

From simple to complex crystal chemistry in the RE - Au - Tt systems ($RE = La, Ce, Pr, Nd, Ho$; $Tt = Ge, Sn, Pb$)

Sogol Lotfi¹, Roy Arrieta¹, Gordon Peterson¹, Pablo Delgado¹, Jakoah Brgoch^{1,2*}

¹*Department of Chemistry, University of Houston, Houston, Texas 77204, United States*

²*Texas Center for Superconductivity, Houston 77204, Texas, United States*

Abstract

Polar intermetallics are an intriguing class of compounds with complex relationships between composition and structure that are not fully understood. This work reports a systematic study of the underexplored ternary composition space RE - Au - Tt ($RE = La, Ce, Pr, Nd, Ho$; $Tt = Ge, Sn, Pb$) to expand our knowledge of the intriguing chemistry and diversity achievable with these metallic constituents. These composition spaces are particularly interesting because of the potential to find Au -bearing, highly polar intermetallic compounds. The elements were first reacted through arc welding under an inert atmosphere followed by annealing at 850°C. X-ray diffraction of the products identified unreported eight compounds ranging from the simple $NaTl$ -type compounds $La_{1.5}Au_2Pb_{0.5}$, $Nd_{2-x}Au_2Pb_x$, and $Ho_{2-x}Au_2Sn_x$, to the more structurally complex La_5AuPb_3 in the Hf_5CuSn_3 -type structure and Pu_3Pd_4 -type RE_3Au_3Ge ($RE = La, Ce, Pr, Nd$). First-principles electronic structure calculations revealed that a combination of Fermi surface-Brillouin zone interactions, electrostatic interactions, and delocalized metallic bonding contributes to the formation of these phases. These calculations show that a mixture of electrostatic and metallic bonding plays a dominant role in these phases. The RE - Au - Tt composition space remains full of potential for discovering materials with relevant magnetic and quantum properties, provided the crystal chemistry can be comprehended.

Introduction

Polar intermetallic compounds, a subset of metal-rich solids, have received much interest in academic laboratories and industrial research settings due to their complex crystal chemistry and potential for fascinating physical properties. Strictly defined, polar intermetallics are compounds that have a ratio of valence electrons per atom between $1.2 \leq (e/a) \leq 4$, existing between the limits of Hume-Rothery and Zintl phases, which contain $1 \leq (e/a) \leq 2$ and $(e/a) \geq 4$, respectively.¹⁻⁴ Varying the e/a ratio and chemical composition provides a diversity of crystal structures and distinct chemical bonding motifs ranging from networks to clusters and quasicrystals.⁵⁻⁷ The complexity of polar intermetallics can be justified because they contain structural and bonding features from both Hume-Rothery and Zintl type compounds. Unlike Hume-Rothery and Zintl phases, polar intermetallics suffer from complicated electron counting rules and the inability to assign definitive oxidation states, making predictions of crystal chemistry challenging.⁸ This is further convoluted by the wide range of compositions and stoichiometries that can be combined to form polar intermetallics, leaving large swathes of phase space unexplored. Therefore, to further our understanding, we must find new compounds that can help us unravel the intricacies of polar intermetallics, understand their structural tendencies, and further interpret their chemical bonding and overall crystal chemistry.

Ternary rare-earth (*RE*) noble metal (*M*) tetrels (*Tt*) are an exciting composition space to conduct such a study due to the relatively large electronegativity differences between the constituent elements. These phases can be quickly synthesized by arc-melting followed by annealing at accessible temperatures.⁹ The products crystallize easily, and numerous ternary compounds have been identified and characterized. Indeed, these compounds are of great interest owing to their fascinating structural chemistries and physical properties, including superconductivity (e.g., $RE_2Pt_3Ge_5$, $RE_2Ir_3Ge_5$),¹⁰ magnetocaloric effects (e.g., $GdRu_2Ge_2$, RE_2M_2Sn),^{11, 12} complex magnetic ordering (e.g., $RECrGe_3$, $Nd_{117}Co_{54}Sn_{111}$, RE_2Ni_2Pb),^{13, 14} and other quantum phenomena (e.g., $RE_{n+1}M_nTt_{3n+1}$).¹⁵ The

magnetic properties stem from the interaction between the localized $4f$ electrons of a rare-earth atom and the d electrons of transition metal.¹⁶ However, there are no apparent mechanisms for controlling magnetism in these polar intermetallic compounds, even though some systems like *RE-Ni-Ge* have been exhaustively studied.¹⁷⁻¹⁹

It is possible to add further complexity to the crystal chemistry of polar intermetallics by studying gold-containing compounds. Au has the highest electronegativity of the noble metals, indicating that the most polarized intermetallics may exist in $M = \text{Au}$ compositional spaces. However, many *RE-Au-Tt* ternary phase spaces remain underexplored, with most systems reporting only one or two compounds. One common thread is the *REAuTt* phase, which crystallizes in rhombohedral *LiGaGe* structure type with space group $P6_3mc$ (No. 186).²⁰⁻²² The $[\text{AuGe}]^n$ - anionic sublattice in this compound features a strong polar-covalent bond between Ge–Au and Au–Au, generating a three-dimensional polyanionic backbone. *REAu₂Ge₂* phases in the tetragonal *ThCr₂Si₂* structure type have also been identified in some *RE* systems like Ce and Pr, and are reported to order antiferromagnetically with Néel temperatures of 16 K and 11.9 K, respectively.^{19, 23, 24} More complex and unique topologies also pervade these systems, such as the orthorhombic *Ce₃Pd₆Sb₅* type formed in the *RE-Au-Sn* systems (*RE* = Ce, Nd, Sm).²⁵

This work identifies eight new compounds in the *RE-Au-Tt* (*RE* = La, Ce, Pr, Nd; *Tt* = Ge, Sn, Pb) ternary phase space through a systematic study of these composition spaces at 850°C. These compounds adopt three structure types spanning simple to complex crystal chemistry across the Au-rich to Au-poor composition range. They include *RE_{2-x}Au₂Pb_x* (*RE* = La, Nd) and *HoAu₂Sn* in the *NaTl*-type, *La₅AuPb₃* in the *Hf₅CuSn₃* type, and *RE₃Au₃Ge* with *RE* = La, Ce, Pr, Nd in the *Pu₃Pd₄* structure type. Density functional theory (DFT) calculations were performed to interpret the origin of structural favorability for these phases and examine the nature of the covalent, ionic, and metallic

contributions to polar intermetallic bonding. The results of this work will further our fundamental understanding of these systems and gold-containing polar intermetallic phases in general.

Experimental

Synthesis. The starting metals – gold (splatter, 99.999%, Materion Advanced Chemical), tetrels Ge (powder, 99.99%, Alfa Aesar), Sn (powder, 99.5%, Alfa Aesar), and Pb (shot, W. H. Curtin & Co.), and the rare-earth elements La, Ce, Pr, Nd, and Ho (filings, 99.8%, HEFA Rare Earth), were weighed out in the desired stoichiometric ratios and ground together with an agate mortar and pestle to form a uniform sample with a total weight of 200 mg. The samples were cold-pressed into 6 mm pellets using a maximum pressure of 2500 psi and reacted under argon gas in a Centorr 5SA arc furnace with a current of 30-45 A. All samples were flipped and melted multiple times to ensure homogeneity. The weight loss for each sample after arc-melting was less than 2%. Each resulting ingot was subsequently sealed in an evacuated fused silica tube (less than 4×10^{-2} torr) and annealed in a Thermo Scientific Lindberg Blue M muffle furnace at 850°C for 200 h, then cooled back to room temperature over 24 hours. The final products had a silvery metallic luster and were all brittle. The La-containing products showed some sensitivity to air fading to a dull black color over several days to weeks when left at ambient conditions. As a result, all products were stored in an argon atmosphere glove box ($O_2 < 0.1$ ppm; $H_2O < 0.1$ ppm). The preparation of $LaAuGe_3$, $LaAuGe_2$, $La_4Au_5Ge_{11}$, $LaAu_2Ge$, $LaAu_3Ge$, La_2AuGe , and La_2Au_2Ge was also attempted following the same synthetic procedure; however, the products from these reactions were all multiphase based on powder X-ray diffraction and fully indexed to known compounds.

Powder X-ray diffraction. X-ray powder diffractograms were collected at room temperature using a PANalytical X'Pert powder diffractometer equipped with Cu $K\alpha$ radiation ($\lambda = 1.54183$ Å). The samples were prepared by grinding the annealed ingots in the glovebox using an agate mortar and

pestle. The fine powder was then spread on a zero-diffraction silicon plate and measured from 5° to 90° 2 θ . Le Bail refinements were carried out on the collected data of all compositions to confirm phase purity and determine the lattice parameters using the EXPGUI interface for the General Structure Analysis System (GSAS).^{26, 27} Refined unit cell parameters for all synthesized compounds are given in Table 1, and Le Bail refinement of powder X-ray diffraction data is shown in Figure S1. A shifted-Chebyshev function was used to model the background. All crystal structures were visualized using VESTA²⁸ and Diamond 3.²⁹

Table 1. Refined unit cell parameters for all compounds from powder X-ray diffraction.

	a (Å)	b (Å)	c (Å)	α (°)	β (°)	γ (°)
La ₃ Au ₃ Ge	14.0300(4)	14.0300(4)	6.2015(6)	90	90	120
Ce ₃ Au ₃ Ge	13.865(2)	13.865(2)	6.150(1)	90	90	120
Pr ₃ Au ₃ Ge	13.8118(5)	13.8118(5)	6.1249(5)	90	90	120
Nd ₃ Au ₃ Ge	13.7075(4)	13.7075(4)	6.0935(5)	90	90	120
La ₅ AuPb ₃	9.692(1)	9.692(1)	7.0087(9)	90	90	120
La _{1.5} Au ₂ Pb _{0.5}	7.2252(1)	7.2252(1)	7.2252(1)	90	90	90
Nd _{2-x} Au ₂ Pb _x	7.0906(6)	7.0906(6)	7.0906(6)	90	90	90
Ho _{2-x} Au ₂ Sn _x	6.86690(4)	6.86690(4)	6.86690(4)	90	90	90

Single-crystal X-ray diffraction. Single crystals were harvested from crushed samples of the La-containing phases and mounted on the end of pulled glass fibers. Crystals were silvery grey and lustrous and generally formed as small cubes or plates approximately 10-50 μm in size. Diffraction data sets were collected as omega scans (0.5° scan width at 60 μm detector distance) on a Bruker Apex II platform diffractometer equipped with a 4KCCD Apex II detector and Mo K α radiation source at 296 K. Peak hunting, indexing, data integration, and finalization were performed with the provided Bruker APEX II software. The structures of each crystal were solved using the shelXle program package for SHELX refined on F_o^2 .³⁰ Anisotropic atomic displacement parameters for each structural solution are given in Table S1. Solved structures have been submitted to the CCDC and can be

obtained under deposition numbers 2129946–2129948. Crystal structures were visualized with the Crystal Impact Diamond 3 and VESTA software packages.^{28, 29}

Table 2. Crystallographic data for the nominally loaded La_{1.5}Au₂Pb_{0.5}, La₅AuPb₃, and La₃Au₃Ge from single-crystal X-ray diffraction

Nominal formula	La _{1.5} Au ₂ Pb	La ₅ AuPb ₃	La ₃ Au ₃ Ge
Refined formula	La _{1.58(3)} Au ₂ Pb _{0.42(3)}	La ₅ Au _{0.91(1)} Pb ₃	La ₃ Au _{3.17(1)} Ge _{0.83(1)}
Formula mass (g mol ⁻¹)	700.37	1494.83	1101.55
Space group; <i>Z</i>	<i>Fd</i> $\bar{3}m$; 4	<i>P6</i> ₃ / <i>mcm</i> ; 2	<i>R</i> $\bar{3}$; 6
<i>a</i> , <i>b</i> (Å)	7.2315(4)	9.7121(3)	14.04(1)
<i>c</i> (Å)	7.2315(4)	7.0033(3)	6.220(5)
<i>V</i> (Å ³)	378.17(6)	572.08(4)	1062(2)
ρ_{calc} (g cm ⁻³)	12.3006	8.67731	6.88628
Absorption correction		Multi-scan	
Radiation		Mo K α	
μ (mm ⁻¹)	113.162	73.701	83.445
θ range (deg.)	4.88 – 34.225	2.421 – 30.501	2.901 – 27.563
<i>hkl</i> ranges	$-10 \leq h \leq 9$ $-11 \leq k \leq 10$ $-11 \leq l \leq 9$	$-13 \leq h \leq 13$ $-11 \leq k \leq 13$ $-10 \leq l \leq 9$	$-18 \leq h \leq 17$, $-13 \leq k \leq 18$, $-8 \leq l \leq 7$
No. reflections; <i>R</i> _{int}	743; 0.0124	6479; 0.0426	1691; 0.055
No. unique reflections	51	343	539
No. parameters	4	15	26
<i>R</i> (<i>F</i>) for $F_o^2 > 2\sigma(F_o^2)$ ^a	0.0270	0.0331	0.0439
<i>R</i> _w (<i>F</i> _o ²) ^b	0.0538	0.0791	0.1132
Goodness of fit	1.230	1.081	1.056
($\Delta\rho$) _{max} , ($\Delta\rho$) _{min} (e Å ⁻³)	0.815, -1.969	2.455, -1.983	4.097, -2.838

$$^a R(F) = \sum ||F_o| - |F_c|| / \sum |F_o|$$

$$^b R_w(F_o^2) = [\sum [w(F_o^2 - F_c^2)^2] / \sum wF_o^4]^{1/2}; w^{-1} = [\sigma^2(F_o^2) + (Ap)^2 + Bp] \quad \text{where}$$

$$p = [\max(F_o^2, 0) + 2F_c^2] / 3$$

Table 3. Refined atomic coordinates and equivalent isotropic displacement parameters for the nominally loaded compounds (a) La_{1.5}Au₂Pb_{0.5}, (b) La₅AuPb₃, and (c) La₃Au₃Ge.

Compound	atom	Wyck.	Occ.	<i>x</i>	<i>Y</i>	<i>z</i>	<i>U</i> _{eq} (Å ²) ^a
(a) La _{1.5} Au ₂ Pb _{0.5}							

Au1	8a	1	$\frac{1}{8}$	$\frac{5}{8}$	$\frac{5}{8}$	0.0212(4)
La1	8d	0.79(2)	$\frac{3}{8}$	$\frac{7}{8}$	$\frac{7}{8}$	0.0277(6)
Pb1	8d	0.21(2)	$\frac{3}{8}$	$\frac{7}{8}$	$\frac{7}{8}$	0.0277(6)
<hr/>						
(b) La ₅ AuPb ₃						
Pb1	6g	1	0.6132(1)	1	$\frac{3}{4}$	0.0202(3)
Au1	2b	0.907(9)	1	1	$\frac{1}{2}$	0.0310(7)
La1	4d	1	$\frac{1}{3}$	$\frac{2}{3}$	$\frac{1}{2}$	0.0192(3)
La2	6g	1	1	0.2619(2)	$\frac{3}{4}$	0.0213(4)
<hr/>						
(c) La ₃ Au ₃ Ge						
Au1	18f	0.89(1)	0.72301(7)	0.94251(7)	0.2178(1)	0.0174(3)
Ge1	18f	0.11(1)	0.72301(7)	0.94251(7)	0.2178(1)	0.0174(3)
La1	18f	1	0.4988(1)	0.8761(1)	0.4019(2)	0.0178(5)
Au2	3a	0.56(2)	$\frac{1}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0.037(1)
Ge2	3a	0.44(2)	$\frac{1}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0.037(1)
Au3	3b	0.43(2)	$\frac{1}{3}$	$\frac{2}{3}$	$\frac{1}{6}$	0.041(2)
Ge3	3b	0.57(2)	$\frac{1}{3}$	$\frac{2}{3}$	$\frac{1}{6}$	0.041(2)

^a U_{eq} is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

Table 4. Selected refined bond lengths [Å] for La_{1.5}Au₂Pb_{0.5}, La₅AuPb₃, and La₃Au₃Ge from single-crystal X-ray diffraction.

La _{1.5} Au ₂ Pb _{0.5}		La ₅ AuPb ₃		La ₃ Au ₃ Ge	
Au1 – Au1	3.131(1)	Pb1 – La2	3.3206(7)	Au1 – Au1	3.020(2)
Au1 – La1	3.131(1)	Pb1 – La2	3.413(2)	Au1 – La1	3.026(2)
Au1 – La1	3.6158(2)	Pb1 – La1	3.4825(7)	Au1 – La1	3.125(3)
La1 – La1	3.1313(2)	Pb1 – La1	3.4844(7)	Au1 – Au1	3.170(2)
		Pb1 – La2	3.7061(6)	Au1 – La1	3.128(3)
		Au1 – La2	3.087(1)	Au1 – La1	3.231(3)
		La1 – La1	3.5016(2)	Au1 – La1	3.334(3)
		La1 – La2	3.5017(2)	Au1 – La1	3.385(3)
		La1 – La2	4.034(1)	Au1 – La1	3.455(2)
		La1 – La2	4.035(1)	La1 – Au3	3.059(2)
				Au2 – Au3	3.110(2)

Electronic Structure Calculations. Density functional theory (DFT) calculations using the Vienna Ab-initio Simulation Package (VASP) version 5.4.4 were performed to optimize the geometries with a convergence criterion of 1×10^{-3} eV/Å and calculate the wave functions and charge densities of each reported compound with a convergence criterion of 1×10^{-8} eV.^{31,32} DFT optimized total energies, unit cell parameters, and atomic positions are listed in Tables S2-S5. Calculations were done using the projector augmented wave (PAW) potentials with exchange and correlation described by Perdew-Burke-Ernzerhof (PBE) with a Γ -centered Monkhorst-Pack k -point grid containing at least 1000 k -points atom⁻¹.^{33, 34} Density of states (DOS) and crystal orbital Hamilton population (COHP) calculations were carried out using the Local-Orbital Basis Suite toward Electronic Structure (LOBSTER).^{35,36} Bader charges on each atomic position were determined using the Bader program for VASP.³⁷⁻³⁹

Results and Discussion

Synthesis and Structural Characterization. Seven ternary intermetallic systems containing a rare earth (RE) metal, gold, and a main group tetrel metal (Tt) were synthetically explored: La–Au–Pb, Nd–Au–Pb, Ho–Au–Sn, La–Au–Ge, Ce–Au–Ge, Pr–Au–Ge, and Nd–Au–Ge. In each case, elements were mixed in stoichiometric ratios, arc welded under flowing Ar, and sealed in fused silica ampoules under vacuum and annealed at 850°C for 200 h. Structural characterization using single-crystal and powder X-ray diffraction of the resulting products indicated the formation of eight previously unknown compounds in three distinct classes: A NaTl structure type for $RE_{2-x}Au_2Tt_x$ ($La_{1.5}Au_2Pb_{0.5}$, $Nd_{2-x}Au_2Pb_x$, $Ho_{2-x}Au_2Sn_x$), followed by La_5AuPb_3 in the Hf_5CuSn_3 structure type, and the most complex RE_3Au_3Ge (La_3Au_3Ge , Ce_3Au_3Ge , Pr_3Au_3Ge , Nd_3Au_3Ge) in the Pu_3Pd_4 structure type.

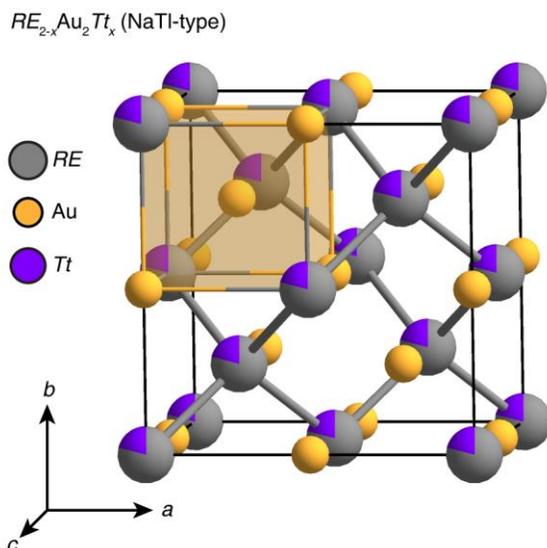


Figure 1. The structure of $RE_{2-x}Au_2Pb_x$ in the cubic NaTl-type.

The first class of compounds presented in this work are three newly discovered $RE_{2-x}Au_2Tt_x$ ($RE = La, Nd, Ho, Tt = Pb, Sn$) compounds adopting the NaTl structure type: $La_{1.5}Au_2Pb_{0.5}$, $Nd_{2-x}Au_2Pb_x$, and $Ho_{2-x}Au_2Sn_x$. These compounds, illustrated in Figure 1, form an ordered superstructure of the simple body-centered cubic arrangement, in which Au atoms alternate with statistically mixed RE and Tt sites. The refined unit cell parameters of all three compounds were determined through Le Bail refinement of powder X-ray diffraction, and the fit diffractogram for the $La_{1.5}Au_2Pb_{0.5}$ phase is shown in Figure S1a (refined cell parameters for all structures given in Table 1). For the La–Au–Pb analog, the RE/Tt elemental mixing was determined through single-crystal X-ray diffraction to be 79(2)% La and 21(2)% Pb, leading to an overall composition of $La_{1.58(3)}Au_2Pb_{0.42(3)}$, which is in agreement with the nominally loaded $La_{1.5}Au_2Pb_{0.5}$ composition. Similar statistical mixing is expected for the Nd and Ho structures. Crystallographic and structural parameters for this structure solution are provided in Tables 2–4.

NaTl-type phases are classically considered Zintl compounds, and many examples of binary alkali-main group metal NaTl-type compounds are known. The ternary compositions related to this group of compounds containing Au are Li_2AuSb , $Li_2Au_{0.75}Si_{1.25}$, and $Li_2Au_{0.25}In_{1.75}$ systems,⁴⁰ their

conventional classification as Zintl compounds conforms with a calculation of valence electrons per atom. For example, the most electron-rich of these species, Li_2Au lies just at the upper bound of the Zintl edge (2 e/a). The NaTl-type structure containing lanthanide atoms will form slightly above this limit, including CeMg_3 and $\text{Dy}_{0.67}\text{Mg}_{1.33}$, but so far only when having the small and electropositive element Mg.^{41,42} By contrast, the *RE*-Au-*Tt* phases presented here significantly eclipse this threshold, with $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$ forming at a valence density of 2.625 e/a . This is indicative that these compounds represent a step into a previously unexplored compositional region of non-Zintl NaTl-type phases.

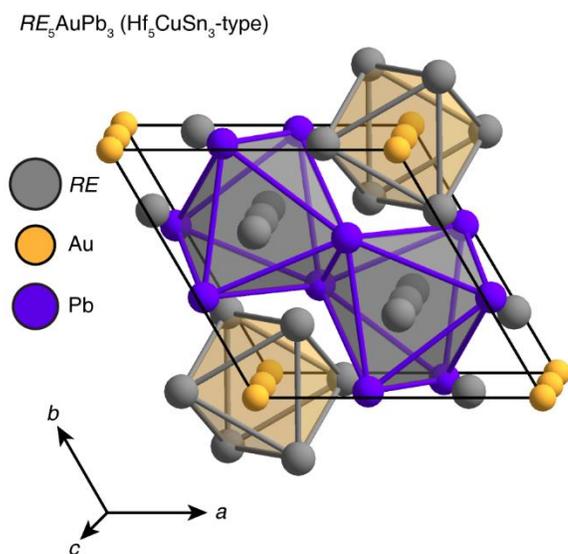


Figure 2. The structure of Hf_5CuSn_3 -type La_5AuPb_3 .

The next compound identified is La_5AuPb_3 forms in the rhombohedral Hf_5CuSn_3 structure type.⁴³ The structure of La_5AuPb_3 is shown in Figure 2, and refined unit cell parameters from Le Bail powder (Figure S1d) and single-crystal diffraction are given in Tables 1 and 2, respectively. This structure type is, in itself, a derivative of the classic Mn_5Si_3 structure,⁴⁴ which consists of two crystallographically distinct columns of face-sharing octahedra that run along the *c* axis. In the Hf_5CuSn_3 -type, noble metal atoms stuff the usually empty *RE* octahedra centered at the unit cell vertices, creating a one-dimensional chain of 91% occupied Au sites within a distance comparable to

metallic bonding interactions. These Au@La₆ octahedra are tiled in the *ab* plane with La@Pb₆ octahedra, which share faces along the *c* axis and edges the in *ab*-plane.

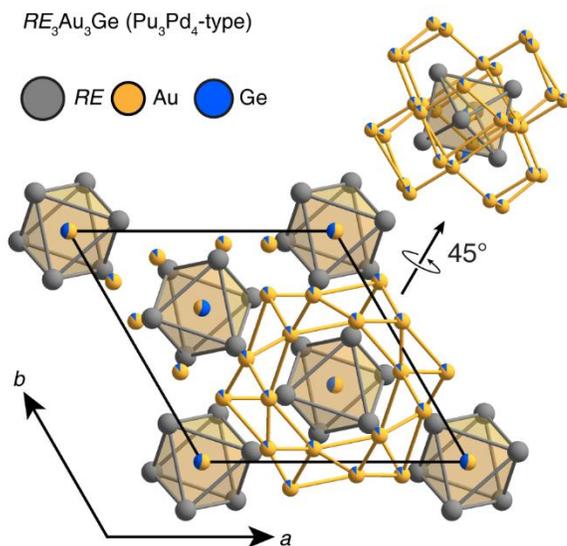


Figure 3. The structure of Pu₃Pd₄-type La₃Au₃Ge, highlighting the CsCl-like La₈(Au/Ge)₃₃ cluster.

The final and most complex series of compounds discovered crystallize in the Pu₃Pd₄ structure type with the generic formula RE₃Au₃Ge (*RE* = La, Ce, Pr, Nd). The Pu₃Pd₄ structure type is present in the Inorganic Crystal Structure Database (ICSD) for *RE*-Au binary systems,^{45, 46} including Nd₃Au₄ and Th₃Au₄.⁴⁷⁻⁴⁹ However, it has only once been reported in a ternary system in the form of Nd₃Pd_{3.79}Ru_{0.21}.⁵⁰ Figure 3 shows the large rhombohedral unit cell of this structure type solved from single-crystal diffraction data for La₃Au₃Ge (crystallographic data provided in Tables 2-4), and the refined cell parameters are provided for the RE₃Au₃Ge family prepared here in Table 1. The solved La₃Au₃Ge structure is characterized by an AlB₂-like arrangement of *RE* octahedra centered by a disordered mixture of Au (43%) and Ge (57%). Forming a scaffolding layer between the octahedra is an Au-rich (89%) network of atoms forming hexagonal channels that run along the *c*-axis of the structure. This leads to an overall refined composition of La₃Au_{3.17(1)}Ge_{0.83(1)} for this structure. Contact

distances between Au atoms in this network range from 2.8 Å to 3.5 Å, within standard ranges of aurophilic contacts.^{51, 52} Interestingly, through a roughly 45° rotation, the scaffolding lattice and octahedral $\text{La}_8(\text{Au/Ge})_{33}$ unit can be viewed together as a highly distorted CsCl-like fragment, in which cubes of Au and Ge house the *RE* atoms. The intergrowth of this cubic motif with octahedral units suggests that primarily polar interactions between the Au-rich structural units and *RE* domains stabilize the structural building blocks. These interfaces between the metallicly delocalized electrons in the Au bonding network and Au-centered *RE* polyhedra also hint at some intriguing structural chemistry that can be investigated through DFT electronic structure calculations.

Electronic Structure Investigation with DFT. The electronic stability of polar intermetallic compounds is understood to be controlled by a complicated mixture of structurally-related effects. Differing interpretations of the interatomic interactions in polar intermetallic compounds lead to disparate frameworks for understanding these structure-properties relationships. A classical Hume-Rothery approach would connect stability to valence electron count and Fermi surface-Brillouin zone interactions,⁵³ whereas looking through the Zintl lens, charge transfer and filled octets are paramount.⁵⁴ To parse the relative contributions of these effects in highly-polar Au-containing *RE*-*Au-Tt* phases, density functional theory (DFT) calculations can be employed to investigate the electronic structure of these newly reported compounds directly.

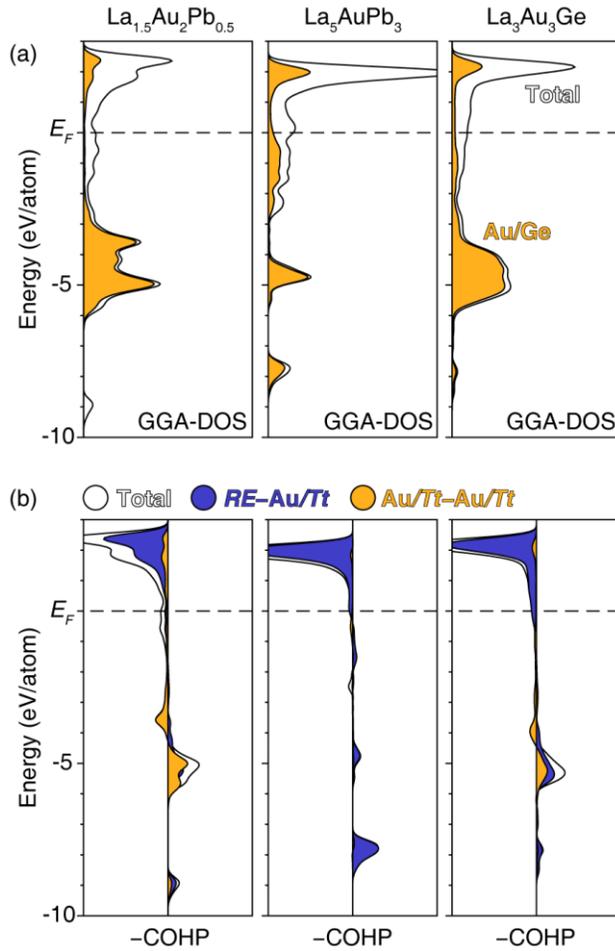


Figure 4. Electronic structure calculations on $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$, La_5AuPb_3 , and $\text{La}_3\text{Au}_3\text{Ge}$ show (a) density of states (DOS) and, (b) crystal orbital Hamilton population ($-\text{COHP}$) curves showing the total (black), RE-Au/Tt (blue), and Au/Tt-Au/Tt (gold) interactions.

Interactions between the Fermi surface and Brillouin zone can lead to structural stability in intermetallics via the electronic structure.⁵⁵ One way to visualize this is with a density of states (DOS) plot, such as those shown for $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$, La_5AuPb_3 , and $\text{La}_3\text{Au}_3\text{Ge}$ in Figure 4a. The band population for each structure is plotted against energy, with E_F marking the level below which bands are filled with electrons. In this picture, a peak in the DOS shows a high population of bands at a particular energy value, whereas a local minimum, or pseudogap, in the DOS represents an energy level with relatively few bands. For electronically stable systems, Fermi surface-Brillouin zone interactions open up pseudogaps in the DOS at E_F , which lowers the energies of the highest occupied crystal

orbitals. Therefore, DOS plots that show the presence of a pseudogap at the Fermi level are correlated with energetically favorable phases, whereas E_F falling on a DOS peak is associated with electronic instability. However, the picture is much simpler for the three structures investigated here. The DOS plot near E_F is nearly flat for each compound, indicating few, if any, stabilizing effects coming from atomic orbital overlap in these crystal structures. This is further confirmed by investigating the crystal orbital Hamilton population ($-COHP$) curves. These calculations show the contributions to bonding (positive when plotted as negative COHP) and antibonding (negative when plotted as negative COHP) interactions plotted against energy. In the COHP curve shown for each structure in Figure 4b, the total COHP and specific $RE-Au/Tt$ and $Au/Tt-Au/Tt$ interactions show that very few bonding or antibonding interactions occur near the Fermi level. Thus, the DOS and COHP indicate that these structures are likely not stabilized primarily through orbital overlap.

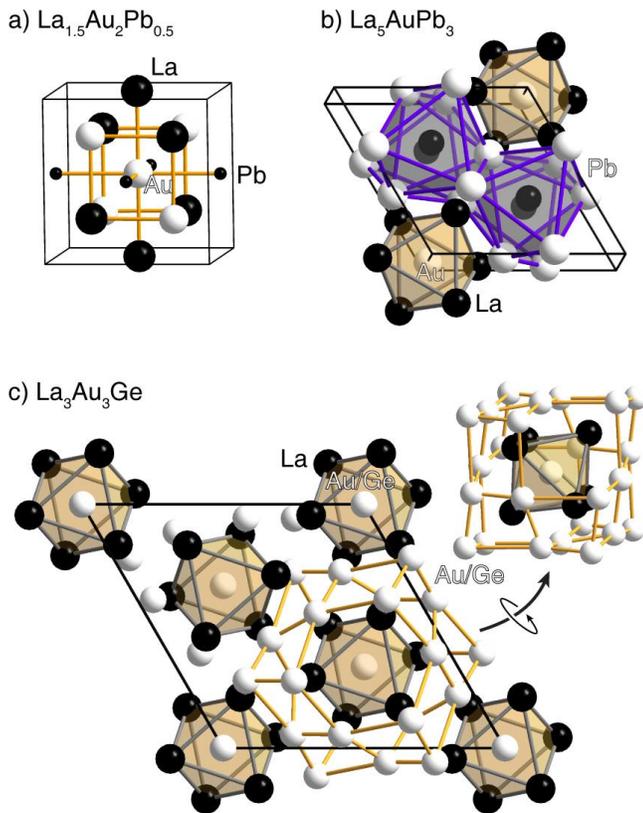


Figure 5. Bader ionicity calculations for a) $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$, b) La_5AuPb_3 , and c) $\text{La}_3\text{Au}_3\text{Ge}$. In this scheme, white spheres represent anionic atoms, and black spheres represent cations. The volume of each sphere is proportional to the magnitude of the charge.

Next, investigating the role of electrostatic interactions shows that significant differences in electronegativity (EN) between *RE* elements and Au ($\text{EN}_{\text{La}} = 1.10$, $\text{EN}_{\text{Au}} = 2.54$) provide a moderate charge transfer. Consequently, electrostatic interactions may have a significant role in the stability of the compounds reported here. To quantitatively assess this charge transfer, DFT-calculated Bader charges were determined for each atom in the La-containing structures. Bader charges are tabulated by assigning the DFT-calculated electron density within a structure to each atom according to the Bader method, which divides space at the zero flux surface of the electron density between atoms.³⁷ The result of this calculation for each structure is plotted in Figure 5, where black and white spheres represent cationic and anionic atoms, respectively, and the volume of each sphere is proportional to the tabulated Bader charge (calculated Bader charges given in Table S5). Examining these Bader schemes for each La-containing structure shows that *RE* atoms are cationic and Au atoms are anionic, as would be expected from their respective electronegativities. In $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$, the cubic Au coordination environment contains half Au contacts and half La/Pb disordered sites. The ability of La and Pb to occupy the same position in this structure is clarified with the observation that both atoms behave as cations relative to the highly electronegative Au atoms, even though Pb is only slightly less electronegative ($\text{EN}_{\text{Pb}} = 2.33$). Nevertheless, Pb adopts cationic character maximizing these favorable secondary electrostatic interactions. Intriguingly, the $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$ phase chooses to adopt the NaTl-type instead of the full Heusler structure, which would seem to be better optimized for maximizing favorable electrostatic interactions. This suggests that the shorter Au–Au contacts of the NaTl-type are crucial to the structure preference and that electrostatic effects do not purely govern this compound

Despite containing the same combination of elements, the ionicity of Pb is inverted in the La_5AuPb_3 structure. In this phase, anionically-centered $\text{Au}@\text{La}_6$ octahedra are intergrown with

ionically opposite La@Pb_6 clusters. This arrangement of charges increases the favorable interactions between positive and negative ions within and between adjacent clusters. Considering Pb's behavior like a cation in $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$, these results suggest that Pb can behave amphionically in this compositional space, filling whatever ionic role is needed to suit the more extreme electronegativities of La and Au.

The $\text{La}_3\text{Au}_3\text{Ge}$ structure contains the same Au@La_6 octahedra as those seen in La_5AuPb_3 . However, without an oppositely charged cluster to satisfy this arrangement, the outlying cationic La atoms are instead buffered by the scaffolding network of Au atoms. The atoms in this layer form distorted cubes around each La, housing each cation within an Au-rich coordination environment. A Bader analysis shows that each structure is arranged to create significantly favorable electrostatic interactions, especially between *RE* and Au atoms as seen in the octahedral clusters in La_5AuPb_3 and $\text{La}_3\text{Au}_3\text{Ge}$. This aligns with expectations given the electronegativities of these elements. However, other aspects of these phases, such as nearest-neighbor Au–Au contacts in $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$ and $\text{La}_3\text{Au}_3\text{Ge}$, seem to run counter to a purely electrostatically-driven structural model. This discrepancy implies that other factors contribute to the stability of these compounds, such as potential delocalized metallic bonding.

The final potential source of stability in these compounds stems from delocalized metallic bonding. Electron localization function (ELF) calculations are beneficial for identifying delocalized electrons within an intermetallic structure.⁵⁶ Figure 6 shows the structures of $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$, La_5AuPb_3 , and $\text{La}_3\text{Au}_3\text{Ge}$ overlaid with slices of the calculated ELF surface. In these plots, values close to zero (deep blue) represent locations in the electronic structure with a very low probability of locating electrons, such as in the space between atoms. Values close to 1 (red), on the other hand, show locations of highly localized electrons, such as in core states, covalent bonds, or lone pairs. In between, ELF values of 0.5 correspond to fully delocalized electrons, such as those in an electron gas. The ELF plots for these structures all show a combination of these features. In the $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$ phase,

delocalized bonding between Au atoms is readily apparent along the (1 0 1) lattice plane, while the (0 0 1) layer shows similar metallic character between Au and Pb. This delocalized bonding network, especially along the Au–Au contacts, hints at the favorability of the NaTl-type structure, which blends electrostatic interactions with metallic Au–Au bonding. La atoms in $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$ remain non-interacting, as seen in the ELF plot, with regions of deep blue ELF minima separating their electron density from their neighbors. A similar picture is seen for La_5AuPb_3 and $\text{La}_3\text{Au}_3\text{Ge}$, where the La atoms are also highly localized, and there is significant delocalization and interaction between Au and the Pb or Au/Ge scaffolding atoms in both structures. Thus, this supports our overall picture of these phases as polar intermetallics, containing a mixture of electrostatically driven interactions, such as those between *RE* and Au atoms, and delocalized metallic bonding, such as in the Au–Au and Au–*Tt* in all structures.

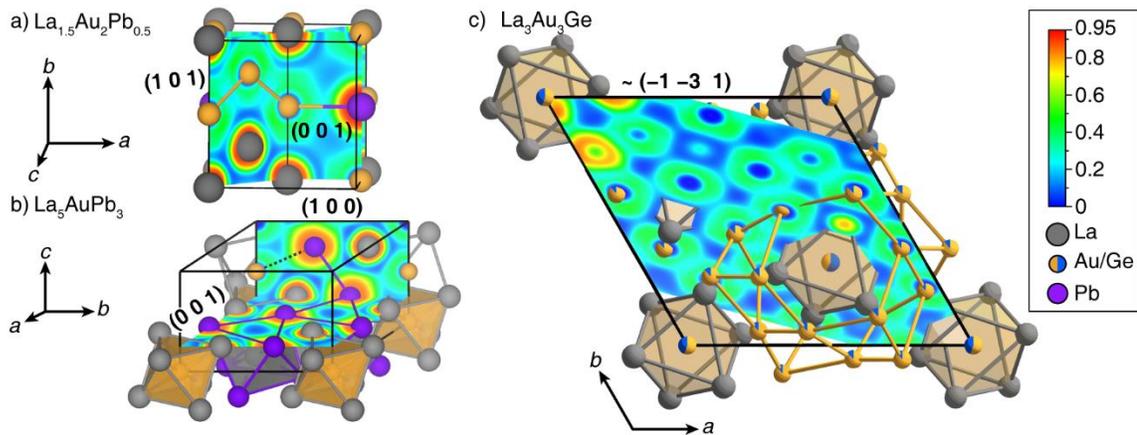


Figure 6. Electron localization function (ELF) slices through a) the (1 0 1) and (0 0 1) planes in $\text{La}_{1.5}\text{Au}_2\text{Pb}_{0.5}$, b) the (1 0 0) and (0 0 1) planes in La_5AuPb_3 , and c) the $\sim(-1 -3 1)$ plane in $\text{La}_3\text{Au}_3\text{Ge}$.

Altogether, an analysis of the electronic structure in these phases gives us a complete picture of the bonding interactions contributing to their stability. Au-containing polar intermetallics offer a step into a region of solid-state composition space where structures are not controlled by either Fermi Surface-Brillouin Zone interactions or by the filling of octets through complete charge transfer. The characteristic mixture of delocalized metallic bonding and favorable electrostatic interactions

potentially presents a unique pathway for forming highly unusual metallic oxidation states and stabilizing structures only accessible through gold's extraordinary electronegativity.

Conclusion

A synthetic investigation into the underexplored RE - Au - Tt ($RE = La, Ce, Pr, Nd, Ho$; $Tt = Ge, Sn, Pb$) composition space revealed eight novel compounds in three structure types: NaTl-type $La_{1.5}Au_2Pb_{0.5}$, $Nd_{2-x}Au_2Pb_x$, and $Ho_{2-x}Au_2Sn_x$, Hf₅CuSn₃-type La_5AuPb_3 , and Pu₃Pd₄-type RE_3Au_3Ge ($RE = La, Ce, Pr, Nd$). Each compound was synthesized through the direct high-temperature reaction of elements and subsequent annealing at 850°C. These compounds are representative polar intermetallics, which are notable for their complex structural features originating from a combination of electronic, electrostatic, and metallic bonding schemes. Au-containing polar intermetallics are of particular interest due to Au's uniquely high electronegativity among transition metals, which enables the stabilization of ternary structures that are not realizable in other systems. Deconvolution of the bonding contributions in these phases can be determined through a DFT investigation of each compound's electronic structure. The density of states and crystal orbital Hamilton populations reveal approximately optimized bonding interactions without a notable pseudogap at the Fermi level, indicating that Fermi surface-Brillouin zone interactions do not govern stability. Visualizations of the calculated Bader charges in these compounds show that electrostatic forces are a vital stabilizing force in these structures, where Au and Tt bonding network maximizes the anionic-cationic interactions. To finally examine the metallic bonding, ELF calculations indicate delocalized electrons in the Au/ Tt bonding networks while RE atoms remain electronically isolated. RE - Au - Tt polar intermetallic compounds present a composition space ripe for exploring novel materials with complex crystalline and magnetic structures.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: XXXXXX.

Powder X-ray diffraction data, Anisotropic displacement parameters for $\text{La}_{1.5}\text{Au}_2\text{Pb}$, La_5AuPb_3 , and $\text{La}_3\text{Au}_3\text{Ge}$, DFT total energies, DFT optimized geometries, DFT calculated Bader charges.

Accession Codes

CCDC reference numbers 2129946, 2129947, and 2129948 contain the supplementary crystallographic data for this paper. These data can be obtained free of charge via www.ccdc.cam.ac.uk/data_request/cif, or by emailing data_request@ccdc.cam.ac.uk, or by contacting The Cambridge Crystallographic Data Centre, 12 Union Road, Cambridge CB2 1EZ, UK; fax: +441223 336033

Author Information

Corresponding Author

*E-mail: jbrgoch@uh.edu

Notes

The authors declare no competing financial interest.

Acknowledgements

The authors would like to thank Prof. Arnold M. Guloy, Dr. Xiqu Wang, and Dr. James D. Korp for their helpful discussions. The authors gratefully acknowledge the generous financial support provided by the Welch Foundation (E-1981) and the Texas Center for Superconductivity at the University of Houston (TcSUH). This research utilized the Maxwell/Opuntia/Sabine cluster(s) operated by the Research Computing Data Core at the University of Houston.

References

1. Miller, G. J.; Schmidt, M. W.; Wang, F.; You, T.-S., Quantitative advances in the Zintl–Klemm formalism. *Zintl phases* **2011**, 1-55.
2. Miller, G. J.; Thimmaiah, S.; Smetana, V.; Palasyuk, A.; Lin, Q., Gold's Structural Versatility within Complex Intermetallics: From Hume-Rothery to Zintl and even Quasicrystals. *MRS Online Proceedings Library (OPL)* **2013**, 1517.
3. Pauling, L.; Ewing, F. J., The ratio of valence electrons to atoms in metals and intermetallic compounds. *Rev. Mod. Phys.* **1948**, *20* (1), 112.
4. Meyer, G.; Naumann, D.; Wesemann, L., *Inorganic chemistry highlights*. John Wiley & Sons: 2002; Vol. 1.
5. Paufler, P.; Villars, P.; Calvert, L., *Pearson's handbook of crystallographic data for intermetallic phases*. Wiley Online Library: 1986; Vol. 1-3, p 3258.
6. Smetana, V.; Rhodehouse, M.; Meyer, G.; Mudring, A.-V., Gold polar intermetallics: structural versatility through exclusive bonding motifs. *Acc. Chem. Res.* **2017**, *50* (11), 2633-2641.
7. Lin, Q.; Corbett, J. D., Interpenetrating networks of three-dimensional Penrose tiles in CaAu_3Ga , the structurally simplest cubic approximant of an icosahedral quasicrystal. *Inorg. Chem.* **2008**, *47* (9), 3462-3464.
8. Lotfi, S.; Brgoch, J., Discovering Intermetallics Through Synthesis, Computation, and Data-Driven Analysis. *Chemistry – A European Journal* **2020**, *26* (40), 8689-8697.
9. Binnewies, M.; Dolinšek, J.; Failamani, F.; Feuerbacher, M.; Fisk, Z.; Guélou, G.; Guo, Q.; Hedo, M.; Henkie, Z.; Ipsen, H., *Crystal growth of intermetallics*. Walter de Gruyter GmbH & Co KG: 2018.
10. Venturini, G.; Meot-Meyer, M.; Marêché, J.; Malaman, B.; Roques, B., De nouveaux isotopes de $\text{U}_2\text{Co}_3\text{Si}_5$ ou $\text{Lu}_2\text{Co}_3\text{Si}_5$ dans les systems RT-Ge (R= elements des terres rares; T= Ru, Co, Rh, Ir). Supraconductivite de $\text{Y}_2\text{Ir}_3\text{Ge}_5$. *Mater. Res. Bull.* **1986**, *21* (1), 33-39.
11. Gil, A.; Szytuła, A.; Tomkowicz, Z.; Wojciechowski, K.; Zygmunt, A., Magnetic properties of RNiSi_2 and RNiGe_2 compounds. *J. Magn. Magn. Mater.* **1994**, *129* (2-3), 271-278.
12. Zhang, Y., Review of the structural, magnetic and magnetocaloric properties in ternary rare earth $\text{RE}_2\text{T}_2\text{X}$ type intermetallic compounds. *J. Alloys Compd.* **2019**, *787*, 1173-1186.
13. Oliynyk, A. O.; Stoyko, S. S.; Mar, A., Many metals make the cut: Quaternary rare-earth germanides $\text{RE}_4\text{M}_2\text{InGe}_4$ (M= Fe, Co, Ni, Ru, Rh, Ir) and $\text{RE}_4\text{RhInGe}_4$ derived from excision of slabs in RE_2InGe_2 . *Inorg. Chem.* **2015**, *54* (6), 2780-2792.
14. Benkaddour, Y.; Abdelaoui, A.; Yakoubi, A.; Khachai, H.; Al-Douri, Y.; Omran, S. B.; Shankar, A.; Khenata, R.; Voon, C. H.; Prakash, D., First-Principle Calculations of Structural, Elastic, and Electronic Properties of Intermetallic Rare Earth $\text{R}_2\text{Ni}_2\text{Pb}$ (R= Ho, Lu, and Sm) Compounds. *J. Supercond. Nov. Magn.* **2018**, *31* (2), 395-403.
15. Weiland, A.; Felder, J. B.; McCandless, G. T.; Chan, J. Y., One Ce, Two Ce, Three Ce, Four? An Intermetallic Homologous Series to Explore: $\text{A}_{n+1}\text{B}_n\text{X}_{3n+1}$. *Chem. Mater.* **2020**, *32* (4), 1575-1580.
16. Bie, H.; Zelinska, O. Y.; Tkachuk, A. V.; Mar, A., Structures and Physical Properties of Rare-Earth Chromium Germanides RECrGe_3 (RE= La– Nd, Sm). *Chem. Mater.* **2007**, *19* (18), 4613-4620.
17. Morozkin, A.; Knotko, A.; Yapaskurt, V.; Yuan, F.; Mozharivskyj, Y.; Pani, M.; Provino, A.; Manfrinetti, P., The Ho–Ni–Ge system: Isothermal section and new rare-earth nickel germanides. *J. Solid State Chem.* **2015**, *225*, 193-201.
18. Rieger, W.; Parthé, E., Ternäre Erdalkali-und Seltene Erdmetall-Silicide und-Germanide mit ThCr_2Si_2 -Struktur. *Monatsh. Chem.* **1969**, *100* (2), 444-454.

19. Szytuła, A.; Kaczorowski, D.; Arulraj, A.; Baran, S.; Penc, B., Magnetic properties of NdAu₂Ge₂. *J. Magn. Magn. Mater.* **2009**, *321* (20), 3402-3405.
20. Rossi, D.; Marazza, R.; Ferro, R., Ternary rare earth alloys: RAuGe compounds. *J. Alloys Compd.* **1992**, *187* (2), 267-270.
21. Schnelle, W.; Pöttgen, R.; Kremer, R.; Gmelin, E.; Jepsen, O., The crystal structure, magnetic susceptibility, electrical resistivity, specific heat, and electronic band structure of RAuGe (R= Sc, Y, La, Lu). *J. Phys.: Condens. Matter* **1997**, *9* (7), 1435.
22. Pöttgen, R.; Borrmann, H.; Kremer, R. K., Ferromagnetic ordering in CeAuGe. *J. Magn. Magn. Mater.* **1996**, *152* (1-2), 196-200.
23. Krimmel, A.; Hemberger, J.; Kegler, C.; Nicklas, M.; Engelmayer, A.; Knebel, G.; Fritsch, V.; Reehuis, M.; Brando, M.; Loidl, A., The evolution from long-range magnetic order to spin-glass behaviour in PrAu₂(Si_{1-x}Ge_x)₂. *J. Phys.: Condens. Matter* **1999**, *11* (36), 6991.
24. Joshi, D. A.; Nigam, A.; Dhar, S.; Thamizhavel, A., Magnetocrystalline anisotropy in RAu₂Ge₂ (R= La, Ce and Pr) single crystals. *J. Magn. Magn. Mater.* **2010**, *322* (21), 3363-3371.
25. Fickenscher, T.; Rodewald, U. C.; Niehaus, O.; Gerke, B.; Haverkamp, S.; Eckert, H.; Poettgen, R., The Stannides RE₃Au₆Sn₅ (RE= La, Ce, Pr, Nd, Sm)–Synthesis, Structure, Magnetic Properties and ¹¹⁹Sn Mössbauer Spectroscopy. *Z. Naturforsch. B* **2015**, *70* (6), 425-434.
26. Toby, B. H., EXPGUI, a graphical user interface for GSAS. *J. Appl. Crystallogr.* **2001**, *34* (2), 210-213.
27. Larson, A.; Von Dreele, R., Report LAUR 86-748. *Los Alamos National Laboratory, New Mexico, USA* **2000**.
28. Momma, K.; Izumi, F., VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data. *J. Appl. Crystallogr.* **2011**, *44* (6), 1272-1276.
29. Impact, C., DIAMOND-Crystal and Molecular Structure Visualization. **2009**.
30. Hübschle, C. B.; Sheldrick, G. M.; Dittrich, B., ShelXle: a Qt graphical user interface for SHELXL. *J. Appl. Crystallogr.* **2011**, *44* (6), 1281-1284.
31. Kresse, G.; Furthmüller, J., Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set. *Phys. Rev. B* **1996**, *54* (16), 11169.
32. Kresse, G.; Joubert, D., From ultrasoft pseudopotentials to the projector augmented-wave method. *Phys. Rev. B* **1999**, *59* (3), 1758.
33. Blöchl, P. E., Projector augmented-wave method. *Phys. Rev. B* **1994**, *50* (24), 17953.
34. Perdew, J. P.; Burke, K.; Ernzerhof, M., Generalized gradient approximation made simple. *Phys. Rev. Lett.* **1996**, *77* (18), 3865.
35. Deringer, V. L.; Tchougréeff, A. L.; Dronskowski, R., Crystal orbital Hamilton population (COHP) analysis as projected from plane-wave basis sets. *J. Phys. Chem. A* **2011**, *115* (21), 5461-5466.
36. Dronskowski, R.; Bloechl, P. E., Crystal orbital Hamilton populations (COHP): energy-resolved visualization of chemical bonding in solids based on density-functional calculations. *J. Phys. Chem.* **1993**, *97* (33), 8617-8624.
37. Sanville, E.; Kenny, S. D.; Smith, R.; Henkelman, G., Improved grid-based algorithm for Bader charge allocation. *J. Comput. Chem.* **2007**, *28* (5), 899-908.
38. Bader, R. F., Atoms in molecules. *Acc. Chem. Res.* **1985**, *18* (1), 9-15.
39. Henkelman, G.; Arnaldsson, A.; Jónsson, H., A fast and robust algorithm for Bader decomposition of charge density. *Comput. Mater. Sci.* **2006**, *36* (3), 354-360.
40. Pauly, H.; Weiss, A.; Witte, H., Phasenbreite und Valenzelektronenkonzentration (VEK) in den ternären kubischen Zintlphasen vom NaTl-Typ. *Int. J. Mater. Res.* **1968**, *59* (7), 554-558.
41. Krypiakewytsch, P.; Evdokimenko, V., Neue Verbindungen im System Dysprosium-Magnesium und in verwandten Systemen. *Z. Anorg. Allg. Chem.* **1967**, *355* (1-2), 104-112.
42. Iandelli, A., Intermetallic compounds of the rare earth metals. *Physical Chemistry of Metallic Solutions and Intermetallic Compounds* **1959**.

43. Rieger, W.; Nowotny, H.; Benesovsky, F., Phasen mit oktaedrischen Bauelementen des Übergangsmetalls. *Monatsh. Chem. Verw. Teile Anderer Wiss.* **1965**, 96 (1), 232-241.
44. Aronsson, B., An Investigation of the $\text{Me}_3\text{Si}_3\text{-MeSi}$ Region of the Mn-Fe-Si and Some Related Systems. *Acta Chem. Scand.* **1958**, 12 (2), 11.
45. Fluck, E., Inorganic crystal structure database (ICSD) and standardized data and crystal chemical characterization of inorganic structure types (TYPIX)—Two tools for inorganic chemists and crystallographers. *J. Res. Natl. Inst.* **1996**, 101 (3), 217.
46. Cromer, D.; Larson, A.; Roof, R., The crystal structure of Pu_3Pd_4 . *Acta Crystallogr. Sect. B: Struct. Sci.* **1973**, 29 (3), 564-567.
47. Fornasini, M.; Saccone, A., Crystal structure of Nd_3Au_4 and $\text{Nd}_{17}\text{Au}_{36}$. *Z. Kristallogr. Cryst. Mater.* **1994**, 209 (8), 657-659.
48. Palenzona, A.; Cirafici, S., The Th-Au phase diagram. *J. Less Common Met.* **1986**, 124 (1-2), 245-249.
49. Palenzona, A., The crystal structure and lattice constants of R_3Pt_4 compounds. *J. Less Common Met.* **1977**, 53 (1), 133-136.
50. Raevskaya, M.; Avertseva, I.; Rusnyak, Y., Interaction of palladium with ruthenium and neodymium[[Previously Titled: Diagram of state of the Pd-Ru-Nd system.]]. *Russ. Metall.* **1994**, 2, 131-135.
51. Seibel, E. M.; Schoop, L. M.; Xie, W.; Gibson, Q. D.; Webb, J. B.; Fuccillo, M. K.; Krizan, J. W.; Cava, R. J., Gold–Gold Bonding: The Key to Stabilizing the 19-Electron Ternary Phases Ln AuSb (Ln= La–Nd and Sm). *J. Am. Chem. Soc.* **2015**, 137 (3), 1282-1289.
52. Schmidbaur, H.; Schier, A., A briefing on aurophilicity. *Chem. Soc. Rev.* **2008**, 37 (9), 1931-1951.
53. Mizutani, U., The Hume-Rothery rules for structurally complex alloy phases. In *Surface Properties and Engineering of Complex Intermetallics*, World Scientific: 2010; pp 323-399.
54. Nordell, K. J.; Miller, G. J., Linking intermetallics and zintl compounds: An investigation of ternary trielides (Al, Ga, In) forming the NaZn_{13} structure type. *Inorg. Chem.* **1999**, 38 (3), 579-590.
55. Mizutani, U.; Kondo, Y.; Nishino, Y.; Inukai, M.; Feuerbacher, M.; Sato, H., Fermi surface–Brillouin-zone-induced pseudogap in $\gamma\text{-Mg}_{17}\text{Al}_{12}$ and a possible stabilization mechanism of $\beta\text{-Al}_3\text{Mg}_2$. *J. Phys.: Condens. Matter* **2010**, 22 (48), 485501.
56. Silvi, B.; Savin, A., Classification of chemical bonds based on topological analysis of electron localization functions. *Nature* **1994**, 371 (6499), 683-686.

Table of Contents

