

1 Concerted effects of local and nonlocal plasmons on
2 the broadband nonlinear optical response in tip-
3 enhanced nanophotonics

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11 KEYWORDS: tip-enhanced second harmonic generation, near-field optics, plasmonic
12 nanocavity, nonlinear nanophotonics, plasmonics

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16 ABSTRACT: We report critical impacts of local and nonlocal geometries of plasmonic tips on the
17 broadband nonlinear optical responses in tip-substrate nanocavities. Using gold tips with varied
18 geometries, we demonstrated for the first time that not only the nanometer-scale sharpness of tip
19 apices but also the micrometer-scale geometry of tip shafts directly affects the enhancement
20 properties of second-harmonic generation over the visible-to-infrared wavelength range.
21 Numerical simulations of the tip-substrate plasmonic field revealed concerted contributions from
22 spatially nonlocal and local plasmonic modes. Micrometer-scale tip shafts enable the excitation of
23 nonlocal plasmonic modes throughout the tip, enhancing near-to-mid-infrared incoming light.
24 Subsequent radiation of visible-to-near-infrared second harmonics is boosted by localized
25 plasmons at the nanogap. Based on the agreement between experiments and calculations, our
26 results indicate the importance of nanometer- and micrometer-scale geometrical engineering of
27 plasmonic tips and provide a firm basis to understand and finely manipulate nonlinear optical
28 phenomena in tip-substrate nanocavities.

29

30 Light confined by tip-substrate plasmonic nanocavities provides site-specific information
31 on physical properties at the molecular/atomic scale. When combined with scanning probe
32 microscopy, the outstanding ability of nanocavities to shrink light beyond the diffraction limit
33 renders them highly attractive for nanoscale photonics. In recent decades, a considerable number
34 of studies have been conducted using this tip enhancement technique. Although linear optical
35 responses (e.g., light scattering^{1,2} and photoluminescence^{3,4}) are a major focus in this field, several
36 meaningful attempts at nanoscale detection of nonlinear optical processes have been made in
37 recent years.⁵ Sufficient sensitivity and spatial resolution have been demonstrated for second-

38 harmonic generation,⁶⁻¹² sum-frequency generation,^{7,11} coherent anti-Stokes Raman scattering,¹³⁻
39 ¹⁶ and nonlinear four-wave mixing.^{11,17,18} Further development of such tip-enhanced nonlinear
40 optical techniques will promote a deeper understanding of correlated chemical and topographic
41 information with ultimate spatial and temporal resolution.

42 The manipulation of tip-enhanced nonlinear optical effects and their application to the
43 spectroscopic analysis of materials requires a fundamental understanding of the nonlinear optical
44 properties of tip-substrate nanocavities. Particularly, the optical wavelength range over which tip
45 enhancement works effectively must be considered. Nonlinear optical processes are often
46 accompanied by drastic frequency conversion between incoming and outgoing light. Therefore, a
47 spectrally broad plasmonic enhancement that can simultaneously affect such separated frequencies
48 is required to efficiently enhance nonlinear optical phenomena.¹⁹⁻²¹ Characterizing and exploiting
49 the operating wavelength range of field enhancement is therefore essential for controlling
50 nonlinear optical processes in tip-substrate nanocavities.

51 Despite such fundamental importance, there has been no conclusive studies on broadband
52 nonlinear optical responses in tip-substrate nanogaps. Although most studies have given basic
53 demonstration of tip-enhanced nonlinear optics as a nanoscale spatial imaging technique, little
54 effort has been devoted to characterizing the optical properties of tip-substrate nanocavities in the
55 spectral domain. Recently, tip-enhanced second-harmonic generation (TESHG) in the visible-to-
56 infrared range was investigated for specific 2D semiconductors.¹² However, owing to the exciton
57 absorption, the excitonic resonance enhancement dominated the observed spectral features of
58 TESHG. Therefore, the plasmonic nonlinear optical responses intrinsic to the tip-substrate
59 nanocavities in the broad wavelength range remain to be fully understood.

60 In this Letter, we for the first time investigate the inherent SHG response of a tip-substrate
61 nanocavity over a visible-to-infrared broad wavelength range of 650–2000 nm. By performing
62 systematic experiments using tips with different geometries and a metallic substrate free from
63 electronic resonance effects, we found that not only the nanometer-scale but also the micrometer-
64 scale structure of tips has significant impact on the nonlinear optical responses in the nanogap over
65 a broad wavelength range. Based on finite-difference time-domain (FDTD) simulations of
66 plasmonic fields incorporating realistic tip geometries, we reveal that this geometrical effect of the
67 tips is closely related to two types of plasmonic modes with distinct spatial scales. Micrometer-
68 scale tip shafts play critical roles in trapping and enhancing infrared excitation pulses through
69 supporting collective oscillation of electrons throughout the tip, which can be regarded as nonlocal
70 plasmonic modes. Subsequently, localized nanosized plasmons excited at the nanoscale tip apexes
71 predominantly boost the radiation of second-harmonics in the visible range. These micrometer-
72 and nanometer-scale geometrical effects of the tips jointly enable the enhancement of the nonlinear
73 optical processes encompassing the visible-to-infrared broadband spectral region.

74 Figure 1a shows the experimental setup. To form a tip-substrate nanocavity, we employed
75 a scanning tunneling microscope (STM) unit placed inside a UHV chamber (UNISOKU,
76 USM1400SA-TL01). The second-order nonlinear optical signal was generated by irradiating a tip-
77 substrate nanocavity with infrared excitation pulses (300 fs) at a high repetition rate (50 MHz).
78 Plasmonic STM tips were fabricated by electrochemically etching gold wires. Typical scanning
79 electron micrographs of a fabricated tip are shown in Figures 1b and c. We denote this tip as tip
80 #1 for later discussion. Note that based on previous work,²² we can reproducibly fabricate tips with
81 smooth shafts, minimal roughness, and apexes with sub-micron scale curvature radii, as shown in
82 Figures 1b and c.

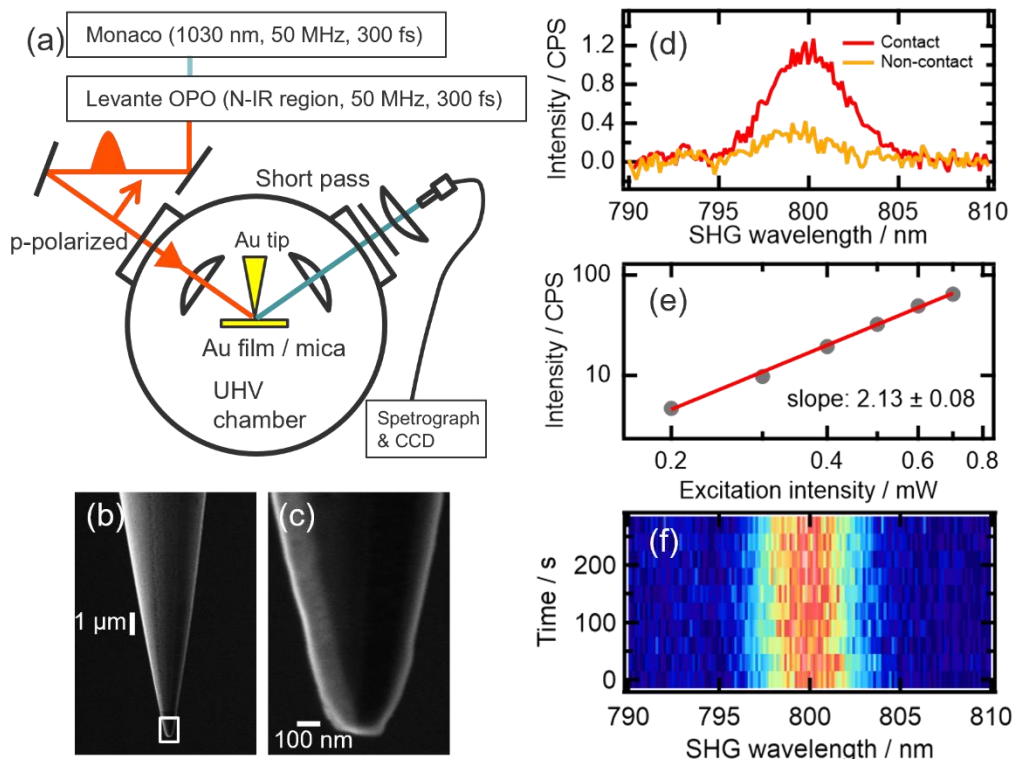


Figure 1. (a) Schematic representation of our experimental setup for TESHG measurement. (b) Scanning electron micrograph of the Au tip. (c) Zoomed-in view of the white square region in (b). (d) Spectrally resolved SHG signals obtained with (red) and without (orange) tunneling contact. (e) A logarithmic plot of the excitation power dependence of the spectrally integrated TESHG intensity (gray filled circles). The red line represents a power fit to the corresponding data points. (f) Time series of TESHG spectra measured consecutively with an excitation power of 0.7 mW. The acquisition time for each spectrum was 30 s.

83 We chose an atomically flat, clean Au(111) surface with wide terraces as a substrate to
 84 form a nanogap. Nanocavities formed between well-defined smooth gold tips and a substrate are
 85 suitable platforms for investigating the intrinsic nonlinear optical response of nanocavities, free
 86 from the influence of electronic resonances. The edge of the interband transition of bulk gold (5d
 87 \rightarrow 6sp) is located at around 2.3 eV (539 nm),²³ below which no appreciable electronic transitions

88 of the bulk exist. Moreover, previous studies on scanning tunneling spectroscopy for clean gold
89 substrates²⁴⁻²⁶ confirmed that gold possesses no surface states below 3.5 eV (longer than 354 nm).
90 Owing to the absence of such surface states or bulk electronic transitions in a certain energy range,
91 we are able to disregard the large electronic-resonance-assisted optical enhancement effects by
92 carefully choosing the range of the excitation—and hence radiation—wavelength. In this context,
93 the center wavelength of incident pulses was scanned from 1300 nm to 2000 nm, resulting in SHG
94 output between 650 nm and 1000 nm. These wavelengths are off-resonant with the inherent
95 electronic transitions of gold; we can therefore focus on the intrinsic nonlinear optical responses
96 in the tip-substrate nanocavity.

97 Signals were recorded when (i) the tip and the substrate were in tunneling contact regime
98 and (ii) the tip-substrate distance was elongated by 30 nm. Note that the signals obtained in
99 situation (ii) correspond to far-field SHG without plasmonic enhancement effects. Figure 1d shows
100 the typical SHG spectra for these two situations. The SHG intensity increased in the tunneling
101 contact regime. This is because the optical enhancement effect was present when a plasmonic
102 nanocavity was formed between the substrate and the apex of the tip. In all experimental results
103 shown below, the far-field signals obtained in situation (ii) were subtracted from the signals in
104 situation (i), which contained both near- and far-field contributions. This allowed us to focus on a
105 pure near-field signal.

106 Signal stability in tip-enhanced nanophotonics is vulnerable to the atomistic structural
107 fluctuations of a plasmonic nanocavity.²⁷ Such fluctuations can be promoted by the excessive peak
108 power density of excitation pulses.^{28,29} To perform stable experiments, the threshold of the
109 excitation intensity above which signals become unstable must be carefully ascertained.
110 Considering this, we measured TESHG intensity by varying the excitation power (Figure 1e).

111 Below 0.8 mW, the intensity of the TESHG signal scaled quadratically, as is generally expected
112 for second-order nonlinear optical processes. Within this power range, the TESHG intensity
113 remained almost constant for over 300 s (Figure 1f). In contrast, when the power was increased to
114 1 mW, the TESHG intensity started to fluctuate and deviated from the quadratic dependence
115 (Figure S1). These results indicate that as long as the excitation power is kept sufficiently low (\leq
116 0.7 mW), the output of TESHG signal is stable without any appreciable signal fluctuations.

117 To investigate the spectral properties of the TESHG, we tuned the center wavelength of the
118 incident pulses and monitored the variation in the TESHG spectra. The excitation intensity was
119 kept low and constant (0.3 mW) over the entire swept-wavelength range. Figure 2 shows a series
120 of TESHG spectra and their peak-top intensities measured at various excitation wavelengths using
121 the tip #1 shown in Figures 1b and c. TESHG output was observed over an excitation wavelength

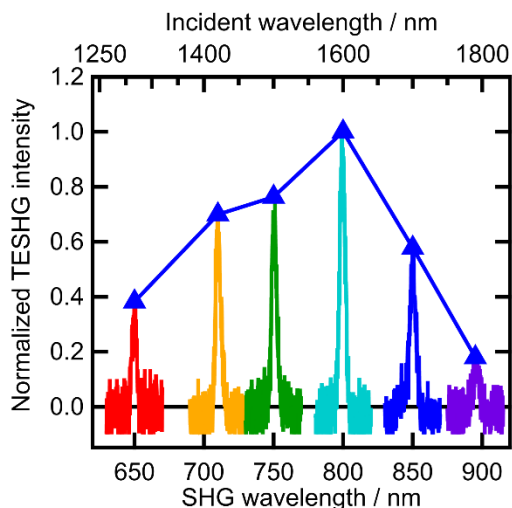


Figure 2 (Colored spectra) TESHG spectra obtained by tuning the center wavelength of incident pulses. (Blue triangles) Variation of the TESHG intensities at the peak-top of the individual spectra. All data in the figure are normalized by the peak-top value obtained when the excitation wavelength is 1600 nm and plotted as a function of SHG wavelengths (bottom axis) and corresponding incident beam wavelengths (top axis).

122 of several hundred nanometers. Because the scanned wavelength range is detuned from any
 123 electronic transitions of gold, the wavelength dependence of the second-order nonlinear
 124 susceptibility ($\chi^{(2)}$) of gold should be small. Hence, the observed dependence is considered to
 125 originate from other factors not discussed yet.

126 Additional experiments using gold tips with different structures showed that the nonlinear
 127 optical properties of nanogaps are highly influenced by tip geometry. To demonstrate this, we
 128 fabricated a gold tip (tip #2) with a macroscopic shaft shape similar to that of tip #1 but a sharper
 129 tip apex (Figures 1b and c), as shown in Figures 3a and b. The intensity of TESHG from this tip
 130 sharply declined with an increase in the input infrared wavelength, as shown in Figure 3c, which

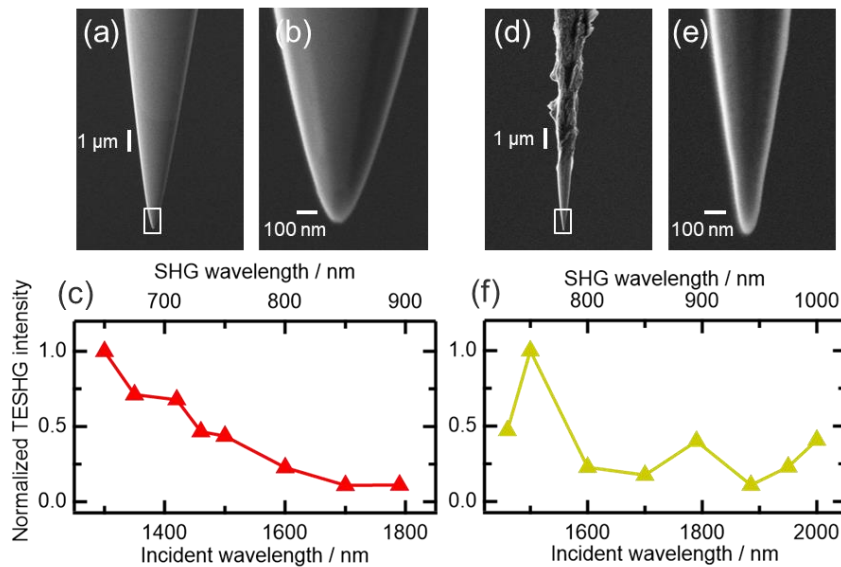


Figure 3. Scanning electron micrographs of (a, b) tip #2 and (d, e) #3. Zoomed-in views of white square regions in (a) and (d) are shown in (b) and (e), respectively. (c, f) The intensities of TESHG obtained for (c) tip #2 and (f) #3. Data are normalized by their maximum values and plotted as a function of the center wavelengths of the incident beams (bottom axis) and corresponding SHG wavelengths (top axis).

131 is in stark contrast to the result for tip #1 (Figure 2). These results clearly indicate the critical
132 importance of nanoscale tip sharpness for plasmonic nonlinear optical properties.

133 In addition to the nanometer-scale tip apexes, micrometer-scale structure of the tip shafts
134 also has a significant impact on nonlinear optical responses from tip-substrate nanocavities. As
135 shown in Figure 3f, the tip with micrometer-scale surface roughness introduced on the shaft (tip
136 #3, Figure 3d) exhibited drastically distinct nonlinear optical behavior. Although the surface
137 around the apex of tip #3 was smooth (Figure 3e) and the bumps on the shaft were separated from
138 the apex by as much as $\sim 3 \mu\text{m}$, a multimodal structure emerged in the spectral profile of the
139 TESHG from the nanogap (Figure 3f). This indicates that in addition to the nanometer-scale
140 curvature of the tip apex, the micrometer-scale surface geometry of the shaft also determines the
141 spectral properties of SHG enhancement inside nanocavities. The dependence on tip geometry
142 suggests the existence of two different plasmonic effects: spatially local effects that occur at
143 nanometer-scale tip apexes and nonlocal effects governed by micrometer-scale tip shafts.

144 To gain detailed insights into these local and nonlocal effects, we provide an overview of
145 the basic concepts of TESHG. The TESHG process consists of three steps: (i) field enhancement
146 at the nanogap, (ii) excitation of second-order nonlinear polarization, and (iii) radiation of second-
147 harmonics. First, the incident laser ($E_0(\omega)$) is plasmonically enhanced at the nanogap. We define
148 the ratio of the resulting enhanced field ($E_{gap}(\omega)$) to the incident field as the enhancement factor
149 $K_{gap}(\omega)$:^{30,31}

$$150 \quad E_{gap}(\omega) = K_{gap}(\omega)E_0(\omega). \quad (1)$$

151 This enhanced field induces the second-order nonlinear polarization $P^{(2)}(2\omega)$:

152
$$P^{(2)}(2\omega) = \chi^{(2)}(2\omega; \omega, \omega)E_{gap}^2(\omega) = \chi^{(2)}(2\omega; \omega, \omega)K_{gap}^2(\omega)E_0^2(\omega), \quad (2)$$

153 where $\chi^{(2)}(2\omega; \omega, \omega)$ is the second-order nonlinear susceptibility. The induced $P^{(2)}(2\omega)$ then
 154 emits second harmonics ($E_{TESHG}(2\omega)$):

155
$$E_{TESHG}(2\omega) \propto L_{gap}(2\omega)P^{(2)}(2\omega), \quad (3)$$

156 where $L_{gap}(2\omega)$ is the radiation efficiency of TESHG from $P^{(2)}(2\omega)$.³¹ The resultant TESHG
 157 intensity ($I_{TESHG}(2\omega)$) is given by

158
$$I_{TESHG}(2\omega) \propto |E_{TESHG}(2\omega)|^2 \propto |L_{gap}(2\omega)|^2 |\chi^{(2)}(2\omega; \omega, \omega)|^2 |K_{gap}(\omega)|^4 I_0^2(\omega), \quad (4)$$

159 where $I_0(\omega)$ is the intensity of the incident light and the relationship of $I_0(\omega) \propto |E_0(\omega)|^2$ has
 160 been applied. Note that $I_0(\omega)$ was kept constant (0.3 mW) within the wavelength range swept in
 161 this experiment. Moreover, because both incident excitation light and emitted SHG light are non-
 162 resonant with electronic transitions of gold, we can assume that the frequency dependence of
 163 $\chi^{(2)}(2\omega; \omega, \omega)$ is small.^{32–34} Therefore, the overall frequency profile of $I_{TESHG}(2\omega)$ is
 164 approximated as

165
$$I_{TESHG}(2\omega) \propto |K_{gap}(\omega)|^4 |L_{gap}(2\omega)|^2. \quad (5)$$

166 This indicates that the observed TESHG responses for various tips (Figure 2 and 3) can be
 167 generally described by considering the tip dependence of local and nonlocal effects in $K_{gap}(\omega)$
 168 and $L_{gap}(2\omega)$. To provide microscopic insights into the tip-dependent TESHG responses in wide
 169 frequency (wavelength) range, we quantitatively analyzed these two factors using FDTD method
 170 (See Supporting Information for details of the calculation procedures).

171 We start by modeling an STM tip as a nanosphere without a shaft^{35–40} (Figure 4a) to focus
 172 on the local plasmonic effects that occur at the nanogap between the substrate and tip apexes.
 173 Figures 4b and c show the wavelength dependence of K_{gap} and L_{gap} calculated for the

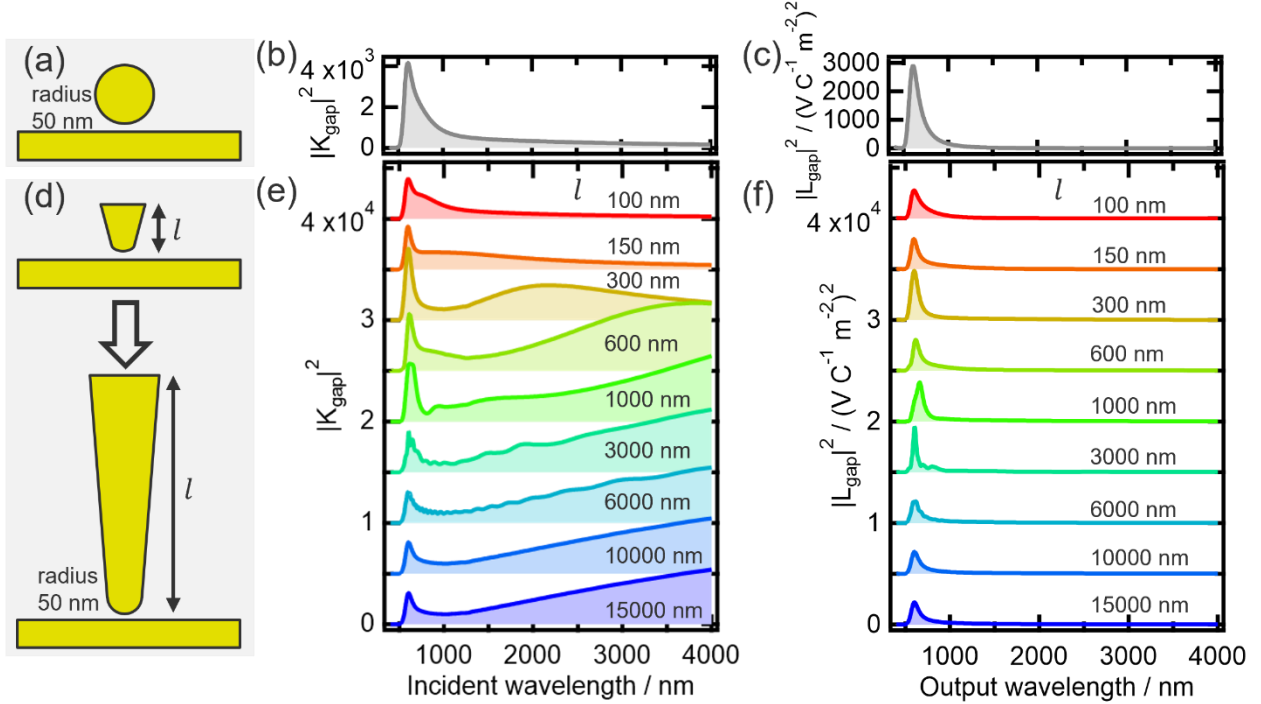


Figure 4 (a) Schematic representation of nanosphere-substrate configuration. The radius of the nanosphere is 50 nm. (b) $|K_{gap}|^2$ and (c) $|L_{gap}|^2$ spectra of the nanogap in a nanosphere-substrate system calculated through the FDTD method. (d) Schematic representation of tip-substrate configuration. A rounded cone tip with a 30° opening angle and 50 nm radius of curvature was adopted in the calculation. The tip length l was changed from 100 nm to 15000 nm. (e) and (f): Tip-length dependent (e) $|K_{gap}|^2$ and (f) $|L_{gap}|^2$ spectra of a tip-substrate nanocavity calculated through the FDTD method. The tip lengths are indicated in the figures and the tip-substrate distance d was taken as 1 nm for all these calculations.

174 nanosphere-substrate system, respectively. The spectra only exhibit a single band in the visible
 175 region, indicating that only visible light is enhanced in the nanosphere-substrate system. This has
 176 been proven to be a typical signature of the gap-mode plasmon excitation localized between the
 177 nanogap.^{37,41-43} Conversely, both of the K_{gap} and L_{gap} values in the infrared region seem to be too

178 small to describe the enhancement of infrared-light induced TESHG. This implies that micrometer-
179 scale tip shafts, which were not considered in the nanosphere-substrate system, play an important
180 role in the enhancement of the infrared region.

181 We then investigated the influence of macroscopic shafts of cone-shaped tips (Figure 4d).
182 Although short tips ($l \leq 150$ nm) exhibit enhancement limited to the visible range, tips with
183 macroscopic shafts (particularly $l \geq 600$ nm) extend the spectral range of the field enhancement
184 to the near- and even mid-infrared region (Figure 4e). The drastic enhancement in the infrared
185 region is a clear manifestation of the nonlocal effects caused by the tip shafts. This can be attributed
186 to the so-called antenna effect caused by the collective oscillation of electrons over the entire tip
187 (See Supporting Information for details).⁴⁴⁻⁴⁷ In contrast, in the radiation process, this nonlocal
188 effect is not pronounced. As shown in Figure 4f, efficient radiation occurs only in the visible region
189 regardless of the tip length l . Although the tip length causes slight differences in the strength and
190 shape of the L_{gap} spectra, the wavelength range of efficient radiation from nanocavities is
191 predominantly determined by gap-mode plasmons.

192 The spectral behaviors of K_{gap} and L_{gap} in long tips are key to understand the mechanism
193 of TESHG. The broad enhancement of incident light in the near-to-mid-infrared region (K_{gap}) and
194 relatively narrow radiation efficiency in the visible-to-near-infrared region (L_{gap}) encompassed
195 the excitation (1300–2000 nm) and SHG radiation (650–1000 nm) wavelength ranges in our
196 experiments, respectively. This indicates that local and nonlocal effects jointly contribute to
197 TESHG; the nonlocal plasmonic response over the micrometer-scale tip shafts enables the
198 enhancement of incident infrared excitation pulses, while the local gap-mode plasmons effectively
199 intensify the radiation of second harmonics.

200 As both nanometer-scale tip apexes and micrometer-scale tip shafts critically influence the
201 TESHG process, our results suggest that controlling the geometries of these domains in tips should
202 enable us to actively manipulate the nonlinear optical properties of the tip-substrate nanocavities.
203 In this regard, tip tuning through varying tip sharpness (tips #1 and #2) and introducing surface
204 roughness on the shaft (tip #3) can be regarded as first-step demonstrations of the geometrical
205 engineering of tip-enhanced nonlinear optical processes. To examine the specific effects of such
206 structural modulation, we again performed an FDTD simulation using the realistic tip geometries
207 of tips #1, #2, and #3 (Figures 5a–c) obtained from their scanning electron micrographs shown in
208 Figures 1 and 3.

209 The variation in the TESHG intensity induced by changing the nanometer-scale tip
210 sharpness (tips #1 and #2) can be understood in terms of gap-mode plasmon tuning. As shown in
211 Figures 5d and e, in the range $\lambda_{2\omega} \leq 1000$ nm, the sharper tip (tip #2) has a higher-energy gap-
212 mode resonance; the resonance peak for tip #1 is in the experimentally scanned SHG wavelength
213 range (blue-shaded area) while the peak for tip #2 is blue-shifted from there. This sharpness
214 dependence of resonance energy is consistent with the previous reports on STM luminescence⁴⁸,
215 tip-enhanced Raman scattering,⁴⁹ and theoretical calculations of plasmonic field^{41,42,46} reporting
216 that a smaller apex can support higher-energy gap-mode plasmons. Reflecting these spectral
217 structures, significant differences in the overall wavelength dependence of the TESHG intensity
218 emerge between the two tips (Figures 5g and h): a single broad peak structure for tip #1 and a
219 monotonical decrease for tip #2. Notably, these behaviors qualitatively agree with the experimental
220 results for tips #1 and #2 (Figures 2 and 3c). This demonstrates the importance of tuning the local
221 nanometer-scale apexes on the nonlinear optical properties of tip-substrate nanocavities.

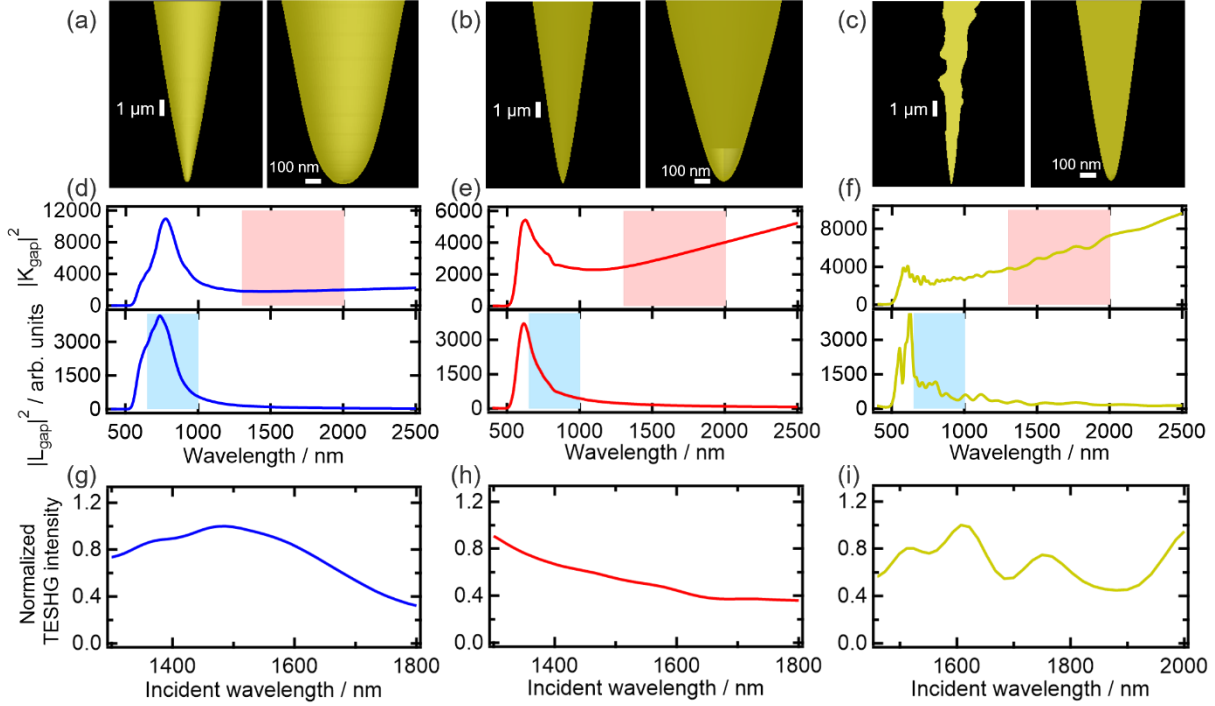


Figure 5 (a)-(c): Structures of (a) tip #1, (b) tip #2, and (c) tip #3 used in the FDTD simulation, which were depicted by tracing the outlines of the scanning electron micrographs shown in Figure 3. The scale bar lengths for left and right panels are 1 μm and 100 nm, respectively. (d)-(f): $|K_{gap}|^2$ (upper panels) and $|L_{gap}|^2$ (lower panels) spectra calculated by using realistic tip geometries for (d) tip #1, (e) tip #2, and (f) tip #3. The excitation (ω) and radiation (2ω) wavelength ranges swept in our experiment are indicated by the red and blue shaded areas, respectively. (g)-(i): The excitation wavelength–dependence of the TESHG intensity calculated by Eq. 5. (g), (h), and (i) show the results for tip #1, tip #2, and tip #3 respectively.

222 The introduction of surface roughness on the shaft (tip #3) has a more complicated
 223 influence. The roughness induces several irregular antenna-modes that are absent in the smooth
 224 tips, giving rise to a complex oscillatory structure in the K_{gap} and L_{gap} spectra (Figure 5f). The
 225 resultant wavelength dependence of the TESHG intensity thus exhibits an irregular shape (Figure
 226 5i), which qualitatively captures the characteristics of the observed TESHG behavior for tip #3

227 (Figure 3f). This indicates that micrometer-scale processing of tip shafts can be used to drastically
228 modulate the nonlinear optical responses at the nanogap.

229 The consistency between the experimental and simulated results also indicates that when
230 exact nanometer-scale and micrometer-scale tip geometries are given, we can generally predict the
231 plasmonic nonlinear optical properties of tip-substrate nanocavities over a wide wavelength range.
232 This predictability allows optimization of tips by computational design for the efficient
233 enhancement of nonlinear optical processes. More precise modulation of local and nonlocal tip
234 geometries by nanoscale adjustments of the apex curvature and grooving patterns on the tip shafts
235 is a key for intentionally controlling nonlinear optical properties. Such fine control of tip
236 geometries can be achieved by exploiting more sophisticated tip processing technologies, such as
237 focused ion beam processing.⁵⁰ Based on the present work, our forthcoming study on the interplay
238 between theoretical modeling and high-level tip fabrication techniques will further accelerate the
239 development of tip-enhanced nonlinear optics.

240 In summary, we showed that the local and nonlocal geometries of plasmonic tips have a
241 prominent influence on the visible-to-infrared nonlinear optical responses in tip-substrate
242 nanocavities. TESHG measurements with structurally tuned tips revealed the critical roles played
243 by nanosized tip apexes and macroscale tip shafts in the broadband enhancement processes of
244 nonlinear optical phenomena. These structural effects can be understood by the contributions of
245 local gap-mode and nonlocal antenna-mode plasmons; micrometer-scale tip shafts promote the
246 collective oscillation of electrons throughout the tip (antenna-mode), which enhances the incoming
247 infrared field, while local gap-mode plasmons intensify the radiation of second harmonics in the
248 visible domain. We verified that the concerted contributions of these local and nonlocal effects are
249 the origin of the enhancement of nonlinear optical phenomena ranging in visible-to-infrared

250 broadband wavelength region. Based on this understanding of the tip-enhancement mechanism,
251 our experimental results for the differently structured tips were successfully described. This will
252 serve as a firm basis for more precise nano- and micrometer-scale tip engineering to finely
253 manipulate nonlinear optical processes at the nanogap.

254

255 ASSOCIATED CONTENT

256 **Supporting Information.**

257 The Supporting Information is available free of charge.

258 Methods, threshold of excitation intensity, and discussion on the non-local effects of tip shafts
259 (PDF)

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278 **Notes**

279 The authors declare no competing financial interest.

280 **ACKNOWLEDGMENT**

281 The authors would like to thank Prof. Maki Kawai and Prof. Toshihiko Yokoyama for their great
282 support in starting up this project, Ekuko Nohno and Dr. Hikaru Saito for developing the
283 fabrication method of the Au tips at an early stage of the project, and the Equipment Development
284 Center of Institute for Molecular Science for technical assistance. We also thank Hiroko Yoshino
285 and Prof. Takashi Kumagai for helpful advice on STM operation and tip-forming, and Prof.
286 Akihito Ishizaki for allowing us to use a computer cluster of his group. This work was supported
287 by JST-PRESTO JPMJPR1907; JST-CREST JPMJCR22L2; JSPS KAKENHI Grant-in-Aid for
288 Scientific Research (A), No. 19H00865, and 22H00296; Grant-in-Aid for Research Activity Start-
289 up No. 19K23640; Grant-in-Aid for Early-Career Scientists, No. 20K15236; Grant-in-Aid for
290 JSPS Fellows No. 22J01438; CASIO SCIENCE PROMOTION FOUNDATION No. 38-06; and
291 Research Foundation for Opto-Science and Technology.

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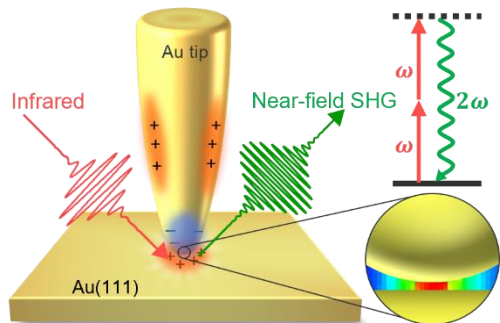
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