

Materials discovery for high-temperature, clean-energy applications using graph neural network models of vacancy defects and free-energy calculations[†]

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We present a graph neural network modeling approach that fully automates the prediction of the DFT-relaxed vacancy formation enthalpy of any crystallographic site from its DFT-relaxed host structure. Applicable to arbitrary structures with an accuracy limited principally by the amount/diversity of the data on which it is trained, this model accelerates the screening of vacancy defects by many orders of magnitude by replacing the DFT supercell relaxations required for each symmetrically unique crystal site. It can thus be used off-the-shelf to rapidly screen 10,000s of crystal structures (which can contain millions of unique defects) from existing databases of DFT-relaxed crystal structures. This modeling approach therefore provides a significant screening and discovery capability for a plethora of applications in which vacancy defects are the primary driver of a material’s utility. For example, by high-throughput screening the Materials Project’s metal oxides, we rapidly “re-discover” and identify new high potential candidate materials for hydrogen generation via solar thermochemical water splitting and energy storage, for CO₂ conversion via reverse water gas shift chemical looping, and for cathodes in solid oxide fuel cells. Thermodynamic modeling on the basis of the high-throughput screening results allows us to connect the predicted defect energies to high temperature process conditions relevant to the different application areas, and we extract the reduction entropies as an additional selection criterion for high-performance materials. Further model development and accumulation of additional training data will only serve to expand the significant utility of this generalizable defect model to solving materials discovery problems in clean energy applications and beyond.

1 Introduction

High-accuracy calculations of vacancy defect formation enthalpies elucidate the primary and critical figure of merit needed to assess a material’s utility across a large variety of applications. These can range anywhere from catalysis (e.g., oxides for water splitting¹⁻³), to degradation resistance in extreme environments (e.g., radiation hardness of transition metal dichalcogenides^{4,5}), to neuromorphic computing (e.g., tuning metal-to-insulator transition with oxygen vacancy formation^{6,7}), to multiferroics (e.g., oxygen vacancy induced magnetic phase transitions⁸).

Density functional theory (DFT) is the method of choice to compute these vacancy formation enthalpies in a high throughput fashion. However, given the need for supercell construction, atomic force relaxation, and the general presence of multiple non-equivalent atomic sites, the computational effort of defect calculations far exceeds that of the computation of the ideal defect-free material in the primitive cell. Thus, explicit DFT defect calculations exist so far only for a small fraction of the O(100) compounds contained in existing computational databases like the Materials Project (MP),^{9,10} Open Quantum Materials Database (OQMD),¹¹ NREL Materials Database (NRELMatDB),¹²⁻¹⁴ Joint Automated Repository for Various Integrated Simulations (JARVIS),¹⁵ and the Quantum Point Defect database (QPOD).¹⁶ Additional, potentially combinatorial, complexity arises from the desire to predict defect behavior in non-ideal materials, e.g., in the presence of atomic site disorder. A

successful surrogate modeling approach that avoids the cost requirements of DFT is therefore critical in order to efficiently facilitate materials discovery efforts in these applications.

Previous efforts to predict vacancy formation enthalpies span various methods and material classes within which the models are applicable. Notable examples include modeling vacancy formation enthalpy using a simple hand-derived or machine learning (ML) model based on hypothesized important features¹⁷⁻²¹ and descriptor derived properties to train ML regression models for defect property prediction in semiconductors.^{22,23} For 2D materials consisting of TMDs, hexagonal boron nitride, and other selected wide band gap 2D materials, similar utilization of hand-engineered features and random forests predicted vacancy defect formation enthalpies.²⁴ These examples provide highly useful models in specific situations by capitalizing on physical intuition regarding important material descriptors. But they do not provide a generalized solution that (1) automatically predicts the vacancy formation enthalpy of any crystal site in any material class and (2) negates the need for manual feature-engineering of material descriptors.

Various deep learning techniques, such as graph or convolutional neural networks, can circumvent such limitations. Rather than requiring the hand-crafting of an input feature vector to describe a training example, the model directly learns a feature representation from iterative convolutions and non-linear transformations of the input data, i.e. a graph representation of the crystal structure. The general success of graph neural networks at performing property prediction on crystal structures is evident from their recent explosion in popularity across a host of materials science applications.²⁵⁻³⁶ In this work, we extend the graph neural network concept for directly predicting vacancy defect formation enthalpies (abbreviated dGNN for short). The only re-

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60 quired input is the non-defected, DFT-relaxed host structure, and
 61 the model output is the predicted relaxed vacancy formation en-
 62 thalpy of any site in the structure. The surrogate model therefore
 63 replaces the need to do an expensive DFT supercell relaxation
 64 for each symmetrically nonequivalent atomic site in the host, of
 65 which there can be a sizable number (up to about 100 in the
 66 present work) in compositionally and structurally complex materi-
 67 als. Other quantities typically derived from a DFT-relaxed struc-
 68 ture like band gap (E_g), effective electron mass (m^*), compound
 69 formation enthalpy (ΔH_f), and oxidation state (s) can readily be
 70 encoded into the material’s graph if available to further improve
 71 prediction accuracy. Existing computational databases contain-
 72 ing 10,000s of compounds with potentially up to millions of non-
 73 equivalent defect sites can be screened in an automated fashion
 74 using desktop computational resources with a prediction accuracy
 75 limited mainly by the amount and diversity of the vacancy defect
 76 training data.

77 As a specific use case, we first focus on the discovery of new so-
 78 lar thermochemical (STCH) water splitting oxides, widely consid-
 79 ered a promising route for renewable hydrogen production.³⁷⁻³⁹
 80 DFT investigations play a critical role in understanding these ma-
 81 terials and helping to guide experiments,⁴⁰⁻⁴⁵ but can only be ac-
 82 complished on a limited scale. Due to the complexity of the asso-
 83 ciated vacancy defect calculations using DFT, approximately one
 84 year’s work was required to build our training database (~ 200
 85 host oxide compounds consisting of ~ 1500 unique defects). Our
 86 highly generalizable dGNN model then extends upon capabilities
 87 of previous work that requires carefully hand-engineered features
 88 in specific crystal systems (e.g., perovskites)^{21,46} and obtains a
 89 similar expected mean absolute error in oxygen vacancy forma-
 90 tion enthalpy (MAE < 450 meV) in unseen compounds (assum-
 91 ing its cations are represented in the training data). Depending
 92 on the model’s defect predictions, oxide stability, and the strin-
 93 gency of these down-selection criteria, we then narrow down a
 94 small number of priority candidates for experimental efforts from
 95 10,000s of possible MP oxides (among which are known STCH
 96 oxides we “re-discover” through our screening procedure).

97 Finally, optimal candidates for other clean energy applications
 98 are highlighted where target ranges for oxygen vacancy formation
 99 enthalpies have been proposed as a primary metric for material
 100 down-selection, such as catalysts for CO₂ conversion and cath-
 101 odes for solid oxide fuel cells.^{47,48} We even extend our analysis
 102 to predict defect density for all materials at finite temperatures,
 103 a capability that can only be achieved due to our method’s abil-
 104 ity to rapidly predict vacancy formation enthalpies of all sites in
 105 the crystal structure (i.e., account for configurational entropy).
 106 Thus materials can be assessed beyond the static picture of single
 107 vacancy defect calculations at 0K for a limited set of materials.
 108 With continued accumulation of training data, this success paves
 109 the way for automated materials discovery in other vacancy de-
 110 fect dependent applications and lays the groundwork for more
 111 complicated machine learning tasks such as correlated vacancy
 112 formation enthalpy or vacancy mobility predictions. All data,
 113 code, and scripts needed to reproduce this study are provided
 114 open source.⁴⁹

2 Results and Discussion 115

2.1 Developing a diverse database of vacancy defects 116

117 We developed an automated workflow for DFT vacancy defect
 118 calculations (Figure 1) as follows: (1) import the stoichiomet-
 119 ric host oxide crystal structures from the ICSD⁵⁰ that are avail-
 120 able in NRELMatDB; (2) relax the host supercell in ferromagnetic
 121 and different possible anti-ferromagnetic spin configurations; (3)
 122 choose the minimum energy host atomic and magnetic structure;
 123 and (4) perform point defect calculations on the supercell using
 124 the automated defect framework.⁵¹ In the data acquisition step,
 125 we extract host properties (from step 3) and calculate vacancy
 126 formation energies (after step 4), which then supplies input and
 127 target properties, respectively, for training the machine learning
 128 model. Further details on the DFT settings are provided in Sec-
 129 tion S1.^{14,44,52-58} DFT is currently the preferred method for high-
 130 throughput supercell defect calculations. True benchmark calcu-
 131 lations require total-energy methods beyond DFT, such as quan-
 132 tum Monte Carlo or the random phase approximation, which are
 133 currently available only for few defect systems and with restric-
 134 tions in cell size and atomic relaxations.^{44,59,60} Given the DFT-
 135 relaxed crystal structure, \mathcal{C}_h , of the host oxide with total energy
 136 E_h and the DFT-relaxed defected structure, \mathcal{C}_d , with total energy
 137 E_d (calculated using the standard supercell approach of Ref. 61),
 138 we compute the enthalpy of defect formation via

$$\Delta H_d = E_d - E_h + \sum_i n_i \mu_i^{\text{ref}}. \quad (1)$$

139 Here the reference chemical potential of added or removed atoms
 140 ($n_i = -1$ and $+1$, respectively) are taken as the fitted elemental
 141 reference energies (FERE)^{14,57}, $\mu_i^{\text{ref}} = \mu_i^{\text{FERE}}$, which improve the
 142 description of thermochemical properties in DFT calculations⁶².
 143 For an oxygen vacancy, Equation (1), simplifies to $\Delta H_{V_O} = E_{V_O} -$
 144 $E_h + \mu_O^{\text{ref}}$.

145 Our final DFT training database consists of ~ 1500 unique de-
 146 fect sites from ~ 200 parent oxides, which span 15 cations (Mg,
 147 Al, Ca, Ti, Mn, Fe, Co, Ni, Sr, Y, Nb, In, Ba, La, Ce), 63 space
 148 groups, and 51 unique stoichiometries. The choice of chemi-
 149 cal space (Figure 2) is motivated by previous literature,^{58,63-65}
 150 which provides guidance on cations that form stable oxides and
 151 play an active role in tuning oxygen vacancy formation energy
 152 via their redox activity. Previous STCH material searches have
 153 targeted perovskite (ABO₃) stoichiometry and related structures
 154 systems (cubic, orthorhombic, tetragonal). Our training data is
 155 more diverse and spreads across all seven crystal structure sys-
 156 tems and includes a wide range of stoichiometries to cover dif-
 157 ferent coordination environments and metal ion oxidation states
 158 varying from 2+ to 5+.

2.2 A graph neural network model for vacancy defects 159

160 We create a vacancy defect graph neural network (dGNN) sur-
 161rogate model f_{dGNN} , parameterized by weights θ , of the general
 162 form

$$\Delta \hat{H}_d = f_{\text{dGNN}}(\mathcal{C}_h, i', \mathbf{v}_g, \mathbf{s}; \theta), \quad (2)$$

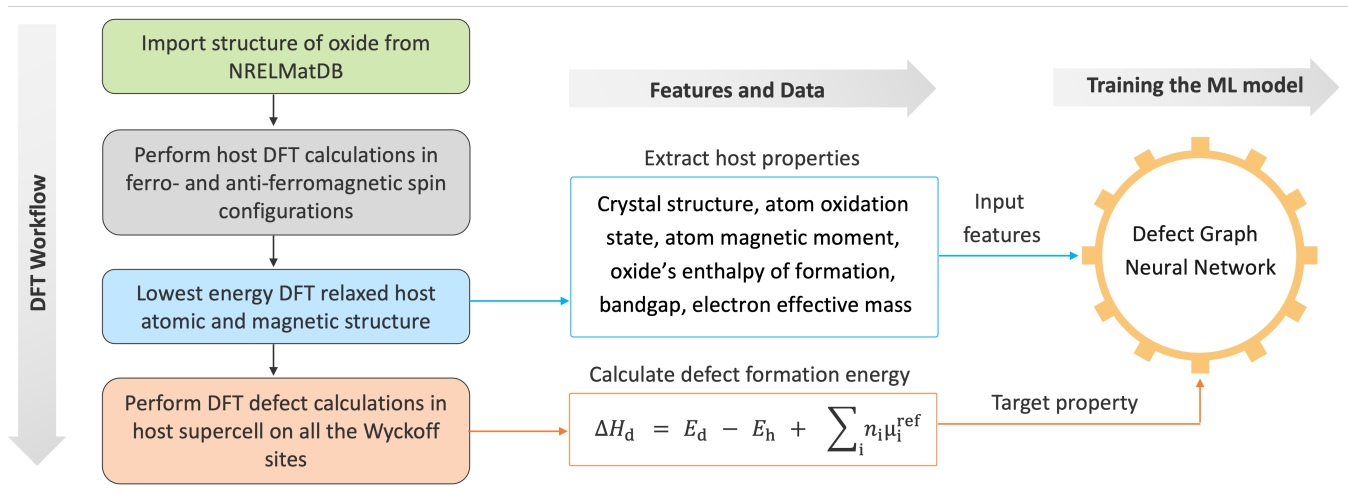


Fig. 1 The automated DFT vacancy defect calculation workflow combined with the data acquisition and curation necessary to develop the training dataset for a machine learning model.

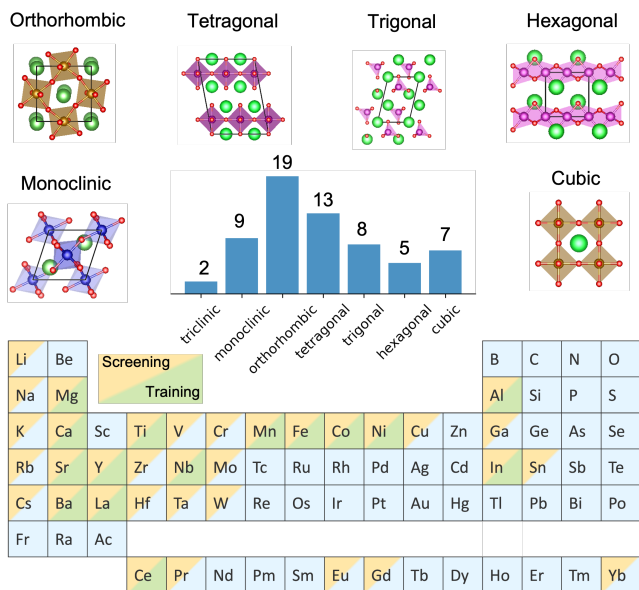


Fig. 2 The chemical and structural search space (cations in binary and ternary oxides and the number of unique space groups in each of the seven crystal systems) explored via DFT defect calculations. Cations considered in training are shown in green, along with ones that should eventually be considered for screening in yellow.

163 that will drastically reduce the computational cost associated with
 164 Equation (1) when performing high-throughput materials screening.
 165 Here, $\mathbf{v}_g = \{E_g, m^*, \Delta H_f\}$ refers to a set of global input fea-
 166 tures as derived from the host compound (e.g., the band gap, ef-
 167 fective electron mass, and compound formation enthalpy, respec-
 168 tively) while $\mathbf{s} = \{s_1, s_2, \dots\}$ refers to site specific input fea-
 169 tures for each atom, (e.g., s_1 is the oxidation state of atom 1 in the host
 170 structure). Intuitively, for example, we expect oxides with cations
 171 in high oxidation states to form O vacancies (i.e., to reduce) more
 172 easily than when cations are in lower oxidation states, hence moti-
 173 vating the inclusion of these properties derived from the relaxed
 174 host structure.

175 Requiring only \mathcal{C}_h and the index of the atom to be defected, i' ,
 176 as an input, the model negates the cost of a DFT supercell relaxa-
 177 tion for each unique symmetry site when predicting $\Delta \hat{H}_d$, and ex-
 178 ecuting the ML screening is of negligible computational cost when
 179 querying \mathcal{C}_h from existing repositories like MP or NRELMatDB.
 180 The inputs for model training (the host's relaxed POSCAR file, for-
 181 mation enthalpy, bandgap, effective electron mass, and oxidation
 182 states) and neutral vacancy formation energies (for both oxygen and
 183 cations) are provided in our open-source data repository.⁴⁹
 184 Our dGNN closely follows the original Crystal Graph Convolutional
 185 Neural Network (CGCNN) method of Ref. 31, for which we highlight
 186 the necessary modifications to predict defect formation
 187 enthalpies. The deep learning framework is composed of three
 188 major steps.

Crystal embedding. First, \mathcal{C}_h is embedded as a graph with
 189 nodes, $V = \{v_0, v_1, \dots\}$, corresponding to each atom and edges
 190 $B = \{b_{ij}\}$ corresponding to bonds that are defined between atoms
 191 i and j below a cutoff radius and up to a maximum number of
 192 nearest neighbors. CGCNN One-Hot encodes⁶⁶ and concatenates
 193 a node's elemental solid properties, $\mathbf{v}_e = \text{One-Hot}(\text{Mendelev}$
 194 $\text{number, atomic weight, melting temperature, covalent radius,}$
 195 $\text{electronegativity, ground state volume per atom, ground state}$
 196 $\text{band gap, ground state magnetic moment, and space group num-}$
 197 $\text{ber})$ as the initial feature vector, $\mathbf{v}_i^{(0)} = \mathbf{v}_e$. We additionally con-
 198 catenate a One-Hot encoding of the site's oxidation state, as calcu-
 199 lated in our DFT defect database, to increase model accuracy
 200

$$\mathbf{v}_i^{(0)} = \mathbf{v}_e \oplus \text{OneHot}(s_i). \quad (3)$$

201 Two atoms of the same element type are no longer guaran-
 202 teed to share an identical encoding due to their dependence on
 203 s_i since various elements can assume different oxidation states
 204 depending on their local environment. Since One-Hot encod-
 205 ing increases sparsity and dimensionality of the initial node fea-
 206 ture vectors and removes any quantitative ordering of a phys-
 207 ical property, we also investigate whether a purely continu-
 208 ous encoding strategy can improve performance. This alter-

209 native approach involves the scaling of each elemental prop-
 210 erty between $[0,1]$, which can be combined with the ele-
 211 ment’s ground state electron configuration and valence elec-
 212 trons (e.g., $\left\{\frac{1s}{2}, \frac{2s}{2}, \frac{2p}{6}, \dots, \frac{5d}{10}, \frac{6p}{6}, \frac{v_s}{2}, \frac{v_p}{6}, \frac{v_d}{10}, \frac{v_f}{14}\right\}$),³⁵ to yield a
 213 continuously-scaled elemental representation, \mathbf{v}'_e . This vector can
 214 further be concatenated with s'_i , scaled between $[0,1]$, to produce
 215 a $\mathbf{v}_i^{(0)}$ that is lower dimensionality, less sparse, and preserves or-
 216 dering of physical quantities.

217 CGCNN³¹ also utilized a discretized Gaussian filter applied to
 218 the distance between two atoms, r_{ij} , to generate the initial edge
 219 features, \mathbf{b}_{ij} , but this representation can be sparse and sensitive to
 220 an arbitrary choice of the filter’s standard deviation. A more sys-
 221 tematic approach is to use a radial basis set expansion (e.g., sim-
 222 ilar Behler and Parinello’s G^{II} functions⁶⁷) to generate the initial
 223 feature vector according to a set of gaussian widths (η), centers
 224 (R_s), and a cutoff radius (r_c):

$$\mathbf{b}_{ij} = \left\{ \exp \left[-\eta (r_{ij} - R_s)^2 / r_c^2 \right] \right\}. \quad (4)$$

225 This simultaneously reduces the sparsity and dimensionality
 226 of \mathbf{b}_{ij} for a moderate basis set size ($\eta = \{0.5, 1.0, 1.5\}$, $R_c =$
 227 $\{1.0, 2.0, 3.0, 4.0, 5.0\}$). Such modifications facilitate distinguish-
 228 ing between very similar crystal structures.

229 **Convolutions.** Automated feature extraction is then performed,
 230 whereby the feature vector for each node is iteratively updated
 231 via convolutions with its neighboring nodes and edges. Mathe-
 232 matically, the output of the t^{th} convolutional layer can be written
 233 as³¹

$$\mathbf{v}_i^{(t+1)} = g \left(\mathbf{v}_i^{(t)} + \sum_j \sigma \left(\mathbf{z}_{ij}^{(t)} \mathbf{W}_1^{(t)} + \mathbf{b}_1^{(t)} \right) \odot g \left(\mathbf{z}_{ij}^{(t)} \mathbf{W}_2^{(t)} + \mathbf{b}_2^{(t)} \right) \right). \quad (5)$$

234 Here $\mathbf{z}_{ij} = \mathbf{v}_i \oplus \mathbf{v}_j \oplus \mathbf{b}_{ij}$ is the concatenation of information from
 235 connected nodes in the graph, $\mathbf{W}_1, \mathbf{b}_1$ and $\mathbf{W}_2, \mathbf{b}_2$ represent
 236 weights and biases of different learnable weight matrices (i.e.,
 237 fully connected neural network layers), σ denotes a sigmoid ac-
 238 tivation function, g denotes a softplus activation, and \odot denotes
 239 element-wise multiplication. This step remains unaffected for the
 240 dGNN.

241 **Property prediction.** Following T total convolutions, the origi-
 242 nal CGCNN method acquires an overall feature vector represent-
 243 ing the crystal by pooling all nodes in the structure

$$\mathbf{v}_c = \text{Pool} \left(\mathbf{v}_0^{(T)}, \mathbf{v}_1^{(T)}, \dots, \mathbf{v}_N^{(T)} \right), \quad (6)$$

244 which, for example, consists of a summation operation. Thus
 245 crystals of arbitrary size are described by a vector of the same
 246 dimensionality. The model predicts some final *global* property by
 247 applying one (or more) fully connected layers to \mathbf{v}_c .

248 However, we are interested in the defect formation enthalpy
 249 and therefore isolate the information contained only on the host
 250 node/atom to be defect-ed (specified at index i') following the T
 251 total convolutions. We therefore replace eq. (6) with

$$\mathbf{v}_d = g \left(\left(\mathbf{v}_{i'}^{(T)} \oplus \mathbf{v}_g \right) \cdot \mathbf{W} + \mathbf{b} \right). \quad (7)$$

We incorporate the global compound features at this step, $\mathbf{v}_g =$
 $\{E_g, m^*, \Delta H_f\}$, before applying the subsequent fully connected
 layer. Additional feed-forward layers may be applied before the
 final property prediction of $\Delta \hat{H}_d$ is then computed through one fi-
 nal output layer. Equation (7) is specifically designed for predict-
 ing defect formation enthalpies for the limit of infinite dilution
 in this work, but could be changed to, for example, expand its
 applicability to correlated vacancy defects.

All training data, model structures, and hyperparameters used
 in this study can be found in our Zenodo repository, from which
 all results can be reproduced when used in conjunction with
 the dGNN implementation built in Pytorch⁶⁸ provided at <https://github.com/mwitman1/cgcnndefect/tree/Paper1> (modified
 from Ref. 31). In brief, due to the small size of our training
 data set, a dGNN model of minimal complexity is required to
 facilitate training. In practice the number of trainable param-
 eters often exceeds the number of training examples in deep
 learning applications and explicit regularization isn’t even always
 needed to achieve low generalization error.⁶⁹ Nonetheless, our
 minimal complexity architecture consists of $T = 2$ convolution
 steps, $\mathbf{v}_i \in \mathbb{R}^8$, and $\mathbf{v}_d \in \mathbb{R}^{16}$, leading to a GNN with only $\sim 2,000$
 learnable parameters. After fixing the architecture, the learning
 rate was adjusted to minimize K-fold test set performance (next
 section), and over-fitting was minimized via early-stopping using
 the mean absolute error on a 10% validation set within each train
 fold.

2.3 Defect GNN validation and performance

We executed three different cross-validation (CV) strategies,
 demonstrated by the toy examples in Figure 3a, to gauge model
 performance. For defect-wise and compound-wise CV, we uti-
 lize $K = 10$ -fold cross validation. For each k -fold, 10% of the
 training data is held as a validation set for early stopping, and
 the mean absolute error over all n defects in the test set is com-
 puted, $\text{MAE}_k^Y = (1/n) \sum_n |\Delta \hat{H}_{d,n}^Y - \Delta H_{d,n}^Y|$. The model’s expected
 prediction error is then estimated across all folds, $\langle \text{MAE}^Y \rangle_K =$
 $(1/K) \sum_{k=1}^K \text{MAE}_k^Y$. Here $Y = \text{O}$ or $Y = \text{Other}$ filters evaluation of
 the MAE by a defect’s specific element type to delineate model
 performance between oxygen and non-oxygen vacancy predic-
 tions. The standard deviation in MAE across all K models,
 $\sigma_K(\text{MAE}^Y)$, should be small once sufficient data has been col-
 lected, i.e., the sampled distribution of training data no longer
 changes significantly between each fold.

Validating the dGNN with defect-wise CV is a less challenging
 task, since train and test sets may contain defects from the same
 material in similar chemical environments (i.e., just above the
 symmetry tolerance). Validating with compound-wise CV is more
 challenging, since the test set contains all the defects from a given
 material (none of which may appear in the training set). This bet-
 ter reflects the practical performance for materials discovery, be-
 cause one is usually interested predicting for materials for which
 no DFT vacancy calculations have been performed and thus not a
 single defect site could exist in training set. Finally, element-wise,
 leave-one-out CV proves the hardest challenge, where all defects
 for a compound containing the held-out element are placed in the

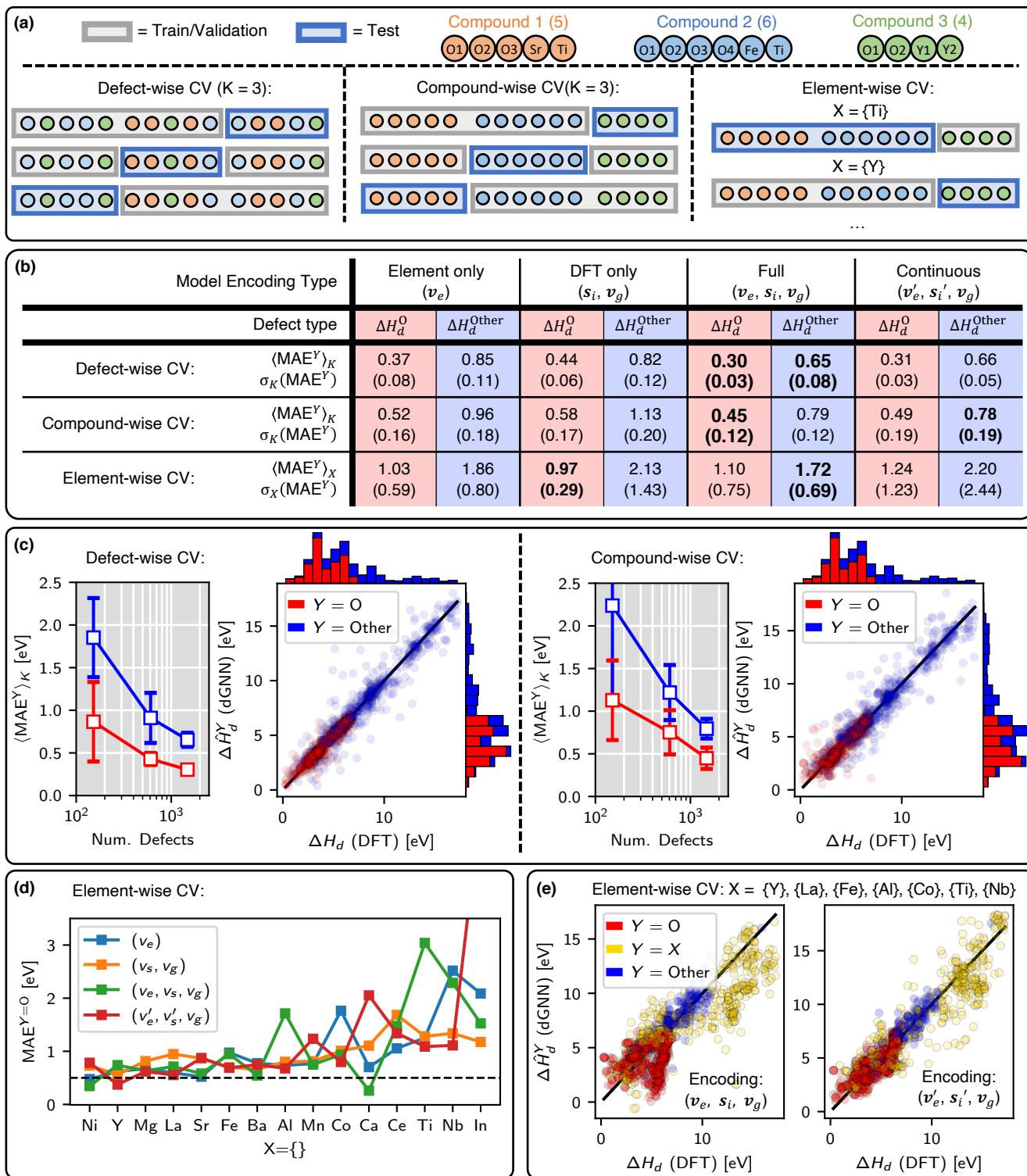


Fig. 3 (a) Demonstration of different CV strategies in a toy dataset. In defect-wise CV, different defects from the same compound can appear in both train/validation and test splits, whereas in compound-wise CV, the train/validation and test stratification is performed such that all of compound's defects can only appear in either train/validation or test splits. The number of compounds is kept constant between folds, leading to small variations in the number of unique defects contained per K-fold test set. In element-wise, leave-one-out CV, all defects in any compound containing the test element, X , are placed in the test set. (b) Summary of expected prediction errors and a heuristic uncertainty metric (mean MAE and standard deviation of MAE across K-fold test sets) for different cross-validation (rows) and graph encoding strategies (columns). (c) MAE averaged across the CV test sets ($K = 10$) models as a function of training data size and the parity plots of the test set predictions with DFT for the "Full" encoding strategy. (d) MAE $^{Y=0}$ for the element-wise, leave-one-out CV, separated by test element and encoding strategy. (e) Test set predictions for the $X = \{Y\}, \{\text{La}\}, \{\text{Fe}\}, \{\text{Al}\}, \{\text{Co}\}, \{\text{Ti}\}, \{\text{Nb}\}$ models.

306 test set (thus there are $X = 15$ models and test sets, corresponding
307 to the number of cation types in the training data). At inference
308 time, the ML model is supplied with a graph encoding containing
309 node features that may not be represented by the training data.

310 Figure 3b shows the evaluation metrics for each CV strategy,
311 with the MAE separated by predictions on oxygen and all other
312 vacancy types. Cation vacancies tend to have higher enthalpies,
313 but the mean relative errors between O and non-O defects are
314 quite similar. This CV analysis was repeated for four different
315 encoding strategies. "Element-only" encoding uses \mathbf{v}_e , while \mathbf{s}_i
316 and \mathbf{v}_g are empty. Conversely, "DFT-only" encoding keeps \mathbf{s}_i and
317 \mathbf{v}_g but \mathbf{v}_e is empty. The "Full" encoding strategy incorporates all
318 information, while the "Continuous" encoding replaces the one-
319 hot encoding of elemental properties and oxidation state with \mathbf{v}'_e
320 and \mathbf{s}'_i . Three key observations arise from the defect-wise and
321 compound-wise CV. First, our strategy to encode both elemental
322 and DFT data via the "Full" and "Continuous" models provides im-
323 proved accuracy; nonetheless, "Element-only" and "DFT-only" en-
324 coding strategies both lead to reasonable accuracy on their own.
325 Second, the best accuracy for compound-wise CV is obtained with
326 the "Full" model with a $\langle \text{MAE} \rangle_K^O < 0.45$ eV. Third, the ability of the
327 model to predict $\Delta H_d^{\text{Other}}$ validates the generality of this approach
328 and its usefulness in other applications requiring predictive mod-
329 eling beyond oxygen vacancies.

330 Figure 3c demonstrates the continued decrease in the CV MAE
331 as more defects are added to the training data. While the MAE de-
332 crease with defect-wise CV starts to plateau, the compound-wise
333 CV still benefits from a log-linear decrease in MAE with increasing
334 data, highlighting the model can still be significantly improved
335 as more training data is acquired. This highlights the need for
336 continued, high-quality DFT defect calculations with automated
337 workflows⁵¹ (see Section S1 for recommended settings to build
338 a larger training dataset consistent with this work). The parity
339 plots correspond to the test set results concatenated across all CV
340 models, with good performance between both oxygen and non-
341 oxygen vacancy defect predictions.

342 Figure 3d shows the results of the element-wise, leave-one-out
343 CV for each of the four different encoding strategies. While this
344 is not a task that one might expect a deep learning approach to
345 succeed at, several elements are well predicted and close to the
346 target error of 0.5 eV, regardless of encoding type. Yet other ele-
347 ments are poorly predicted for all encoding types. Without any *a*
348 *priori* knowledge of which held-out elements are well-predicted,
349 it is not possible to assume that predictions on materials with
350 unseen cation types can achieve $\langle \text{MAE} \rangle_K^O < 0.97$ eV (Figure 3).
351 We therefore recommend this current generation of models only
352 be used on compounds containing the fifteen cations spanned by
353 the training database. Nonetheless, Figure 3e demonstrates how
354 the continuous encoding strategy significantly improves property
355 prediction across selected element types. This could be due to
356 the continuous encoding's preservation of quantitative periodic
357 trends (e.g., electronegativity, mean volume per atom, etc.). In
358 order to expand the quantitative applicability of the model for
359 materials discovery outside of the current cation set, we plan to
360 include a larger chemistry space in the future.

2.4 Comparison with previous modeling efforts

361 Our cross-validation performance with the current training
362 dataset is comparable to the performance of linear models derived
363 via careful feature engineering to predict neutral oxygen vacancy
364 formation enthalpies. Deml et al. trained a model on 45 binary
365 and ternary oxides and achieved around 0.4 eV MAE on a small
366 test set of 18 oxides that had not been included in model devel-
367 opment.¹⁷ Wexler et al. computed SCAN+U vacancy formation
368 enthalpies of 341 ABO₃ perovskites and derived a linear model
369 that globally achieved an MAE of 0.7 eV and an MAE of 0.45 eV
370 for the subset (142 materials) with hull energies less than 0.025
371 eV/atom. Another in depth validation of these studies with ours
372 is presented in Section S3. These linear models are more inter-
373 pretable than our approach due to the small number of manually
374 derived features, but are less generalizable. For example, they are
375 not capable of predicting neutral cation vacancies, whereas our
376 trained model predicts either. Our model architecture was not
377 designed specific to oxides and could be applied to any material
378 class since it operates generally on any crystal structure, whereas
379 the linear models contain features that can only be calculated if
380 the structure contains O. Figure 3c also demonstrates strong evi-
381 dence for continued significant model improvement with more
382 training data, which is unclear for the linear models. This pat-
383 tern of comparable accuracy but increased generalizability also
384 holds true for our method relative to other machine learning ef-
385 forts for defect predictions, e.g., Frey et al.'s model for transition
386 metal dichalcogenides²⁴ with MAE=0.67 eV and Cheng et al.'s
387 model for amorphous GeTe.⁷⁰ Finally, in a concurrent preprint
388 with ours,^{71,72} Choudary et al. used graph neural networks mod-
389 els to predict total energy of a host structure and with an atom re-
390 moved to estimate vacancy formation enthalpies, but this neglects
391 the relaxation of the host upon vacancy formation and yields an
392 MAE prediction of 1.5 eV for a single test set, including 2.3 eV for
393 oxides.

2.5 Predictions on known STCH materials.

394 Before utilizing the dGNN model to screen potential candidate
395 materials for STCH water splitting, it is instructive to first validate
396 against additional DFT calculations for experimentally known
397 STCH oxides. The materials behavior for the STCH redox pro-
398 cesses can be expressed in terms of reduction enthalpies and
399 entropies.^{40,73} For workable and economic thermodynamic con-
400 ditions, these considerations lead to a desirable value for the
401 oxygen vacancy defect formation energy in an interval of about
402 [2.3, 4.0] eV.^{21,41,64} Lower formation energies impair the abil-
403 ity to produce hydrogen in the oxidation step, while higher en-
404 ergies prevent significant changes of the O stoichiometry in the
405 reduction step. To predict the defect formation energies for
406 these "unseen" materials, we utilize the expectation across K -
407 fold models, $\langle \Delta \hat{H}_d^Y \rangle_K = K^{-1} \sum_{k=1}^K \hat{H}_{d,k}^Y$, and the standard deviation,
408 $\sigma_K(\Delta \hat{H}_d^Y) = \sqrt{K^{-1} \sum_{k=1}^K (\hat{H}_{d,k}^Y - \langle \hat{H}_{d,k}^Y \rangle)^2}$, as a heuristic estimate of
409 the uncertainty in the property prediction.^{74,75}

410 As a first test case, we consider the family of BXM oxides
411 (B=Ba; X=Ce,Nb,Pr; M=Mn)⁷⁶ which have a higher degree
412 of compositional complexity than the materials in the training
413
414

415 dataset. Figure 4a compares the $\langle \Delta \hat{H}_d^O \rangle_K$ with DFT for BXM ox-
 416 ides for both “Full” and “DFT-only” encoded models. On aver-
 417 age, “DFT-only” predictions are only more accurate when struc-
 418 tures contain unseen cation types missing from the training set
 419 (e.g., Pr), but are generally less accurate if all of a structure’s
 420 cation types are in the train set (Figure 3b,d). Nonetheless, both
 421 models are quite similar in qualitatively ranking and quantita-
 422 tively capturing ΔH_d^O . We additionally tested our model on newly
 423 discovered disordered perovskite oxides, $\text{Sr}_{1-x}\text{Ce}_x\text{MnO}_3$ (SCM),
 424 which demonstrate suitable STCH performance.⁷⁷ In contrast to
 425 the BXM family which are line compounds, the SCM family can
 426 accommodate a wide range of Ce doping, thereby providing bet-
 427 ter control over water splitting capabilities by varying Ce con-
 428 centration. To model SCM alloy structure we employ the special
 429 quasirandom structure (SQS) approach⁷⁸ and generate two
 430 80-atom supercell structures representing random alloying with
 431 differing Ce content. Figure 4b shows the “Full” encoding model
 432 predictions on both SQS’s. While the absolute value of the predic-
 433 tions are slightly below the generally accepted optimal range of
 434 [2.3, 4.0] eV, the ML model predicts the SQS with higher Ce con-
 435 tent to have oxygen vacancy enthalpies closer to the target range,
 436 which is experimentally consistent with its improved water split-
 437 ting capabilities from the increased Ce content.⁷⁷

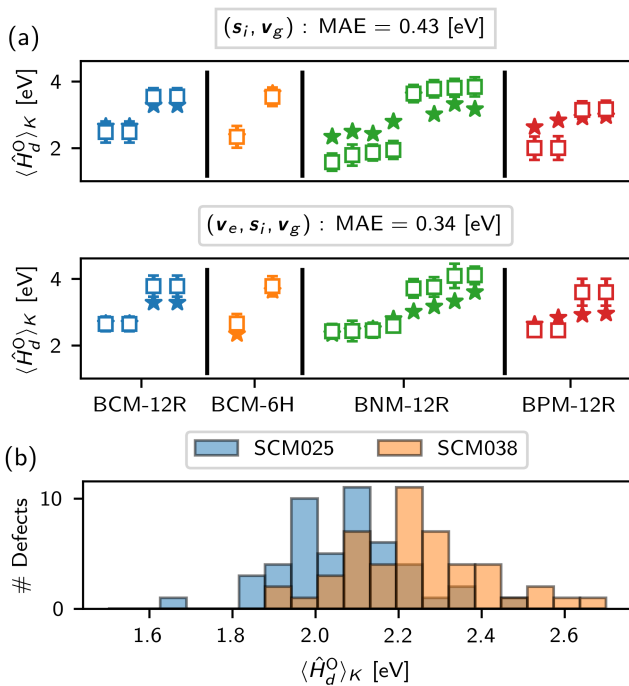


Fig. 4 (a) Defect-wise CV model predictions (open squares) and DFT values (stars) for each O vacancy in NRELMatDB structures of known 4 known STCH materials including BCM-12R = $\text{Ba}_4\text{CeMn}_3\text{O}_{12}$ (blue), BCM-6H = $\text{Ba}_3\text{CeMn}_2\text{O}_9$ (orange), BNM-12R = $\text{Ba}_4\text{NbMn}_3\text{O}_{12}$ (green), and BPM-12R = $\text{Ba}_4\text{PrMn}_3\text{O}_{12}$ (red). Error bars correspond to $\sigma_K(\Delta \hat{H}_d^O)$. (b) Distribution of $\langle \Delta \hat{H}_d^O \rangle_K$ for the $(\text{Sr}_{1-x}\text{Ce}_x\text{MnO}_3)$ SCM family of alloys with differing Ce concentrations with $x = 0.25$ and 0.38 in SCM025 and SCM038, respectively.

2.6 High-throughput screening for new STCH materials.

Our “element-only” encoding models can perform consistent predictions on input host crystal structures in which the DFT settings for host relaxations are not identical to those used to create the training set (see Section S2 and Figure S2 for details). Thus we can now efficiently predict ΔH_d across 10,000s of DFT-relaxed crystal structures included in open source repositories beyond NRELMatDb, such as Materials Project (v2021.03.22). We employ the “Element-only” encoding model at the expense of slightly lower accuracy since Materials Project (MP) data doesn’t necessarily contain all the features needed for the “Full” encoding models. Figure 5a shows that the space of $\sim 35,000$ oxides (excluding non-metals) is reduced to about $\sim 2,200$ structures by setting a maximum energy above the hull requirement, $E_H < 0.1$ eV/atom, and discarding any materials with cations not present in the training set. From these remaining $\sim 2,200$ host oxides, we predict $\langle \Delta \hat{H}_d \rangle_K$ for the $\sim 48,000$ symmetrically unique defect sites. Before proceeding with candidate down-selection, we perform yet another hold-out validation by comparing our MP screening predictions with existing first principles calculations and model predictions that could be easily mined from the literature (see Section S3).

Although we omit host structures with cations outside the training set in this study, adding a small number of training structures in the future (the full search space from Figure 2) could further expand the model’s applicability. Figure 5b shows the predicted $\langle \Delta \hat{H}_d^O \rangle_K$ vs. ΔH_f , and, although correlation is evident across the entire enthalpy range, there is little correlation within [2.3, 4.0] eV. Furthermore, a simple model using features derived only from the host composition would clearly be insufficient due to an inability to distinguish individual oxygen vacancies. Within a single structure, these can span a very large range as shown for the min, median, and max predictions for MP structure mp-1247717 ($\text{Ca}_4\text{Mn}_3\text{AlO}_{11}$).

Assessing an oxide’s STCH potential first requires determining ΔH_d^O of all sites and computing the fraction above the minimum threshold of 2.3 eV, denoted x_{\min} , and the fraction of defects in the optimal range of [2.3, 4.0] eV, denoted x_{rng} . If the material contains any defects below the target range, the reduced metal oxide cannot readily be regenerated at the oxidation conditions relevant for STCH, and thus we require $x_{\min} = 1$. It may be ideal for all defects to fall within in the target range ($x_{\text{rng}} = 1$) to increase capacity and defect mobility, but these considerations are beyond the scope of this study. In practice, only one defect needs to fall within the targeted range to be considered a promising STCH material ($x_{\text{rng}} > 0$).

Recent total energy calculations for defects in hercynite FeAl_2O_4 have found good agreement between DFT+U, hybrid functional, and the random phase approximation, but uncertainties on the order of a few tenths of an eV should be expected for DFT calculations in transition metal oxides.⁴⁴ We therefore extend the defect screening metrics to be uncertainty inclusive ($x_{\min,1}, x_{\text{rng},1}$), agnostic ($x_{\min,2}, x_{\text{rng},2}$), or exclusive ($x_{\min,3}, x_{\text{rng},3}$) for increasingly strict down-selection. Given a host’s N_s symmetry sites and the set of all predictions $\{\langle \Delta \hat{H}_d^O \rangle_K\} \equiv H = \{H_1 \dots H_{N_s}\}$

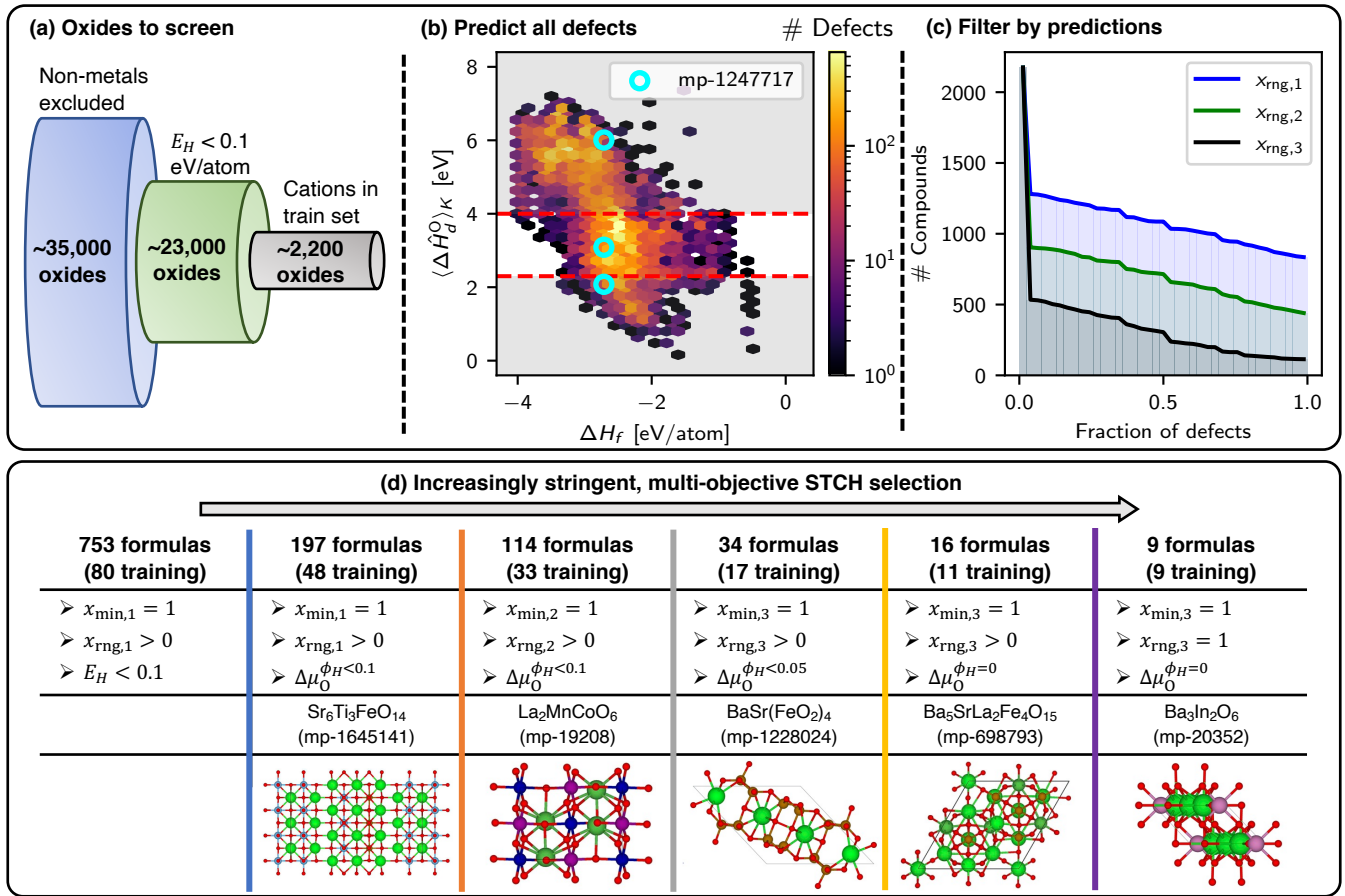


Fig. 5 (a) Removing MP oxides containing non-metals, those with $E_H > 0.1$ eV/atom, and those with elements outside the training set yields $\sim 2,200$ structures for screening. (b) Screening predictions using the “Element-only” encoding, defect-wise CV models vs. ΔH_f . (c) The cumulative histogram of compounds that contain a specific fraction of defects predicted to satisfy the range criteria, x_{rng} , as defined in Table 1. (d) Utilization of increasingly stringent defect and host compound criteria (x_{rng} , x_{min} , E_H , and $\Delta\mu_{\text{O}}^{\phi_H < X}$) to narrow the list of potential STCH candidates. At each down-selection stage, we show the number of unique remaining formulas, the number of which overlap with the training data, and an exemplar structure.

Uncertainty	C for x_{min}	C for x_{rng}
Inclusive	$H_i + U_i > 2.3$	$[H_i - U_i, H_i + U_i] \cap [2.3, 4.0] \neq \emptyset$
Agnostic	$H_i > 2.3$	$H_i \in [2.3, 4.0]$
Exclusive	$H_i - U_i > 2.3$	$[H_i - U_i, H_i + U_i] \in [2.3, 4.0]$

Table 1 Criteria for Equation (8) to determine the defect fractions, x_{min} and x_{rng} , for increasingly strict uncertainty inclusive, agnostic, or exclusive down-selection.

493 and uncertainties $\{\sigma_K(\Delta\hat{H}_d^{\text{O}})\} \equiv U = \{U_1 \dots U_{N_s}\}$, these defect
 494 fractions can be calculated subject to a criteria C ,

$$x = \frac{1}{N_s} \sum_{i=1}^{N_s} \begin{cases} 1 & \text{if } C \\ 0 & \text{otherwise} \end{cases} \quad (8)$$

495 which is summarized in Table 1. Figure 5 shows the impact of
 496 applying these increasingly strict defect criteria and that a significant
 497 number of candidates remain even when using an uncertainty exclusive
 498 filter and requiring $x_{\text{rng}} \rightarrow 1$. See Section S4 for a more detailed
 499 discussion on uncertainty.

500 Down-selection must also consider host oxide stability under
 501 STCH relevant conditions. For oxygen chemical potential $\mu_{\text{O}} =$

$\mu_{\text{O}}^{\text{ref}} + \Delta\mu_{\text{O}}$, typical STCH operating conditions necessitate that
 502 the host is stable in a target range $\Delta\mu_{\text{O}}^{\text{target}} = [-3.0, -2.5]$ eV.^{40,44}
 503 Given the compound’s energy above the hull in the grand ensemble,
 504 $\phi_H(\Delta\mu_{\text{O}})$, we define the chemical potential range over which
 505 the host stability is below some threshold X ,
 506

$$\Delta\mu_{\text{O}}^{\phi_H \leq X} = [\Delta\mu_{\text{O}} | \phi_H(\Delta\mu_{\text{O}}) \leq X]. \quad (9)$$

507 Setting $X \leq 0.1$ eV/atom, for example, helps avoid false nega-
 508 tives during materials’ selection due to the synthesizability of
 509 metastable structures⁷⁹ or due to uncertainties originating from
 510 the specific DFT approach and the convex hull analysis. Our final
 511 down-selection criteria requires that the target and stability
 512 chemical potential ranges intersect,

$$\Delta\mu_{\text{O}}^{\phi_H \leq X} \cap \Delta\mu_{\text{O}}^{\text{target}} \neq \emptyset. \quad (10)$$

513 The vacancy defect fractions and host stability criteria can be
 514 tuned for custom down-selection using our open access data and
 515 post-processing scripts.⁴⁹

516 Figure 5d shows how increasingly stringent x_{min} , x_{rng} , and
 517 $\Delta\mu_{\text{O}}^{\phi_H \leq X}$ criteria can narrow the candidate space from thousands
 518 of oxides to just a handful. At each down-selection criteria

519 we have highlighted one material among many that appear
 520 interesting due to relatively low prediction uncertainty, relatively
 521 wide stability range, high cation/structure complexity, verified
 522 experimental synthesis,^{80–84} and a lack of any STCH-specific
 523 experimental investigations that we are aware of. Importantly,
 524 this screening “rediscovers” the known STCH material BCM-12R.
 525 However, it is eliminated by stricter down-selection criteria
 526 since the “Element-only” encoding model under-predicts the
 527 oxygen vacancy enthalpies with $\{2.0 \pm 0.3, 2.9 \pm 0.4\}$ eV for
 528 the two O sites in BCM, compared to the “Full” encoding
 529 predictions, $\{2.6 \pm 0.3, 3.8 \pm 0.5\}$ eV, and DFT predictions,
 530 $\{2.66, 3.29\}$ eV⁸⁵ (Figure 4). This emphasizes the prudence
 531 of considering materials inclusive of their uncertainty, espe-
 532 cially since the “Element-only” model necessitated by MP
 533 screening has slightly higher CV error. Some oxides with a
 534 relatively simple composition satisfying strict down-selection
 535 criteria include: Mn_3O_4 ,⁸⁶ Fe_3O_4 ,⁸⁷ Fe_2O_3 ,⁸⁷ $\text{Ba}_2\text{Fe}_2\text{O}_5$,⁸⁸
 536 Mn_2CoO_4 ,^{89,90} $\text{Mn}(\text{FeO}_2)_2$,⁹¹ $\text{Sr}_2\text{Mn}_2\text{O}_5$,⁸⁴ $\text{Sr}_3(\text{FeO}_3)_2$,⁹²
 537 $\text{Ba}(\text{FeO}_2)_2$,⁹³ $\text{Ba}_3\text{In}_2\text{O}_6$,⁹⁴ Fe_2NiO_4 ,⁸⁷ and $\text{Sr}_5\text{Mn}_5\text{O}_{13}$.⁸⁴ All
 538 have been experimentally synthesized in the literature. Notably,
 539 several have already been investigated in the context STCH
 540 performance^{86,87,89} or other water splitting approaches.⁹⁰
 541 Rediscovering these known STCH materials further validates our
 542 approach, and we have now identified many new candidates from
 543 which promising STCH materials can be experimentally targeted
 544 (see Table S6 for details and the comprehensive list). Raw data
 545 for all predicted defect properties and customizable open source
 546 scripts for reproducing or modifying the down-selection criteria
 547 can be found in the project’s Zenodo repository.⁴⁹

548 2.7 Beyond STCH: materials discovery across diverse energy 549 applications

550 Our dGNN methodology and high-throughput database of va-
 551 cancy predictions can be used to rapidly screen candidate materi-
 552 als in other important clean energy applications. The reverse wa-
 553 ter gas shift-chemical looping (RWGS-CL) approach operates in a
 554 concept very similar to STCH. H_2 gas is used to reduce a metal ox-
 555 ide, after which oxidation with CO_2 produces CO for downstream
 556 hydrogenation to carbon-based fuels. Like STCH, the process is
 557 driven by thermodynamics of oxygen vacancy formation. Ref. 47
 558 strongly correlated the energetics of vacancy formation to other
 559 computed properties like O_2 surface-adsorbate binding energy to
 560 conclude, “It is thus best said that E_{vac} can solely describe the
 561 RWGS-CL process and is capable of predicting the CO_2 conver-
 562 sion ability of perovskite oxides.” Based on a previously known
 563 CO_2 -splitting perovskite ($\text{La}_{0.75}\text{Sr}_{0.25}\text{FeO}_3$) for which they com-
 564 puted an average oxygen vacancy formation enthalpy of 3.4 eV,
 565 they concluded that candidate materials with similar thermody-
 566 namics (e.g., $\Delta\hat{H}_d^O \in [3.0, 4.0]$ eV) would be highly active. This
 567 was confirmed by synthesizing new perovskites with the desired
 568 vacancy thermodynamics and measuring their outstanding activ-
 569 ity. By this metric, one can readily use our model to identify opti-
 570 mal candidates for RWGS-CL. Similar to our STCH screening, we
 571 “re-discover” experimentally known CO_2 -splitting oxides, e.g., the
 572 $\text{La}_2\text{MnCoO}_6$ system.⁹⁵, while discovering new ones (Figure 6).

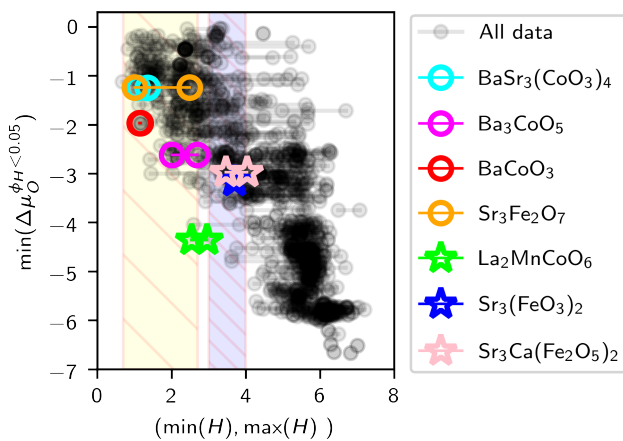


Fig. 6 Identification of candidate materials for CO_2 conversion via RWGS-CL (stars) and SOFC cathodes (circles). For each host oxide we plot the lower bound on stability vs the min and max of all vacancy enthalpies. Some top candidates are noted whose vacancy enthalpy ranges fall within or close to the RWGS-CL and SOFC target ranges (blue and yellow shading, respectively) while simultaneously displaying stability to the most reducing conditions.

573 Oxygen vacancy formation enthalpy has also been corre-
 574 lated with the critical performance metrics for perovskite ox-
 575 ide cathodes in solid oxide fuel cells. Ref. 48 discovered
 576 a simple linear relationship for SOFC perovskite cathodes be-
 577 tween $\Delta\hat{H}_d^O$ and a metric for the macroscale oxygen-transfer
 578 performance, the area-specific resistance (ASR). The authors
 579 noted that successful materials should approximately be tar-
 580 geted with $\text{ASR} \in [0.02 \Omega \text{ cm}^2, 0.24 \Omega \text{ cm}^2]$, or between the ASR
 581 values in the optimized $\text{Ba}_{0.5}\text{Sr}_{0.5}\text{Co}_{0.75}\text{Fe}_{0.25}\text{O}_{3-\delta}$ (BSCF) and
 582 $\text{La}_{0.625}\text{Sr}_{0.375}\text{Co}_{0.25}\text{Fe}_{0.75}\text{O}_{3-\delta}$ (LSCF) systems, respectively. This
 583 essentially represents the trade-off between the correlated stabil-
 584 ity (high defect formation enthalpy) and low operating temper-
 585 ature (low defect formation enthalpy). Using DFT to compute
 586 the average $\Delta\hat{H}_d^O$ in model BSCF and LSCF crystal structures, the
 587 authors established guidelines that $\Delta\hat{H}_d^O \in [0.7, 2.7]$ eV should be
 588 targeted.

589 Once again, we can rapidly target such materials with our ap-
 590 proach. BCSF-like $\text{BaSr}_7\text{Fe}_6(\text{CoO}_{12})_2$ (mp-1099936) with $\Delta\hat{H}_d^O \in$
 591 $[0.7, 1.5]$ and LCSF-like are $\text{Sr}_4\text{LaFe}_2(\text{CoO}_5)_3$ (mp-1218676) with
 592 $\Delta\hat{H}_d^O \in [0.7, 1.5]$ are “re-discovered” in the screening to further val-
 593 idate our approach. Interestingly, the BCSF-like structure is only
 594 metastable with $\min(\Delta\mu_O^{\phi_H < 0.1}) = -0.88$ eV, while the LCSF-like
 595 is stable with $\min(\Delta\mu_O^{\phi_H = 0}) = -0.35$ eV, an observation consis-
 596 tent with the reduced stability of BCSF. For example, some Fe-
 597 lacking analogs not discussed in Ref. 48 but computationally in-
 598 vestigated elsewhere⁹⁶ maintain low predicted vacancy forma-
 599 tion enthalpy but improve upon phase stability according to MP
 600 phase diagrams. Furthermore, non-simple perovskite compounds
 601 can be identified that display similarly desirable vacancy proper-
 602 ties and stability (Figure 6).

603 2.8 High Temperature Defect Thermodynamics

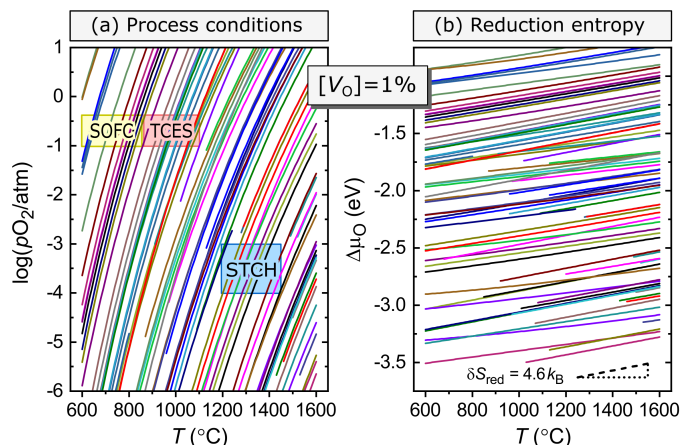
604 Thus far we have discussed materials selection purely in terms of
 605 zero kelvin predictions of the defect formation enthalpies. How-
 606 ever, our approach additionally permits the rapid assessment of
 607 defect densities at high temperatures, which is critical in predict-
 608 ing their behavior under realistic process conditions. The defect
 609 formation energies ΔH_{V_O} were defined above for the reference en-
 610 ergy μ_{O}^{ref} , i.e., the zero temperature limit. At finite temperatures
 611 T and partial pressures p_{O_2} , a corresponding chemical potential
 612 $\Delta\mu_O(T, p_{O_2})$ is added to obtain the formation energy under the
 613 respective thermodynamic condition (*cf.* eq. 1). In a given oxide
 614 with multiple O sites i and respective reference formation energies
 615 $\Delta H_{V_O,i}$, minimization of the free energy of defect formation⁴⁰
 616 yields the dimensionless fractional concentration of O vacancies
 617 relative to the nominal O stoichiometry of the respective oxide,

$$[V_O] = \sum_i g_i \frac{\exp[-(\Delta H_{V_O,i} + \Delta\mu_O)/k_B T]}{1 + \exp[-(\Delta H_{V_O,i} + \Delta\mu_O)/k_B T]}. \quad (11)$$

618 Here, k_B is the Boltzmann constant, and $g_i = m_i / \sum_i m_i$ are the
 619 normalized degeneracies of the different oxygen sites with their
 620 respective multiplicities m_i .

621 To identify oxides which develop a desired degree of O-
 622 deficient off-stoichiometry under high-temperature thermody-
 623 namic conditions (T, p_{O_2}), suitable for different application areas,
 624 we numerically invert Equation (11) to solve for the chemical po-
 625 tential $\Delta\mu_O$ at a given target concentration $[V_O]$. At the same time,
 626 the respective oxide must be stable under this condition and not
 627 decompose into other phases. Here, we include the consideration
 628 of a stability threshold X as defined above. For any given tem-
 629 perature, the chemical potential $\Delta\mu_O$ can be translated into the
 630 corresponding partial pressure p_{O_2} (or vice versa) using the ideal
 631 gas law. Note that many "stoichiometric oxides" do not accom-
 632 modate high levels of defect concentrations, but instead prefer to
 633 form a more reduced, ordered phase with lower O content. In this
 634 case, there may not be any (p_{O_2}, T) conditions for the target $[V_O]$.
 635 On the other hand, oxides that are able to develop a desired level
 636 of off-stoichiometry under suitable conditions are considered as
 637 potential candidates for functional O-deficient materials in the
 638 different application areas.

639 For a target vacancy concentration of $[V_O] = 1\%$, Figure 7a
 640 shows the p_{O_2} vs temperature diagram for oxides within $X <$
 641 0.05 eV/at from the convex hull, using the ML screening of the
 642 MP data (*cf.* Section 2.6). This concentration is generally con-
 643 sidered as a demarcation between the dilute, defect-like, and
 644 concentrated, alloy like, limits of non-stoichiometric materials,
 645 but a similar analysis can be made for any value of $[V_O]$. Desir-
 646 able process conditions are indicated in Figure 7a for Solid
 647 Oxide Fuel Cells (SOFC)^{97,98}, Thermochemical Energy Storage
 648 (TCES)^{99,100}, and STCH^{38,76}, using the reduction step for the lat-
 649 ter two. A spreadsheet with the oxides falling into the respective
 650 regions of interests is included in the SI. All three applications
 651 depend crucially on the formation of O vacancies,¹⁰¹ although
 652 there are of course other materials considerations that we do not
 653 address here. Therefore, the present screening should give valu-
 654 able insights about potential candidate materials at least for the



655 **Fig. 7** (a) p_{O_2} vs temperature diagram for oxides with constant O-
 656 deficiency of $[V_O] = 1\%$ between 600-1600 $^{\circ}\text{C}$. Each line represents one
 657 out of the 82 materials out of the high-throughput screening dataset that
 658 attain this defect concentration while simultaneously fulfilling a stability
 659 criterion of $X = 0.05$ eV/atom. Regions of interest for solid oxide fuel
 660 cells (SOFC), thermochemical energy storage (TCES) and solar ther-
 661 mochemical hydrogen (STCH) are highlighted. (b) Same data, except
 662 presented as $\Delta\mu_O(T)$. The graphs are approximately linear with a slope
 663 corresponding to the reduction entropy δS_{red} . The ideal configurational
 664 entropy of mixing ($4.6 k_B$ at $[V_O] = 1\%$) is indicated at the bottom.

665 aspect of O deficient off-stoichiometry.

666 The list of STCH oxides contains barium, strontium, and lan-
 667 thanum manganates, which are previously identified classes of
 668 oxides for this application^{37,76,77}, but also new suggestions like
 669 $\text{Ba}_2\text{Fe}_2\text{O}_5$. On the other hand, it also contains BaMnO_3 , which
 670 at first sight appears to be a false-positive, because this oxide
 671 is known to reduce too easily and therefore be unable to split
 672 water⁷⁶. However, it is just one (mp-19267) out of 9 differ-
 673 ent BaMnO_3 structures in the MP database, which it is not the
 674 ground state. With a ML predicted minimum V_O formation en-
 675 ergy of $\Delta H_d = 3.0$ eV it would be a useful water splitter, but the
 676 corresponding energy is only 2.2 eV for the BaMnO_3 ground state
 677 (mp-1205336) in the MP database, which is too low. Thus, the
 678 ML model is consistent with experimental observations, and this
 679 example illustrates the tradeoff in choosing the tolerance for the
 680 stability criterion. Finally, we note that the list does not contain
 681 BCM, an apparent case of a false-negative, resulting from under-
 682 estimation of the defect energy in the "element-only" encoding
 683 used for the MP screening (see Section 2.6). Using the energy
 684 from the direct DFT calculation or the "full" encoding ML model,
 685 BCM would indeed fall into the STCH process window indicated
 686 in Figure 7a.

687 Our thermodynamic modeling affords direct access to the re-
 688 duction entropy,^{40,73} which is of great benefit to applications that
 689 utilize a temperature swing, like STCH and TCES. For example,
 690 a large entropy facilitates high $\text{H}_2/\text{H}_2\text{O}$ ratios in the STCH oxi-
 691 dation step⁴⁰. Figure 7b represents the same data as Figure 7a,
 692 but showing the O chemical potential $\Delta\mu_O$ as ordinate instead
 693 of the O_2 partial pressure. The relevant quantity is the differen-
 694 tial reduction entropy with change in defect concentration (short-
 695 hand δS_{red}), which equals the slope of the chemical potential,
 696

686 i.e., $\delta S_{\text{red}} = \partial/\partial T[\Delta\mu_{\text{O}}(T)]$, as described in detail in Ref.⁴⁰. We
687 observe in Figure 7b significant variations in δS_{red} between the
688 different oxides, which originates from the distribution of de-
689 fect energies over different O sites. The ideal configurational en-
690 tropy of $4.6 k_{\text{B}}$ for $[V_{\text{O}}] = 1\%$ is indicated in Figure 7b, and the
691 material-specific, numerically determined values are included in
692 the spreadsheet (SI) for the three process windows, giving addi-
693 tional guidance on materials selection over the enthalpy criterion
694 via ΔH_{d} alone. We further note that additional electronic entropy
695 effects¹⁰² can arise in certain materials, in particular when the O
696 vacancies assume a charged defect state,⁴⁰ where the excess elec-
697 trons either form small polarons or occupy itinerant conduction
698 band states. Such effects are relatively rare in transition metal ox-
699 ides, where the redox activity is typically dominated by the tran-
700 sition metal ions close to the O defect. They could, however, play
701 a role in the extraordinary behavior of CeO_2 ^{76,103,104}. Our high-
702 throughput screening and thermodynamic analysis is a valuable
703 starting point for identifying new potential high-entropy materi-
704 als.

705 3 Conclusions

706 We have developed a powerful, generalized GNN approach for
707 predicting vacancy formation enthalpies of relaxed, defected
708 structures using the relaxed host geometry as input. Therefore,
709 only one DFT relaxation of the host is needed to derive the model
710 inputs, and the model efficiently replaces the computationally in-
711 tensive supercell calculations with numerous defect relaxations
712 (one per symmetry site) needed to obtain the vacancy formation
713 enthalpies. The model’s applicability is not limited to structures
714 in specific crystal/symmetry classes or elemental compositions,
715 and it’s accuracy is primarily limited by their representation in
716 the training data. Through careful cross validation, we have thor-
717 oughly highlighted the advantages and limitations of the model.
718 The best model performance was achieved by integrating DFT-
719 computed host compound properties beyond just the relaxed crys-
720 tal structure into the featurization process (i.e., oxidation states,
721 compound formation enthalpy, band gap, and effective electron
722 mass) to achieve a expected prediction error below 450 meV for
723 relaxed oxygen vacancy defect formation enthalpy. Nonetheless,
724 models trained only on the crystal structure exhibited just $\sim 15\%$
725 higher MAE, since properties like oxidation state and compound
726 formation enthalpy are already indirectly encoded in the crystal
727 structure. ΔH_{d} of any element/crystal site can be predicted us-
728 ing the same model architecture and learned parameters. Fur-
729 thermore, so long as two nominally identical materials (relaxed
730 under different DFT settings) have very similar structures, our
731 “element-only” encoding model provides close agreement on the
732 predicted vacancy formation enthalpies because it relies only on
733 the host crystal structure as input. This means that no new DFT
734 is required to screen different databases (e.g., Materials Project)
735 than the models were trained on (e.g., NRELMatDb) as predic-
736 tions on nominally identical materials provides the same quanti-
737 tative and qualitative outlook for vacancy formation enthalpies.
738 While our training database consists of 15 cation elements, we
739 tested an element-wise CV strategy to gauge model performance
740 when predicting vacancies in compounds whose elements were

741 missing from the training set. Finally, since the complexity of the
742 DFT defect relaxations limits the size of the training data that can
743 be collected, we have shown that the model error is still expected
744 to decrease significantly as more data is collected in the future.

745 We demonstrated the model’s significant utility for novel mate-
746 rials discovery in an exercise of identifying promising candidate
747 oxides in the context of various clean energy applications: solar
748 thermochemical water splitting and energy storage, CO_2 conver-
749 sion, and SOFC cathodes and electrolytes. We screened struc-
750 tures drawn from a different database (Materials Project) than
751 the source of the training structures (NRELMatDB) using the sim-
752 plest, “Element-only” graph encoding strategy (i.e., requiring only
753 the host crystal structure as input). Narrowing down the $\sim 35,000$
754 oxides initially queried to as few as ~ 10 depending on the strin-
755 gency of down-selection criteria, we identify candidates exhibit-
756 ing the greatest potential based on predicted vacancy defect en-
757 thalpy and host oxide stability criteria, which also “rediscover”
758 known materials from previous experimental literature. This ML
759 strategy therefore efficiently reveals a handful of top candidates
760 from an intractably large space for brute-force DFT or experi-
761 ments, and will help facilitate the discovery of optimal materi-
762 als in the future (along with significant potential for more chem-
763 istry and structural diversity in the training data). Even stricter
764 down-selection can now additionally be explored based on more
765 detailed properties from first principles calculations that are only
766 tractable across a small number of materials. The final critical
767 contribution of this study is the prediction of defect formation
768 enthalpies across all sites to rapidly estimate defect densities at
769 finite temperatures. By accounting for configurational entropy
770 in high-throughput, we can assess material performance at finite
771 temperatures, rather than relying purely on a zero kelvin picture
772 from individual defect predictions across just a handful of mate-
773 rials.

774 Conflicts of interest

775 There are no conflicts to declare.

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795 Data availability statement

796 The datasets generated during and/or analysed during the
797 current study are available in the Zenodo repository: "A
798 database of vacancy formation enthalpies for materials discovery"
799 at <https://zenodo.org/record/5999073> (DOI: 10.5281/zeno-
800 do.5999073).⁴⁹ All data generated or analysed during this study
801 are included in this published article (and its supplementary in-
802 formation files).

803 Code availability statement

804 The open-source CGCNN code for training models that directly
805 predict vacancy formation enthalpies has been distributed on
806 the "Paper1" branch at the following GitHub repository (<https://github.com/mwitman1/cgcndefect/tree/Paper1>), which is
807 a modified fork of the original open-source CGCNN code (<https://github.com/txie-93/cgcnn>).
808
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810 Notes and references

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