The Impact of the Different Geometrical Restrictions on the Nonadiabatic Photoisomerization of Biliverdin Chromophore

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 Abstract: The photoisomerization mechanism of the chromophore of bacterial biliverdin (BV) phytochromes is explored with the nonadiabatic dynamics simulation by using the on-the-fly trajectory surface-hopping method at the semi-empirical OM2/MRCI level. Particularly, the current study focuses on the influence of the geometrical constrains on the nonadiabatic photoisomerization dynamics of the BV chromophore. Here a rather simplified approach is employed in the nonadiabatic dynamics to capture the features of geometrical constrains, which adds the mechanical restriction on the specific moieties of the BV chromophore. This simplified method provides a rather quick approach to examine the influence of the geometrical restrictions on the photoisomerization. As expected, different constrains bring the distinctive influences on the photoisomerization mechanism of the BV chromophore, giving either strong or minor modification of both involved reaction channels and excited-state lifetimes after the constrains are added in different ring moieties. These observations not only contribute to the primary understanding of the role of the spatial restriction caused by biological environments in photoinduced dynamics of the BV chromophore, but also provide useful ideas for the artificial regulation of the photoisomerization reaction channels of phytochrome proteins.

1. Introduction

 Phytochromes are photosensitive proteins, which are widely found in plants, bacteria 3 and algae.¹ Plant phytochrome (PΦB) promotes the seed germination and the 4 chlorophyll synthesis in plants.² Phycocyanin (PCB) and biliverdin (BV) phytochromes that are found in algae and bacteria, respectively, can synthesize biological pigments 6 and promote growth. $3-5$ In addition, BV was also used to design the near-infrared 7 fluorescent proteins in the research of diseases such as cancers.^{$6-10$} Owing to their 8 importance, phytochromes have been extensively studied over decades.^{9,11-18}

Figure 1. BV model in Pr (*ZsZsZa*) configuration

 existence of many isomers. In order to label these configurations, the bridged carbon- carbon double and single bonds are defined as *Z/E* and *syn/anti(s/a)* isomerism, respectively. Some studies have determined that the Pr of PΦB is in the *ZaZsZa* form,²⁰ 4 while the Pr of PCB and BV has the $ZsZsZa$ form (Figure 1).^{21,22} In contrast, the Pfr 5 configuration is still not fully clarified, which may be dependent on $Pr \rightarrow Pfr$ 6 photoreaction processes.²³ Therefore, the study of Pr \rightarrow Pfr reaction not only deepens the understanding of the photoisomerization process, but also helps to determine the Pfr conformation.

9 Considerable efforts were made to understand the $Pr \rightarrow Pf$ r photoisomerization mechanism. The photoisomerization process of BV and PΦB in the protein 11 environments is believed to be around the $C_1C_6C_16$ double bond.^{24–29} Differently, Ulijasz 12 et al. proposed that the twist of C_4C_5 double bond is the key to the isomerization of 13 PCB.²³ At the same time, some studies also pointed out that the rotation of the C₁₀C₁₁ 14 double bond was noticeable in the BV and P Φ B isomerization,^{30–32} at least in the gas phase. In addition, the hydrogen-bond network patterns greatly affect the photoisomerization channels of central chromophores, when different deprotonation 17 status exist in these pyrrole rings.^{33,34} These works demonstrated that the photoisomerization of phytochrome chromophores may be adjusted by the distinctive confinement of chromophores in the vacuum and in the surrounding environment. In a vacuum, the chromophore is a "free" molecule and the rotation of any carbon-carbon bond is not affected by external factors. In living organisms, nonetheless, chromophores can be spatially constrained by their surrounding residuals, placing additional restrictions on their photoisomerization process. For example, one common idea is that Ring D in BV (Figure 1) and PΦB is not rigorously constrained due to the fact that it is β located in a relatively loose protein cavity.^{25,35} This leads to a high chance to realize the rotation of Ring D. This view was also supported by the work of Burgie et al., who showed that Ring A and Ring B are sandwiched in protein secondary domains and 6 covalently linked to the protein for $P\Phi B$ ²⁵ In addition, the C₁₀ methyl bridge between Ring B and Ring C is tightly wrapped by surrounding residues in BV, preventing the 8 photoisomerization at the C_{10} position.²¹

 Here, we are interested in several detailed aspects of the photoisomerization mechanism of the BV chromophore. The BV chromophore attracts our attention due to 11 its unique properties.^{16,20,36} It is not only the chromophore of phytochrome in Deinococcus radiodurans, but also the heme-metabolism intermediate of all aerobic 13 organisms.^{7,8,37} It can be engineered into monomeric infrared fluorescent proteins 14 (IFPs)^{38,39} that may be potentially used in disease diagnosis.^{6,9}

 In the present work, we specifically focus on the possible influences of the restricted motions in the BV chromophore. Particularly, we wish to provide a rather preliminary view of the steric effects by surrounding environments on the photoisomerization though a quick computational study, instead of giving a very comprehensive description of the role of realistic environments in nonadiabatic dynamics. Therefore, the efficient treatment of the spatial constraints becomes very essential. In principle, the dynamics of molecules constrained by the biological environment can be simulated by the quantum mechanical/molecular mechanics (QM/MM) method, which can include all

1 degrees of freedom of the protein environment and solution compounds explicitly.⁴⁰⁻⁴⁴ However, it requires rather large computational costs once performing the nonadiabatic dynamics simulations. Instead, we wish to treat the geometrical restriction in the nonadiabatic dynamics using a rather simplified approach with much less computational cost. Previously, many efforts have been made to mimic the biological environmental influence on the nonadiabatic dynamics in the simplified way. For example, Warshel simulated the restriction of protein by constraining the movements of terminal atoms in retinal molecules, rather than considering the motions of all 9 atoms.⁴⁵ Barbatti et al. imposed the geometrical constraints by increasing the nuclear mass of the terminal hydrogen atom in the nonadiabatic dynamics simulation of the 11 protonated Schiff bases linked to proteins.⁴⁶ This idea was also successfully used to 12 study the environmental effects in the photochemistry of aminopyrimidines. $47-49$ The employment of this "heavy-mass" approach shows many advantages: it can greatly reduce the computational costs and is easy to implement in the nonadiabatic dynamics simulations. Inspired by these works, we decide to take a similar idea in the trajectory surface hopping (TSH) simulations. The geometrical restriction of the surrounding environments is taken into account by using the very heavy atomic mass in the restricted moieties of the BV chromophore. We hope to elucidate the role of the possible surrounding environment on the photoinduced nonadiabatic processes, and further deepen the understanding of the photoisomerization mechanism of the BV chromophore in biological proteins.

2. Computational Details

2.1 Electronic Structure Calculation

 The electronic structure calculations were performed with the semi-empirical 4 orthogonalized-model (OM2) method.⁵⁰ The excited-state wave function was described by the multireference configuration interaction (MRCI) method within the configuration interaction scheme based on the Graphical Unitary Group Approach (GUGA-CI).51,52 The molecular orbitals were generated by using the restricted open- shell Hartree-Fock (ROHF) approach. All electronic configurations were generated from five reference configurations [the closed-shell, two single (HOMO-1 to LUMO and HOMO to LUMO) and two double (HOMO-1 to LUMO and HOMO to LUMO) excitations]. The active space (16, 12) was employed which distributes 16 electrons in 12 12 orbitals: six π orbitals, two *n* orbitals and four π^* orbitals. The state minima (S₀ min 13 and S_1 min) and minimum-energy S_0/S_1 conical intersection (CI) geometries were 14 optimized.⁵³ To get a direct view of the excited-state reaction pathways, we constructed the potential energy (PE) profiles by linear interpolation of the internal coordinates (LIICs) from the ground-state minimum to the minimum-energy CI structures. All semi-empirical calculations were performed by using the MNDO2020 package.⁵⁴

2.2 Nonadiabatic Dynamics

 The photoinduced nonadiabatic dynamics were simulated by the on-the-fly TSH simulations at the OM2/MRCI level. Previous works have demonstrated that this approach provides an efficient and reasonable description on the excited-state

2.3 Molecular model construction

 All calculations were simulated using a simplified model with the *ZsZsZa* structure 20 that was identified as the main isomer of the Pr form in BV photochrome.²¹ Here, several side groups (thioether bonds, propionic acid carboxyl groups on Rings B and C) should have minor contribution on the skeleton motion in the excited state dynamics, we simply replaced them by the methyl group to reduce computational costs.

 We wish to gain a deep understanding of the steric effect on the photoisomerization dynamics of BV molecules. Here, the BV molecules possess four five-membered rings. To get a full understanding of the impacts of different geometrical constraints, we considered as many restriction situations as possible, and totally constructed nine models, as shown in Table 1 and Figure 1. **Model 0** represents the original simplified BV chromophore model. In **Models Ⅰ-Ⅳ**, a single ring is constrained. In **Models Ⅴ- Ⅶ**, two adjacent rings were constrained, along with their connecting parts. We also built **Model Ⅷ**, in which two side rings (A and D in Figure 1) were constrained. On this basis, we set the atomic masses in the restricted part of the BV molecule to 99999999 au and the initial velocity to 0 in the nonadiabatic dynamics simulation.

 According to the simulation results (see discussions below), nine models were divided into four groups with rather different decay features: Group 1 includes **Models 0, Ⅰ, Ⅳ** and **Ⅷ**; Group 2 includes **Models Ⅱ** and **Ⅴ**; Group 3 includes **Models Ⅲ** and **Ⅶ**; and Group 4 includes **Model Ⅵ**.

 Table 1. All BV models with different geometrical constraints. The constrained parts are labelled by different colors in Figure 1.

Models	Constrained part of the BV molecule	Group
$\bf{0}$	-	
I	Ring A (green part)	
П	Ring B (yellow part)	

2 **3. Results and Discussion**

3 **3.1 CI Structures and Channels**

 The Pr→Pfr photoisomerization mechanism is closely related to the ultrafast nonadiabatic process governed by the conical intersections. To clarify the role of the CIs in the nonadiabatic dynamics, we optimized the several CI geometries (Figure 2). Table S1 and S2 (in supporting information (SI)) show the key internal coordinates at 8 S₀_min, S₁_min and CIs. These four important CIs display the below geometrical features:

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$$
 CI₁: C₉C₁₀C₁₁N_C dihedral angle rotates to -85.4° with the elongated C₁₀C₁₁ bond and

11 the shortened
$$
C_9C_{10}
$$
 bond;

12 \cdot CI₂: N_BC₉C₁₀C₁₁ dihedral angle rotates to -93.4° with the elongated C₉C₁₀ bond and

13 the shortened $C_{10}C_{11}$ bond;

 14 **•** CI₃: C₁₄C₁₅C₁₆N_D dihedral angle rotates to 95.0° with the elongated C₁₅C₁₆ bond and

15 the shortened $C_{14}C_{15}$ bond;

16 \cdot CI4: N_AC₄C₅C₆ dihedral angle rotates to 89.6° with the elongated C₄C₅ bond and the

1 shortened C_5C_6 bond.

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Figure 2. Four important S_0/S_1 minimum-energy CI structures and their major dihedral angles (marked by red circles) (a) $CI₁$; (b) $CI₂$; (c) $CI₃$; (d) $CI₄$.

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4 To get a direct view of the excited-state reaction pathways, we constructed the PE 5 profiles from the ground-state minimum to the CI structures. In Figure 3a and 3b, the 6 excited-state pathways from S_0 min to both CI₁ and CI₂ are barrierless, and the former 7 one is steeper. Moreover, the energy of $CI₁$ is lower than that of $CI₂$. While the other 8 two channels towards CI₃ and CI₄ show some visible barriers (see Figure 3c and 3d), 9 and the CI⁴ channel exists a slightly higher energy barrier.

10 It is necessary to point out that the torsional motions at the $C_{14}C_{15}$ and $C_{5}C_{6}$ bonds 11 also lead to the CIs, giving CI⁵ and CI⁶ (see Figure S1), respectively. However, as shown 12 in Figure S2, the reaction pathways towards them display very high barriers, preventing 13 the possibility of these two photoisomerization channels. Thus, we do not discuss them 14 here.

Figure 3. Potential energy curves along the linear interpolated pathway from S_0 min to the four conical intersections (a) $CI₁$; (b) $CI₂$; (c) $CI₃$; (d) $CI₄$.

3.2 Photoisomerization Pathways

 We performed the nonadiabatic dynamics simulation for all nine models mentioned above. After collecting all hop geometries and analyzing their correlations with 6 optimized CIs, four CIs $(Cl_1, Cl_2, Cl_3,$ and CI₄) were identified to play key roles in the nonadiabatic decay. By analyzing the hopping structures in TSH dynamics, we can divide all nine BV models into four groups according to their involved decay channels, as shown in Table 2.

Model	CI ₁	CI ₂	CI ₃	CL ₄	No Hop
$\boldsymbol{0}$	94.1%	5.9%	0.0%	0.0%	0.0%
I (Ring A)	94.3%	1.0%	3.6%	0.0%	1.1%
IV ($Ring D$)	95.7%	3.8%	0.0%	0.0%	0.5%
VIII (Rings A and D)	87.0%	3.5%	0.0%	0.0%	9.5%
II (Ring B)	67.0%	1.1%	21.9%	0.0%	10.0%
V (Rings A and B)	63.1%	1.4%	30.3%	0.0%	5.2%
III (Ring C)	45.5%	14.1%	4.3%	1.0%	35.1%
VII (Rings C and D)	31.4%	13.3%	0.0%	6.4%	48.9%
VI (Rings B and C)	0.0%	0.0%	42.0%	8.0%	50.0%

Table 2. The branching ratio of different reaction channels in each constrained BV

 The first group includes **Models 0**, **Ⅰ**, **Ⅳ** and **Ⅷ**. Among them, **Model 0** represents the free BV model. **Models I**, **II** and **VIII** refer to the situations in which the constraints are added in two terminal rings, namely Rings A, D and both, respectively. As shown 7 in Table 2, Figure 4a and Figure S4, the $CI₁$ controlled pathway is the predominant decay channel in these four models. Following this channel, the trajectories experience 9 the significant changing of the $C_9C_{10}C_{11}N_C$ angle up to $\sim 85.4^\circ$, as shown in Figure 2. 10 However, the other CIs only make very small contributions. For instance, the $CI₂$ plays a little role here, and the CI³ channel only appears in the TSH dynamics of **Model I**. This result can be well understood by the PE curves. As we discussed previously, there 13 is no barrier existing in the first excited-state decay pathways from S_0 min to CI₁ and CI2, and the former PE surface is steeper. At the same time, the other two channels towards CI³ and CI⁴ display visible energy barriers along the excited-state pathways. 16 As a consequence, in **Model 0**, the channel via $CI₁$ becomes dominant while only a 1 small number of trajectories decay via CI₂ here. Since the motions of Rings A and D are constrained in **Models I**, **Ⅳ** and**Ⅷ**, we expect that the major torsional around the carbon-carbon double bond between Rings B and C should not be largely hindered. This explains why their nonadiabatic decay channels are similar to that of **Model 0**. Overall, the CI¹ pathway is the dominant channel in the nonadiabatic dynamics of **Models 0, Ⅰ, Ⅳ** and **Ⅷ** in Group 1, in which the photoisomerization mainly takes 7 place at the $C_{10}C_{11}$ bond.

8 The second group includes **Model Ⅱ** and **Model Ⅴ**, with Ring B and Rings A and B 9 are constrained, respectively. For these two models, most of trajectories decay via CI¹ 10 while the secondary channel goes to the CI₃ (see Table 2, Figure 4b and Figure S5). 11 Compared to the models in Group 1, the contributions of both $CI₁$ and $CI₂$ become 12 decreased, while the role of CI³ starts to be visible. The change of the branching ratio 13 to different channels can be explained as follows. Once Ring A and Ring B are 14 immobilized, the torsional motion along the C_9C_{10} bond becomes limited, resulting in 15 the reducing of the $CI₂$ channel. In addition, the analysis of trajectory propagation 16 clarifies that the motion of Ring B is necessary in the $C_{10}C_{11}$ isomerization channel, as 17 shown in Figure S3 in SI for details. Therefore, the constrains on Ring B leads to the 18 decreasing of the CI₁ channel. Due to the reducing of both CI₁ and CI₂ channels, 19 trajectories should move by following either CI₃ or CI₄ channel, and both show barriers 20 on the excited-state reaction pathway. Although the PE barrier in the CI₃ controlled 21 channel is only 0.06 eV lower than that of the CI₄ dominated channel, the difference in 22 the proportion of the channel is obvious. This feature may be attributed to the reasons

1 photoisomerization at the $C_{10}C_{11}$ bond is still dominant in Group 3, while its ratio is 2 largely reduced. The secondary channel is governed by the $CI₂$ that shows the 3 isomerization site at C_9C_{10} bond.

 The fourth group includes only **Model Ⅵ**, in which both two central Rings, B and C are constrained. In this model, the vast majority of the trajectories decay through CI³ and small number of trajectories decay via CI4, see Table 2, Figure 4d and Figure S7. Since both Rings B and C are restricted, the dihedral angle between them almost cannot 8 rotate, leading to the vanishing of the $CI₁$ and $CI₂$ channels. Due to the less geometrical rearrangement discussed above, the CI³ channel is dominant one in Group 4. In this 10 case, the photoisomerization mainly takes place at the $C_{15}C_{16}$ site. Nevertheless, this model shows the similar geometrical constraints at the BV chromophore in protein environments.

Figure 4. The branching ratios of different CI channels in each group of restricted models. The red, green and yellow circles in the left diagram indicate the constrained moieties. (a) Group 1 includes **Models 0, Ⅰ**, **Ⅳ** and **Ⅷ**(**Model 0** represents the free BV model); (b) Group 2 includes **Models Ⅱ** and **Ⅴ**; (c) Group 3 includes **Models Ⅲ** and **Ⅶ**; (d) Group 4 includes **Model Ⅵ**.

2 **3.3 Population**

3 The above discussions clearly point out that different decay channels are responsible 4 for the nonadiabatic dynamics of nine constrained BV models. The trajectories follow

 distinct reaction channels with different PE profiles, we expect that the evolution of electronic populations of these models should also be different. In principle, the models belonging to the same group should display similar population dynamics, since their underling channels are rather similar.

 Figure 5 shows the evolution of a few key dihedral angles with time being, from starting conditions to hopping events. Figure 6 shows their population dynamics. Clearly, the photoisomerization rate is strongly controlled by the dominant CI channel that is significantly modified by different geometric constraints.

9 Group 1 includes **Models 0, I, IV** and **VIII**. In Group 1, the CI₁ is the most dominant 10 decay channel. As shown in Figure S3, the motion of Ring C is important in the $CI₁$ channel, while the motion of the Ring B is also involved necessary. The Rings B and C 12 are completely unconstrained in structure, and have no effect on the torsion of the CI₁ channel. Therefore, the nonadiabatic dynamics in this group display the fastest 14 population decay (see Figure 6a). For this group, most trajectories access the $CI₁$ around 400 fs (Figure 5 a–d). Only for **Model VIII,** we noticed that 9.5% of trajectories stay on the first excited state at the end of simulation. As a consequence, more than 50% of 17 trajectories jump back to the S_0 state within 500 fs, and most of the trajectories return to the ground state within 2000 fs.

19 Compared with Group 1, the branching ratio towards to the CI₃ channel increased 20 significantly in all models of Group 2, while the $CI₁$ channel is still the most important 21 one. As depicted in Figure S3, the motion of Ring B plays the visible role in the $CI₁$ channel, and thus the employment of the constrain in Ring B slows down this channel. This is confirmed by Figure 5 e and f, which show that the many nonadiabatic 2 transitions at $CI₁$ take place around 400 fs, while some hops happen at the later time ~400–800 fs. In addition, about 10.0% and 5.2% of the trajectories do not hop back to the ground state for both **Model Ⅱ** and **V**, respectively. As the result, a slightly longer decay in the population dynamics appears for all models in Group 2. Figure 6b reflects 6 that more than 50% of the trajectories decay to the S_0 state within 700 fs, and most of 7 the trajectories back to the S_0 state at the end of simulation.

8 In Group 3 (**Models III** and **VII**), the CI₁ channels is still the most dominant one, although its contribution is further decreased in all models. The Ring C is constrained 10 and greatly affects the molecular rotation through the $CI₁$ channel, see Figure S3. Therefore, the dynamics is quite different with respect to those of the first two groups. 12 The photoisomerization via the CI_1 channel becomes much slower (Figure 5) and many hops take place around 1600 fs (see Figure 5 g and h). And in **Models Ⅲ** and **Ⅶ**, 35.1% and 48.9% of the trajectories do not hop up to 2 ps. Overall, the population decay becomes much slower.

16 Completely different from the above three groups, $CI₁$ and $CI₂$ channels do not exist 17 in the model of Group 4. Here, all trajectories decay visit CI₃ or CI₄. The transitions 18 take place mainly through the CI_3 channel, in which the $C_{15}C_{16}$ double bond rotates more slowly (see Figure 5i). In this case, most hops take place around 1200-1600 fs, and 50% of the trajectories do not jump back to the ground state up to 2 ps. As a consequence, Group 4 shows the slowest decay dynamics in Figure 6d.

Figure 5. Time evolution of key dihedral angles $(C_9C_{10}C_{11}N_C$ for most models and $C_{14}C_{15}C_{16}N_D$ for Model VI). The red dotted line represents the dihedral angle at the dominant CI structure. The cross labels show the hopping events.

Figure 6. Time-dependent fractional occupations of the S_0 and S_1 electronic states of the nine models in the nonadiabatic dynamics staring from the S_1 state. (a) Group 1; (b) Group 2; (c) Group 3; (d) Group 4.

4. Conclusion

 In this work, the photoisomerization processes of BV chromophore are investigated by employing the surface hopping nonadiabatic dynamics simulation at the OM2/MRCI level. Different geometrical constraints are considered, and the corresponding models give distinct decay channels.

 The unconstrained BV chromophore (**Model 0)** and the constrained terminal rings (Ring A in **Model I**, Ring D in **IV**, and Rings AD in **VIII**, respectively) have similar

1 dynamics. The trajectories decay rapidly from S_1 state, with 50% of the trajectories 2 decaying within 500fs. Most trajectories choose to follow the CI₁ channel, characterized 3 by isomerization around $C_{10}C_{11}$ bond. **Models II** and **V** constrain the motion of Ring B and the Rings A and B, leading to the slight increasing of the excited-state lifetime with respect to **Models I**, **IV** and **VIII**. 6 Except the major channel via $CI₁$, the secondary channel is governed by the $CI₃$ channel, 7 in which the photoisomerization takes place at the $C_{15}C_{16}$ bond. **Models III** and **VII**, which are characterized by the restricted motion of Ring C and Rings C and D, show the significantly longer excited-state decay times. Although the $CI₁$ channel is still the primary channel, the ratio of the $CI₂$ channel with the 11 photoisomerization at the C_9C_{10} bond increases significantly. **Model VI** with the two middle rings fixed show completely different dynamics features, with 50% of the nondecay trajectories at the end of the simulation time 2000 fs. Such slow decay is attributed to the fact that **Model VI** decays mainly through the 15 CI₃ channel in which the $C_{15}C_{16}$ bond torsion is involved. By simply mechanically restricting the motion of a specific moiety, we try to study the spatial effects of surrounding environment on the photoisomerization dynamics of the BV chromophore with very small computational cost. Our work clearly describes the impact of various possible steric effects on the nonadiabatic dynamics processes. It provides a guideline for the regulation of the photoisomerization reaction channel, which can further propose some novel ideas for the design of phytochrome proteins. In

this sense, the current work provides the preliminary but useful understandings of this

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