A Polarizable Cationic Dummy Metal Ion Model

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Abstract

A novel locally polarizable multisite model based on the original cation dummy atom (CDA) model is described for molecular dynamics simulations of ions in condensed phases. Polarization effects are introduced by the electronegativity equalization model (EEM) method where charges on the metal ion and its dummy atoms can respond to the environment. This approach allows us to enhance the original fixed charge CDA model where the charge distribution can adapt to the local solvent structure. To illustrate the new CDA^{pol} model, we examined properties of the Zn²⁺ ion in aqueous solution. Polarizable model and Lennard-Jones parameters were refined for an octahedrally coordinated Zn²⁺ CDA to reproduce thermodynamic and geometrical properties. Using this locally polarizable model, we were able to obtain the experimental hydration free energy, ion-oxygen distance and coordination number coupled with the standard 12-6 Lennard-Jones model. This model can be used in myriad other applications where local polarization and charge transfer is important.

\mathbf{M} etal ions play significant roles in biochemistry and materials science. Around one third of the

proteins in the protein databank contain metal ions¹. Metal ions form complexes with surrounding amino acids and serve significant functional roles in biological systems² including structural³, electron transfer and catalysis⁴. Modeling of systems including transition metals represent one of the more challenging tasks using standard classical simulations. The charge on transition metals is not constant and is affected by factors like the environment, nature of coordinated ligands and oxidation state of the metal. There is no general solution to date for the representation of transition metals in molecular force fields and it is still a matter of on-going development. The electronic cloud is usually distributed non-symmetrically around the metal ion and can further change and redistribute in response to changes in the surrounding environment (Figure 1). Transition metals have d and f orbitals as their outermost orbitals which permit complicated chemical bonding patterns.



Figure 1. Polarizable models achieve higher fidelity than classical atom-centered fixed charge models through more accurate electrostatic interactions which leverage dynamically updated charge distributions. Zn²⁺ is coordinating with six water molecules in shown in (a) classical description and (b) with electron density distribution

Classical molecular dynamics (MD) simulations are mostly based on fixed atomic charge models that don't allow the electrostatic parameters to change as a function of geometry or respond to electrostatic potentials generated by nearby atoms. The simple idea of electrostatic interactions using fixed-point charges isn't entirely successful in many circumstances because the electrons are spread out in space and atomic charges change continuously. This has led to the creation of a range of polarizable force fields^{5, 6}. Properties of metal ions in aqueous solution are not well modeled by simple Lennard-Jones potentials which make the approximation that the ion has a formal charge⁷. Lennard-Jones potentials

don't account for ion-induced dipole interactions, while fixed charge models don't account for polarization effects. Hence, further advances in modeling d and f-block elements can significantly improve the performance of models for these ions.

Polarizable models with proper tuning can accurately predict charge distributions in molecular simulations, as such incorporation of polarization effects to traditional force fields is an ongoing effort^{5, 6,} $^{8-11}$. Polarizable force fields allow the electrostatic variables to change as a function of geometry or in response to the electrostatic potentials generated by nearby atoms and update the charges accordingly during a simulation. Applications of polarizable force fields to various problems such as protein-ligand binding⁸, pKa prediction⁹ and ion solvation¹⁰ have been reported. Despite the benefits of polarizable models, they are computationally demanding due to their complexity. With continuing improvements in the speed of computational hardware, more accurate and consequently more computationally expensive molecular dynamics simulations can be afforded. Although quantum chemistry methods can be used to predict and update charges in systems of interest, QM methods are still limited to small systems simulated over shorter time scales only. The computational cost of the QM region also remains the rate limiting factor in hybrid quantum mechanics/molecular mechanics (QM/MM) simulations. In this regard, polarizable force fields offer significant improvements at the cost of an acceptable increase in the computational cost of a molecular simulation. In this paper, we utilize the recently developed hybrid ReaxFF/AMBER MD tool¹², which introduces polarizability capabilities within the AMBER MD package (freely available in AMBERTools 21)¹³ and allows us to use AMBER's thermodynamic integration (TI) capabilities for ReaxFF calculations. The ReaxFF/AMBER MD tool has been implemented by developing an efficient interface to the open source PuReMD Reactive MD program^{14, 15} and uses the electronegativity equalization model (EEM) model within PuReMD for charge equilibration ¹⁵. In EEM , one electronegativity and hardness parameter are assigned to each element and these parameters are optimized against QM-charge distributions. The energy is expressed as a function of the electronegativity and hardness parameters:

$$E_{elec} = \left(\chi q + \frac{1}{2}\eta q^2\right) + E_{Coulomb} \tag{1}$$

In Eq (1) for the self-energy contributions, χ represents the Mulliken electronegativity of an atom and η represents twice the Parr-Pearson hardness. In the polarizable potential used in this study, Coulomb interaction with electrostatic shielding is adopted to prevent excessively high repulsion between nearby atoms as shown in Eq (2), where C is the Coulomb constant in a vacuum, q_i and q_j denote the atomic

charges, r_{ij} is the distance between atoms i and j, and γ_{ij} is the electrostatic shielding between the types of atoms i and j.

$$E_{Coulomb} = C \cdot \frac{q_i q_j}{\left[r_{ij}^3 + (\frac{1}{\gamma_{ij}})^3\right]^{\frac{1}{3}}}$$
(2)

The EEM model is based on atom-centered point charges, whereas a more realistic charge distribution should be smooth and anisotropic. To capture the anisotropic features, induced dipole models and/or off-center sites can be added to obtain a hybrid polarizable model^{16, 17}. The cationic dummy atom (CDA) model of Åqvist and Warshel¹⁸ is an attractive way to add multi-site charge distribution to a metal ion atom center. An octahedral geometry is the most common topological scheme for CDA simulations but other topological schemes like tetrahedral, tetrahedral-like with three dummy atoms and an empty site or pentagonal bipyramidal have also been used^{19,20}. A tetrahedral CDA model with zinc as the central metal ion was used to evaluate the binding free energy of zinc to proteins and the free energy of binding contributed by the conformational fluctuations of the zinc-binding site was enhanced using this model compared to the standard, spherical ion model²¹. Pentagonal bipyramidal CDA models were used to improve the solvation, binding thermodynamics, and coordination geometries of Ca²⁺ and Mg²⁺ ions ²⁰. Octahedral CDA models have been used for enhancing the modeling of systems including Mg^{2+22} , Cu^{2+23} , Mn²⁺²⁴, Ni²⁺²⁵, and more²⁶. While these models use standard 12-6 Lennard-Jones (LJ) potential and neglect polarization and ion-induced dipole interactions, attempts to develop a new type of LI potential (12-6-4) by adding an additional $\frac{1}{m^4}$ term²⁷ to describe the ion induced dipole interactions for ions represented by standard single atom²⁸ and ions represented by CDA²⁹ have been reported.

In this work, we describe a novel CDA model, called CDA^{pol}, where polarization and ion-induced electrostatic interactions are explicitly incorporated using the fluctuating charge (FC) model. The CDA^{pol} model is very similar to the Drude model^{6, 16} in spirit in which part of the mass and charge of the ion is fractioned into multiple sites anchored to the ion center. This model delocalizes a part of the total charge on dummy atoms placed around the ion center to mimic covalent bonds. To illustrate CDA^{pol}, we report the results for an exemplar transition metal ion (Zn²⁺) using both the standard CDA and the CDA^{pol} models. Six fractional positive charges were added to dummy atoms which are connected to the Zn²⁺ ion in an octahedral geometry at a constant distance (specifically, 0.9Å); the CDA interacts with one LJ center on the central atom and seven (one middle ion and six dummy atoms) electrostatic centers on all CDA atoms. While reproducing properties of highly charged ions using fixed charge models has been

challenging, we demonstrate that the novel CDA^{Pol} model addresses many of these issues and outperforms the standard CDA model.

Separate electronegativity and hardness parameters were assigned to the middle ion and dummy atoms; these parameters were then optimized to allow the charges to fluctuate within the partial and total charge constraints specified in the CDA^{pol} model. For modeling CDA^{pol} solvation simulations, one or two different potentials were required depending on the method used (non-polarizable or polarizable). If the polarizable model is used, in addition to the AMBER potential, a separate potential is required for modeling the polarizable region. Consequently, two separate potential parameter optimizations were required. First, the polarizable potential parameters were tuned to reproduce the CDA^{pol} hydration by optimizing the middle ion and dummy atoms electrostatic energy parameters. Second, AMBER 12-6 LJ parameters were tuned to reproduce the target hydration free energies (HFE) and ion-oxygen distance (IOD) values (Figure 2). The details of the parameter optimizations procedures and training data for the model used in this work can be found in the supporting information. Using this locally polarizable model in combination with TI calculations, we can examine the effect of the CDA^{pol} model charge updates in response to environmental changes. To evaluate the fluctuations in the CDA charges, the charges on middle ion and dummy atoms were collected during a 50 ps equilibration of the solvated CDA ion. The charge fluctuation on the middle ion and dummy atoms and the deviations of charges on dummy atoms from the target value are shown in Figures S.3 and S.4 in the supporting information. These data show that the charges on these atoms place a slightly positive charge on the central ion (target was 0 charge and on average a charge of ~0.019 was observed during simulations) while the dummy atom charges fluctuate around the target value of +0.33 (Table 1).



Figure 2. Flowchart of CDA_{pol} potentials training and modeling

The dipole moment of the CDA^{pol} model was calculated with respect to the molecule's center of mass as follows:

$$x_{c} = \left(\frac{1}{M}\right) \sum_{i=1}^{n} (m_{i} \times x_{i}) \quad ; \quad y_{c} = \left(\frac{1}{M}\right) \sum_{i=1}^{n} (m_{i} \times y_{i}) \quad ; \quad z_{c} = \left(\frac{1}{M}\right) \sum_{i=1}^{n} (m_{i} \times z_{i})$$

$$P_{x} = \sum_{i=1}^{n} [q_{i} \times (x_{i} - x_{c})] \quad ; \quad P_{y} = \sum_{i=1}^{n} [q_{i} \times (y_{i} - y_{c})]$$

$$P_{z} = \sum_{i=1}^{n} [q_{i} \times (z_{i} - z_{c})]$$

$$P = \sqrt{P_{x}^{2} + P_{y}^{2} + P_{z}^{2}}$$
(5)

where x_i , y_i , and z_i are atom coordinates, m_i are the atomic masses, M is the total mass of the molecule, (x_c , y_c , z_c) are the center of mass coordinates, q_i are atom charges, and P is the dipole moment. The dipole moment fluctuations for CDA^{pol} during a 50 ps NPT equilibration is shown in Figure 3. The average of these 1000 snapshot points is 0.22 D which is not an unexpected value for the CDA^{pol} model.

Atom	Target charge	Average charge	SD
Zn	0	0.0009	0.002
D1	0.333	0.3321	0.016
D2	0.333	0.3330	0.016
D3	0.333	0.3330	0.017
D4	0.333	0.3340	0.016
D5	0.333	0.3328	0.016
D6	0.333	0.3341	0.017

Table 1. Averages and standard deviations (SD) for CDA^{pol} atomic charges during 50ps equilibration(1k data points).



Figure 3. Instantaneous dipole moments of the CDA^{pol} molecule in solution during the simulation. The average value of the 1000 snapshots during 50 ps is 0.25 D.

Three-point Gaussian integration of free energy difference of two states yielded the HFE shown in Figure 4. These contour graphs include the final HFE values in the LJ scanning space using non-polarizable or polarizable models. When using the non-polarizable purely classical AMBER model, the HFE values vary from -330 Kcal/mol to -440 Kcal/mol in the LJ scanning space. However, when using the polarizable model, the HFE values vary from -450 Kcal/mol to -500 Kcal/mol in the LJ scanning space (note the different HFE scales in Figure 4). Hence, AMBER with fixed CDA charges is more sensitive to changes in LJ parameters relative to the CDA^{pol} model where the charges fluctuate. IOD values were calculated from radial distribution functions (RDF) obtained with a grid resolution of 0.01 Å based on the average volume of the trajectories in the range 0 Å to 10.0 Å. The IOD values were obtained based on the protocol previously used for calculating the IOD values of highly charged metal ions²⁷. The coordination number (CN) values were determined via integrating the ion-oxygen RDF from the origin to its first minimum in the RDF plots. The resulting IOD values from both non-polarizable and polarizable models are shown in Figure 5.

HFE values represent a thermodynamic property, while IOD and CN represent structural properties. The experimental target HFE, IOD and CN for Zn^{2+} are -467.3 Kcal/mol, 2.1 Å and 6, respectively³⁰. During LJ parameter scanning, the LJ parameter ϵ was varied from 1 kcal/mol to 3.4 kcal/mol in increments of 0.1, while the $R_{min}/2$ parameter was scanned from 0.6Å to 1.0Å with a 0.1Å interval. Using the non-polarizable model and the 12-6 LJ nonbonded model only, we couldn't reproduce the target HFE and IOD values simultaneously. However, the polarizable model using a 12-6 LJ potential reproduced the target HFE, IOD and CN values with good accuracy together at two different LJ parameter sets (see Table S.1 in the supporting information) demonstrating the greater flexibility of CDA^{pol}. Overall, the best value



Figure 4. HFE values obtained from scanning LJ parameters. Absolute values are reported in figure legends.

is $R_{min}/2$ of 0.9 Å and an ε of 1.1 Kcal/mol, which we have chosen as the default for the current model. This shows that with the local polarizability in CDA^{pol}, while the total charge of the CDA^{pol} molecules is constrained to a constant value, the atomic charges respond to their environment yielding an instantaneous dipole that allows the thermodynamic and geometrical properties to be well reproduced using physically meaningful \Box parameters³¹.



Figure 5. IOD values obtained from scanning LJ parameters.

To obtain an estimate of the execution time of the simulations using non-polarizable or polarizable models, the average of the total simulation time of 500 NPT equilibration simulations using Simulated Annealing with NMR-Derived Energy Restraints (Sander) AMBER or Sander ReaxFF/AMBER of the solvated CDA^{pol} were calculated. Each simulation was performed for 50 ps using a single Intel Xeon E5-2680v4 core. These benchmark calculations showed a 35% increase in computational cost when using the CDA^{pol} model. This shows that a modest increase in computational cost is sufficient to reap the benefits of a polarizable CDA model for more accurate calculations of thermodynamic and geometrical properties.

In summary, a novel cation dummy atom model with polarization effects, called CDA^{pol}, was described. CDA^{pol} includes polarization effects induced by a solvent surrounding highly-charged ions as well as including ion-induced dipole interactions which corresponds to non-symmetric charge distributions in the CDA^{pol} dummy atoms. In a proof-of-concept demonstration with the CDA^{pol} model, experimental thermodynamic and geometrical observables for Zn²⁺ ion hydration were reproduced. The parameterization was performed through a scan of the 12-6 LJ potential and electrostatic parameters of the polarizable force field. The charges within the CDA^{pol} model were updated at every step with a constraint on the total charge of +2. Our CDApol model showed less sensitivity to the changes in LJ parameters which can be attributed to the inclusion of polarization and induced dipole effects in this model. It was demonstrated that this locally polarizable model reproduces the experimental HFE, IOD and CN simultaneously with a standard 12-6 LJ potential, while this was not observed using the classic CDA model under similar modeling conditions. Using the CDA^{pol} model for the simulation of ion hydration is advantageous over fixed charge CDA and conventional spherical models not only because it allows a greater flexibility in parameterization, but it is also able to better reproduce the thermodynamic and geometrical observables simultaneously. The ability to capture local environmental events in large systems using this polarizable model opens a range of problems that can be tackled using CDA^{pol} to address both chemical and biological processes.

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