.86	-5.72	-5.37	-13.67	8.30	-9.66	6.36	-2.41	3.95	-8.05	2.63	
$\text{H}_2\text{O}^{\text{A}}\text{-H}_2\text{O}^{\text{B}}$	-4.86	-4.53	-3.78	-9.56	5.78	-6.63	3.51	-1.42	2.09	-7.01	1.29	
Sum <sup>9</sup>	-14.74	-12.86	-11.79	-27.91	16.12	-19.42	10.87	-4.31	6.56	-18.36	4.48	
<i>(n = 3)</i>												
$\text{NH}_3(\text{H}_2\text{O})_3$	-29.07	-26.80	---	---	---	-33.25	20.87	-14.41	6.45	-32.38	7.41	
$\text{NH}_3\text{-H}_2\text{O}^{\text{A}}$	-1.70	-1.47	-1.62	-1.42	-0.20	-1.23	-0.17	-0.06	-0.24	-1.33	-0.14	
$\text{NH}_3\text{-H}_2\text{O}^{\text{B}}$	-2.37	-2.02	-1.79	-6.04	4.26	-3.60	2.45	-0.86	1.58	-3.98	0.84	
$\text{NH}_3\text{-H}_2\text{O}^{\text{C}}$	-7.17	-5.90	-5.57	-15.83	10.27	-11.30	8.19	-2.79	5.40	-9.08	3.11	
$\text{H}_2\text{O}^{\text{A}}\text{-H}_2\text{O}^{\text{B}}$	-4.99	-4.74	-3.72	-11.20	7.47	-7.75	4.82	-1.81	3.01	-8.08	1.66	
$\text{H}_2\text{O}^{\text{A}}\text{-H}_2\text{O}^{\text{C}}$	-4.80	-4.45	-3.46	-12.12	8.65	-8.21	5.71	-1.94	3.76	-8.60	2.05	
$\text{H}_2\text{O}^{\text{B}}\text{-H}_2\text{O}^{\text{C}}$	-1.52	-1.32	-1.43	-1.26	-7.75	-1.15	-0.12	-0.04	-0.17	-1.31	-0.11	
Sum <sup>9</sup>	-22.55	-19.90	-17.59	-47.87	22.70	-33.25	20.87	-7.51	13.35	-32.38	7.41	
<i>(n = 4)</i>												
$\text{NH}_3(\text{H}_2\text{O})_4$	-38.89	-35.92	---	---	---	-42.72	24.89	-18.09	6.80	-43.08	9.30	
$\text{NH}_3\text{-H}_2\text{O}^{\text{A}}$	-6.10	-5.48	-4.59	-12.84	8.25	-8.73	5.53	-2.29	3.25	-7.69	2.16	
$\text{NH}_3\text{-H}_2\text{O}^{\text{B}}$	-1.57	-1.37	-1.49	-1.31	-0.18	-1.14	-0.17	-0.06	-0.22	-1.39	-0.14	
$\text{NH}_3\text{-H}_2\text{O}^{\text{C}}$	-2.37	-2.07	-2.09	-3.84	1.76	-2.49	0.94	-0.52	0.42	-2.51	0.40	
$\text{NH}_3\text{-H}_2\text{O}^{\text{D}}$	0.34	0.48	0.44	0.66	-0.22	0.83	-0.24	-0.11	-0.35	1.21	-0.06	
$\text{H}_2\text{O}^{\text{A}}\text{-H}_2\text{O}^{\text{B}}$	-4.15	-3.84	-2.59	-13.53	10.94	-8.70	6.89	-2.03	4.86	-8.36	2.58	
$\text{H}_2\text{O}^{\text{A}}\text{-H}_2\text{O}^{\text{C}}$	-2.21	-1.95	-2.08	-1.94	-0.13	-1.68	-0.21	-0.07	-0.28	-2.39	-0.15	
$\text{H}_2\text{O}^{\text{A}}\text{-H}_2\text{O}^{\text{D}}$	-3.95	-4.01	-3.04	-7.53	4.48	-4.92	1.92	-1.01	0.91	-5.95	0.82	
$\text{H}_2\text{O}^{\text{B}}\text{-H}_2\text{O}^{\text{C}}$	-4.37	-3.73	-3.02	-12.39	9.37	-8.30	6.60	-2.03	4.57	-8.63	2.53	
$\text{H}_2\text{O}^{\text{B}}\text{-H}_2\text{O}^{\text{D}}$	-1.73	-1.52	-1.62	-1.43	-0.18	-1.33	-0.14	-0.05	-0.19	-1.81	-0.12	
$\text{H}_2\text{O}^{\text{C}}\text{-H}_2\text{O}^{\text{D}}$	-4.41	-4.11	-3.33	-9.17	5.84	-6.27	3.76	-1.60	2.16	-5.58	1.28	
Sum <sup>9</sup>	-30.51	-27.59	-23.41	-63.32	39.91	-42.72	24.89	-9.75	15.14	-43.08	9.30	

<sup>1</sup> Total SAPT(DFT)    <sup>2</sup> Electrostatics    <sup>3</sup> Exchange + induction + dispersion    <sup>4</sup> Atomic multipoles interactions

<sup>5</sup> Van der Waals + Polarization    <sup>6</sup> Polarization    <sup>7</sup> Van der Waals    <sup>8</sup> Charge-charge interactions    <sup>9</sup> Sum of pairwise interactions

<sup>5</sup> Van der Waals

Table 5: Vertical interaction energies and energy decomposition analysis for the  $\text{Li}^+(\text{H}_2\text{O})_n$  system (energies in kcal/mol).

	Vertical Interaction Energy		Energy Decomposition Analysis									
	M06-2X		SAPT(DFT)			AMOEBA			AMBER			
	AMOEBA	AMBER	Total <sup>1</sup>	Elect <sup>2</sup>	E+I+D <sup>3</sup>	Mult <sup>4</sup>	vdW <sup>5</sup>	Pol <sup>6</sup>	vdW+Pol <sup>7</sup>	q-q <sup>8</sup>	vdW <sup>5</sup>	
$(n = 1)$												
$\text{Li}^+-\text{H}_2\text{O}$	-36.99	-29.88	-32.09	-33.08	0.99	-33.27	12.30	-14.25	-1.95	-41.69	11.81	
$(n = 2)$												
$\text{Li}^+(\text{H}_2\text{O})_2$	-69.02	-64.63	---	---	---	-63.01	21.50	-23.12	-1.61	-78.40	19.12	
$\text{Li}^+-\text{H}_2\text{O}^{\text{A}}$	-36.94	-34.87	-32.08	-32.18	0.10	-32.29	10.81	-13.39	-2.58	-40.45	9.63	
$\text{Li}^+-\text{H}_2\text{O}^{\text{B}}$	-36.94	-34.87	-32.21	-32.18	-0.03	-32.29	10.81	-13.39	-2.58	-40.45	9.63	
$\text{H}_2\text{O}^{\text{A}}-\text{H}_2\text{O}^{\text{B}}$	1.82	1.39	1.35	1.51	-0.16	1.56	-0.12	-0.06	-0.18	2.50	-0.14	
Sum <sup>9</sup>	-72.05	-68.36	-62.94	-62.85	-0.10	-63.01	21.50	-26.85	-5.35	-78.40	19.12	
$(n = 3)$												
$\text{Li}^+(\text{H}_2\text{O})_3$	-94.70	-86.11	---	---	---	-88.81	29.01	-26.31	2.70	-108.87	24.70	
$\text{Li}^+-\text{H}_2\text{O}^{\text{A}}$	-36.84	-34.55	-32.26	-31.57	-0.69	-31.57	9.84	-12.82	-2.98	-39.54	8.32	
$\text{Li}^+-\text{H}_2\text{O}^{\text{B}}$	-36.84	-34.55	-32.15	-31.57	-0.58	-31.57	9.84	-12.82	-2.98	-39.54	8.32	
$\text{Li}^+-\text{H}_2\text{O}^{\text{C}}$	-36.84	-34.54	-32.25	-31.57	-0.68	-31.56	9.83	-12.81	-2.98	-39.53	8.32	
$\text{H}_2\text{O}^{\text{A}}-\text{H}_2\text{O}^{\text{B}}$	2.08	1.68	1.69	1.73	-0.04	1.96	-0.17	-0.11	-0.28	3.24	-0.09	
$\text{H}_2\text{O}^{\text{A}}-\text{H}_2\text{O}^{\text{C}}$	2.08	1.69	1.70	1.73	-0.03	1.96	-0.17	-0.11	-0.28	3.25	-0.09	
$\text{H}_2\text{O}^{\text{B}}-\text{H}_2\text{O}^{\text{C}}$	2.08	1.69	1.70	1.73	-0.03	1.97	-0.17	-0.11	-0.28	3.26	-0.09	
Sum <sup>9</sup>	-104.28	-98.58	-91.57	-89.52	-2.06	-88.81	29.01	-38.77	-9.76	-108.87	24.70	
$(n = 4)$												
$\text{Li}^+(\text{H}_2\text{O})_4$	-114.43	-100.90	---	---	---	-109.27	33.65	-25.28	8.37	-131.12	27.89	
$\text{Li}^+-\text{H}_2\text{O}^{\text{A}}$	-36.41	-33.94	-31.97	-30.62	-1.35	-30.52	8.71	-12.13	-3.42	-38.17	6.90	
$\text{Li}^+-\text{H}_2\text{O}^{\text{B}}$	-36.42	-33.95	-31.87	-30.63	-1.23	-30.53	8.72	-12.14	-3.42	-38.19	6.91	
$\text{Li}^+-\text{H}_2\text{O}^{\text{C}}$	-35.92	-33.32	-31.51	-29.94	-1.57	-29.80	8.49	-12.01	-3.52	-37.54	6.64	
$\text{Li}^+-\text{H}_2\text{O}^{\text{D}}$	-36.18	-33.78	-31.79	-30.47	-1.31	-30.18	8.25	-11.85	-3.60	-37.25	6.36	
$\text{H}_2\text{O}^{\text{A}}-\text{H}_2\text{O}^{\text{B}}$	2.37	1.75	1.88	1.96	-0.08	2.00	-0.16	-0.09	-0.25	2.97	-0.14	
$\text{H}_2\text{O}^{\text{A}}-\text{H}_2\text{O}^{\text{C}}$	1.93	1.75	1.81	1.49	0.32	2.00	-0.11	-0.15	-0.26	3.46	0.16	
$\text{H}_2\text{O}^{\text{A}}-\text{H}_2\text{O}^{\text{D}}$	2.09	1.78	1.89	1.63	0.26	2.05	-0.13	-0.14	-0.28	3.38	0.07	
$\text{H}_2\text{O}^{\text{B}}-\text{H}_2\text{O}^{\text{C}}$	1.94	1.75	1.81	1.50	0.31	2.01	-0.11	-0.15	-0.26	3.46	0.15	
$\text{H}_2\text{O}^{\text{B}}-\text{H}_2\text{O}^{\text{D}}$	2.10	1.78	1.90	1.64	0.26	2.06	-0.14	-0.14	-0.28	3.38	0.06	
$\text{H}_2\text{O}^{\text{C}}-\text{H}_2\text{O}^{\text{D}}$	1.27	1.55	1.52	0.62	0.91	1.63	0.14	-0.22	-0.08	3.39	0.77	
Sum <sup>9</sup>	-133.24	-124.63	-116.31	-112.83	-3.49	-109.27	33.65	-49.01	-15.37	-131.12	27.89	

<sup>1</sup> Total SAPT(DFT)    <sup>2</sup> Electrostatics    <sup>3</sup> Exchange + induction + dispersion    <sup>4</sup> Atomic multipoles interactions    <sup>5</sup> Van der Waals    <sup>6</sup> Polarization

<sup>7</sup> Van der Waals + Polarization    <sup>8</sup> Charge-charge interactions    <sup>9</sup> Sum of pairwise interactions

Table 6: Vertical interaction energies and energy decomposition analysis for the  $F^-(H_2O)_n$  system (energies in kcal/mol).

	Vertical Interaction Energy		Energy Decomposition Analysis																	
	B3LYP	AMOEBA	SAPT(DFT)			AMOEBA			OPLS											
			Total <sup>1</sup>	Elect <sup>2</sup>	E+I+D <sup>3</sup>	Mult <sup>4</sup>	vdW <sup>5</sup>	Pol <sup>6</sup>		vdW+Pol <sup>7</sup>	q-q <sup>8</sup>	vdW <sup>5</sup>								
<i>(n = 1)</i>																				
$F^- - H_2O$	-31.56	-22.91	-20.01	-43.78	15.18	-34.75	30.78	-18.94	11.84	-35.56	15.54									
<i>(n = 2)</i>																				
$F^-(H_2O)_2$	-51.41	-45.75	-38.93	---	---	-58.06	39.14	-26.83	12.31	-59.31	20.38									
$F^- - H_2O^A$	-28.47	-27.19	-20.20	-36.38	10.69	-29.60	19.62	-17.21	2.41	-30.42	10.23									
$F^- - H_2O^B$	-28.47	-27.19	-20.19	-36.38	10.69	-29.60	19.62	-17.21	2.41	-30.42	10.23									
$H_2O^A - H_2O^B$	0.93	0.93	1.46	1.06	-0.22	1.14	-0.11	-0.10	-0.20	1.53	-0.07									
Sum <sup>9</sup>	-56.01	-53.44	-38.93	-71.70	21.17	-58.06	39.14	-34.52	4.61	-59.31	20.38									
<i>(n = 3)</i>																				
$F^-(H_2O)_3$	-67.42	-64.40	-57.97	---	---	-77.19	42.29	-29.50	12.79	-79.40	21.43									
$F^- - H_2O^A$	-26.89	-28.30	-20.47	-32.25	7.90	-26.73	14.23	-15.80	-1.57	-27.70	7.24									
$F^- - H_2O^B$	-26.89	-28.30	-20.47	-32.25	7.90	-26.73	14.22	-15.80	-1.57	-27.70	7.23									
$F^- - H_2O^C$	-26.89	-28.30	-20.47	-32.25	7.90	-26.73	14.22	-15.80	-1.57	-27.70	7.23									
$H_2O^A - H_2O^B$	0.81	0.77	1.14	0.93	-0.23	1.00	-0.13	-0.10	-0.23	1.23	-0.09									
$H_2O^A - H_2O^C$	0.81	0.77	1.14	0.93	-0.23	1.00	-0.13	-0.10	-0.23	1.23	-0.09									
$H_2O^B - H_2O^C$	0.81	0.77	1.14	0.93	-0.23	1.00	-0.13	-0.10	-0.23	1.23	-0.09									
Sum <sup>9</sup>	-78.23	-82.59	-57.97	-93.97	23.03	-77.19	42.29	-47.69	-5.40	-79.40	21.43									
<i>(n = 4)</i>																				
$F^-(H_2O)_4$	-80.74	-80.00	-77.57	---	---	-93.12	40.83	-27.71	13.11	-97.85	20.28									
$F^- - H_2O^A$	-25.95	-28.08	-19.87	-30.25	6.73	-25.23	12.27	-15.12	-2.86	-26.05	6.18									
$F^- - H_2O^B$	-25.95	-28.08	-19.87	-30.25	6.73	-25.23	12.27	-15.12	-2.86	-26.05	6.18									
$F^- - H_2O^C$	-24.85	-28.06	-21.35	-22.77	4.93	-23.25	8.42	-13.23	-4.80	-25.50	4.16									
$F^- - H_2O^D$	-24.85	-28.06	-21.35	-22.77	4.93	-23.25	8.42	-13.23	-4.80	-25.50	4.16									
$H_2O^A - H_2O^B$	0.96	0.96	1.07	1.04	-0.14	1.08	-0.06	-0.06	-0.11	1.11	-0.04									
$H_2O^A - H_2O^C$	0.00	-0.51	0.25	-0.86	0.76	-0.08	-0.15	-0.29	-0.44	0.35	-0.10									
$H_2O^A - H_2O^D$	0.82	0.81	1.04	0.76	-0.16	0.94	-0.07	-0.06	-0.13	1.09	-0.05									
$H_2O^B - H_2O^C$	0.82	0.81	1.04	0.76	-0.16	0.94	-0.07	-0.06	-0.13	1.09	-0.05									
$H_2O^B - H_2O^D$	0.00	-0.51	0.25	-0.86	0.76	-0.08	-0.15	-0.29	-0.44	0.35	-0.10									
$H_2O^C - H_2O^D$	0.93	0.94	1.21	1.00	-0.13	1.04	-0.05	-0.05	-0.10	1.26	-0.04									
Sum <sup>9</sup>	-98.07	-109.78	-77.57	-113.75	24.25	-93.12	40.83	-57.49	-16.66	-97.85	20.28									

<sup>1</sup> Total SAPT(DFT)    <sup>2</sup> Electrostatics    <sup>3</sup> Exchange + induction + dispersion    <sup>4</sup> Atomic multipoles interactions

<sup>5</sup> Polarization    <sup>6</sup> Van der Waals + Polarization    <sup>7</sup> Charge-charge interactions    <sup>8</sup> Sum of pairwise interactions

<sup>9</sup> Sum of pairwise interactions    <sup>5</sup> Van der Waals

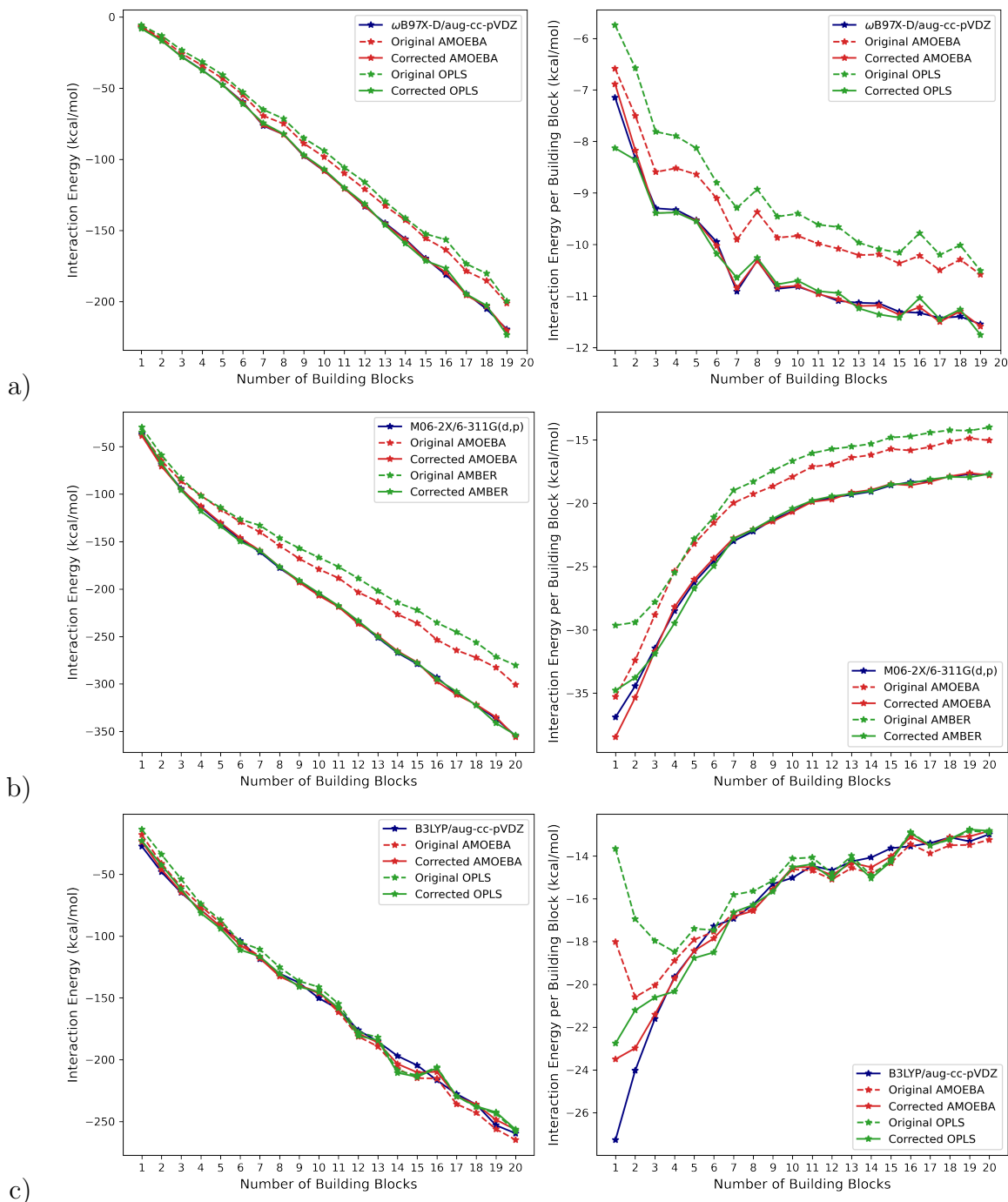


Figure 6: Corrected interaction energies for: a)  $\text{NH}_3(\text{H}_2\text{O})_n$  system.  $y = 1.044x - 0.743$  and  $y = 1.181x + 1.202$  have been used to correct the adiabatic interaction energies for the AMOEBA and OPLS force fields, respectively. b)  $\text{Li}^+(\text{H}_2\text{O})_n$  system.  $y = 2.725x + 0.448$  and  $y = 3.600x + 1.535$  have been used to correct the adiabatic interaction energies for the AMOEBA and AMBER force fields, respectively. c)  $\text{F}^-(\text{H}_2\text{O})_n$  system.  $y = -0.724x + 6.217$  and  $y = -0.564x + 9.661$  have been used to correct the adiabatic interaction energies for the AMOEBA and OPLS force fields, respectively.



By separating the AMOEBA intermolecular interaction energy into atomic multipoles, van der Waals, and polarization contributions, we can see that the absolute cooperativity only arises from polarization. This is because both the interaction between atomic multipoles and van der Waals interactions are the same in both the cluster and the sum of pairwise interactions. To verify the accuracy of the intermolecular interaction calculations, we compared the electrostatic energy of SAPT(DFT) with the interaction of atomic multipoles or charge-charge interactions for the AMOEBA and OPLS force fields, respectively. Since Psi4 only allows for SAPT(DFT) calculations for dimers, we compute these quantities for every possible dimer in the same first four clusters. The contributions of exchange, induction, and dispersion are compared with the van der Waals interactions, and in the case of AMOEBA, with the sum of van der Waals and polarization. For both the AMOEBA and OPLS force fields, the errors in the electrostatic interaction energy and van der Waals interactions, or van der Waals plus polarization in the case of AMOEBA, increase as the system size grows. Both contributions are underestimated, with some canceling each other out. However, the average deviation per dimer is around +3 kcal/mol and -3 kcal/mol for the electrostatic and van der Waals interactions, respectively.

In Table 5, we present the vertical interaction energies per dimer for the  $\text{Li}^+(\text{H}_2\text{O})_n$  system. We calculated an absolute cooperativity of +3.03 kcal/mol for the  $\text{Li}^+(\text{H}_2\text{O})_2$  cluster using the M06-2X/6-311+G(d,p) level of theory. This positive value indicates that the sum of the pairwise interactions is more stable than the total vertical interaction energy in the cluster. Therefore, it represents negative cooperativity. With the AMOEBA force field, we observed a negative cooperativity of 3.73 kcal/mol. For the  $\text{Li}^+(\text{H}_2\text{O})_3$  and  $\text{Li}^+(\text{H}_2\text{O})_4$  systems, we calculated negative cooperativity values of 9.58 and 18.81 kcal/mol using the M06-2X/6-311+G(d,p) level of theory, and 12.47 and 23.73 kcal/mol with the AMOEBA force field, respectively. As we can see, the AMOEBA force field successfully predicts the behavior obtained from electronic structure calculations, although it overestimates negative cooperativity. In the separation of the vertical interaction energy, the results indicate that the

difference in energy arises exclusively from polarization. On the other hand, as expected, the AMBER force field did not exhibit any energy change when calculating the total interactions in the cluster or considering pairwise interactions.

The comparison of electrostatic interactions between the force fields and SAPT(DFT) reveals deviations of less than 1 kcal/mol per dimer for the AMOEBA force field, but deviations of up to -8.6 kcal/mol for the AMBER force field in the smallest cluster. The comparison between the sum of exchange, induction, and dispersion with van der Waals plus polarization (for AMOEBA) shows deviations smaller than -3 kcal/mol. In the case of AMBER, the deviations reach up to 10.8 kcal/mol for the smallest cluster. These results demonstrate that error compensation between electrostatic interactions and van der Waals contributions is more pronounced with the AMBER force field.

In Table 6, we present the vertical interaction energies of the  $F^-(H_2O)_n$  system. Using the B3LYP/aug-cc-pVTZ level of theory, we calculated a negative cooperativity of 4.6 kcal/mol for the  $F^-(H_2O)_2$  cluster, 10.81 kcal/mol for the  $F^-(H_2O)_3$  cluster, and 17.33 kcal/mol for the  $F^-(H_2O)_4$  cluster. In contrast, with the AMOEBA force field, we obtained negative cooperativities of 7.69, 18.19, and 29.78 kcal/mol for the  $F^-(H_2O)_2$ ,  $F^-(H_2O)_3$ , and  $F^-(H_2O)_4$  systems, respectively. Once again, with the OPLS force field, there is no difference between the total vertical interaction calculated in the cluster and the sum of pairwise interactions. Upon reviewing the changes in the different contributions to the vertical interaction energy, we conclude that polarization effects are necessary to reproduce absolute cooperativity in force fields. This is because they depend on the entire system and cannot be accurately estimated by considering pairwise interactions alone.

When we examine the separation of intermolecular interaction energies into their respective contributions for each dimer and compare them to the results obtained using SAPT(DFT), it becomes evident that the AMOEBA and OPLS force fields fail to accurately describe the electrostatic interactions. Specifically, deviations of 9.0 and 8.2 kcal/mol are observed for the  $F^-(H_2O)_2$  cluster when using the AMOEBA and OPLS force fields,

respectively. However, these deviations per dimer decrease as the cluster size increases. Surprisingly, the OPLS force field displays remarkable accuracy in representing van der Waals interactions, with deviations of less than 1 kcal/mol for all the studied dimers. Conversely, the AMOEBA force field exhibits significant deviations, reaching up to -8 kcal/mol for the  $F^-(H_2O)_2$  system.

In order to demonstrate the efficacy of error compensation in obtaining accurate energetics, we performed calculations to assess the errors in adiabatic interaction energies and frustration energies for each cluster (see Figures S7-S9). We then computed trend lines in the form of  $y = mx + b$  equations and utilized these equations to correct the errors in each cluster (see Figures 6). Our results illustrate that the corrected adiabatic interaction energies exhibit a much-improved performance in reproducing the curves obtained through electronic structure methods.

The interaction energy differences between the classical and quantum representations arise from the limitation of force fields to accurately describe many-body effects.<sup>51</sup> Force fields such as AMBER and OPLS can only explicitly account for one- and two-body contributions, and use pre-polarized atom-centered charges to reproduce liquid properties (parametrically including some many-body effects). Conversely, AMOEBA incorporates some approximate many-body contributions through the use of an explicit polarization term. Nevertheless, multipoles and van der Waals interactions are still described solely by two-body contributions. Thus, the results presented herein shed light on the drivers for the observed cooperativity effects by classical potentials previously reported in the literature.

## Conclusions

Our findings demonstrate the essential role of polarization effects in qualitatively reproducing what we refer to as absolute cooperativity. This refers to the energy gain or loss observed when calculating the total interaction energy within a given cluster, which cannot

be accounted for by simply summing up pairwise interactions. In other words, it requires the calculation of many-body interactions. Specifically, only the AMOEBA polarizable force field was capable of capturing both positive and negative instances of absolute cooperativity. In contrast, the OPLS and AMBER force fields failed to exhibit any form of absolute cooperativity due to their limited consideration of contributions beyond pairwise interactions.

However, in this work we show that polarizable and non-polarizable force fields, can reproduce the previously examined relative adiabatic interaction energy achieved using Density Functional Theory. Our findings suggest that the primary factors responsible for imitating the relative cooperativity are the electrostatic interactions. Nevertheless, our results offer valuable insights into the existence of an error compensation mechanism when comparing SAPT(DFT) interaction energies with electrostatic and van der Waals interactions in non-polarizable force fields, or van der Waals interactions combined with polarization in polarizable force fields. The interaction energy errors can be explained in terms of the limitations of force fields in precisely representing the energies involving many-body interactions. Non-polarizable force fields like AMBER and OPLS only explicitly consider one and two-body contributions and parametrically include some many-body effects through fitting to bulk properties, while AMOEBA includes some aspects of many-body interactions through polarization. However, multipoles and van der Waals interactions in these force fields are still based solely on two-body contributions. The error compensation mechanism provides insights on the reasons why previous studies with non-polarizable force fields imitate cooperative effects.

On the other hand, frustration is a different phenomenon that arises from alterations in the internal structure of molecules, with the bond stretching term playing the main role in optimized DFT structures and a combination of bond stretching and angle bending terms in optimized FF structures. Our results indicate that whether optimized structures with force fields are used or not, it has an impact on the individual contributions. Our finding can contribute to the development of advanced force fields.

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## Supporting Information Available

Single-point and optimized adiabatic and vertical interaction energies, comparison between DFT and force field geometries, root mean square deviation for optimized structures, adiabatic interaction and frustration energy errors, and single point and optimized structures in tinker format are available in the supporting information.

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