

Quantum-chemical calculation of two-dimensional infrared spectra using localized-mode VSCF/VCI

Julia Brüggemann¹, Mario Wolter², Christoph R. Jacob^{*,3}

Technische Universität Braunschweig, Institute of Physical and Theoretical Chemistry,
Gaußstraße 17, 38106 Braunschweig, Germany

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¹ORCID: 0000-0003-4252-4980

²ORCID: 0000-0001-6948-6801

³ORCID: 0000-0002-6227-8476, E-Mail: c.jacob@tu-braunschweig.de

Abstract

Computational protocols for the simulation of two-dimensional infrared (2D IR) spectroscopy usually rely on vibrational exciton models, which require an empirical parametrization. Here, we present an efficient quantum-chemical protocol for predicting static 2D IR spectra that does not require any empirical parameters. For the calculation of anharmonic vibrational energy levels and transition dipole moments, we employ the localized-mode vibrational self-consistent field (L-VSCF) / vibrational configuration interaction (L-VCI) approach previously established for (linear) anharmonic theoretical vibrational spectroscopy [Panek and Jacob, *ChemPhysChem* **15**, 3365–3377 (2014)]. We demonstrate that with an efficient expansion of the potential energy surface using anharmonic one-mode potentials and harmonic two-mode potentials, 2D IR spectra of metal carbonyl complexes and of dipeptides can be predicted reliably. We further show how the close connection between L-VCI and vibrational exciton models can be exploited to extract the parameters of such models from those calculations. This provides a novel route to the fully quantum-chemical parametrization of vibrational exciton model for predicting 2D IR spectra.

1 Introduction

Two-dimensional infrared (2D IR) spectroscopy is a modern experimental method used to sensitively probe molecular structures and dynamics.¹⁻⁵ Since its inception by Hamm, Lim, and Hochstrasser 25 years ago,⁶ it has flourished into a broadly applicable experimental method.⁷ Applications in chemical biology include the elucidation of the structure^{8,9} and dynamics of proteins¹⁰⁻¹⁶ in solution. Recent experimental advances allow for studying biomolecules at interfaces,^{17,18} enable transient spectroscopy for following non-equilibrium protein dynamics,¹⁹ and implement spectro-electrochemistry to study redox-active proteins.^{20,21} Moreover, 2D IR spectroscopy is employed to investigate ground-state and excited-state dynamics in model systems such as metal carbonyl complexes²²⁻²⁵ and can be applied in material science to shine light on the ion dynamics in lithium ion batteries.²⁶

However, the interpretation of 2D IR spectra critically depends on computations.²⁷⁻²⁹ Only by comparison to computational predictions, detailed information on the structure and dynamics can be extracted from experimental 2D IR spectra. Simply speaking, in 2D IR spectroscopy one performs a pump-probe experiment, in which a pump pulse excites a molecule from the vibrational ground state to a singly-excited vibrational state, followed by a probe pulse that results in stimulated emission or in an excitation to a doubly excited vibrational state.^{4,30} This way, 2D IR spectroscopy reveals the anharmonicities of the vibrational modes as well as couplings between them. By spreading out the spectroscopic information in two dimensions, 2D IR spectroscopy can reveal information that is hidden in conventional vibrational spectra. Furthermore, by varying the delay between the pump and the probe pulses, dynamical information can be assessed. Because it specifically probes anharmonicity, for a computational treatment of 2D IR spectroscopy one has to go beyond the harmonic approximation³¹ that is commonly used in theoretical vibrational spectroscopy.^{2,4,32,33}

Common protocols for the simulation of 2D IR spectroscopy rely on empirical frequency maps in combination with vibrational exciton models (for an exhaustive review, see Ref. 34). Such models parametrize the frequencies and transition dipole moments of local vibrational modes as well as the harmonic couplings between them as functions of the molecular structure and the local electric field. Furthermore, the anharmonicity of the local modes is included as an empirical shift. This allows for the efficient calculation of the vibrational energy levels, which can be combined with molecular dynamics simulations and used as input for the simulation of 2D IR spectra.

Such a protocol is efficient and has been successfully applied in numerous studies over the past 25 years. For commonly studied systems, reliable frequency maps that have been carefully parametrized with the help of quantum-chemical calculations are available, most importantly for the amide I vibrations in proteins^{35–40} and for the O–H and O–D stretching vibrations in water.^{41–43} However, the construction of frequency maps for new systems can be tedious and its parametrization requires a significant effort. Therefore, the reliance on such parametrizations has slowed down the progress in 2D IR spectroscopy. For instance, the interpretation of amide I 2D IR spectra of peptides containing proline required a dedicated parametrization.⁴⁴ For promising 2D IR experiments studying proteins beyond the amide I vibrations⁴⁵ or investigating nucleic acid bases or DNA^{46–48} suitable parametrizations became available only years after the initial experiments^{49–53} and the interpretation of such experiments partly remains elusive.

Quantum-chemical methods of theoretical vibrational spectroscopy allow for the calculation of vibrational energy levels without the need for system-specific parametrizations and can thus close this gap. The calculation of vibrational spectra within the harmonic approximation is well-established and routinely applied for molecules with hundreds of atoms (see, e.g., Refs. 54–57), including molecular systems in aqueous solution.^{58–61} While the calculation of anharmonic vibrational energy levels is less established, most impor-

tantly because it is associated with a higher computational effort, tremendous progress has been made in the past decades.⁶²⁻⁷⁰ Most importantly, efficient approximate schemes for the inclusion of anharmonicities in theoretical vibrational spectroscopy have become available that are applicable to medium-sized molecules, including polypeptides.⁷¹⁻⁷⁴

Here, we extend one such approach, the localized-mode vibrational self-consistent field (L-VSCF) method in combination with the localized-mode vibrational configuration interaction (L-VCI) method,^{75,76} for the calculation of 2D-IR spectra. When applied together with an anharmonic one-mode potential energy surface with harmonic two-mode couplings between localized modes, this approach has been shown to be able to predict anharmonic vibrational spectra accurately and efficiently.^{73,77} Moreover, it allows for a direct connection with vibrational exciton models,⁷⁸ without the need for any empirical parametrization.

Previously, some attempts have been made to obtain 2D IR spectra from quantum-chemical calculations. Mukamel and coworkers employed a fourth-order Taylor expansion of the potential-energy expansion as basis of an exciton Hamiltonian.⁷⁹ Subsequently, second-order vibrational perturbation theory has been applied for modeling 2D IR spectra of metal carbonyls²³ and of deuterated glycolaldehyde.⁸⁰ Sibert and co-workers constructed a model of harmonically-coupled Morse oscillators and applied it to model the 2D IR spectra of carbonyl complexes.⁸¹ More recently, Besley and coworkers⁸² employed calculations in the harmonic approximation in combination with a localization of normal modes⁸³ to extract the parameters of an exciton model (local-mode frequencies and harmonic couplings). They then applied an empirical anharmonicity on top of this model to simulate the amide I 2D IR spectra of small peptides. Bowman, Tokmakoff, and coworkers employed high-level VSCF/VCI calculations in combination with a local monomer approximation for protonated water clusters in order to interpret 2D IR spectra.⁸⁴

Here, our goal is to devise a computational protocol that is efficient and parameter-free

and that allows for both the direct prediction of 2D IR spectra for arbitrary molecular systems and can serve as reference for the parametrization of vibrational maps as needed for empirical exciton models.

This work is organized as follows. In Section 2, we review the methodology applied for the quantum-chemical calculation of anharmonic vibrational energy levels and transition dipole moments with L-VSCF and L-VCI (Sections 2.1 and 2.2), discuss the connection to vibrational exciton models (Section 2.3), and recall the theory for the calculation of 2D IR spectra (Section 2.4). In Section 3 we give the details of our computational protocol. In Section 4, we apply this protocol for selected test cases, specifically for two carbonyl complexes and two dipeptides. We compare the different approximations for the potential energy surface in L-VSCF/L-VCI and exciton models derived from the quantum-chemical calculations. Finally, concluding remarks and an outlook are presented in Section 5.

2 Theory

2.1 Harmonic approximation and localized modes

In the harmonic approximation, the starting point for the calculation of vibrational spectra is the calculation of the Hessian matrix $\mathbf{H}^{(m)}$, which contains the second derivatives of the potential energy surface with respect to mass-weighted Cartesian coordinates.^{31,85} By diagonalizing this Hessian,

$$\tilde{\mathbf{H}}^{(q)} = \mathbf{Q}^T \mathbf{H}^{(m)} \mathbf{Q} \quad (1)$$

one obtains the harmonic normal modes \mathbf{Q} as eigenvectors with the eigenvalues $H_{ij}^{(q)}$, which are related to the vibrational frequencies $\omega_i = \sqrt{H_{ij}^{(q)}}$, and give rise to the vibrational

energy levels,

$$E_{v_1, \dots, v_M} = \sum_{i=1}^M \hbar \omega_i \left(v_i + \frac{1}{2} \right), \quad (2)$$

where M is the number of vibrational degrees of freedom. In the double-harmonic approximation, the transition dipole moments for the fundamental transitions are given by the derivatives of the molecular dipole moment with respect to the normal-mode coordinates, i.e., $\boldsymbol{\mu}_i = d\boldsymbol{\mu}/dq_i$.

Using mass-weighted normal-mode coordinates q_i , the harmonic approximation to the molecular potential energy surface is given by

$$V^{\text{harm}}(q_1, \dots, q_M) = \sum_{i=1}^M \frac{1}{2} \omega_i^2 q_i^2. \quad (3)$$

For anharmonic theoretical vibrational spectroscopy, it can be advantageous to expand the potential energy surface in localized-mode coordinates instead of normal-mode coordinates.^{75-77,86} To this end, all vibrational modes that contribute to a specific band or are of interest are collected into the subset \mathbf{Q}^{sub} . For 2D IR spectroscopy, this will usually be only a small number of vibrational modes, such as the carbonyl stretching vibrations in metal carbonyls or the amide I vibrations in peptides. For this subset of modes, a unitary transformation \mathbf{U} is determined such that the resulting modes,

$$\tilde{\mathbf{Q}}^{\text{sub}} = \mathbf{Q}^{\text{sub}} \mathbf{U} \quad (4)$$

are maximally localized, as measured by a suitable criterion.⁸³ Here and in the following, a tilde denotes quantities that refer to localized modes. The Hessian with respect to localized-mode coordinates,

$$\tilde{\mathbf{H}}^{\text{sub}} = \mathbf{U}^T \mathbf{H}^{(q), \text{sub}} \mathbf{U} \quad (5)$$

is no longer diagonal, but the localization re-introduces non-diagonal elements that describe the harmonic coupling between localized modes, i.e., the harmonic approximation

to the potential energy surface now becomes

$$V^{\text{harm}}(\tilde{q}_1, \dots, \tilde{q}_M) = \sum_{i=1}^M \frac{1}{2} \tilde{\omega}_i^2 q_i^2 + \sum_{i<j}^M \tilde{H}_{ij} \tilde{q}_i \tilde{q}_j, \quad (6)$$

where $\tilde{\omega}_i = \sqrt{\tilde{H}_{ii}}$ are the localized-mode frequencies and \tilde{H}_{ij} are the off-diagonal elements of the Hessian with respect to localized modes.

2.2 L-VSCF and L-VCI

To account for anharmonic effects in theoretical vibrational spectroscopy, one needs to go beyond the harmonic approximation to the potential energy surface given by Eq. (3) or Eq. (6). Commonly, this is done by using a truncated n -mode expansion, which we perform in localized-mode coordinates. When including up to two-mode contributions, this corresponds to^{87,88}

$$V^{\text{2-mode}}(\tilde{q}_1, \dots, \tilde{q}_M) = \sum_{i=1}^M \tilde{V}_i^{(1)}(\tilde{q}_i) + \sum_{i<j}^M \tilde{V}_{ij}^{(2)}(\tilde{q}_i, \tilde{q}_j) \quad (7)$$

Here, the one-mode potentials $\tilde{V}_i^{(1)}(\tilde{q}_i)$ and the two-mode potentials $\tilde{V}_{ij}^{(2)}(\tilde{q}_i, \tilde{q}_j)$ are evaluated numerically on suitable grids of displacements along localized-mode coordinates.⁷⁵

As a further approximation, the full two-mode potentials can be replaced by their harmonic counterparts, i.e.,

$$V^{\text{1-mode+2h}}(\tilde{q}_1, \dots, \tilde{q}_M) = \sum_{i=1}^M \tilde{V}_i^{(1)}(\tilde{q}_i) + \sum_{i<j}^M \tilde{H}_{ij} \tilde{q}_i \tilde{q}_j \quad (8)$$

Note that for this approximation, the number of required single-point calculations scales linearly with the number of considered localized modes, as the harmonic two-mode couplings can be extracted from the Hessian with respect to localized modes.

Using these approximations, the vibrational Schrödinger equation can be solved using L-VSCF / L-VCI.^{75,77} L-VSCF uses a product ansatz for the vibrational wavefunction,

$$\Psi_{n_1, n_2, \dots}^{\text{L-VSCF}}(\tilde{q}_1, \dots, \tilde{q}_M) = \prod_i^M \phi_i^{n_i}(\tilde{q}_i), \quad (9)$$

with the modals (i.e., one-mode wavefunctions) $\phi_i^{n_i}(\tilde{q}_i)$ for the i -th localized mode \tilde{q}_i , with the corresponding vibrational quantum number n_i . The modals can be obtained from the self-consistent solution of one-mode equations,⁸⁹

$$\left[-\frac{1}{2} \frac{\partial^2}{\partial \tilde{q}_i^2} + \tilde{V}_i^{(1)}(\tilde{q}_i) + V_i^{\text{eff},0}(\tilde{q}_i) \right] \phi_i^{n_i}(\tilde{q}_i) = \tilde{\epsilon}_i^{n_i} \phi_i^{n_i}(\tilde{q}_i), \quad (10)$$

in which the effective potential $V_i^{\text{eff},0}(q_i)$ depends on the one-mode wavefunctions.

In L-VCI, one then uses a configuration interaction expansion of the vibrational wavefunction as linear combination of the L-VSCF wavefunctions $\Psi_{n_1, n_2, \dots}^{\text{L-VSCF}}$, i.e.,⁹⁰

$$\Psi_k^{\text{L-VCI}}(\tilde{q}_1, \dots, \tilde{q}_M) = \sum_I^{N_{\text{states}}} c_I^{(k)} \Psi_{\mathbf{n}_I}^{\text{L-VSCF}}(\tilde{q}_1, \dots, \tilde{q}_M). \quad (11)$$

Generally, one has to truncate the L-VCI expansion. Here, we use an L-VCISD expansion, which includes the ground state as well as singly and doubly excited states, which is the minimum necessary for modeling 2D IR spectroscopy. This approximation is usually sufficient when considering weakly coupled localized modes.^{73,77,78}

By diagonalizing the L-VCI matrix,

$$H_{\mathbf{n}, \mathbf{n}'} = \left\langle \Psi_{\mathbf{n}}^{\text{VSCF}} \left| \hat{H} \right| \Psi_{\mathbf{n}'}^{\text{VSCF}} \right\rangle. \quad (12)$$

one can obtain the expansion coefficients $c_I^{(n)}$ as well as the corresponding energy eigenvalues E_n . The anharmonic excitation frequencies are then given by $\bar{\omega}_n = E_n - E_0$, where the bar is used to distinguish the anharmonic frequencies from the harmonic fundamental frequencies ω_i .

Using the L-VCI expansion coefficients, the transition dipole moments between the corresponding vibrational states.

$$\boldsymbol{\mu}_{nm} = \left\langle \Psi_n^{\text{L-VCI}} \left| \hat{\boldsymbol{\mu}} \right| \Psi_m^{\text{L-VCI}} \right\rangle \quad (13)$$

can be calculated with the help of a one-mode expansion of the dipole moment surfaces. For a more detailed discussion of L-VSCF/L-VCI and well as benchmark calculations assessing its accuracy, we refer to Refs. 73, 75, 77.

of the i -th local mode. This can be used to set up a matrix representation of the dipole moment operator. For the case of only two modes [in analogy to (15)], one obtains,

$$\boldsymbol{\mu} = \left(\begin{array}{c|cc|cc} & \tilde{\boldsymbol{\mu}}_1 & \tilde{\boldsymbol{\mu}}_2 & & & \\ \hline \tilde{\boldsymbol{\mu}}_1 & & & \sqrt{2}\tilde{\boldsymbol{\mu}}_1 & 0 & \tilde{\boldsymbol{\mu}}_2 \\ \tilde{\boldsymbol{\mu}}_2 & & & 0 & \sqrt{2}\tilde{\boldsymbol{\mu}}_2 & \tilde{\boldsymbol{\mu}}_1 \\ \hline & \sqrt{2}\tilde{\boldsymbol{\mu}}_1 & 0 & & & \\ & 0 & \sqrt{2}\tilde{\boldsymbol{\mu}}_2 & & & \\ & \tilde{\boldsymbol{\mu}}_2 & \tilde{\boldsymbol{\mu}}_1 & & & \end{array} \right). \quad (16)$$

Transforming this matrix using the matrix \mathbf{C} of eigenvectors of the exciton Hamiltonian, the transition dipole moments between the vibrational states can be obtained.^{4,6}

Different strategies can be employed for obtaining the parameters of the above vibrational exciton Hamiltonian. First and most commonly, vibrational maps can be used,³⁴ which provide an empirical parametrization of the local-mode frequencies $\tilde{\omega}_i$, the harmonic coupling constants J_{ij} , and the local-mode transition dipoles $\tilde{\boldsymbol{\mu}}_i$ as functions of the molecular structure and the electrostatic environment of the local oscillators. This is commonly combined with a fixed value for the local-mode anharmonic shift Δ .

A second strategy was proposed by Hanson-Heine *et al.*⁸² which is based on quantum-chemical calculations. From a harmonic frequency calculation followed by a localization of the relevant normal modes (see Section 2.1), the localized-mode frequencies $\tilde{\omega}_i$ and local-mode transition dipoles $\tilde{\boldsymbol{\mu}}_i$ can be extracted directly. The harmonic coupling constants J_{ij} can be obtained as elements of the coupling matrix $\mathbf{J} = (\tilde{\mathbf{H}}^{\text{sub}})^{1/2}$, i.e., the matrix square root of the Hessian with respect to localized modes.⁸³ These parameters are then used in combination with an empirical anharmonic shift Δ to construct the vibrational exciton Hamiltonian. We will refer to this parametrization as “ Δ -exciton model”.

Here, we will explore a third strategy, which exploits the connection between the L-VCISD matrix and the vibrational exciton Hamiltonian.⁷⁸ To this end, we use the frequencies

of the L-VSCF eigenstates (i.e., the diagonal elements of the L-VCISD matrix) on the diagonal of the vibrational exciton Hamiltonian (“L-VSCF exciton model”). This way, the anharmonicity is taken into account directly and no empirical anharmonic shift is required. The off-diagonal elements of the vibrational exciton Hamiltonian and the transition dipole moments are handled as above (i.e., they are obtained from the harmonic localized modes).

2.4 2D IR spectra

The anharmonic vibrational excitation energies $\bar{\omega}_n$ and transition dipole moments $\boldsymbol{\mu}_{nm}$ calculated either quantum-chemically or with the help of a vibrational exciton model can be used as input for the calculation of 2D IR spectra.⁴ Here, we will only consider the static case, i.e., the 2D IR spectra are calculated for a fixed molecular structure. For additional theoretical background as well as the discussion of the dynamical case, we refer to Refs. 33,91,92.

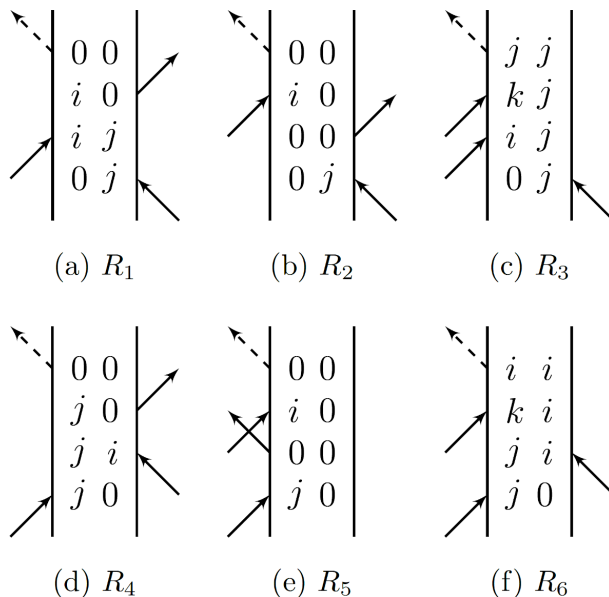


Figure 1: Double-sided Feynman diagrams for any number of coupled eigenstates. R_1 , R_2 , and R_3 are rephasing diagrams describing the third-order nonlinear response in the phase-matching $\mathbf{k}_I = -\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3$ direction, whereas R_4 , R_5 , R_6 describe the non-rephasing diagrams in the $\mathbf{k}_{II} = +\mathbf{k}_1 - \mathbf{k}_2 + \mathbf{k}_3$ direction.

2D IR spectroscopy probes the third-order nonlinear response. In general, three IR laser pulses are used, which lead to different Feynman pathways (see Fig. 1), rephasing and non-rephasing, depending on the wave vector $\mathbf{k} = \mp \mathbf{k}_1 \pm \mathbf{k}_2 + \mathbf{k}_3$. The third-order response functions $R_n(t_1, t_2, t_3)$ are thus described by six double-sided Feynman diagrams that generate 2D IR spectra for any number of coupled eigenstates.^{4,33,91} Conceptually, each response function represents a different process. The R_1 and R_4 functions represent stimulated emission, R_2 and R_5 represent ground-state bleaching, and R_3 and R_6 represent excited-state absorption.

The rephasing and non-rephasing response functions for any given number of eigenstates are calculated as

$$R_1(t_1, t_2, t_3) = i \sum_{i,j} \langle C_{j,i,j,i} \rangle \cdot e^{+i\bar{\omega}_i t_1 + i(\bar{\omega}_j - \bar{\omega}_i) t_2 - i\bar{\omega}_i t_3} e^{-(t_1+t_3)/T_2} \quad (17)$$

$$R_2(t_1, t_2, t_3) = i \sum_{i,j} \langle C_{j,j,i,i} \rangle \cdot e^{+i\bar{\omega}_j t_1 - i\bar{\omega}_i t_3} e^{-(t_1+t_3)/T_2} \quad (18)$$

$$R_3(t_1, t_2, t_3) = i \sum_{i,j,k} \langle C_{j,i,ik,jk} \rangle \cdot e^{+i\bar{\omega}_j t_1 + i(\bar{\omega}_j - \bar{\omega}_i) t_2 - i(\bar{\omega}_k - \bar{\omega}_j) t_3} e^{-(t_1+t_3)/T_2} \quad (19)$$

and

$$R_4(t_1, t_2, t_3) = i \sum_{i,j} \langle C_{j,i,i,j} \rangle \cdot e^{-i\bar{\omega}_j t_1 + i(\bar{\omega}_j - \bar{\omega}_i) t_2 - i\bar{\omega}_j t_3} e^{-(t_1+t_3)/T_2} \quad (20)$$

$$R_5(t_1, t_2, t_3) = i \sum_{i,j} \langle C_{j,j,i,i} \rangle \cdot e^{-i\bar{\omega}_j t_1 - i\bar{\omega}_i t_3} e^{-(t_1+t_3)/T_2} \quad (21)$$

$$R_6(t_1, t_2, t_3) = i \sum_{i,j,k} \langle C_{j,i,jk,ik} \rangle \cdot e^{-i\bar{\omega}_j t_1 - i(\bar{\omega}_j - \bar{\omega}_i) t_2 - i(\bar{\omega}_k - \bar{\omega}_i) t_3} e^{-(t_1+t_3)/T_2}. \quad (22)$$

Here, $\bar{\omega}_n$ are the (anharmonic) frequencies of the vibrational excitations, with the indices i and j referring to singly excited states and the index k referring to doubly excited states. The variables t_i are the delay times between laser pulses and T_2 is the dephasing time parameter.

The $\langle C_{\alpha,\beta,\gamma,\delta} \rangle$ are the four-point correlation functions for a given polarization condition of the laser pulses. For each response function R_n there is a different pathway, leading to

different polarization conditions. The response functions can be generalized by writing the polarizations relative to one another, in the form of the four-point correlation function as described by Hochstrasser⁹³

$$\begin{aligned}
\langle C_{\alpha,\beta,\gamma,\delta} \rangle &= \left\langle \left(\hat{\mu}_\alpha \cdot \hat{E}_a \right) \left(\hat{\mu}_\beta \cdot \hat{E}_b \right) \left(\hat{\mu}_\gamma \cdot \hat{E}_c \right) \left(\hat{\mu}_\delta \cdot \hat{E}_d \right) \right\rangle \\
&= \frac{1}{30} \left[\cos \theta_{\alpha\beta} \cos \theta_{\gamma\delta} (4 \cos \theta_{ab} \cos \theta_{cd} - \cos \theta_{ac} \cos \theta_{bd} - \cos \theta_{ad} \cos \theta_{bc}) \right. \\
&\quad + \cos \theta_{\alpha\gamma} \cos \theta_{\beta\delta} (4 \cos \theta_{ac} \cos \theta_{bd} - \cos \theta_{ab} \cos \theta_{cd} - \cos \theta_{ad} \cos \theta_{bc}) \\
&\quad \left. + \cos \theta_{\alpha\delta} \cos \theta_{\beta\gamma} (4 \cos \theta_{ad} \cos \theta_{bc} - \cos \theta_{ab} \cos \theta_{cd} - \cos \theta_{ac} \cos \theta_{bd}) \right]
\end{aligned} \tag{23}$$

where \hat{E}_n are polarizations of the laser pulses (which are determined by the experimental setup) and $\hat{\mu}_\alpha$ are the transition dipole moments. The angles θ_{ab} (with latin letters) are angles between the laser pulses, whereas $\theta_{\alpha\beta}$ (with greek letters) are angles between transition dipole moments. The specific combination of transition dipole moments relevant for each of the six response functions is given by the subscripts of $\langle C_{\alpha,\beta,\gamma,\delta} \rangle$ in Eqs. (17) to (22), where single indices i, j, k refer to transitions from the ground state to the specified excited state, and double indices ik and jk refer to the transition from the singly-excited state i or j to the doubly excited state k .

Since the third-order response is commonly visualized in the frequency domain, the response functions are double Fourier transformed with respect to the t_1 and t_3 coherence times,^{4,22,79}

$$S_n(\omega_3, t_2, \omega_1) = \int_0^\infty \int_0^\infty iR_n(t_3, t_2, t_1) e^{i\omega_1 t_1} e^{i\omega_3 t_3} dt_1 dt_3, \tag{24}$$

with the variable parameter t_2 determined by the delay time between the second and third laser pulse in the experiment. Now, the real parts of the response functions are summed up and double Fourier-transformed in order to get purely absorptive spectra

$$R(\omega_1, t_2, \omega_3) = \Re \left[\sum_{n=1}^6 R_n(\omega_1, t_2, \omega_3) \right]. \tag{25}$$

Other evaluation methods, e.g., plotting the imaginary part or the photon echo signals that are only generated in the \mathbf{k}_I direction, are easily accessed by altering the function in Eq. (25), but will not be considered here.

3 Computational Details

All quantum-chemical calculations were performed using density-functional theory (DFT) with the TURBOMOLE V7.5.1 program package.⁹⁴ We employed the B3LYP exchange-correlation functional⁹⁵ and the def2-TZVP basis set.⁹⁶ Solvation effects were included using the COSMO model.^{97,98} For the metal carbonyl complexes, we used default COSMO parameters for *n*-hexane, whereas for the dipeptides we used default parameters for water. For the dipeptides, the *N*-deuterated structures were considered in all vibrational calculations. The quantum-chemical calculations were automated using the PYADF scripting framework.^{99,100}

First, the molecular structures were optimized using TURBOMOLE and harmonic vibrational frequencies and normal modes were calculated using the SNF program.^{56,85} For the localization of the relevant normal modes (consisting of the CO stretch modes for the metal carbonyls and of the amide I vibrations for the dipeptides), we employed our LOCVIB Python package.^{56,83,101} This localization provides localized-mode coordinates as well as localized-mode harmonic frequencies, transition dipole moments, and harmonic coupling constants.⁸³

The anharmonic potential energy surfaces in terms of localized modes were constructed using our VIBRATIONS code for anharmonic theoretical vibrational spectroscopy^{75,77,102} in combination with PYADF and TURBOMOLE. Here, we used two different approximations of the potential energy surface, either including both anharmonic one-mode and two-mode potentials [2-mode, see Eq. (7)], or including only anharmonic one-mode potentials

in combination with harmonic two-mode potentials [1-mode+2h, see Eq. (8)]. In both cases, we used grids of 16 points along each local mode coordinate as described in Ref. 75. Subsequently, L-VSCF/L-VCI were performed with VIBRATIONS. Here, the singly and doubly excited states were included in the VCI expansion, corresponding to an L-VCISD approximation. For further details, we refer to Refs. 75,77.

These L-VSCF/L-VCI calculations provided anharmonic vibrational frequencies and transition dipole moments for singly and doubly excited states, which could then be used as input for the calculation of the 2D IR spectra. Alternatively, parameters for the construction of a vibrational exciton model as described in Section 2.3 were extracted from the harmonic calculation and the localization as well as the L-VSCF calculation. We considered two different exciton models, termed L-VSCF exciton model and Δ -exciton model. By diagonalizing the matrix representation of the vibrational exciton model, the same input data for the calculation of 2D IR spectra (i.e., anharmonic vibrational frequencies and transition dipole moments) can be obtained.

Using the anharmonic vibrational frequencies and transition dipole moments for singly and doubly excited states, the 2D IR spectra are calculated as described in Section 2.4. For the dephasing time, which influences the peak broadening, we chose $T_2 = 2$ ps for all calculations as this is a time scale often found in amide I vibrations.⁴ For the waiting time t_2 we used no time delay (i.e., $S(\omega_3, t_2 = 0, \omega_1)$). Our code for simulating 2D IR spectra is written using Python 3 and makes use of Numpy.^{103,104} All spectra are plotted using Matplotlib.^{105,106}

A data set containing coordinates of all considered molecular structure, output data from the harmonic vibrational frequency calculations, the localization of normal modes and the anharmonic L-VSCF/L-VCI calculation as well as Python code and Jupyter notebooks that can be used for the calculation of 2D-IR spectra from this data and for generating the plots presented here is available at Ref. 107.

4 Results and Discussion

For our quantum-chemical calculations we consider four test cases that correspond to typical applications of 2D IR spectroscopy in experiment. First, we investigate the CO stretching vibrations in two metal-carbonyl complexes, dicarbonyl(acetylacetonato)rhodium(I) (DAR) and iron(0)-pentacarbonyl (IPC). Second, we examine the amide I region for two dipeptides, 2,5-dioxopiperazine (DKP) and *N*-acetylglycine-methylamide (NAGMA). The molecular structures of these test cases are shown in Fig. 2.

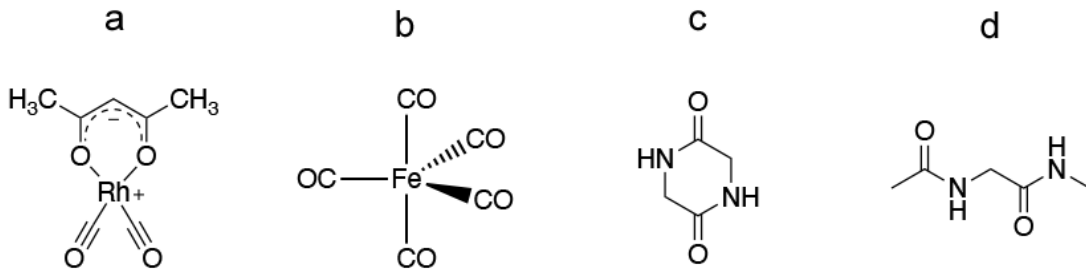


Figure 2: Molecular structures of (a) dicarbonyl(acetylacetonato)rhodium(I) (DAR), (b) iron(0)-pentacarbonyl (IPC), (c) 2,5-dioxopiperazine (DKP), and (d) *N*-acetylglycine-methylamide (NAGMA).

The first test case is the well-studied DAR molecule, which shows a prototypical 2D IR spectrum.^{22,30,108} It features two strongly-coupled anharmonic CO stretch vibrations, with an asymmetric stretch mode at $\bar{\omega}_a$ and a symmetric stretch mode at $\bar{\omega}_s$, both of which carry strong IR intensity. These two fundamental vibrations give rise to three overtone and combination bands.

The calculated 2D IR spectra of DAR are shown in Fig. 3. The fundamentals show up as negative peaks on the diagonal, which are each accompanied by a negative peak that is due to the excitation to the corresponding overtone. The coupling between the modes results in cross-peaks, where the anharmonically shifted cross-peaks correspond to the excitation of the combination band.³⁰ Different polarization conditions vary the intensities of the

cross-peaks, which are comparably weak in the $\langle ZZZZ \rangle$ polarization condition, but can be strongly enhanced by using the $\langle ZZXX \rangle$ polarization condition.²²

In our calculations of the 2D IR spectrum of DAR, we compare different computational approximations. Our most sophisticated approach uses a two-mode approximation potential-energy surface [see Eq. (7)] in combination with L-VSCF/L-VCISD calculations. The corresponding results are shown in Fig. 3a and b for the $\langle ZZZZ \rangle$ and $\langle ZZXX \rangle$ polarization conditions, respectively. These spectra serve as reference for the following, more approximate models. As a first simplification, we only calculate the anharmonic one-mode potentials and approximate the two-mode potential harmonically [see Eq. (8)]. This drastically cuts down the computational costs for the construction of the potential energy surface. The resulting 2D IR spectra are shown in Fig. 3c and d and are virtually indistinguishable from those obtained with the fully anharmonic two-mode potentials, which confirms that this approximation is valid.

As another approximation, we construct a vibrational exciton model using the anharmonic L-VSCF energy levels for the local-mode vibrations, the harmonic local-mode transition dipole moments and the harmonic coupling constants (L-VSCF exciton model). The corresponding 2D IR spectra are shown in Fig. 3e and f, which are almost identical to those from the L-VSCF/L-VCI calculations. This agreement demonstrates that an exciton model with suitable parameters is able to reproduce the results of fully anharmonic L-VSCF/L-VCI calculations, i.e., the approximations that are made in the construction of exciton models⁷⁸ are justified here.

The local-mode frequencies and coupling constants of this L-VSCF exciton models are summarized in Table I. The anharmonic L-VSCF local-mode frequencies in this model can be approximated by introducing an anharmonic shift of $\Delta = 21 \text{ cm}^{-1}$ on top of the harmonic local-mode frequencies, resulting in a simplified Δ -exciton model [see Eq. (15)]. Again, this Δ -exciton model results in 2D IR spectra (see Fig. 3g and h) that are indis-

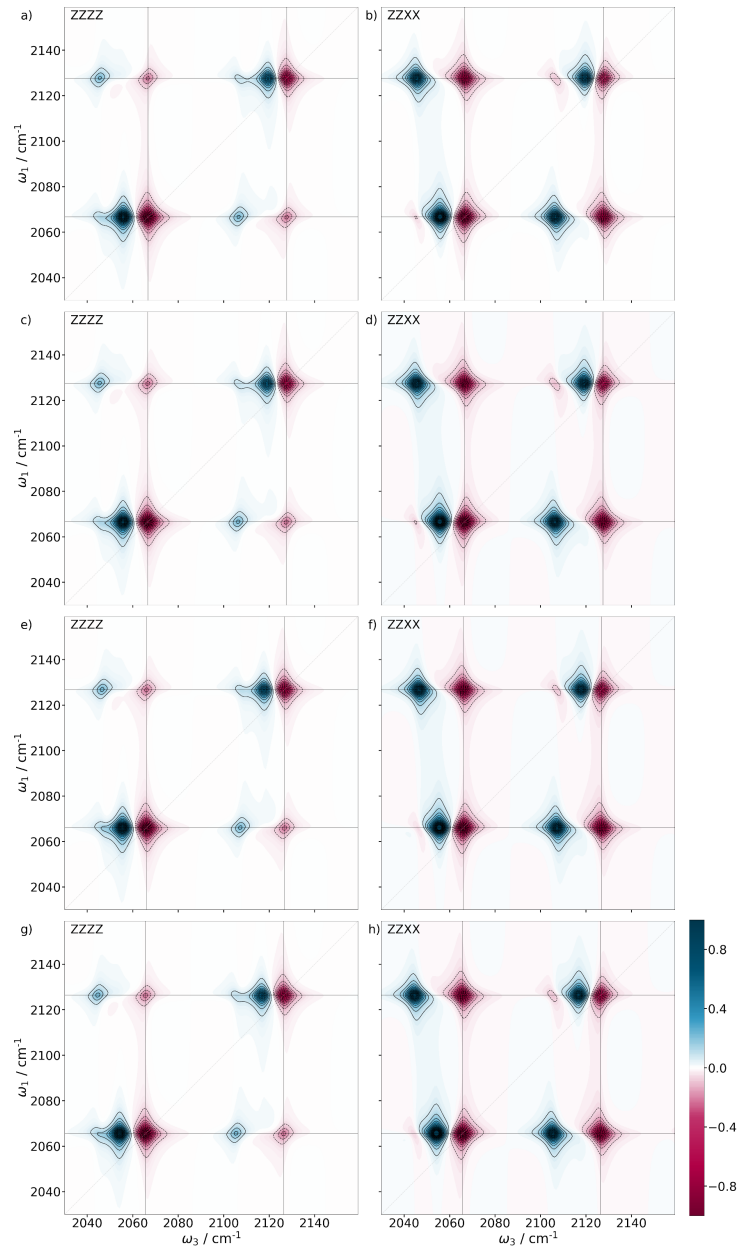


Figure 3: Calculated 2D IR spectra of DAR for the $\langle ZZZZ \rangle$ (left) and $\langle ZZXX \rangle$ (right) polarization conditions. (a) and (b) L-VSCF/L-VCISD calculations with anharmonic one- and two-mode potentials, (c) and (d) L-VSCF/L-VCISD calculations with anharmonic one-mode potentials and harmonic two-mode potentials, (e) and (f) anharmonic L-VSCF exciton model, (g) and (h) harmonic Δ -exciton model with an anharmonic shift of $\Delta = 21 \text{ cm}^{-1}$. All plots are normalized to the intensity of the highest peak. Horizontal and vertical lines indicate the frequencies of the fundamentals.

Table I: Local-mode frequencies and coupling constants used in the vibrational exciton model for DAR. Values obtained within the harmonic approximation are given for comparison. For the L-VSCF exciton model, the local-mode frequencies are extracted from the anharmonic L-VSCF calculation. For the Δ -exciton model, an anharmonic shift of $\Delta = 21 \text{ cm}^{-1}$ is applied. All values are given in cm^{-1} .

	$\tilde{\omega}_{1,0} = \tilde{\omega}_{0,1}$	$\tilde{\omega}_{2,0} = \tilde{\omega}_{0,2}$	$\tilde{\omega}_{1,1}$	J_{12}
harmonic	2117	4234	4234	30.4
L-VSCF exciton	2096	4173	4193	30.4
Δ -exciton	2096	4171	4192	30.4

tinguishable from the other approximations.

Comparing our results to the experimental spectra measured by Khalil *et al.*²² shows a good agreement with the overall line shapes and relative peak positions, but we find that our spectra are shifted to higher wavenumbers. For a more detailed comparison, Table II lists our calculated fundamental transition frequencies and anharmonic shifts and compares them to the values extracted from the experimental 2D IR spectra in Ref. 22 as well as to those from previous calculations in Refs. 79 and 4.

For all calculations, the positions of the fundamentals are shifted compared to experiment, which is due to the shortcoming of density-functional theory as employed for the vibrational frequency calculations. However, our calculations provide a rather good agreement for the splitting between the two fundamentals, which is calculated as 61 cm^{-1} , while it amounts to 69 cm^{-1} in experiment. The calculations of Hamm and Zanni in Ref. 4 yield a similar splitting of 59 cm^{-1} , while the model of Moran *et al.* in Ref. 79 predicts a splitting of only 27 cm^{-1} .

In addition, Table II compares three different anharmonicities: the anharmonicity of the doubly-excited antisymmetric CO stretch mode $\Delta_{2a,a}$ (i.e., the difference between the two

Table II: Comparison of fundamental transition frequencies for the antisymmetric and symmetric stretch modes, $\bar{\omega}_a$ and $\bar{\omega}_s$, and of the anharmonic shifts $\Delta_{2a,a}$, $\Delta_{as,a/s}$, and $\Delta_{2s,s}$ for the DAR molecule. Included are the values calculated with our different approximations as well as previous experimental and computational results. All values are given in cm^{-1} . An extended version of this table is provided in the Supporting Information (Table S1).

	$\bar{\omega}_a$	$\bar{\omega}_s$	$\Delta_{2a,a}$	$\Delta_{as,a/s}$	$\Delta_{2s,s}$
Experiment (Khalil <i>et al.</i> ²²)	2015	2084	14	26	11
Calculation (Moran <i>et al.</i> ⁷⁹)	1923	1950	12	20	8
Calculation (Hamm and Zanni ⁴)	1889	1948	11	23	11
L-VSCF/L-VCISD 2-mode	2067	2128	11	21	8
L-VSCF/L-VCISD 1-mode+2h	2067	2128	11	21	8
L-VSCF exciton model	2066	2127	11	20	9
Δ -exciton model	2066	2126	11	21	10

peaks in the lower left corner of the 2D IR spectra), the anharmonicity of the doubly-excited symmetric CO stretch mode $\Delta_{2s,s}$ (i.e., the difference between the two peaks in the upper right corner), and the anharmonicity of the the combination band $\Delta_{as,a/s}$ (i.e., the difference between the two peaks in the upper left and in the lower right corner). All calculations are in good agreement with the experimental anharmonicities, even though they underestimate them by a few wavenumbers.

As second example, we consider the 2D IR spectrum for the CO stretch vibrations in iron(0)-pentacarbonyl (IPC). The five local CO stretch vibrations give rise to five normal modes, of which three are IR active. Two of them are the degenerate equatorial vibrational modes $\bar{\omega}_{\text{eq}}$, the other one is the axial vibrational mode $\bar{\omega}_{\text{ax}}$. The remaining two modes are not IR active.

Figure 4 shows the calculated 2D IR spectra for the two considered polarization condi-

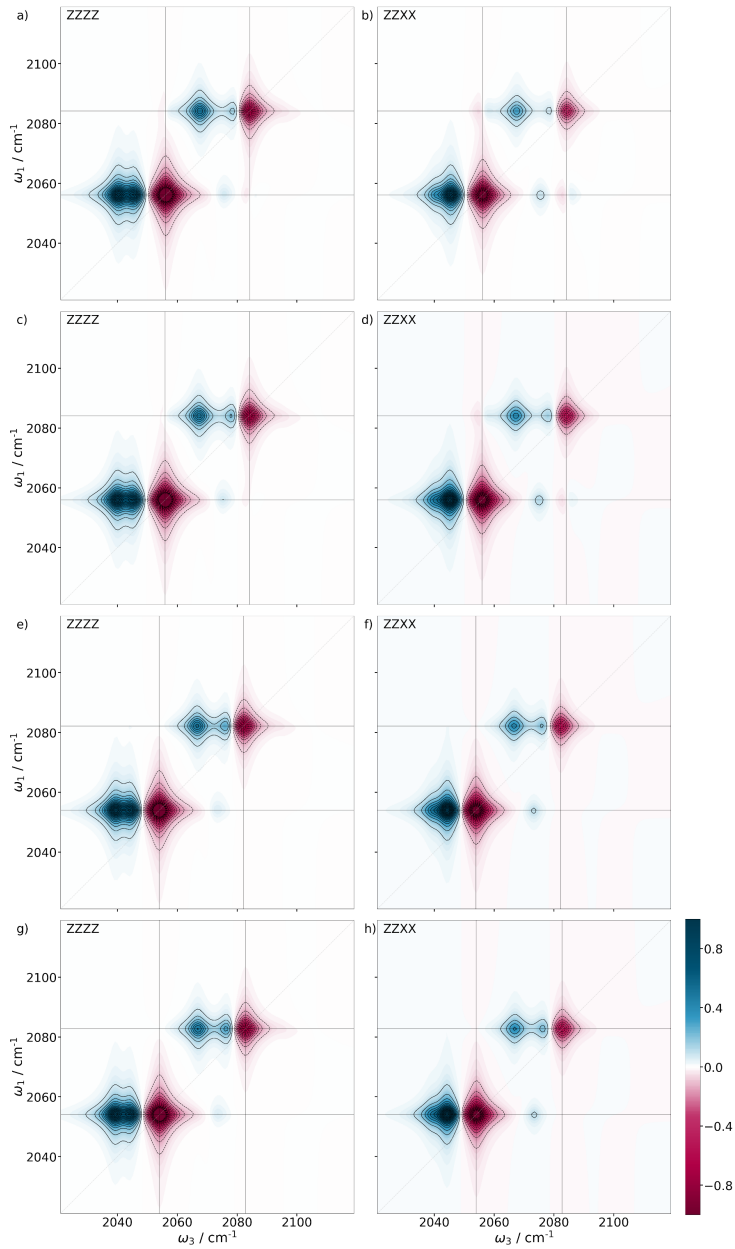


Figure 4: Calculated 2D IR spectra of IPC for the $\langle ZZZZ \rangle$ (left) and $\langle ZZXX \rangle$ (right) polarization conditions. (a) and (b) L-VSCF/L-VCISD calculations with anharmonic one- and two-mode potentials, (c) and (d) L-VSCF/L-VCISD calculations with anharmonic one-mode potentials and harmonic two-mode potentials, (e) and (f) anharmonic L-VSCF exciton model, (g) and (h) harmonic Δ -exciton model with an anharmonic shift of $\Delta = 21 \text{ cm}^{-1}$. All plots are normalized to the intensity of the highest peak. Horizontal and vertical lines indicate the frequencies of the fundamentals.

Table III: Comparison of fundamental transition frequencies for the equatorial and axial CO stretch modes, $\bar{\omega}_{\text{eq}}$ and $\bar{\omega}_{\text{ax}}$, and of the corresponding anharmonic shifts Δ_{eq} and Δ_{ax} for the IPC molecule. Included are the values calculated with our different approximations as well as previous experimental results. All values are given in cm^{-1} .

	$\bar{\omega}_{\text{eq}}$	$\bar{\omega}_{\text{ax}}$	Δ_e		Δ_a	
Experiment (Cahoon <i>et al.</i> ¹⁰⁹)	1999	2022	12		15	
L-VSCF/L-VCISD 2-mode	2056	2084	16	11	17	5
L-VSCF/L-VCISD 1-mode+2h	2056	2084	16	11	17	5
Exciton model	2054	2082	15	10	16	6
Δ -Exciton model	2054	2083	11	7	16	6

tions, and Table III lists the fundamental frequencies as well as the anharmonic shifts found in these spectra. The degenerate modes $\bar{\omega}_{\text{eq}}$ coincide and result in peaks that are twice as intense as the $\bar{\omega}_{\text{ax}}$ peaks (see also Ref. 110 for the assignment of the vibrational modes in IPC). For each of these two vibrations, the calculated 2D IR spectra show two anharmonically-shifted positive signals. An inspection of the relevant transitions in the L-VSCF/L-VCISD calculations allows us to provide an assignment of these features: For $\bar{\omega}_{\text{eq}}$ (see lower left corner of the 2D IR spectra) this is because the two degenerate vibrations of the equatorial CO stretch modes give rise to two overtones as well as one combination band, which both carry IR intensity and appear at different frequencies. For $\bar{\omega}_{\text{ax}}$ (see upper right corner of the 2D IR spectra), the overtones of the axial CO stretch vibration are close in energy with the overtone of one of the totally-symmetric CO stretch vibrations, which gives rise to a Fermi resonance. The 2D IR spectra show no visible cross-peaks.

A comparison of the 2D IR spectra calculated using L-VSCF/L-VCISD with full anharmonic two-mode potentials (see Fig. 4a and b) and with harmonically approximated two-mode potentials (see Fig. 4c and d) shows only minor differences, in particular for the

Fermi resonance of the overtone of the axial CO stretch vibrations. This confirms that the computationally efficient approximation of using L-VSCF/L-VCI with anharmonic one-mode potentials and harmonic two-mode potentials (1-mode+2h) is applicable for the CO stretch vibrations in carbonyl complexes.

Table IV: Local-mode frequencies and coupling constants used in the vibrational exciton model for IPC. Values obtained within the harmonic approximation are given for comparison. For the L-VSCF exciton model, the local-mode frequencies are extracted from the anharmonic L-VSCF calculation. For the Δ -exciton model, an anharmonic shift of $\Delta = 21 \text{ cm}^{-1}$ is applied. All values are given in cm^{-1} .

	fundam.		overtones		combinations			couplings		
	$\tilde{\omega}_{\text{eq}}$	$\tilde{\omega}_{\text{ax}}$	$\tilde{\omega}_{2\text{eq}}$	$\tilde{\omega}_{2\text{ax}}$	$\tilde{\omega}_{\text{eq,eq}}$	$\tilde{\omega}_{\text{eq,ax}}$	$\tilde{\omega}_{\text{ax,ax}}$	$J_{\text{eq,eq}}$	$J_{\text{eq,ax}}$	$J_{\text{ax,ax}}$
harmonic	2095	2124	4190	4248	4190	4219	4248	20.0	15.8	20.1
L-VSCF exciton	2074	2102	4127	4183	4147	4176	4204	20.0	15.8	20.1
Δ -exciton	2075	2103	4127	4185	4148	4177	4206	20.0	15.8	20.1

Based on this approximation, it is possible to set up the L-VSCF exciton model as described above. The frequency parameters used in this model are listed in Table IV. The resulting 2D IR spectra (see Fig. 4e and f) are in very good agreement with the L-VSCF/L-VCISD results, even though the peak positions are shifted by a few wavenumbers (see also Table III). These differences are due to the approximations inherent to the vibrational exciton model compared to a full L-VCISD treatment.⁷⁸ The L-VSCF exciton model can be closely approximated by using the harmonic local-mode frequencies in combination with an anharmonic shift of $\Delta = 21 \text{ cm}^{-1}$ (see Table IV). The corresponding 2D IR spectra for this Δ -exciton model (see Fig. 4g and h) are almost indistinguishable from those based on the L-VSCF exciton model.

Comparing our calculated 2D IR spectra to the experimental spectra recorded in solution¹⁰⁹ and in the gas-phase¹¹¹ shows an overall good agreement (see also Table III). Note that in experiment the peaks are broadened because of additional dynamical effects that

are not included in our static calculations. As for DAR, the positions of the fundamentals are shifted, but the splitting between the two vibrational modes are reproduced quite well (28 cm^{-1} vs. 21 cm^{-1} in the experimental spectrum). The splitting of the anharmonically shifted peaks is not resolved in experiment, but the anharmonic shifts are in very good agreement.

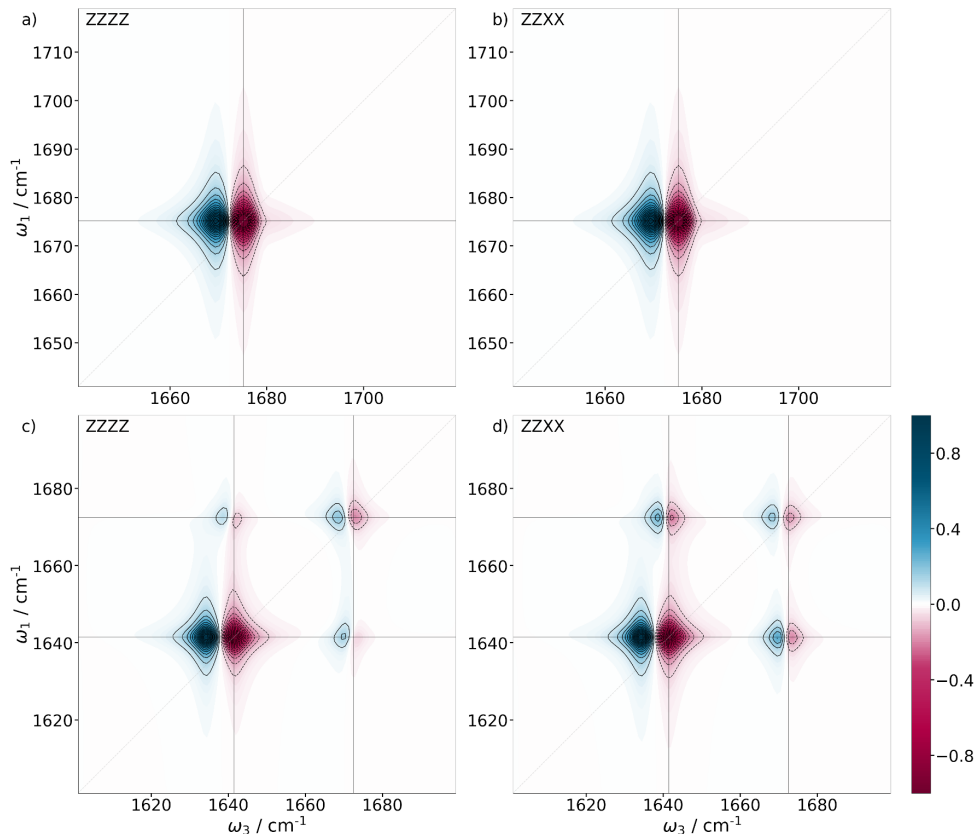


Figure 5: Calculated 2D IR spectra for the $\langle ZZZZ \rangle$ (left) and $\langle ZZXX \rangle$ (right) polarization conditions from. (a) and (b) are for the DKP molecule, (c) and (d) are for the NAGMA molecule.

As additional test cases, we turn to two prototypical dipeptides. DKP is the simplest cyclic dipeptide with two amide I normal modes, a symmetric ω_s and an asymmetric ω_a one, which are calculated to be at very similar frequencies, i.e., the local amide I oscillations are only weakly coupled. The symmetric mode is not IR active due to the inversion symmetry of the molecule. The second dipeptide, NAGMA, also has two amide I modes, both of which are IR active. Here, the coupling between the two local amide I

oscillations is stronger, leading to a larger frequency difference between the two amide I normal modes.

Table V: Local-mode frequencies and coupling constants used in the vibrational exciton models for DKP and NAGMA. Values obtained within the harmonic approximation are given for comparison. For the L-VSCF exciton models, the local-mode frequencies are extracted from the anharmonic L-VSCF calculations. For the Δ -exciton models, an anharmonic shift of $\Delta = 4 \text{ cm}^{-1}$ and of $\Delta = 7 \text{ cm}^{-1}$ is applied for DKP and NAGMA, respectively. All values are given in cm^{-1} .

		fundam.		overtones & comb.			coupling
		$\tilde{\omega}_{1,0}$	$\tilde{\omega}_{0,1}$	$\tilde{\omega}_{2,0}$	$\tilde{\omega}_{1,1}$	$\tilde{\omega}_{0,2}$	$J_{1,2}$
DKP	harmonic	1677	1677	3354	3354	3354	1.1
	L-VSCF exciton	1676	1678	3347	3348	3353	1.1
	Δ -exciton	1676	1678	3352	3354	3356	1.1
NAGMA	harmonic	1654	1675	3308	3329	3350	9.5
	L-VSCF exciton	1644	1669	3282	3314	3335	9.5
	Δ -exciton	1651	1679	3302	3330	3358	9.5

The 2D IR spectra of DKP and NAGMA calculated with L-VSCF/L-VCISD with anharmonic one-mode and harmonic two-mode potentials are shown in Fig. 5a, b and in Fig. 5c, d, respectively. The parameters of the vibrational exciton models based on our harmonic and L-VSCF calculations are listed in Table V. The 2D IR spectra calculated using L-VSCF/L-VCISD with full anharmonic two-mode potentials as well as those based on the L-VSCF and Δ -exciton models are given in Figs. S1 and S2 in the Supporting Information. As for the previous test cases, the 2D IR spectra calculated with all four approaches are almost indistinguishable. Table S2 in the Supporting Information further lists the fundamental transition frequencies as well as anharmonic shifts extracted from our calculations.

For DKP, the 2D IR spectrum shows only one negative peak corresponding to $\bar{\omega}_a$ on the

diagonal, together with an anharmonically shifted positive peak. The calculated anharmonic shift amounts to $\Delta_{a,2a} = 4 \text{ cm}^{-1}$. For NAGMA, the calculated 2D IR spectrum shows the two fundamentals on the diagonal, along with the corresponding overtones, with an anharmonic shift of $\Delta_{a,2a} = 7 \text{ cm}^{-1}$ for the more intense antisymmetric mode at lower wavenumbers, and of $\Delta_{s,2s} = 4 \text{ cm}^{-1}$ for the less intense symmetric mode. On the off-diagonal, peaks corresponding to the combination band appear, with an anharmonic shift of $\Delta_{as,a/s} = 2 \text{ cm}^{-1}$.

A direct comparison to experimental spectra is not possible for DKP and NAGMA, but we can compare to the spectra calculated by Hanson-Heine *et al.* using a vibrational exciton model based on harmonic localized-mode frequencies and coupling constants.⁸² Overall, the calculated 2D IR spectra show a very good agreement. This is not surprising, since the parameters of the vibrational exciton models corresponding to our calculations (see Table V) are very similar to those used in Ref. 82. The main difference is in the anharmonic shifts. Hanson-Heine *et al.* used an anharmonic shift of $\Delta = 16 \text{ cm}^{-1}$ for the local modes, as originally extracted by Hamm *et al.*⁶ from 2D-IR spectra. This similar values were also obtained from VPT2 calculations for model systems¹¹² and this value is therefore used in all empirical amide I models.

Here, we do not rely on an empirical parameter, but are able to calculate this local-mode anharmonic shift directly. From our calculations, we obtain $\Delta = 4 \text{ cm}^{-1}$ and $\Delta = 7 \text{ cm}^{-1}$ for DKP and NAGMA, respectively. These local-mode anharmonic shifts, which is significantly lower than the commonly used empirical value, and also indicate that this anharmonic shift might show significant variations. This is in line with earlier computational studies of the anharmonicity of amide I modes in small peptides, which have been shown to vary substantially depending on the considered conformation.¹¹³

5 Conclusions and Outlook

As 2D IR spectroscopy is commonly applied to probe anharmonic vibrations of coupled local oscillators, methods of anharmonic theoretical vibrational spectroscopy that are based on localized vibrational modes are ideally suited for computational 2D IR spectroscopy. Here, we have demonstrated that the L-VSCF/L-VCI method^{75,77} can be used for predicting 2D IR spectra.

We have restricted the treatment to the relevant modes (e.g., CO stretch vibrations or amide I modes) and have shown that a potential energy surface constructed using anharmonic one-mode potentials and harmonic two-mode potentials is sufficiently accurate. This provides a computationally efficient quantum-chemical route to the relevant anharmonic energy levels. In addition to a conventional, harmonic frequency calculation (which requires one calculation of the Hessian matrix), only a fixed number of additional single-point energy calculations per considered mode is required. This is significantly more efficient than other quantum-chemical methods for the calculation of anharmonic energy levels, such as second-order vibrational perturbation theory, which requires at least two additional calculations of the Hessian per considered normal mode.

The approach presented here is solely based on quantum-chemical calculations and thus does not rely on any empirical parameters. If necessary, all approximations within the L-VSCF/L-VCI approach can be alleviated by (a) using a more reliable methods for the quantum-chemical calculations in the construction of the potential energy surface, (b) using a more complete representation of the potential-energy surface by including additional modes and/or by extending the number of n -mode potentials that are calculated explicitly, and (c) by extending the size of the expansion space in the L-VCI calculations, albeit each of these will increase the required computational effort.⁷⁷ We believe that the efficient protocol applied here provides a reasonable starting point for the prediction of

2D IR spectra in the most common cases, as demonstrated by the examples considered here.

Because the L-VSCF/L-VCI approach is parameter-free, it will be particularly useful for the interpretation of 2D IR spectra in cases in which no reliable empirical exciton models are available, i.e., if vibrations other than the amide I region in polypeptides or the stretching vibrations in water are examined. Examples include 2D IR spectroscopy of nucleic acid bases or DNA⁴⁶⁻⁴⁸ and the 2D IR spectroscopy of polypeptides beyond the amide I region,⁴⁵ which we plan to address in the future.

In this work, we only considered static 2D IR spectra that were calculated for a single molecular structure. When extending the presented approach to the dynamical case, it will become necessary to consider a large number of additional structures. As any quantum-chemical approach will quickly become infeasible for larger systems and when considering thousands of structural snapshots from molecular dynamics simulations, this usually requires the use of empirically parametrized vibrational exciton models. However, as we have demonstrated L-VSCF/L-VCI also provides access to all the parameters required for the construction of such models.⁷⁸ The local-mode anharmonic energy levels can be extracted from the L-VSCF calculation, whereas the harmonic coupling constants as well as the local-mode transition dipole moments are available from the harmonic frequency calculation in combination with the localization of the normal modes.^{82,83} This can be used as basis for the parametrization of vibrational exciton models, which we will also explore in our future work in order to enable the quantum-chemical prediction of 2D IR spectra of dynamical systems.

Data Availability

The data that support the findings of this study are openly available in Zenodo at <http://doi.org/10.5281/zenodo.7328312>.

Author Contributions

Julia Brüggemann: Methodology (lead), Software (lead), Investigation (lead), Visualization (lead), Data Curation (lead), Writing – Original Draft (lead), Writing – Review and Editing (equal). **Mario Wolter:** Supervision (lead), Methodology (supporting), Software (supporting), Writing – Review and Editing (supporting). **Christoph R. Jacob:** Conceptualization (lead), Methodology (supporting), Data Curation (supporting), Writing – Review and Editing (equal)

Conflicts of Interest

The authors have no conflicts to disclose.

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