1	First Principles Analysis of Ethylene
2	Oligomerization on Single-site Ga³⁺ Catalysts
3	Supported on Amorphous Silica
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19 Abstract

Amorphous, single site, silica-supported main group metal catalysts have recently been found to 20 promote olefin oligomerization with high activity at moderate temperatures and pressures (~250°C 21 22 and 1 atm). Herein, we explore the molecular-level relationship between active site structures and the associated oligomerization mechanisms by developing amorphous, silica-supported Ga³⁺ 23 models from periodic, first-principles calculations. Representative Ga³⁺ sites, including three- and 24 25 four-coordinated geometries, are tested for multiple ethylene oligomerization pathways. We show that the three-coordinated Ga^{3+} site promotes oligomerization through a facile initiation process 26 that generates a Ga-alkyl intermediate, followed by a Ga-alkyl-centered Cossee-Arlman 27 mechanism. The strained geometry of a three-coordinated site enables a favorable free energy 28 landscape with a kinetically accessible ethylene insertion transition state (1.7 eV) and a previously 29 unreported β -hydride transfer step (1.0 eV) to terminate further C-C bond formation. This result, 30 in turn, suggests that Ga³⁺ does not favor polymerization chemistry, while microkinetic modeling 31 confirms that ethylene insertion is the rate-determining step. The study demonstrates a promising 32 33 flexibility of main group ions for hydrocarbon transformations and, more generally, highlights the importance of the local geometry of metal ions on amorphous oxides in determining catalytic 34 35 properties.

36 Introduction

Light olefins (ethylene and propylene) are the fundamental building blocks of the 37 petrochemical industry. The molecules are readily available and can be converted to a wide range 38 of useful intermediate and final products.^{1–3} The production of short linear alpha olefins (LAOs), 39 in particular, has been of significant interest in the olefin industry for the past few decades, as they 40 form the key ingredients of various plastics, lubricants, fuels, and surfactants.³⁻⁶ Production of 41 LAOs, such as 1-butene, 1-hexene, and 1-octene, through selective catalytic olefin oligomerization 42 has, in turn, become a core research topic in the olefin community due to the existence of many 43 emerging alternative sources of light olefins and the increasing demand for polyethylene.⁷⁻⁹ 44 Presently, homogeneous catalysts, using ligand-modified transition metals, are among the most 45 active and selective catalysts for olefin oligomerization.^{10,11} Among the transition metals, nickel 46 complexes are commonly used, where the Ni²⁺ compounds modified with alkyl or hydride moieties 47 are the catalytic centers responsible for olefin oligomerization.^{10–13} Many efforts have also been 48 devoted to developing heterogeneous catalysts for olefin oligomerization, given their greater 49 50 facility for catalyst regeneration and product separation. As an example, reactive transition metal 51 species, inspired by analogous structures on homogeneous catalysts, can be supported on porous structures, such as zeolites and amorphous silica, but these catalysts suffer from poor 52 oligomerization activity or low selectivity to LAOs.¹⁴⁻¹⁹ 53

Density functional theory (DFT)-based studies are becoming increasingly important in elucidating the structures and properties of active sites, as well as the reaction mechanisms, of heterogeneously catalyzed olefin oligomerization processes.^{20–22} For instance, a recent firstprinciples study by Brogaard *et al.* investigated Ni(0), Ni⁺, and Ni²⁺ supported on an SSZ-24 framework in the context of ethylene oligomerization. The work revealed that the most plausible

pathway starts from a [Ni(II)-ethylene-H]⁺ complex, analogous to a Ni-alkyl ligand in the 59 homogeneous context, and the oligomerization chemistry follows the classic Cossee-Arlman (C-60 A) mechanism, where ethylene coordinates and inserts between the species and the Ni ion, 61 resulting in chain growth.²² The process is terminated via an ethylene-assisted β -hydride 62 elimination step that restores the [Ni(II)-ethylene-H]⁺ moiety. In another mechanistic study by 63 64 Metzger *et al.*, investigating Ni-MFU-4*l* for ethylene dimerization, a combination of isotope tracing, molecular probes, and DFT calculations were used to demonstrate that the catalytic cycle 65 also follows a C-A mechanism, where ethylene insertion and β -hydride elimination are the key 66 elementary steps.²³ 67

To expand the space of possible heterogeneous catalysts for olefin oligomerization, single-68 site, silica-supported main-group Ga ions have recently been explored and found to selectively 69 catalyze ethylene and propylene oligomerization to higher molecular weight linear olefins, up to 70 at least C₁₈, at 250 °C and an atmospheric pressure.²⁴ Through a combination of in-situ and ex-situ 71 X-ray absorption spectroscopy (XAS), H/D exchange, IR techniques, and DFT calculations, it was 72 determined that Ga³⁺ sites catalyze the oligomerization reaction. The mechanism starts from a site 73 activation process, where a Ga³⁺-O bond is activated, resulting in Ga-vinyl and Si-OH moieties 74 (species 1 to 2, Fig. 1). After the activation step, ethylene insertion and β -hydride elimination occur, 75 leading to butadiene and a Ga-hydride site (species 6_b, Fig. 1). The Ga-hydride was proposed to 76 be responsible for the subsequent oligomerization cycle, following a C-A mechanism (cycle c, Fig. 77 $1).^{24}$ 78



Figure 1. Possible ethylene oligomerization pathways on Ga^{3+} . Proton transfer cycle occurs on the empty Ga^{3+} site (region a); alternatively, formation of Ga-hydride or Ga-alkyl leads to pathway transfer (region b) to Cossee-Arlman mechanisms for ethylene oligomerization (either Ga-hydride-centered (region c) or Ga-alkyl-centered (region d)). The corresponding energies and geometries are shown in Figures 3-5.

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To further elucidate the mechanistic and structural aspects of oligomerization on Ga-based silica catalysts, it is of interest to explore whether additional factors, such as the intrinsic heterogeneity of amorphous silica, can accommodate activation of other oligomerization pathways. It is well-known that many heterogeneous catalytic reactions are highly sensitive to the structure of active sites.^{25–27} The Cr³⁺-silica geometry in the Philips catalyst for ethylene polymerization is a useful example, wherein the reactivity of different Cr sites in terms of initiation, propagation, and termination energetics vary significantly with the local strain condition, causing a small percentage of the Cr sites to dominate the polymerization chemistry, $^{27-29}$ Further, in recent works, an alternate C-A cycle with alkene-assisted β -hydride transfer has been explored on both Ni, for oligomerization²², and Cr, for polymerization,³⁰ and favorable energy landscapes are observed. Similar considerations may apply to the Ga³⁺-silica system, underlining the need to further explore the link between oligomerization pathway selectivity and the structural diversity of the Ga³⁺ singlesites.

Herein, we develop amorphous silica-supported Ga³⁺ models based on periodic DFT calculations 94 to study ethylene oligomerization mechanisms of the previously synthesized Ga/SiO₂ catalysts. 95 96 The energetics of three primary cycles are compared, as shown in Figure 1. A proton transfer cycle can occur on the empty Ga³⁺ site starting from ethylene activation by Ga³⁺, followed by insertion 97 of another ethylene unit (species 1 to 4, Fig. 1). The Ga-butenyl species can then desorb via a 98 proton transfer step, forming n-butene, completing the oligomerization cycle via proton transfer 99 and reforming of the empty Ga³⁺ site (region a, Fig. 1).^{30,31} Alternatively, the Ga-butenyl species 100 may activate pathway transfer processes (region b, Fig. 1). β-hydride elimination can activate 101 another oligomerization cycle, where butadiene and Ga-hydride are formed, proceeding to a C-A 102 mechanism (species 4- 6_b , Fig. 1). Further, as mentioned above, β -hydride elimination can be 103 104 assisted by an incoming alkene molecule, which accepts a hydrogen atom and becomes an alkyl intermediate, which may be another key intermediate in the C-A cycle (species 4-7_c, Fig. 1). 105 Following the pathway transfer process, the C-A cycle can be either Ga-hydride-centered (region 106 c, Fig. 1) or Ga-alkyl-centered (region d, Fig. 1), and the two cycles differ by terminating the 107 oligomer chain growth through β-hydride elimination or by directly transferring hydrogen to an 108 ethylene molecule. In our Ga/SiO₂ system, we report that only the less-constrained, three-109 coordinated Ga³⁺ site is responsible for the oligomerization reactivity through the Ga-alkyl 110

centered C-A cycle, of which the free energy landscape is significantly more favorable than the 111 competing proton transfer and the hydride-centered C-A mechanisms. The selective ethylene 112 dimerization observed in experiments is enabled by an unreported transition state of the ethylene-113 assisted β-hydride transfer step to terminate lengthening of the carbon backbone, and the activation 114 energy is much lower than that of the ethylene insertion step. Finally, a detailed microkinetic 115 116 analysis is carried out, based on the DFT results, which establishes that the ethylene insertion step is rate-limiting. In aggregate, these insights establish a comprehensive mechanistic understanding 117 of how amorphous silica-supported main group single sites catalyze olefin oligomerization. 118

119 Methods

Single-site Ga^{3+} -silica structures are developed starting from a recently reported amorphous silica slab model.³² The amorphous structure originates from an annealing procedure using molecular dynamics and continuous dehydration processes.³² The periodic model has a sufficiently large unit cell to incorporate the possibility of long-range reconstructions and interactions (Figure 2). To create each single-atom Ga^{3+} site, a Si atom in the amorphous model is replaced with Ga, and a proton is added to an adjacent oxygen atom to maintain a charge balance.

The DFT calculations are based on self-consistent, periodic density functional theory using 126 the Vienna Ab-initio Simulation Package (VASP).³³⁻³⁶ The BEEF-VdW exchange-correlation 127 functional³⁷ with projector augmented wave (PAW) pseudopotentials is employed.³⁸ A dipole 128 layer is applied in the vacuum to eliminate the electrostatic interaction errors between mirror image 129 slabs. A **k**-point grid of 2×2×1 is used based on Monkhorst-Pack **k**-sampling, and the convergence 130 of the binding energy with respect to the k-point set is confirmed. A cutoff energy of 400 eV and 131 a force-convergence criterion of 20 meV Å⁻¹ for local energy minimization are used. The climbing-132 image nudged-elastic-band (CINEB) method with seven intermediate images is used to locate the 133

geometry of transition states^{39,40}, with initial guesses generated using the Image Dependent Pair Potential tool.⁴¹ After the CINEB calculations converge to a force below 80 meV Å⁻¹ for each image, the Lanczos diagonalization approach is employed to refine the transition state.⁴² The forceconvergence criterion of the Lanczos optimizations is 40 meV Å⁻¹.

Free energies are evaluated at 523 K and are calculated using the equation $G = E_{DFT} + E_{ZPE}$ -138 139 TS, where E_{DFT} is the ground-state potential energy from DFT. The zero-point energy corrections (E_{ZPE}) are calculated from the harmonic vibrational states. For vibrational modes with wave 140 numbers above 150 cm⁻¹, harmonic partition functions are employed to estimate entropies, while 141 for modes with lower frequencies, particle-in-a-box (PIB) and free rotor schemes, depending on 142 the geometric characteristics of the vibrations, are used (see Supporting Information for an 143 example). The adsorption energies (G_{ads}) are referenced to empty sites (G_{Ga}) and appropriate 144 amounts of gaseous ethylene molecules at 1 atm ($G_{ethylene}$). However, the free energy of Ga-hydride 145 or Ga-alkyl moieties is used for the G_{Ga} term in the C-A cycles. 146

The microkinetic model simulates a continuous stirred-tank reactor (CSTR) with no 147 concentration or temperature gradients. The reaction conditions used in the model are configured 148 to be close to the experimental setup. Ethylene oligomerization is modeled at a temperature of 523 149 150 K and a total pressure of 1 atm. The reactor has a dimension of 1 cm \times 1 cm \times 1 cm. The feed stream contains 20% of ethylene and 80% inert gas, and the feed volumetric flow rate is 1 cm³ s⁻¹. 151 The total number of available Ga sites is used to adjust the conversion of ethylene. Here, a total 152 number of 0.85×10^{-4} mol of Ga sites per 1 g of catalyst is used, corresponding to a catalyst loading 153 of 0.3%. We use this value because a Ga loading of 3 wt% was used in the experiments in the 154 previous work, and we assume that approximately 10% of the total Ga sites are reactive. 155

156 **Results and Discussion**

157 *Ga site creation*

As mentioned in the Methods section, each single site Ga^{3+} ion in an amorphous silica model is introduced by a substitution technique, resulting in a Si-OH moiety. In total, five Si atoms, as shown in Figure S(1), are considered and substituted individually. Since a Si atom binds to four O atoms, there are four possible locations where a proton can be added. Therefore, a total of 20 DFT optimizations are performed to develop the Ga site structures for ethylene oligomerization on Ga/SiO₂.

As different Ga sites are created, the resulting oxygen atom of the Si-OH group can be 164 either distant from, or close to, Ga. The possible extremes in active site structure are, in turn, 165 represented by two Ga sites with substantially different Ga - Si-OH distances, and these are used 166 as illustrative cases in the analysis that follows. In one case, the original Si-O bonds are elongated 167 (Figure 2b: a=1.80 Å, b=1.66 Å, c=1.76 Å, and d=1.69 Å). As a result, the addition of hydrogen 168 to the oxygen atom, leading to the cleavage of the bond (a), gives a final Ga-O distance of 4.57 Å 169 after DFT optimization. In the second case, the Si atom used for creating the Ga site is located in 170 a much more constrained framework, reflected by the shorter Si-O bonds (a=1.66 Å, b=1.62 Å, 171 c=1.67 Å, and d=1.64 Å). As a result, the newly formed Si-OH group gives a Ga-O bond length 172 of 2.02 Å. In the first of these cases, the Ga atom covalently binds to three oxygen atoms, which 173 174 makes the Ga site three-coordinated. In the second case, the additional, short, Ga-Si-OH bond is 175 considered as another coordination. Hence, the two extremes are defined as the three- and fourcoordinated Ga sites (3CN and 4CN). 176

A complete list of Ga-hydroxyl distance of the 20 tested sites is included in the Supporting
Information. We emphasize that the 3CN and 4CN sites, described above, bound the range of the

calculated Ga-hydroxyl distances in all considered configurations. We also note that, in our experimental results, XAS on Ga/SiO₂ indicates that the majority of sites are Ga³⁺, containing four Ga-O bonds, consistent with the 4CN site model. However, because XAS is a bulk technique, the possible formation of a small amount of 3CN Ga³⁺ sites (<10%) cannot be excluded,²⁴ and exploration of the catalytic relevance of these possible minority sites is a further motivation for the inclusion of the 3CN Ga sites in our analysis.





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Figure 2. (a) Top view of unit cell of the amorphous silica model with locations of the Si atoms used for creating 3CN and 4CN sites, and (b) bonding conditions of the original Si atoms and corresponding Ga sites after DFT optimization (Ga=green, O=red, Si=blue, and H=white)

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189 Ga^{3+} site activation process on 3CN site

Free energy diagrams of three pathways on the 3CN Ga site, evaluated at 523 K, are
outlined in Figure 3a: the proton transfer mechanism (species 1 to 5_a in Fig. 1), and two pathway

transfer processes forming either Ga-hydride (species 6_b) or Ga-alkyl (species 7_c) intermediates.
The proton transfer step closes an oligomerization cycle and reforms the empty Ga site (region a,
Fig. 1). The Ga-hydride and Ga-ethyl moieties are, in turn, key intermediates in the C-A
oligomerization mechanism (regions c and d, Fig. 1).

Starting from the empty Ga site (species 1 in Fig. 4a), a C-H bond in ethylene is 196 197 heterolytically cleaved, producing a vinyl group, and the resulting proton (H_a) from the cleavage goes to an oxygen (O_a) and breaks the Ga-O bond. The newly formed Si-OH group becomes distant 198 from the Ga site, with a Ga-O distance of 4.2 Å. The heterolytic cleavage is exothermic, with a 199 200 free energy change of -1.0 eV and an activation energy of 0.9 eV (step 1 to 2). Before the subsequent ethylene insertion occurs, a local energy minimum is found where ethylene is 201 physisorbed on the Ga site (species 3). The C=C double bond coordinates to the planar, triangle 202 geometry created by the Ga atom and two adjacent oxygen atoms (O_b and O_c). The physisorption 203 is exothermic on the 3CN site (step 2 to 3, -0.2 eV), after which the migratory insertion of another 204 ethylene molecule leads to a Ga-butenyl species with an activation barrier of 1.5 eV (step 3 to \ddagger^2). 205 In the transition state (species \ddagger^2), the vinyl group rotates slightly towards the ethylene molecule 206 and interacts with both Ga and a carbon atom (C_a), which eventually becomes the β -carbon of the 207 208 Ga-butenyl species.

209 Pathway transfer on the 3CN site

As the C₄ intermediate forms, the ethylene-assisted β -hydride transfer is the most favorable pathway due to a generally lower free energy landscape (species 4 to 7_c, Fig. 3a). In this pathway, the physisorption of a third ethylene moiety is exothermic (step 4 to 5_c, -0.3 eV), and the activation barrier of β -hydride transfer is 0.8 eV (step 5_c to \ddagger^c). Overall, the free energy of forming a Gaethyl intermediate from a clean 3CN Ga (species 1 in Fig. 4a) site is -1.7 eV, which is an exothermic process, and the Ga-ethyl species is thus quite likely to form. In contrast to this β hydride transfer, high barriers are observed for both the proton transfer and the β -hydride elimination steps. Indeed, the proton transfer step entails recovery of the cleaved Ga-O bond, which is quite high in energy due to the strained nature of the 3CN site. We note, in passing, that similarly high activation barriers for β -hydride elimination have also been observed for Zn-propyl species during propane dehydrogenation.⁴³



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Figure 3. Free energy diagrams of proton transfer and pathway transfer (through β -hydride elimination and ethylene-assisted β -hydride transfer) processes on (a) 3CN and (b) 4CN Ga sites (T = 523 K). The adsorption energies are referenced to empty sites and appropriate amounts of gaseous ethylene molecules at 1 atm. The same species numbers are used in Figure 1.



Figure 4. Schematics of proton transfer and pathway transfer on the (a) 3CN site and (b) 4CN Ga site (Ga=green, O=red, Si=blue C=black, and H=white, and the same species numbers are used in Figure 1.)

Free energy diagrams (523 K) of proton transfer (species 1 to 5_a, Fig. 1), β-hydride 224 225 elimination (species 4 to 6_b), and ethylene-assisted β -hydride transfer (species 4 to 7_c) pathways 226 on the 4CN Ga site are shown in Figure 3b. The 4CN Ga site has a different free energy landscape for site activation than does the 3CN site. Before the migratory insertion of ethylene, the 227 228 physisorption step is greatly endothermic (step 2 to 3, +1.2 eV), which can be explained by a strong steric hindrance due to the nearby siloxane framework. Although a lower intrinsic activation 229 barrier of ethylene insertion is found (step 3 to \ddagger^2 , +1.2 eV), the transition state is high in free 230 energy if Ga-vinyl is used as a reference (3CN: 1.2 eV, 4CN: 2.5 eV). Similarly, the positive free 231 energy change of ethylene physisorption leads to a significant unfavourability of ethylene-assisted 232 β -hydride transfer (step 4 to 5_c, +1.3 eV), which is, in contrast, a viable pathway on 3CN Ga site. 233 Since the 4CN Ga is in a more constrained environment, the Si-OH group formed due to ethylene 234 activation is not far from the Ga site (2.7 Å, species 4), allowing for a relatively facile proton-235 transfer step to recover the original 4CN Ga site with an accessible activation barrier (step 4 to \ddagger^a , 236 1.1 eV). Therefore, the 4CN site is more likely to catalyze olefin oligomerization through the 237 proton transfer cycle, though a fairly low turnover frequency is expected due to the high barrier of 238 239 olefin insertion. On the other hand, a pathway transfer to C-A mechanism is very likely to occur on the 3CN Ga site, forming a Ga-alkyl intermediate. 240

241 Olefin Oligomerization following a Cossee-Arlman mechanism on 3CN site

In the Ga site activation analysis on 3CN sites, the formation of a Ga-alkyl moiety through β-hydride transfer is the most energetically favorable pathway. Following the site activation, the coordination of an ethylene molecule to the alkyl group occurs, which initiates the C-A oligomerization cycle. Our analysis starts from the Ga-alkyl species, and Figure 5a shows the free energy diagram of C-A mechanism on a 3CN site. However, we analyze two types of C-A
mechanisms (Figure 1) starting from either Ga-hydride or Ga-alkyl These configurations may, in
principle, interconvert. We further analyze the related possibility that 3CN and 4CN sites may
catalyze the C-A mechanism beginning with the Ga-hydride species, which can be produced with
a hydrogen gas treatment.²⁴

251 The ethylene physisorption on Ga-ethyl species is exothermic, with a free energy change of -0.3 eV (species 1-1 to 1-2). The migratory insertion of the second ethylene molecule, which 252 approaches Ga and binds to the ethyl group, has an activation barrier of 1.7 eV (species 1-2 to 1-253 3). Following the physisorption of an additional ethylene molecule, the activation barrier of the β -254 hydride transfer (species 1-4 to 1-5, 1.0 eV) is much lower than that of the ethylene insertion step. 255 The β -hydride transfer step finishes one catalytic cycle and reforms the Ga-alkyl species. We have 256 also calculated the barrier of β -hydride elimination leading to the Ga-hydride moiety, for which 257 the barrier is significantly higher than the ethylene-assisted barrier (species 1-3 to \pm^{b} , 2.4 eV), 258 suggesting that the Ga-hydride is unlikely to form. Overall, based on the free energy analysis, we 259 predict that Ga-alkyl favors the formation of short oligomers, since the termination step (β-hydride 260 transfer) will be faster than the propagation step (migratory insertion) due to a much lower 261 262 activation barrier. This behavior has been observed in the experiments, where butenes are the primary products detected. On the other hand, the C-A mechanism will not be dominated by the 263 Ga-hydride spices, given a high barrier of β -hydride elimination step. 264

We highlight that the transition state geometry of β -hydride transfer on the 3CN Ga site is fundamentally different from the step occurring on a transition metal single site. In the transition states on Ni²⁺ or Cr³⁺ single sites, the hydrogen atom being transferred is close to the metal center, and this interaction contributes to the stabilization of transition state.^{23,30} In the transition state on a 3CN Ga site (^{+a}), however, the hydrogen atom being transferred does not interact closely with
the Ga atom, suggesting that Ga does not directly activate the C-H bond. Nevertheless, a low
barrier is observed. This geometry was reported for early transition metal-based Ziegler-Natta
catalysts, with an associated low barrier being attributed to a pseudo-hydrogen bond effect.^{44,45}
Our results suggest that a similar effect may extend to main group single sites, such as Ga.

274 Olefin oligomerization following the Cossee-Arlman mechanism on a 4CN site

The activation of ethylene on a 4CN Ga site generates a Si-OH group close to Ga. However, 275 second Si-OH group is also present due to the original Ga site creation process (species 2 in Figure 276 277 4b). The close proximity of the two Si-OH groups leads to the possibility of a dehydration step, which gives an oxygen bridged Si pair and a water molecule. The free energy of dehydration is 278 reasonably negative when water is present at low pressures ($P_{water} = 10^{-9}$ atm, calculations included 279 in Supporting Information). The dehydration step can occur as soon as ethylene is activated, and 280 since the two Si-OH groups are removed, the proton transfer pathway, reforming the original 4CN 281 Ga site, would no longer be viable. As with the 3CN site, β -hydride transfer to ethylene would 282 then lead to C-A mechanism dominated by a Ga-ethyl species (see free energy diagram in 283 Supporting Information). 284



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Figure 5. (a) Free energy diagrams of ethylene oligomerization with β -hydride elimination compared to β -hydride transfer pathways on 3CN Ga sites (T = 523 K), (b) Free energy diagrams of ethylene oligomerization on 3CN and 4CN sites with dehydration, and (c) Schematics of ethylene oligomerization intermediates on a 3CN site (T = 523 K). The adsorption energies are referenced to Ga-ethyl species and appropriate amounts of gaseous ethylene molecules at 1 atm. The same species numbers are used in Figure 1.

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Figure 5b shows the energetics of the C-A oligomerization cycle on the two sites: 3CN, and the 4CN Ga with a dehydration step. Among them, the 3CN site generally exhibits a much more favorable energy landscape. Specifically, low activation barriers of both ethylene migratory insertion (3CN: 1.7 eV) and β -hydride transfer (3CN: 1.0 eV) are observed. On the 4CN dehydrated site, the ethylene physisorption steps before insertion and β -hydride transfer have positive changes in free energies (1.4 and 1.6 eV, respectively), leading to significantly higheroverall barriers of ethylene insertion.

294 Olefin oligomerization following Ga-hydride-centered Cossee-Arlman mechanism

As discussed above, a C-A mechanism can possibly be Ga-hydride-centered (region c, Fig. 295 1), and these sites could be produced through a hydrogen gas treatment.²⁴ To explore this 296 possibility, we have analyzed the free energy landscapes of the Ga-hydride-centered C-A 297 mechanism on both 3CN and 4CN sites (Figs. S5-7). High activation barriers are involved in the 298 β -hydride elimination steps (4CN: 2.5 eV, 3CN: 2.3 eV), and the alternative β -hydride transfer, 299 300 producing Ga-ethyl, exhibits much lower activation barriers. Further, high activation barriers of ethylene insertion are consistently observed for the 4CN sites (2.9 eV). Therefore, we predict that 301 the Ga-ethyl-centered C-A mechanism is the most favorable pathway on the Ga/SiO₂ system, and 302 the 3CN Ga sites exhibit a much higher turnover frequency than the 4CN ones. Hence, the 3CN 303 sites likely have a major effect on the overall reactivity of the catalyst. 304

305 *Microkinetic modeling*

Microkinetic modeling enables a direct comparison of the predicted rates and coverages of 306 distinct surface sites. We note that this information is not easily obtained through experiments, 307 308 given the site diversity in amorphous silica. Kinetic parameters are predicted from the free energy diagram of the 3CN site, and 10% of the Ga sites in the experimental loading are assumed to be 309 310 active. We only include the Ga-alkyl-centered C-A cycle because the DFT results have indicated 311 that other cycles will not contribute to the rate or selectivity. With a pure ethylene feed, a conversion of 0.5% is predicted at 523 K and a total pressure of 1 atm, and the turnover frequency 312 (TOF) is 5.7×10^{-3} s⁻¹ (with a dilute feed - 20% ethylene - an ethylene conversion of 1.4% is 313 obtained at 523 K and a total pressure of 1 atm, and a similar TOF, 3.2×10^{-3} s⁻¹, is observed). The 314

computational values are higher than the experimental value $(0.9 \times 10^{-3} \text{ s}^{-1})$. However, we highlight that the experimental values assume that all Ga sites are active, and hence this value is likely a lower limit on the true turnover frequency. Considering that Ga sites in the synthesized sample are, on average, four-coordinated, a relatively small percentage of 3CN sites are likely to be present in the sample and are responsible for the oligomerization chemistry. Indeed, we predict that the 4CN sites exhibit extremely low turnover frequencies due to the endothermic nature of ethylene physisorption steps, as well as a high barrier of ethylene insertion.

We also performed a degree of rate control (DRC) analysis to confirm our prediction of 322 323 rate-limiting step by evaluating the sensitivity of each elementary step to the overall turnover frequency. The DRC analysis has been performed on all steps in an ethylene oligomerization cycle, 324 leading to the conclusion that the ethylene migratory insertion step, having a DRC for 1-butene 325 formation of 0.95, is the rate-determining step. The turnover frequency is much less sensitive to 326 the β -hydride transfer step, whose DRC values are in the order of 10^{-2} . In the results of the dilute 327 feed, the most abundant surface intermediates (MASI) are physisorbed ethylene and Ga-n-butyl 328 species (coverages: 0.54 and 0.46, respectively). The results are consistent with the free energy 329 analysis, where the two species represent reasonable free energy wells. The physisorption step has 330 331 a negative free energy, and given a relatively high barrier of ethylene insertion, ethylene would accumulate before the elementary step occurs, leading to its higher coverage. Consistent results 332 333 are obtained using the pure feed, where the physisorbed ethylene on the Ga-ethyl species has an 334 even higher coverage (coverage: 0.99), and the ethylene insertion step remains the rate determining step (DRC: 0.94). Using a simplified rate expression by assuming ethylene insertion being rate-335 336 determining, an Arrhenius plot from microkinetic modeling is included in the Supporting 337 Information (Fig. S10), where the apparent activation energy from the free energy analysis is

reproduced. This further confirms that the other elementary steps can be treated as quasi-equilibration.

341 Conclusions

We present a first-principles study of ethylene oligomerization on single-site Ga³⁺ catalysts 342 supported on amorphous silica. Energetics of multiple oligomerization pathways are compared on 343 two representative sites: 3CN and 4CN Ga. Although the 4CN sites may in principle promote the 344 ethylene oligomerization cycle through a proton transfer cycle, they are not likely to be responsible 345 for experimentally observed reactivity due to a high ethylene insertion barrier. The 3CN Ga site, 346 however, yields a much more favorable energy landscape, which starts from a site activation 347 process to form a Ga-alkyl species, followed by a Ga-alkyl-centered Cossee-Arlman mechanism. 348 349 With a lower termination barrier than the ethylene insertion step, the 3CN Ga sites favor selective ethylene oligomerization to short oligomers, consistent with the experimental results at 250 °C and 350 1 atm. Microkinetic modeling results confirm that the ethylene insertion step is rate-limiting. 351 Further, we note that the in the transition state of the facile β -hydride transfer step, an unusual 352 geometry is found for the main group Ga catalyst, where the hydrogen being transferred does not 353 interact with Ga center. This study highlights the capability of a oxide-supported main group 354 metals to perform olefin oligomerization and also provides suggestions to design such catalysts, 355 where the local coordination environment of Ga sites may be tuned to improve the catalyst activity. 356 357

358	Supporting Information
359	This material contains detailed free energy information of the analyzed reaction mechanisms,
360	kinetic calculation details, entropy calculations, Ga site schematics, and Arrhenius plots.
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272	
372	Notes
372	Notes The authors declare no competing financial interest.
372 373 374	Notes The authors declare no competing financial interest. Acknowledgments
372 373 374 375	Notes The authors declare no competing financial interest. Acknowledgments This paper is based upon work supported in part by the National Science Foundation through the
372 373 374 375 376	Notes The authors declare no competing financial interest. Acknowledgments This paper is based upon work supported in part by the National Science Foundation through the Center for Innovative and Sustained Transformation of Alkane Resources (CISTAR) under
372 373 374 375 376 377	Notes The authors declare no competing financial interest. Acknowledgments This paper is based upon work supported in part by the National Science Foundation through the Center for Innovative and Sustained Transformation of Alkane Resources (CISTAR) under Cooperative Agreement No. EEC-1647722. Use of the Center for Nanoscale Materials, an Office

- of Basic Energy Sciences, under Contract No. DE-AC02-06CH11357. Use of the National Energy
- Research Scientific Computing Center is also gratefully acknowledged. Y.X. and J.G. would like
- to thank Prof. Brandon C. Bukowski at Johns Hopkins University and Dr. Junnan Shangguan at
- 382 UC Berkeley for insightful discussions.

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