Machine Learning on a Robotic Platform for the Design of Polymer-Protein Hybrids

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11 Polymer-protein hybrids are intriguing materials that can bolster protein stability in non-native environments, thereby 12 enhancing their utility in diverse medicinal, commercial, and industrial applications. One stabilization strategy 13 involves designing synthetic random copolymers with compositions attuned to the protein surface, but rational design 14 is complicated by a vast chemical and composition space. Here, we report a strategy to design protein-stabilizing 15 copolymers based on active machine learning, facilitated by automated material synthesis and characterization ¹⁶ platforms. The versatility and robustness of the approach is demonstrated by the successful identification of 17 copolymers that preserve, or even enhance, the activity of three chemically distinct enzymes following exposure to 18 thermal denaturing conditions. Although systematic screening results in mixed success, active learning appropriately ¹⁹ identifies unique chemistries for each enzyme. Overall, this work broadens our capabilities to design fit-for-purpose ²⁰ synthetic copolymers that promote or otherwise manipulate protein activity, with extensions towards the design of ²¹ robust polymer-protein hybrid materials.

22 23 tractive materials that leverage polymers to improve pro- 54 tions. 24 tein solubility and stability in often denaturing and abio-25 logical environments.²⁻⁶ One strategy, which has resulted 56 form thermostable PPHs with glucose oxidase (GOx), li-²⁶ in remarkable hours-long enzyme activity in toluene,⁷ tai- ₅₇ pase (Lip), and horseradish peroxidase (HRP) (Fig. 1). To 27 lors the composition of random copolymers based on pro- 58 efficiently acquire data, we use automated oxygen-tolerant ²⁸ tein surface chemistry. In principle, copolymers might be ⁵⁹ radical polymerization for copolymer synthesis^{32, 33} and de-29 precisely designed to stabilize any given protein without 60 velop a facile, thermal-stability assay to characterize PPHs. 30 compromising activity. However, identifying such copoly- 61 With this platform and five iterations of active learning for 31 mers, whether via rational design or screening, is chal- 62 each enzyme, we successfully identify PPHs with significant 32 lenging due to a large combinatorial design space (e.g., 63 enzyme activity; these PPHs generally outperform those 33 monomer chemistry, chain length, architecture).⁸ Thus, 64 derived from a systematic screen with over 500 unique 34 fit-for-purpose PPHs could facilitate myriad applications- 65 copolymers. Notably, we demonstrate that our strategy ³⁵ biofuel production,⁹ plastics degradation,^{10,11} pharmaceu- ₆₆ appropriately adapts data acquisition to yield chemically $_{36}$ tical synthesis 12 but a robust strategy for their design $_{67}$ distinct sets of top-performing copolymers for each enzyme. 37 remains elusive.

38 39 dramatically accelerated materials discovery across disci-⁴⁰ plines,^{13–15} enabling more efficient identification of materi-⁴¹ als with target properties.^{13, 16–21} Nonetheless, ML-guided 42 copolymer design is limited by several factors, including 43 the availability of quality data necessary to train the un-44 derlying models.^{8,22–25} Most polymer databases predomi-⁴⁵ nantly feature homopolymers,²⁶ and the laborious nature 46 of polymer synthesis and characterization severely limits ⁴⁷ the number of systems that can be examined "in-house".²⁷ ⁷⁶ Overview of design space and strategy 48 Several copolymer design efforts have thus relied on data 77 To test our ML-based design paradigm, we consider three 49 generated in silico.^{21, 28, 29} Meanwhile, recent experimental 78 chemically distinct enzymes-HRP, GOx, and Lip-with the 50 work has used flow reactors or parallel batch synthesizers 79 design goal to maximize retained enzyme activity (REA) 51 to provide modest data (< 500 samples).^{18,30,31} More scal- 50 following thermal stressing. For reference, a PPH ex-

Polymer-protein hybrids (PPHs) have emerged as at- 53 design copolymers for PPHs and other materials applica-

Here, we use active ML to rapidly design copolymers to 68 Post hoc analysis of our data and ML models reveals impor-Over the last decade, machine learning (ML) has •• tant relationships between specific copolymer chemistries 70 and PPH stability, while biophysical characterization of 71 our most efficacious PPHs provide mechanistic insight into 72 how copolymers may preserve enzyme function under ther-73 mal stress. Overall, this framework will automate and ac-74 celerate the design of copolymers for stable PPHs across 75 applications.

⁵² able approaches would substantially extend capabilities to ⁸¹ hibiting 100% REA provides the same level of activity



Fig. 1| Overview of study. a, Schematic illustration of the surface chemistry for horseradish peroxidase (HRP), glucose oxidase (GOx), and lipase (Lip). Amino acids are colored based on classification as hydrophobic (magenta), hydrophilic (green), or ionic (blue). Scale bar = 2 nm. Images for the protein are rendered using Visual Molecular Dynamics.¹ b, Monomers utilized for copolymer design. The colored boxes delineate rough classifications as hydrophobic (magenta), hydrophilic (green), and ionic (blue). c, Schematic representation of closed-loop learn-design-build-test discovery process used in this work. After initialization with a seed dataset, the process consists of (i) training an enzyme-specific Gaussian process regression (GPR) surrogate model to predict the REA of a PPH based on copolymer charachteristics (learn), (ii) Bayesian optimization of copolymers to satisfy an expected improvement acquisition function and subsequent filtering to propose new copolymers (design), (iii) automated synthesis of proposed copolymers via photoinduced electron/energy transfer reversible addition-fragmentation chain transfer (PET-RAFT) polymerization (build), and (iv) mixing of synthesized copolymers with enzyme to form PPHs that are thermally stressed and assessed for REA (test). Newly acquired data can then be used to restart the closed-loop discovery process.

82 as the enzyme prior to thermal stressing. Because these 95 83 enzymes possess distinct surface chemistries and molec- 96 Test cycle employed here. After constructing an initial seed ⁸⁴ ular weights (Fig. 1a), we consider a copolymer design ⁹⁷ dataset featuring 504 copolymers and corresponding REA ss space with eight possible monomers (Fig. 1b) copoly- as measurements, we performed five iterations for each enso merized with target degree of polymerization (DP) be- so zyme. Within each iteration, we (i) developed ML models 87 tween 50 and 200 in increments of 25. ⁸⁸ monomers are classified as hydrophobic (DEAMA, HPMA, 101 tified batches of 24 candidate copolymers for PPHs using 89 BMA, MMA), hydrophilic (DMAPMA, PEGMA), or ionic 102 active and unsupervised ML, (iii) synthesized candidate ⁹⁰ (SPMA, TMAEMA); this set enables various interactions ¹⁰³ copolymers, and *(iv)* performed thermal activity assays 91 (e.g., van der Waals, hydrogen-bonding, electrostatic) with 104 to determine REA for candidate PPHs; these results aug-92 the enzyme, while balancing aqueous solubility. To encour- 105 mented the dataset to begin the next iteration. 93 age reproducible synthesis and minimize latency, up to four 94 distinct monomers are selected for copolymerization.

Fig. 1c schematically presents the Learn-Design-Build-The chosen 100 to predict REA from copolymer characteristics, (ii) iden-

¹⁰⁶ Inefficiency of screening

108 our seed dataset consisted of a systematic screen over 504 101 and maximum values observed in the seed datasets. For 100 copolymers with distinct monomer combinations and DPs. 162 HRP, the top-performing PPH is found during the initial 110 The vast majority of copolymers in this dataset did not 103 screen, but many of the top hybrids are still identified by ¹¹¹ result in substantial REA, with the median values of 3.2% ¹⁶⁴ AL, including one with an REA of 81.0%. More generally, 112 (HRP), 10.0% (GOx), and 0.118% (Lip). These poor re- 105 we find that a large number of diverse copolymers offer 113 sults are partly explained by the limited design space sur- 106 reasonable stabilization of HRP, and AL identifies some 114 veyed during systematic screening (Fig. S1, S2). Addi- 167 promising regions that are not exposed by our system-115 tionally, the REA for PPHs with Lip, HRP, and GOx vary 168 atic search. Quantitatively, AL-guided copolymers are dis-116 significantly for copolymers in the seed dataset, suggesting 169 proportionately represented as top performers, comprising 117 that copolymers should be tuned to specific enzymes and 118 that systematic screening is likely to have mixed success 171 REA for Lip, GOx, and HRP, respectively. Interestingly, 119 across different enzymes.

120 Active learning in a combinatorial design 175 121 space

122 To guide data acquisition beyond the seed database, we de-123 vised an active learning (AL) paradigm based on Bayesian 124 optimization (BO)³⁴ of a ML surrogate model (see Meth-125 ods). Preliminary comparisons using the seed datasets 126 indidcated that GPR modeling with simple, machine-127 readable copolymer representations as input provided the 128 best predictive performance and was thus selected as our 129 surrogate modeling approach over other ML algorithms $_{130}$ and copolymer featurization strategies³⁵ (Fig. S3). At 131 early stages of the design process, our objective was to it-132 eratively identify batches of copolymers that are likely to 133 exhibit improvements in REA according to our ML mod-134 els and/or explore unknown regions of design space based 135 on model uncertainty. To achieve this balance between ex-136 ploitation and exploration, we optimized copolymer com-137 positions and DP according to a series of modified expected 138 improvement acquisition functions (see Methods, Candi-139 date copolymer generation, Candidate copolymer down-140 selection); similar acquisition functions have been used in ¹⁴¹ previous work related to polymer design.^{36,37} Following 142 four iterations of this data acquisition approach, we transi-143 tioned to a policy of pure exploitation in the fifth iteration; we refer to the fifth iteration as the "exploit round." 144

Fig. 2a-c shows that the AL-BO paradigm facilitated 145 146 identification of numerous, diverse copolymers that en-147 hanced retained activity for each of the three enzymes. 148 The median REA of PPHs found in the intermediate and 149 final iterations of AL show progressive and significant in-150 crease over those in the seed database. In particular, there 206 priately adapted optimization to identify high-performing 151 is a difference of 46.2%, 31.5 %, and 87.6% between the PPHs for each enzyme across chemical space, with less than ¹⁵² median REA of seed PPHs and those found in the exploit ²⁰⁸ 20% additional data beyond the initial systematic screen. ¹⁵³ round for HRP, GOx, and Lip, respectively. Even within 154 the intermediate iterations (1-4), we typically find improve-¹⁵⁵ ments in median REA iteration-over-iteration (Fig. S4), ²⁰⁹ Understanding chemical features driving PPH 156 despite data acquisition sometimes foregoing potentially 210 performance

159 round and exhibit remarkable REA values of 107.9% and ¹⁰⁷ To gain perspective on the viability of brute-force search, ¹⁶⁰ 67.4%, which significantly improve upon both the average 170 70.2%, 40.5%, and 42.5% of the top twentieth percentile of 172 the exploit round also produces three PPHs for Lip that 173 not only preserve but enhance its activity relative to the 174 unstressed enzyme.

> Fig. 2d-i examine both the progression of AL and PPH 176 performance as a function of the chemical constitution of 177 copolymers. Based on the totality of measured REA val-178 ues, we find that best-performing PPHs for each enzyme 179 utilize entirely different copolymer chemistries, which jus-180 tifies a tailored design strategy. In particular, optimal 181 copolymers for HRP stabilization predominantly feature $_{182}$ hydrophobic and ionic monomers and smaller DP (<100) 183 (Fig. 2a,d). While AL-generated candidates primarily fo-184 cus on uncovering this region of the chemical space, there 185 are also many effective PPHs that limit ionic content as 186 identified by the seed dataset (Figs. 2g and S2c). In 187 this case, a wide range of diverse, high-performing PPHs 188 are identified by AL, despite outlier points in the HRP 189 dataset (Table S1). For GOx, optimal copolymers are ei-190 ther predominantly hydrophobic or hydrophilic with very 191 little ionicity and have DP typically in the range of 100-192 150 (Fig. 2b,e). Accordingly, AL for GOx stabilization pre-193 dominantly probed these regions of the chemical space and remained globally stagnant in its search (Fig. 2e,h), fine-¹⁹⁵ tuning relatively promising regions identified in the seed 196 dataset (Fig. S2a). Conversely, optimal copolymers for Lip 197 stabilization possess sizable incorporations of monomers 198 from all three chemical groupings with generally larger 199 DP (Fig. 2c,f). AL-proposed candidates progress towards 200 this promising region of the chemical space with each sub-201 sequent iteration (Fig. 2f,i); notably, this region of the 202 chemical space is completely avoided in the seed dataset ²⁰³ (Fig. S2b). This suggests that the Lip design campaign 204 benefited from both exploration and exploitation data ac- $_{\tt 205}$ quisition polices. Therefore, the AL/BO paradigm appro-

157 promising designs in favor of diversity or uncertainty. For 211 Given the identification of highly stable PPHs for each en-158 Lip and GOx, the best PPHs are found within the exploit 212 zyme, we sought to understand the important chemical



Fig. 2] Machine learning guides design of highly stable polymer-protein hybrids. a-c, Copolymer designs and their measured REAs for HRP, GOx, and Lip. Marginal axes at the top contain Gaussian kernel density estimate distributions of REA in the seed database (blue), active learning iterations 1-4 (orange), and the final exploitation round (green). Medians of distributions are indicated by vertical lines. Main axes show the experimentally measured REA for all tested PPHs; individual markers are vertically located in bins according their degree of polymerization with random fluctuations added within bins to improve visual clarity. The marker color reflects the composition of the copolymer according to the ternary diagram (bottom right). d-f, Representation of active learning path traversed through copolymer chemical space for each enzymes. The chemical space is represented as a ternary diagram with coordinates providing the fraction of incorporation of hydrophobic, hydrophilic, and ionic monomers in copolymers. Colored stars indicate the mean composition of copolymers proposed during a given active learning iteration. The ternary diagrams are additionally colored by maximum REA observed for a PPH in a given region of the chemical space spanned by the ternary axes. g-i, Individual chemical compositions of copolymers proposed during each stage of active learning. The centroid of all points at a given iteration yields the position of the stars d-f. The crosses denote copolymers that showed undesirable gelation during synthesis (see Methods, Handling polymer gelation).



Fig. 3| **Analysis reveals distinct priorities in copolymer features for each protein. a**, Copolymer compositions and degree of polymerization (DP) for the top ten performing PPHs for HRP (orange), GOx (green), and Lip (purple). **b**, Cross-evaluation of top-performing copolymers across enzymes showing mean observed and predicted REA for each copolymer-enzyme pairing. Statistical significance was determined by Mann-Whitney U test. * (p<0.05), ** (p<0.005), *** (p<0.005), unlabeled pairs are not significantly different. Top 10 performers for each enzyme demonstrate high specificity in agreement with predicted activity. c, Normalized mean |SHAP| values calculated for HRP, GOx, and Lip for each model to quantify relative feature importance. d-f, SHAP summary values for GPR models calculated from available data after all five active learning iterations. Each point corresponds to a unique evaluated PPH, and the point's position along the X-axis shows the impact of a feature on predicted REA. g-i, SHAP value distributions demonstrating the effect of degree of polymerization on REA predictions. Polymer chain lengths with maximum calculated SHAP values are distinct between enzymes. Black candlesticks range from second to third quartiles of SHAP values and white dots represent the distribution mean. j-l, Mean |SHAP| values calculated for all model features after model training on the seed dataset and after each iteration of active learning.

²¹³ features of copolymers that gave rise to their performance. ²²³ tally, we empirically confirmed that the REA of PPHs de-²¹⁴ Fig. 3a compares the features of copolymers underlying ²²⁴ signed for a specific enzyme are significantly higher than ²¹⁵ PPHs with the top ten highest REA for each enzyme. Al- ²²⁶ that of PPHs formed by the same copolymers but other ²¹⁶ though top-performing PPHs for a given enzyme tend to ²²⁶ enzymes. Virtual cross-evaluation using enzyme-specific ²¹⁷ have some chemical similarity across effective copolymers, ²²⁷ GPR models trained on all iterations of data similarly ²¹⁸ there is substantial chemical diversity between PPHs for ²²⁸ suggest that REA is significantly diminished when top-²¹⁹ different enzymes. To demonstrate that copolymer pairing ²²⁹ performing copolymers for one enzyme are paired with an-²²⁰ with enzymes is highly specific, we cross-examined the ef- ²³⁰ other. Together, these results not only suggest an intricate ²²¹ ficacy of the copolymers in Fig. 3a to stabilize the other ²³¹ connection between copolymer chemistry and size and the ²²² enzymes; the results are provided in Fig. 3b. Experimen- ²³² stability of PPHs but that such correlations can be effec233 tively learned from data.

234 235 features and PPH activity, we computed Shapley additive ²⁹⁰ chemical space. 236 explanations (SHAP) values^{38,39} to quantify how chemical 237 features of the copolymers (fractions of incorporation and ²³⁸ DP) contributes to REA predictions by our GPR models. ²³⁹ Here, positive SHAP values indicate positive contributions 240 REA (negative SHAP values suggest negative contribu-241 tions), and we use the mean absolute SHAP value of a fea-242 ture as a proxy for its overall importance to model predic-²⁴³ tion. Fig. 3c shows that different copolymer features have 244 distinct impact on REA predictions. To elucidate these dif-245 ferences, we compare SHAP values for the fractions of in-246 corporation for each monomer (Fig. 3d-f) and DP (Fig. 3g-247 i) for each enzyme. Although we previously associated hy-²⁴⁸ drophobic chemistry with high-performing PPHs for HRP 249 (Fig. 2f.i). Fig. 3d reveals that the *exclusion* of BMA is ²⁵⁰ favorable (higher REA), while the *inclusion* of MMA, a 251 similar hydrophobic monomer, is associated with higher 252 REA. Similar observations can be readily identified for 253 Lip (Fig. 3f), for which SPMA and TMAEMA monomers ²⁵⁴ (both highly ionic) represent the most and least important ²⁵⁵ features based on their mean absolute SHAP values. Such 256 differences in SHAP values between monomers with the 257 same chemical classifications underscores the intricacy of ²⁵⁸ designing effective polymer-enzyme pairing.

259 $_{260}$ of copolymer features varies across enzyme models. For $_{314}$ ing, the α -helix content for HRP degrades from ca. 34.8%261 example, we find that different chain length regimes fa- $_{315}$ to 17.4%, while the α -helix content for the HRP-EP1 sys-262 vor high predictions on REA, depending on the enzyme-316 tem is 20.3% after heating. However, following cooling, 263 specific GPR model. (Fig. 3g-i). For HRP, smaller poly- $_{264}$ mers (DP = 50, 75) display the highest SHAP values, while $_{318}$ just 24.6% for HRP alone. This suggests that EP1 fa-265 the highest SHAP values for Lip are observed for $DP = 125_{319}$ cilitates significant refolding of HRP in a chaperone-like $_{266}$ or 150. DP = 200 is generally associated with lower REA, $_{_{320}}$ manner. $_{\bf 267}$ perhaps suggesting that shorter copolymer sequences en- $_{\bf 321}$ able more facile pairing with enzyme chemical domains to 322 teractions, we used SAXS to compare the physical dimen-269 promote stabilization.

270 271 during AL, we compared mean absolute SHAP values 325 showed that both HRP and HRP-EP1 have the same ra-272 for all non-gelling copolymers derived from GPR models 326 dius of gyration (Rg, 24.6 - 25.0 Å) in the pre-stressed state. 273 trained after each stage of data acquisition. Fig. 3j-l shows 327 Similarly, in the pre-stressed state, the pair-distance dis- $_{274}$ that the importance of features can shift significantly, even $_{328}$ tribution function P(r) remains highly similar upon com-275 with the addition of small amounts of data (typically 20 329 plexation of HRP with EP1 (Fig. 4b). Post-stress, the 276 data points added per iteration or less than 4% increase 330 differences are dramatic in the pair-distance distribution 277 in prior data available). This is most evident following 331 function. While the maximum particle diameter (Dmax) 278 for Lip, wherein mean absolute SHAP values for SPMA, 332 of native HRP increases from 80 to 200 Å, that of HRP-279 MMA, DMAPMA, and DP all substantially increase af- 333 EP1 increased only to 94 Å (Table S3). Additionally, while 280 ter the third and fourth iteration. This behavior might be 334 the $R_{\rm g}$ of HRP-EP1 increases only slightly to 26.9 Å, a 281 related to data acquisition over previously unexplored re- 335 larger 51.9 Å component appears in the Guinier plots of 282 gions of chemical space, which is partly shown in Fig. 2e. 336 HRP (Fig. 4c, blue line), likely indicative of a denatured 283 The effects for HRP and GOx are overall less dramatic; 337 or aggregated sub-species of HRP created through thermal 284 most rankings are unchanged between iterations, with oc- 338 stress. Additionally, Kratky plots (Fig. S7) show peaks at 285 casional shifts of one or two ranks upon exposure to new 330 q = 0.065 and 0.075 Å⁻¹ in HRP and HRP-EP1, respec-286 data. Nonetheless, even if the rank-ordering of features is 340 tively, which indicates a compact structure similar to that 287 unchanged, mean improvement in measured REA for PPHs 341 of the native protein. This clearly suggests that the com-

288 across iterations suggests that GPR models had sufficient To further explore the relationship between copolymer ²⁸⁹ fidelity to effectively optimize REA, at least within a local

²⁹¹ Revealing mechanisms with biophysical char-292 acterization

293 Although mechanisms of stabilization for PPHs based on ²⁹⁴ random copolymers have been hypothesized and studied in ²⁹⁵ limited fashion using molecular dynamics simulation,⁷ ex-296 perimental examination of these biophysical interactions is 297 nascent. Therefore, we characterized (Fig. S5) and inves-²⁹⁸ tigated a particular PPH for HRP identified in the exploit 299 round-dubbed HRP-Exploit Polymer 1 (HRP-EP1)- us-300 ing circular dichroism (CD) spectroscopy, small-angle X-301 ray scattering (SAXS), dynamic light scattering (DLS), 302 and quartz crystal microbalance with dissipation (QCM-303 D). HRP was selected due to its amenability to these char-³⁰⁴ acterization techniques, while detailed characterization of 305 other enzyme systems proved challenging due to weak CD 306 spectroscopy signal-to-noise and solubility limitations. We 307 first investigated the impact of heating and cooling on the ³⁰⁸ secondary structure of HRP by CD spectroscopy (Fig. 4a). The corresponding measured α -helix, β -sheet, and random 310 coil content is provided in Table S2. We initially hypoth-311 esized that the addition of copolymer EP1 would reduce ³¹² thermally induced unfolding of HRP; however, the CD data Fig. 3c-i also indicate that the relative importances 313 suggests only a slight retardation of unfolding. Upon heat-317 HRP-EP1 exhibited 31.6% α -helix content compared to

To further understand the nature of the HRP-EP1 in-323 sions of HRP and its complexes in pre- and post-stress To understand the evolution of feature importances 324 states. Guinier analysis of the data (Table S3, Fig. S6)



Fig. 4| Biophysical characterization indicates copolymer-assisted refolding. a, Circular dichroism wavelength scans of HRP (dashed lines) and HRP-EP1 (solid lines) at room temperature (black), upon heating (red), and after cooling for 24hrs (blue), demonstrating that HRP-EP1 promotes retention of secondary structure in HRP during thermal stress and promotes significant protein refolding in comparison to HRP control. b. Pair-distance distribution function of HRP and HRP-EP1 by small-angle X-ray scattering demonstrating retained HRP-PPH morphology and size after exposure to thermal stress in comparison to native enzyme. c, Guinier analysis of HRP and HRP-EP1 before and after heating suggesting the development of a denatured or aggregated sub-population of HRP (blue line) in comparison to a single species observed in HRP, HRP-EP1, and HRP-EP1 after thermal stress (red lines). d, Dynamic light scattering size distributions of HRP with and without polymer EP1, demonstrating that no larger structures were observed after mixing. e, Surface thickness measured by Quartz crystal microbalance with dissipation after direct adsorption of HRP (t = 22 min) followed by injection of polymer EP1 (t = 82 min).

342 plex promotes a certain level of conformational integrity in 362 we developed a robust design framework integrating au-343 HRP even if secondary structure is impacted.

344 345 results by providing the distribution of hydrodynamic radii 365 thermostability for three chemically distinct enzymes. No- $_{346}$ ($R_{\rm h}$) in the samples (Fig. 4d). All samples show peak in- $_{366}$ tably, the machine learning-guided acquisition of data was 347 tensities between 3.0 - 3.3 nm with minimal signal intensity 367 effectively tailored to each enzyme. In addition, by analysas for $R_{\rm h} > 10$ nm. Additionally, measured polydispersity sas sis of developed surrogate machine learning models, we de-349 index remained under 0.2 for all samples, suggesting rela- 369 termined particular chemical features of copolymers that 350 tively monodisperse solutions (Fig. S8, Table S4). These 370 drive increased retained activity for each enzyme. Fur-351 results indicate that stabilization of HRP in PPH-EP1 is 371 thermore, the biophysical characterization of a successful 352 indeed driven by the formation of a complex rather than 372 polymer-protein hybrid design reveals chaperone-like assis-353 via larger macromolecular assembly. Further support of 373 tance in structural refolding as a possible mechanism of sta-354 complex formation by QCM-D showed significant differ- 374 bilization. Taken together, these results highlight the exis-355 ences in the Sauerbrey mass thickness following injection 375 tence of a complex structure-function relationship under-356 of EP1 onto surface immobilized HRP (Figs. 4e and S9). 376 lying protein-polymer hybrid activity that can be learned 357 While native HRP exhibited a thickness of 3.6 nm, HRP- 377 and exploited for materials optimization. 358 EP1 increased to 5.1 nm post injection at 80 minutes.

359 Outlook

363 tomated polymer chemistry and machine learning to ef-Finally, DLS was performed to complement the SAXS 364 ficiently discover polymer-protein hybrids with enhanced

This discovery platform for polymer-protein hybrids 378 379 can be extended in numerous directions. First, it provides 380 an exemplary approach that can be extended to other pro-300 Polymer-protein hybrids offer a powerful approach to sta- 381 teins, other copolymer chemistries, and/or alternative de-361 bilize sensitive proteins in a range of environments. Here, 382 sign objectives, such as other environmental stresses. One 383 intriguing possibility is also to generalize the surrogate 430 10. DelRe, C. et al. 384 models to incorporate chemical features of both proteins 431 385 and their encapsulating polymers. Additionally, the assay 432 386 data collected in this study can be used in conjunction with 433 387 simulation-based models to further elucidate and validate 388 molecular-level mechanisms for stability. Such simulations 435 389 might also aid in identifying and selecting key features for ⁴³⁶ surrogate models or even provide *in silico* figures of merit 391 that correlate with stability. Furthermore, the copolymer 437 12. 392 chemical space is large and flexible to accommodate the 438 393 simultaneous pursuit of multiple design objectives, which 439 394 could accelerate their adoption as functional, commercial 440 395 materials.

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573 Methods

574 Materials. ethyl methacrylate (DEAEMA). 575 2-diethylamino 576 (methacryloyloxy)ethyl] trimethylammonium chloride so- 631 to 245 µL of substrate solution. Absorbance was measured $rac{1}{1}$ such as N-[3-(dimethylamino)propy] si kinetic mode for 5 minutes in 20 second intervals; mea-578 methacrylamide (DMAPMA) were purchased from 633 surements were made at 653 nm, which is the maximum 570 Sigma-Aldrich; methyl methacrylate (MMA) and 3- 634 of the absorption peak. The initial rate of change of absso sulfopropyl methacrylate potassium salt (SPMA) from 635 sorbance was used to calculate the activity of HRP. Native 581 VWR; butyl methacrylate (BMA) from Alfa Ae- 636 HRP activity at time t = 0 served as a positive control, ss2 sar; and poly(ethyleneglycol) (n) monomethyl ether ⁶³⁷ while HRP heated at 60°C for 30 minutes served as the 583 monomethacrylate (PEGMA, $M_n \approx 400$ g/mol) from Poly- 638 negative control. sea sciences. PEGMA was deinhibited prior to use by passing 630 GOx thermal stability assay. The activities of PPHs 585 over mono-methyl ether hydroxyquinone inhibitor removal 640 for GOx were evaluated using an assay buffer contain-556 resin. Ethyl 2-(phenylcarbonothioylthio)-2-phenylacetate, 641 ing glucose, TMB, and HRP. Copolymers were diluted in 557 4-nitrophenyl butyrate (PNB), hydrogen peroxide (H₂O₂), 642 DMSO and then in assay buffer (50 mM sodium acetate, 558 D-(+)-glucose, sodium acetate, lithium bromide were 643 pH 5.0) to a final concentration of 12 µM. Resulting solu-509 purchased from Sigma-Aldrich; zinc tetraphenyl por- 644 tions were mixed with equal volumes of stock GOx solution 500 phyrin (ZnTPP), dimethyl sulfoxide (DMSO), 3,3',5,5'- 645 (5 µg/mL 30 nM) in polystyrene 96 well plates. The so-501 tetramethylbenzidine (TMB) from Fisher Scientific; and 646 lutions were thermally sealed with plate-sealing film and 502 potassium phosphate (mono and dibasic) and sodium ac- 647 then thermally challenged in a water bath at 65°C for 30 593 etate anhydrous from VWR.

⁵⁹⁵ prepared by automated photoinduced electron/energy ⁶⁵⁰ TMB, 0.11 µM HRP in assay buffer). Absorbance was mea-⁵⁹⁶ transfer reversible addition-fragmentation chain transfer ⁶⁵¹ sured in kinetic mode for 5 minutes in 20 second intervals; 597 (PET-RAFT) polymerization in 96 well plates as pre- 652 measurements were made at 653 nm, which is the maxi-⁵⁹⁸ viously described.^{32, 33, 40, 41} Briefly, the sequences and ⁶⁵³ mum of the absorption peak. The initial rate of change ⁵⁹⁹ processes to be conducted by the Hamilton MLSTARlet ⁶⁵⁴ of absorbance was used to calculate the enzyme activity. 600 liquid-handling robot were programmed in Python, indi- 655 Native GOx activity at time t = 0 served as a positive con cating information on sample concentration, reagent vol- 656 control, while GOx heated at 65°C for 30 minutes served 602 umes, and well position. Files containing reaction infor- 657 as the negative control. 603 mation were transferred to the Hamilton MLSTARlet to 658 Lip thermal stability assay. Activities of PPHs for Lip ⁶⁰⁴ prime the robotic transfers. Stock solutions of monomer ⁶⁵⁹ were evaluated using PNB as the substrate. Copolymers 605 (2 M), ethyl 2-(phenylcarbonothioylthio)-2-phenylacetate 660 were diluted in DMSO and then in assay buffer (50 mM 606 (RAFT chain-transfer agent (CTA), 100 or 50 mM) and 601 K₂HPO₄, 16.66 mM K₂HPO₄, pH 7.4) to a final concen-607 ZnTPP (4 or 2 mM) were prepared in DMSO as 1 mL 662 tration of 120 μM. From the 120 μM copolymer solutions, 608 aliquots. Aliquots were loaded into the Hamilton ML- 663 50 μL were mixed with 50 μL of stock lipase solution (0.8 ⁶⁰⁹ STARlet liquid-handling robot and automatically pipet- ⁶⁶⁴ mg/mL 24 μM) in polystyrene 96 well plates. The so-610 ted into 96-wells clear flat-bottom well plates (Greiner bio- 665 lutions were thermally sealed with plate-sealing film and $_{611}$ one). Monomer/CTA ratio was varied from 100-400 while $_{666}$ heated in a water bath at 70°C for one hour. Substrate ⁶¹² ZnTPP/CTA remained at 0.01. Polymer mixtures were ⁶⁶⁷ solution was prepared by diluting stock PNB solution (5.4 613 dispensed to a total volume of 200 µL and final monomer 666 M) first to 10 mM in DMSO, followed by a final dilution 614 concentration of 1 M. The mixtures were then covered with 669 to 0.5 mM in assay buffer. Absorbance was measured in 615 well-plate sealing tape and radiated under 560 nm LED 670 kinetic mode for 10 minutes in 20 second intervals; mea-616 light (5 mW/cm2, TCP 12 Watt Yellow LED BR30 bulb) 671 surements were made at 410 nm to monitor the production 617 for 16 hours.

for HRP were evaluated by its ability to oxidize TMB in 674 tivity at time t = 0 served as a positive control, while Lip $_{620}$ the presence of H_2O_2 . Copolymers were synthesized and $_{675}$ heated at 70°C for one hour served as the negative control. 621 diluted in DMSO before further dilution into assay buffer 676 Circular dichroism spectroscopy. 622 (50 mM sodium acetate, pH 5.0) to a final concentration of 677 and temperature scans of samples were collected using ⁶²³ 22.7 μM (<1% DMSO). From the 22.7 μM polymer sam- 676 an AVIV Model 400 CD spectrometer (AVIV Biomedical 624 ples, 50 μL were mixed with 50 μL of 10 μg/mL HRP 676 Inc.). Wavelength scans consisted of measurements from 625 (0.11 µM) in polystyrene 96 well plates. The solutions were 660 260 nm to 190 nm, collecting points every 0.5 nm with

627 challenged in a water bath at 60°C for 30 minutes. Sub-628 strate solution was prepared by diluting 40 mM of TMB Hydroxy propyl methacrylate (HPMA), 629 in DMSO to a final concentration of 0.4 mM in 1% $\rm H_2O_2$ [2-30] assay buffer. 5 µL of polymer-enzyme mixtures were added

648 minutes. After heating, 20 µL of the PPH samples were 594 Automated PET-RAFT synthesis. Copolymers were 649 added to 100 µL of substrate solution (5% glucose, 0.4 mM

672 of p-nitrophenol. The initial rate of change of absorbance

618 HRP thermal stability assay. The activities of PPHs 673 was used to calculate the enzyme activity. Native Lip ac-CD wavelength 626 thermally sealed with plate-sealing film and then thermally 681 a 1-nm bandwidth for 5 seconds, at all required temper $_{669}$ unfolded state at 90°C. The melting temperature $T_{\rm m}$ was $_{744}$ face thickness. 600 determined by fitting the temperature scans to a Boltz- 745 Polymer characterization.

mann sigmoidal equation. The fractions of α -helices and $_{746}$ (M_w and M_n) and dispersity (\oplus) were measured by gel- $_{692}$ β -sheets in the protein samples were calculated using CD $_{747}$ permeation chromatography using an Agilent 1260 Infindeconvolution algorithms for wavelength scans (Table S2). 748 ity II. Polymer samples were eluted through a Phenomenex

⁶⁹⁵ polymer-enzyme mixtures were performed on a DynaPro ⁷⁵⁰ Phenogel 12 10/300 GL column (Cytiva 17-5173-01, col-696 DLS Plate Reader III, Wyatt Technologies. Concentra- 751 umn L × I.D. 30 cm × 10 mm, 11 m avg. part. size) in 697 tion of HRP for DLS experiments was maintained at 0.2 752 0.5x PBS (0.2% NaN3) using a flow rate of 0.5 ml/min. ⁶⁹⁸ mg/mL while polymer concentration was at 1 mg/mL. The ⁷⁵³ GPC calibration was completed with Agilent PEG standata was collected using a wavelength of 830 nm and a scat- 754 dards. Polymers were prepared at 50:1 eluent/polymer 700 tering angle of 173°. Fifteen acquisitions were collected for 755 ratio in 0.5x PBS (0.2% NaN3) and filtered with a 0.45 701 each sample with an acquisition time of 5 seconds per ac- 756 µm nylon filter. Polymer conversion was calculated by ob-702 quisition using auto attenuation. Regularization analysis 757 taining ¹H NMR spectra using a Varian VNMRS 500 MHz 703 was performed using Rayleigh spheres model for hydrody- 758 spectrometer with mesitylene as an internal standard and 704 namic size measurement.

706 ments were carried out at the Life Science X-ray Scattering 761 were featurized as DP-explicit composition vectors with 707 (LiX) beamline 16-ID of the National Synchrotron Light 762 one-hot encoded fingerprints of the monomer units.³⁵ With 708 Source II (NSLS-II) at Brookhaven National Laboratory 763 eight possible monomers, the resulting feature vector pos-709 (Upton, NY). HRP was prepared at a final concentration 764 sesses nine dimensions, with the first containing the DP 710 of 1 mg/mL in 50 mM sodium acetate (pH 5.15) while 765 of the copolymer divided by 200 and the remaining eight ⁷¹¹ lyophilized polymers were reconstituted in sodium acetate ⁷⁶⁶ containing the fractions of incorporation for each monomer; ⁷¹² buffer and mixed with HRP at a final concentration of 2.61 ⁷⁶⁷ the division in the first dimension represents DP on a sim-713 mg/mL (10:1 molar concentration of polymer:HRP). Sam- 768 ilar scale as the remaining features. Gaussian process re-⁷¹⁴ ples were denatured by heating in a water bath at 65 °C for ⁷⁶⁹ gression (GPR) models, trained to predict the Yeo-Johnson ⁷¹⁵ 1 hour. All solutions were loaded into 96-well PCR plates ⁷⁷⁰ transformation of the REA for a PPH, were preferred due ⁷¹⁶ and mailed in for data collection. An X-ray energy of 15.14 ⁷⁷¹ to their superior predictive performance compared to other ⁷¹⁷ keV was utilized for solution SAXS. Three Pilatus detec-⁷⁷² ML algorithms (Fig. S3). In addition, preliminary compar-T18 tors were employed to provide a q range of 0.005 - 3.13 Å, T73 isons amongst GPR models trained over the seed datasets while the range 0.005 - 0.25 Å was taken as the small-angle ⁷⁷⁴ revealed no evident advantage to using more advanced fin-720 region. For background subtraction, sodium acetate buffer 775 gerprinting strategies over simple one-hot encoding (Fig. ⁷²¹ blanks were run for every three samples. The subtracted ⁷⁷⁶ S3). Using available experimental data of various PPHs, 722 data were analyzed in BioXTAS RAW 2.1 with ATSAS 777 we constructed enzyme-specific datasets wherein each da-723 3.0.4-6. Guinier analysis was performed to quantify the 778 tum is described by this feature vector and labeled by REA. 724 radius of gyration R_g , whereas pair-distance distribution 779 725 analysis by an indirect Fourier transform method was con- 780 features and REA using GPR to both capture the nontriv r_{26} ducted to quantitatively assess R_g , maximum dimension, r_{61} ial, nonlinear mapping and to facilitate AL as GPR nat- $_{727}$ and macromolecular structure. $^{42-44}$

728 Quartz crystal microbalance with dissipation. All 729 quartz crystal microbalance experiments were carried out 730 on the Q-Sense Omega Auto (Biolin Scientific) with 5 MHz 731 sensitivity, less than 1 nm surface roughness, and theo- $_{732}$ retical mass sensitivity of 17.7 ng cm⁻² Hz⁻¹. HRP was 733 dissolved in 50 mM sodium acetate buffer (pH 5.15) at

 $_{692}$ atures. Temperature scans were consisted of measuring $_{737}$ initial equilibration step at 20 μ L/min for 25 min. HRP, 683 mean residue ellipticity at 222 nm from 30 to 90°C with a 738 polymer, and mixtures of HRP with polymer were flowed ⁶⁶⁴ 5-second averaging time and 1.5-nm bandwidth. The ramp ⁷³⁹ at 40 μL/min for 10 min. Sodium acetate was flowed after 685 rate was 2°C/minute, and samples were equilibrated for 740 each step at 20 µL/min for 25 min to remove any loosely 556 5 minutes at each temperature before measurement. The 741 associated enzyme or polymer. Transformations using the fraction of protein unfolding at different temperatures were 742 Sauerbery equation^{45,46} were completed on the fifth har-688 calculated by assuming fully folded state at 30°C and fully 743 monic frequency and dissipation responses to obtain sur-

The molecular weights ⁶⁹⁴ Dynamic light scattering. DLS of copolymers and ⁷⁴⁹ 5.0 µm guard column (50 x 7.5 mm) preceded by superose 759 processed using Mestrenova 11.0.4.

705 Small-angle X-ray scattering. All scattering experi- 760 Machine learning surrogate models. All copolymers

We modelled the relationship between our copolymer 782 urally provides uncertainty estimates on predicted labels. 783 Covariances of points that are modeled by the Gaussian 784 Process are calculated using the squared exponential ker-785 nel basis function:

$$k(\vec{x}, \vec{x}') = \sigma^2 \exp(-\frac{1}{2} \frac{(\vec{x} - \vec{x}')^2}{l^2}) + \sigma_n^2$$

 $_{734}$ 0.2 mg/mL whereas the final concentration of lyophilized $_{786}$ where \vec{x} is the feature vector of the copolymer, and textitl, τ_{35} polymers was set to 0.52 mg/mL (10:1 molar concentration τ_{57} σ , σ_n are kernel hyperparameters. Anisotropic kernels were 736 of polymer:HRP). Sodium acetate buffer was flowed as an 788 explored but did not improve model performance. Hyper789 parameters were tuned using the Tree-structured Parzen 839 copolymer featured fractions of incorporation of any given 700 Estimator Approach (TPE), implemented by the Hyper- 840 monomer that was less than 5%. This filter was imposed to ⁷⁹¹ opt Python package.⁴⁷ s41 establish reasonable margins of experimental control over

792 793 lows: the dataset is first split into five folds. Four of five of 843 robotic arm used to automatically synthesize the copoly-794 the folds are then used to tune the GPR model hyperpa- 844 mers. Second, candidates were subsequently clustered us-795 rameters, which are identified with 20-fold cross-validation 845 ing Density-based spatial clustering of applications with $_{706}$ and optimization by TPE to minimize the mean squared safe noise (DBSCAN) using a distance threshold of $0.05\sqrt{2}$ and 707 error of labels. The optimal hyperparameters, along with 847 a minimum of three points per cluster. Following the for-798 data from four of five folds, are used to train a GPR model \$44 mation of clusters, the copolymer with the shortest Eu-709 that makes predictions on the remaining fold of data. This 840 clidean distance to the centroid poistion of the cluster in soo process is repeated four more times, such that all five of soo the copolymer feature vector space was selected as a repso1 the original folds have served as test sets. The five sets of s51 resentative candidate for futher consideration. All nonso2 optimized hyperparameters are then averaged and used to ss2 clustered candidates, or noise-points, were also considered so define a final GPR model with the full set of data available ss In this fashion, the procedure produced a set of relatively so4 for an enzyme at a given iteration. The five sets of held- ss4 diverse and representative copolymer candidates that fairly 805 out test performance metrics are also averaged to quantify 855 considers "outliers." Third, in cases where DBSCAN proand validate the predictive capabilities of the model. 807 Candidate copolymer generation. We use Bayesian 857 ensured that precisely 24 candidates were proposed by apsos optimization (BO) in tandem with a GPR model to pro- sss plication of k-Means clustering. Here, again, representa-809 pose promising candidate copolymers. For the first four 850 tive candidates are chosen based on proximity to the clussio rounds of active learning, we select candidates that max-so ter centroid. If a cluster consisted of only two points, then

$$f(\vec{x}) = Z\sigma(\vec{x})\Phi(Z) + \sigma(\vec{x})\phi(Z)$$
$$Z = \begin{cases} \frac{(\mu(\vec{x}) - f' - \xi)}{\sigma(\vec{x})} & \sigma(\vec{x}) > 0\\ 0 & \sigma(\vec{x}) = 0 \end{cases}$$

812 given by

where $f(\vec{x})$ is the predicted mean REA from the GPR, f' is so the growing list at that point. the current largest mean REA observed by the model, $\sigma(\vec{x})$ sit is the standard deviation from the GPR, Φ and ϕ are the sit Handling polymer gelation. Upon construction of the sie cumulative and probability density functions of the normal size database and throughout the AL, a handful of copolys17 distribution, respectively, and ξ is a hyperparameter that s72 mers were found to phase separate into a liquid and gel ^{\$13} controls the balance between exploring unobserved regions ^{\$75} phase. While gelling polymers recorded nonzero REA val-810 of the chemical space and exploiting known regions of it to 874 ues, they were excluded from the dataset used to train the 820 obtain high performing polymers.

821 see the exploit-explore spectrum, we sequentially generate 200 srr action environments that could obfuscate model training. $_{223}$ copolymer candidates for distinct ξ values that logarithmi- $_{276}$ However, the penalty function was used during the active s24 cally vary from 0.001 to 30. To avoid proposing previously s79 learning procedure to avoid suggesting polymer candidates ses synthesized polymers or those within the margin of syn- see proximate to gelling polymers across discovery campaigns see thetic experimental error previously synthesized or already set across all three enzymes up to that iteration. While this ⁸²⁷ proposed polymers, an additional penalty function is added ⁸⁸² strategy limited the number of gelled polymers per iter- $\frac{1}{2}$ to the acquisition function based on \vec{x} (see also Support- $\frac{1}{2}$ ation per enzyme to an average of six copolymers in the see ing Information). In the final iteration or exploit round, see first two rounds of AL, it ultimately proved ineffective for ⁸³⁰ copolymers that simply maximize REA predictions from ⁸⁸⁵ GOx as hydrophobic monomers were found to be effecss1 the GPR model are proposed as candidates, although the ss6 tive for GOx stabilization but increased polymer gelation ⁸³² penalty function is retained to avoid redundant proposals. ⁸³⁷ (Fig. S11). To combat this issue, a classifier that leveraged *** Candidate copolymer down-selection. Unsupervised *** knowledge of prior polymer gelation across all enzymes and sad clustering methods were used to select 24 candidates for sad iterations up to that point was designed and integrated in sas synthesis from a larger set of 200 candidates generated soo the AL scheme. The use of the classifier was limited to so by the BO procedure. In particular, the following pro- son and ultimately facilitated the discovery of primarily solu-⁸³⁷ tocol was used for candidate selection in the first four AL ⁸⁰² ble polymers for iterations 4 and 5 of AL for GOx. Fur-*** iterations. First, a filter was applied to ensure that no *** ther discussion on the development and integration of the

GPR models for each enzyme are constructed as fol- 842 the process of dispensing the monomer reagents with the ⁸⁵⁶ duced more than 24 candidates (this always occurred), we ⁸¹¹ imize the expected improvement (EI) acquisition function ⁸⁰¹ the candidate with the higher REA was used. A different ⁸⁶² down-smapling procedure was used in the exploit round, soa since diversity was no longer a priority for selection. Specif-⁸⁶⁴ ically, after producing the 200 polymer designs with BO, sos candidates were ranked by their REA in descending order and iteratively chosen for the final set of 24 candidates, 867 provided they had compositions that were unique (within sos synthetic precision) from any polymers that constituted

875 GPR models from iteration 1 onward due to the poten-To effectively sample copolymer designs that live on 876 tial uncontrolled differences in copolymer - enzyme intersupporting information (Table S5, Fig. S11, Fig. S12).

336 Data and Code availability

⁸⁹⁸ ing models are available in supporting information. In ⁹³⁰ beamline is part of the Center for BioMolecular Structure and available and available and (CBMS), which is primarily supported by the National In-900 for download in .csv format from DataSpace, Zen- 932 stitutes of Health, National Institute of General Medical 901 odo, and Materials Data Facility. ⁹⁰² in the development of the Gaussian process regression ⁹³⁴ and by the DOE Office of Biological and Environmental 903 model development and training will be available on 935 Research (KP1605010). LiX also received additional sup-GitHub (https://github.com/webbtheosim/PPH_public) 936 port from NIH Grant S10 OD012331. As part of NSLS-II, 905 with trained machine learning models available in .pkl for- 937 a national user facility at Brookhaven National Labora-⁹⁰⁶ mat as described on the Github repository. Python scripts ⁹³⁸ tory, work performed at the CBMS is supported in part by 907 used to perform SHAP analysis will also be available. Prior 939 the U.S. Department of Energy, Office of Science, Office ⁹⁰⁸ to publication, these materials are available by reasonable ⁹⁴⁰ of Basic Energy Sciences Program under contract number ⁹⁰⁹ request from the corresponding authors.

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942 Author contributions

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