Crystal Structure of the Intermediate $Na_2V_2(PO_4)_3$ Phase and Electrochemical Reaction Mechanisms in $Na_xV_2(PO_4)_3$ (1 \leq x \leq 4) System

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Abstract

The Na-superionic-conductor (NASICON) Na₃V₂(PO₄)₃ is an important positive electrode material for Na-ion batteries. Here, we investigate the mechanisms of phase transition in $Na_xV_2(PO_4)_3$ (1 $\leq x \leq 4$) upon a non-equilibrium battery cycling. Unlike the widely believed two-phase reaction in $Na_3V_2(PO_4)_3 - Na_1V_2(PO_4)_3$ system, we determine a new intermediate Na₂V₂(PO₄)₃ phase using operando synchrotron X-ray diffraction. Density functional theory calculations further support the existence of the Na₂V₂(PO₄)₃ phase. We propose for the first time two possible crystal structures of Na₂V₂(PO₄)₃ analyzed by Rietveld refinement. The two structure models with the space groups $P2_1/c$ or P2/c for the new intermediate Na₂V₂(PO₄)₃ phase show similar unit cell parameters but different atomic arrangements, including a vanadium charge ordering. As the appearance of the intermediate Na₂V₂(PO₄)₃ phase is accompanied by symmetry reduction, Na(1) and Na(2) sites split into several positions in Na₂V₂(PO₄)₃, in which one of the splitting Na(2) position is found to be a vacancy whereas the Na(1) positions are almost fully filled. The intermediate Na₂V₂(PO₄)₃ phase reduces the lattice mismatch between Na₃V₂(PO₄)₃ and Na₁V₂(PO₄)₃ phases facilitating a fast phase transition. This work paves the way for a better understanding of great rate capabilities of Na₃V₂(PO₄)₃.

Keywords: crystal structure, Na₂V₂(PO₄)₃, phase transition, intermediate phase, metastable, non-equilibrium, operando X-ray diffraction, density functional theory calculations

Introduction

Na-superionic-conductor (NASICON) structured materials are considered as promising electrodes for sodium-ion batteries because of their 3D open-framework crystal structure, resulting in high cyclability and fast rate capability. 1-5 Among them, Na₃V₂(PO₄)₃ has been extensively studied, showing satisfactory energy density and rate performance as well as good thermal stability. 6-13 The crystal structure of Na₃V₂(PO₄)₃ is composed of repeating units called lanterns, into which two VO₆ octahedra are joined together through three corner-sharing PO₄ tetrahedra. Within the 3D framework generated by these lanterns, two crystallographic sodium sites, labeled Na(1) and Na(2), are usually reported. The Na(1) site is located between the lantern units along the [001]_{hexagonal} direction and is surrounded by six oxygen atoms in its first coordination sphere and by six Na(2) atoms in its second one. At maximum, the Na(1) and Na(2) sites (of different multiplicities) can respectively generate one and three Na positions per formula unit, thus leading to the final stoichiometry Na₄V₂(PO₄)₃. During electrochemical reactions, although the Na(1) site is involved in the global Na-ion transport mechanism (Na(2) – Na(1) – Na(2) pathways), it tends to be almost fully occupied regardless of the total Na content into the material, whereas the Na(2) site is partially/fully emptied or filled depending on the compositions.^{8,9,14–16}

It is well known that two Na⁺ ions can be reversibly electrochemically extracted from a Na₃V₂(PO₄)₃ electrode, through a voltage-composition "plateau" at ~3.4 V (vs. Na⁺/Na) utilizing the V^{4+/3+} redox couple (with a theoretical capacity of 117.6 mAh/g).^{13,17–22} The reaction has been described by many authors as a mechanism of two-phase reaction between Na₃V₂³⁺(PO₄)₃ and Na₁V₂⁴⁺(PO₄)₃.^{13,17–22} Additionally, one Na⁺ ion can be inserted into Na₃V₂(PO₄)₃ at ~1.6 V (vs. Na⁺/Na) through the V^{3+/2+} redox couple towards the Na₄V₂(PO₄)₃ composition (theoretical capacity of 58.8 mAh/g).^{18,19,22–27} Recently, Zakharkin et al.²⁰ noticed the signature of an intermediate Na₂V₂(PO₄)₃ phase, which involves the V^{4+/3+} redox couple. Nevertheless, no structural information on the intermediate phase was provided. Other previous reports also suggested the existence of Na₂V₂(PO₄)₃, but the authors barely contemplated the existence of a new intermediate phase.^{18,19} This suggests

that the widely believed two-phase reaction between $Na_3V_2(PO_4)_3$ and $Na_1V_2(PO_4)_3$ needs to be reinvestigated, in particular, providing structural information and the origin of the appearance of the intermediate $Na_2V_2(PO_4)_3$ phase.

Here, we elucidate the mechanisms of phase transition of the $Na_3V_2(PO_4)_3 - Na_1V_2(PO_4)_3$ system including the intermediate $Na_2V_2(PO_4)_3$ phase, utilizing $V^{4+/3+}$ redox couple. We also investigate the $Na_3V_2(PO_4)_3 - Na_4V_2(PO_4)_3$ system involving the $V^{3+/2+}$ redox couple. The intermediate $Na_2V_2(PO_4)_3$ phase was detected by *operando* X-ray synchrotron diffraction as well as predicted by theoretical calculations. Here, we report for the first time on the crystal structure of the $Na_2V_2(PO_4)_3$ phase, compared in detail with those of $Na_xV_2(PO_4)_3$ (x = 1, 3, 4). The intermediate $Na_2V_2(PO_4)_3$ phase appears as reducing the lattice mismatch between $Na_3V_2(PO_4)_3$ and $Na_1V_2(PO_4)_3$ phases, and as the Na(1) and Na(2) sites split into several positions with different Na^+ distributions, including vacancies. This study is highly relevant to better understand the behavior of fast-rate electrode materials that display transient phases, such as the intermediate Li_xFePO_4 phases (x = 0.6–0.75) detected during non-equilibrium battery operations.^{28–36}

Experimental

Synthesis: The carbon-coated Na₃V₂(PO₄)₃ was prepared by a sol-gel-assisted solid-state reaction. Na₂CO₃ (Sigma-Aldrich, 99.5 %), $C_{10}H_{14}O_5V$ (Sigma-Aldrich, 97%), NH₄H₂PO₄ (Sigma-Aldrich, 98.5 %), and citric acid (Alfa Aesar, 99 %) in a molar ratio of 1.5:2:3:2, were dissolved in deionized water and ethanol (50/50 by volume). The solution was stirred overnight at 80 °C in an oil bath before being dried in oven. The obtained powder was ground and pre-heated at 400 °C for 4 h in Ar. The resulting powder was then mixed in a mortar and annealed at 700 °C for 10 h under Ar/H₂ (95/5) atmosphere.

Material Characterization: The chemical composition of the synthesized material was quantified using inductively coupled plasma-optical emission spectroscopy (ICP-OES) with a Varian Model 720-ES spectrometer. The amount of carbon coating on the synthesized

material was measured by thermogravimetric analyses (TGA) with a NETZSCH STA 449C. The morphology of the powder was examined by scanning electron microscopy (SEM) with a Hitachi Model S-4500 microscope.

Operando Synchrotron X-ray Diffraction: Operando synchrotron X-ray powder diffraction (SXRPD) measurements were performed on the MSPD beamline of the ALBA synchrotron in Spain³⁷ with Debye–Scherrer geometry (λ=0.8266 Å) using an *in situ* coin cell with glass windows. Prior to the operando measurements, the SXRPD pattern of the pristine $Na_3V_2(PO_4)_3$ was collected with a 0.3 mm diameter capillary. Two in situ cells containing Na₃V₂(PO₄)₃ electrodes were measured at the same time thanks to the eight-cells holder with an automatic positioning system available at the MSPD beamline.³⁸ Each SXRPD pattern was collected every 30 minutes with an acquisition time of ~3.5 minutes in the 2θ angular range of 2–40°, with a 2θ step size of 0.006° using a MYTHEN detector for rapid pattern collection. The working electrodes were composed of the Na₃V₂(PO₄)₃ powder and carbon black (80/20 in wt%), and Na metal was used as counter/reference electrode. The mass loadings of the active material in the electrodes were 5.33 and 6.12 mg, respectively. One sheet of Whatman glass fiber (GF/D) was used as a separator and the electrolyte was composed of 1 M NaPF₆ in ethylene carbonate (EC) / dimethyl carbonate (DMC) (1:1, w/w) with 2 wt.% of fluoroethylene carbonate (FEC). The first cell was measured for one cycle with a slow electrochemical reaction rate of 0.11 C (1 C = 58.2 mA/g, or about 9 h for the exchange of 1Na⁺ / 1e⁻) with a voltage window of 1 –3.75 V versus Na⁺/Na. The second cell was measured for six cycles with higher C-rates (i.e., 0.37-0.77-0.77-0.37-0.77 C). A large overpotential was observed during the measurements of the second cell, hence the voltage windows were adjusted with the respected C-rates (detailed cycling conditions can be found in Table S1 in the supporting information section).

Density Functional Theory Calculations: To assess the thermodynamic stability of $Na_xV_2(PO_4)_3$ with distinct Na-vacancy orderings at 0 K, we used the spin-polarized density functional theory (DFT), as implemented in VASP.^{39,40} The exchange-correlation was approximated by the strongly constrained and appropriately normed (SCAN) meta-

generalized gradient approximation functional,⁴¹ with a U correction of 1.0 eV on all vanadium atoms to improve the localization of 3d electrons.⁴² The total energies were converged to within 10^{-5} eV/cell, atomic forces (stresses) within 10^{-2} eV/Å (0.29 GPa). The $1^{\rm st}$ Brillouin zone was integrated over a Γ -centered k-point grid of $3 \times 3 \times 3$ for all primitive structures containing 2 formula units (f.u.) with 42 atoms, a $1 \times 3 \times 3$ k-point mesh for all supercells with 4 f.u. (84 atoms), and a $1 \times 1 \times 3$ mesh for 8 f.u. (168 atoms). The valence electrons were treated in terms of plane-waves up to an energy cutoff of 520 eV, while projector augmented wave potentials were used to describe the core electrons,⁴³ with Na $3s^1$, V_pv $3p^63d^44s^1$, P $2s^23p^3$, O $2s^22p^4$.

The average intercalation voltage was derived using **Eq. 1**.

$$V = -\frac{\Delta G^{0}}{yF} \approx -\frac{E(Na_{x+y}V_{2}(PO_{4})_{3}) - [E(Na_{x}V_{2}(PO_{4})_{3}) + y\mu_{Na}]}{yF}$$
(1)

where ΔG^0 is the change of Gibbs free energy, as approximated from our DFT total energies, which ignore the zero-point energy correction, the pV term, and entropic effects. Thus, $E\left(\mathrm{Na}_{x+y}\mathrm{V}_2(\mathrm{PO}_4)_3\right)$, $E\left(\mathrm{Na}_x\mathrm{V}_2(\mathrm{PO}_4)_3\right)$ and μ_{Na} are the DFT total energies of stable Navacancy orderings at compositions x and x+y, and the Na chemical potential of Na metal, respectively. F is the Faraday constant. Mixing enthalpies (H_{mixing}) at different Na compositions, to construct the 0 K phase diagram were defined in **Eq. 2**.

$$H_{mixing}(x) \approx E[\text{Na}_{x}\text{V}_{2}(\text{PO}_{4})_{3}] - \left(\frac{4-x}{3}\right)E[\text{Na}_{1}\text{V}_{2}(\text{PO}_{4})_{3}] - \left(\frac{x-1}{3}\right)E[\text{Na}_{4}\text{V}_{2}(\text{PO}_{4})_{3}]$$
(2)

Results and Discussion

The composition of the as-synthesized $Na_3V_2(PO_4)_3$ powder was determined by elemental analysis using ICP-OES. The Na/V/P ratio was found to be 3.03(2):1.97(3):2.99(6), suggesting that the target composition $Na_3V_2(PO_4)_3$ was achieved through the sol-gel-assisted solid-state reaction. SEM images of the $Na_3V_2(PO_4)_3$ powder (**Figure S1**) show that the particles have no particular shapes as similar to other studies. ^{11-13,17-22} However, relatively large agglomerates ranging from few microns to several tenths of microns were found with the primary particles in the size of a few hundreds of nanometers. The powder is carbon-coated on the surface, ca. 9 wt% of carbon as determined by TGA measurements in air, shown in **Figure S2**.

The SXRPD pattern of the as-synthesized Na₃V₂(PO₄)₃ powder is shown in **Figure 1**. No impurity phases were detected based on the XRD analysis. As previously reported,⁴⁴ at room temperature the crystal structure of Na₃V₂(PO₄)₃ cannot be indexed using a rhombohedral (R3c) cell, but a monoclinic distortion must be considered. This is illustrated by the splitting of the (116)_{rhombohedral} reflection at $d_{hkl} \sim 2.8 \text{ Å}$ into (-511)_{monoclinic}, (-422)_{monoclinic}, and (-313)_{monoclinic}, which are signatures of the monoclinic distortion (inset images of Figure 1). Depending on the thermal history of the sample, Na₃V₂(PO₄)₃ can crystallize either in the monoclinic α or β form at room temperature (the reversible phase transition occurring very close to room temperature with about 10° of hysteresis). 44 In the present study, the crystal structure was refined with the monoclinic β phase since the (111) reflection at 6.74° (λ =0.8266 Å) was not observed, while it is allowed in the α (i.e., Na⁺ ordered) phase, as shown in **Figure S3**. The refined cell parameters using the Rietveld method are a=15.4104(4)Å, b=8.7288(2) Å, c=8.8257(2) Å, θ =126.1202(17) °, and V/Z=239.75(2) Å³ with the space group C2/c. The weak unindexed satellite reflections at low angles are attributed to an incommensurate modulated structure. These modulations originate both from the occupancies and the positions of Na⁺ ions in Na₃V₂(PO₄)₃. No detailed structural study of the incommensurate β phase has been reported yet and thus the SXRPD pattern was refined without modulation vectors.

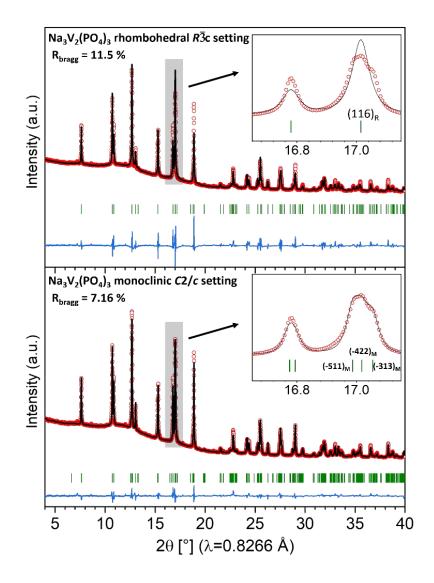


Figure 1. Rietveld refinement results of the as-synthesized Na₃V₂(PO₄)₃ powder with (top) the space group *R*3*c* and (bottom) the space group *C*/2*c*. The corresponding SXRPD pattern was collected at 298 K. It clearly shows that the structure of Na₃V₂(PO₄)₃ contains a monoclinic distortion as, for instance, (116)_R reflection splits into (-511)_M, (-422)_M, and (-313)_M (R and M here stand for rhombohedral and monoclinic, respectively).

To study the (de-)intercalated phases and the Na⁺ insertion/extraction mechanisms in Na₃V₂(PO₄)₃, operando SXRPD measurements were performed. **Figure 2a** displays a 2D view of the SXRPD of a selected 2 θ range during the first electrochemical charge-discharge cycle together with the corresponding galvanostatic data measured within a voltage window of 1.0-3.75 V (vs. Na⁺/Na) at a C-rate of ~0.11 C (for wider 2 θ range, see **Figure S4**). A total number of 89 scans were recorded during the first cycle. From scan number 1 to 30,

Na₃V₂(PO₄)₃ is first oxidized up to 3.75 V vs. Na⁺/Na. During the charge process, two Na⁺ cations are extracted leading to the composition Na₁V₂(PO₄)₃. Close to the mid-charge (i.e., after approximatively 10h of cycling) a weak reflection at $2\theta \approx 7.7^{\circ}$ starts to appear together with the presence of Na₃V₂(PO₄)₃ (corresponding reflection at $2\theta \approx 7.63^{\circ}$) and Na₁V₂(PO₄)₃ (corresponding reflection at $2\theta \approx 7.85^{\circ}$). Na₁V₂(PO₄)₃ is then reduced back to Na₃V₂(PO₄)₃ (scan number 60) and further to Na₄V₂(PO₄)₃ (scan number 89) at a potential of ~1 V vs. Na⁺/Na. During the discharge process, the very same peak at $2\theta \approx 7.7^{\circ}$ re-appears with an increased intensity. This new reflection that is attributed to the new intermediate Na₂V₂(PO₄)₃ phase can be more clearly seen in the selected SXRPD patterns (scan number 40-60) of **Figure 2b**. The appearance of the Na₂V₂(PO₄)₃ phase indicates that the electrochemical mechanisms of Na⁺ insertion/extraction in Na₃V₂(PO₄)₃, involving the V^{4+/3+} redox couple at ~3.4 V (vs. Na⁺/Na), are different from what has been reported before. ^{13,17-} ²²

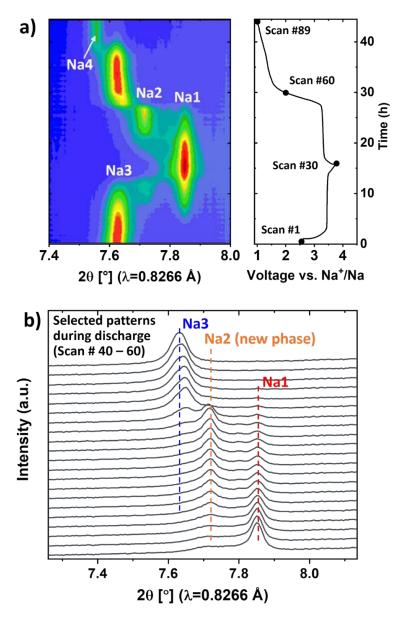


Figure 2. a) Operando SXRPD patterns using Na₃V₂(PO₄)₃ as positive electrode material in a half cell versus Na metal upon charge and discharge, with a voltage window of 1.0 − 3.75 V vs. Na⁺/Na at a Crate of 0.11 C (≈1 Na⁺ in 9 h). b) Selected SXRPD patterns (from scan number 40-60 during discharge), where the intermediate Na₂V₂(PO₄)₃ phase appears more clearly. Na_x (x = 1, 2, and 3) refers to Na_xV₂(PO₄)₃.

The intermediate $Na_2V_2(PO_4)_3$ phase tended to coexist with the $Na_3V_2(PO_4)_3$ and $Na_1V_2(PO_4)_3$ phases at low C-rate (0.11 C). However, when a higher current density was applied (i.e., towards a non-equilibrium state), the $Na_2V_2(PO_4)_3$ phase became more isolated. Similarly, in the operando study of LiFePO₄, a higher C-rate (1 C to 10 C) allowed a more intense appearance of the intermediate Li_xFePO_4 phase.³⁰ Even though the C-rates used in this study

were relatively low, the battery cells already reached a non-equilibrium condition. This is probably because (i) the $Na_3V_2(PO_4)_3$ powder contains relatively large particles (see **Figure S1**); and (ii) the electrodes without binder can induce a higher overpotential.⁴⁵ This is further confirmed by the observation of the large polarization of ~150 mV using the *in situ* cell compared to a low polarization of 30 mV observed using a normal coin cell, cycled at the same C-rate of 0.11 C (**Figure S5**). **Figure S6** shows *operando* SXRPD data collected during six cycles with the C-rates of 0.37-0.77-0.77-0.77-0.37-0.77 C (which are about three to seven times higher current densities than 0.11 C). To increase the chance of isolating a 'pure' $Na_2V_2(PO_4)_3$ phase, multiple cycles were measured. The SXRPD pattern which appears mostly composed by the $Na_2V_2(PO_4)_3$ phase was obtained during the last cycle (see **Figure S6** for more details).

Figure 3 shows a comparison of the SXRPD patterns among the $Na_xV_2(PO_4)_3$ (x = 1, 2, and 3) compositions. Importantly, a careful evaluation of the SXRPD pattern of $Na_2V_2(PO_4)_3$ reveals the appearance of weak Bragg peak at a very low 20 angle (~ 3.85°, d_{hkl} = 12.29 Å). With *operando* technic, this weak Bragg peak at such a low angle (equivalent to ~7.2° in $Cu_{K\alpha}$ radiation) may be missed with a standard laboratory X-ray equipment, while we clearly observed it with a synchrotron X-ray source. This provides critical information to solve the crystal structure of $Na_2V_2(PO_4)_3$.

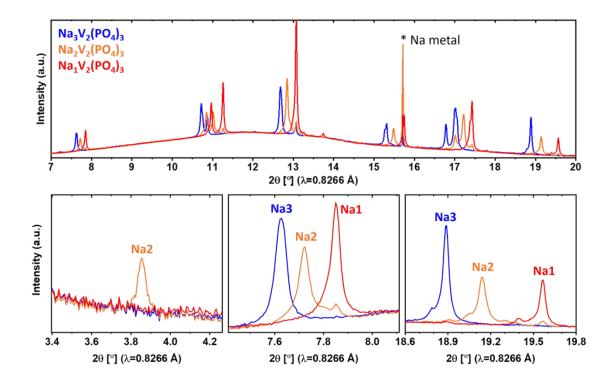


Figure 3. The SXRPD patterns of $Na_3V_2(PO_4)_3$ (blue), $Na_2V_2(PO_4)_3$ (orange), and $Na_1V_2(PO_4)_3$ (red) with different angular domains. The Bragg peak at 3.85 ° is only observed for the new $Na_2V_2(PO_4)_3$ phase. The overall positions of the Bragg peaks manifest the appearance of the intermediate phase which can be differentiated from $Na_3V_2(PO_4)_3$ and $Na_1V_2(PO_4)_3$ phases.

The powder pattern of $Na_2V_2(PO_4)_3$ presented in **Figure 3** was then used to solve its crystal structure. The indexing of the powder pattern, the space group determination, and the cell transformation with group-subgroup relationships were carried out using Dicvol,⁴⁶ Chekcell,⁴⁷ and POWDERCELL⁴⁸ software, to fully resolve the crystal structure of $Na_2V_2(PO_4)_3$. During the steps of indexing and space group determination, it was found that the reflection at $2\theta = 3.85^{\circ}$ excludes the rhombohedral lattices (**Figure S7**) as well as *C*-centered monoclinic-type cells (**Figure S8**). Possible space groups are then primitive, and thus several structure models with different space groups were examined to solve the structure. The initial atomic positions of each model were deduced from the group-subgroup relationships starting from the *R3c* rhombohedral cell. The highest to lowest symmetry of the examined space groups are $P2_1/c$, P2/c, $P2_1/m$, and P/m (corresponding to 22, 23, 42, and 46 independent atoms per cell, respectively). We attempted unsuccessfully to solve the structure using the two space groups ($P2_1/m$, and P/m). The structure model, namely "Model 1", using the $P2_1/c$ space group showed slightly better results than that

using a *P*2/*c* space group (i.e., Model 2). The detailed comparisons between Models 1 and 2 are discussed later in this paper.

For the structure of Na₂V₂(PO₄)₃ using the space group $P2_1/c$ (Model 1), the refined cell parameters are: α =15.2377(5) Å, b = 8.6082(5) Å, c = 8.7391(4) Å, θ = 126.281(3), V/Z= 231.02(2) Å³. The results of Rietveld refinement are presented in Figure 4a, illustrating that the reflection at $2\theta = 3.85^{\circ}$ can be fully explained. The final refinement was performed using Na₃V₂(PO₄)₃ and Na₁V₂(PO₄)₃ as secondary phases with final weight fractions of 8.4(5) and 7.1(3) %, respectively. The global structural information, including atomic coordinates, atomic displacement parameters, and occupancy factors, are listed in Table 1. The crystal structure of Na₂V₂(PO₄)₃ contains two different vanadium Wyckoff positions, V(1a) and V(1b), involved in the same lantern unit as illustrated in Figure 4b. From the examination of the V-O bond distances (**Table S2**), it appears that the environment of both V(1a) and V(1b) are similar with an average V-O bond distance of 1.99(9) Å, which suggests that V3+ and V4+ are randomly distributed over the V(1a) and V(1b) positions. For the Na crystallographic sites, the Na(1) and Na(2) sites split into two Na(1) (labeled Na(1a) and Na(1b)) and three Na(2) positions (labeled Na(2a₁), Na(2a₂), and Na(2b)) in the space group P2₁/c. The refined occupancy factor for Na(2a₂) position was 0.08(7), which can be considered as fully empty. The refined occupancy factors for Na(1a), Na(1b), Na(2a₁), and Na(2b) are 1, 0.98(8), 0.36(7), and 0.73(10), respectively, yielding a composition $Na_{2.1(3)}V_2(PO_4)_3$.

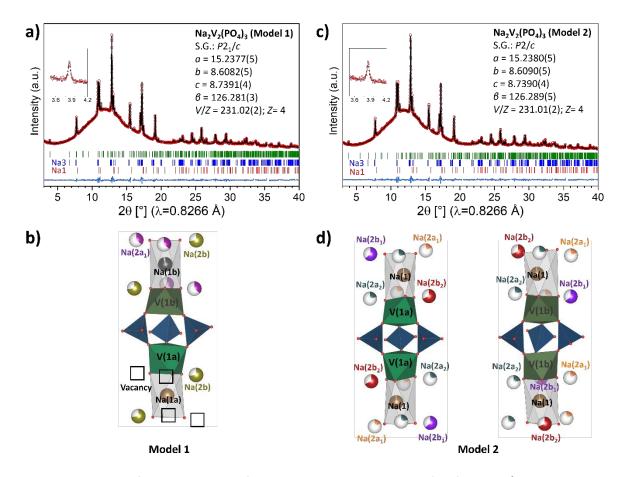


Figure 4. Rietveld refinement results of the intermediate phase Na₂V₂(PO₄)₃ using a) the space group P2₁/c (Model 1) and b) the space group P2/c (Model 2). c) Lantern unit with adjacent Na⁺ ions in the crystal structure of Na₂V₂(PO₄)₃, refined with the space group P2₁/c. V(1a) and V(1b) atoms are involved in a single lantern unit. Vacant Na⁺ positions are shown as empty squares. d) Lantern units with adjacent Na⁺ ions in the crystal structure of Na₂V₂(PO₄)₃, refined with the space group P2/c. Two different lantern units exist in the structure: each vanadium position forms a distinct lantern unit.

We tested another structural model for Na₂V₂(PO₄)₃ using the space group P2/c (Model 2), which showed similar agreement factors with the following cell parameters: a = 15.2380(5) Å; b = 8.6090(5) Å; c = 8.7390(4); b = 126.289(5), b = 126.289(5)

Na(2b₂). The refined occupancy factors for Na(1), Na(2a₁), Na(2a₂), Na(2b₁), and Na(2b₂) are 0.98(3), 0.17(7), 0.21(7), 0.63(11), and 0.68(11), respectively, yielding a composition Na_{2.0(3)}V₂(PO₄)₃. Detailed structural information is listed in **Table S3**.

Table 1. Refined structural parameters of the intermediate phase $Na_2V_2(PO_4)_3$ using the space group $P2_1/c$ (Model 1). ^aRefined and fixed at the last stages of refinement.

$Na_2V_2(PO_4)_3$

Space group: $P2_1/c$ (#14); Z =4 a =15.2377(5) Å; b = 8.6082(5) Å; c = 8.7391(4); θ = 126.281(3); V= 924.069(8) ų; V/Z= 231.02(2) ų R_{wp} = 13.3 %; R_{p} = 19.5 %; R_{bragg} = 6.21 %

Atom	Wyckoff position	x/a	y/b	z/c	Uiso, Ų	Occ.
V(1a)	4e	0.848(2)	0.492(5)	0.630(4)	0.026(3)	1
V(1b)	4e	0.640(2)	0.493(5)	0.834(4)	0.026(3)	1
P(1a)	4e	0.1047(10)	0.3521(17)	0.958(2)	0.033(4)	1
P(1b)	4e	0.3965(10)	0.3581(17)	0.564(2)	0.033(4)	1
P(2)	4e	0.2572(10)	0.7725(14)	0.262(2)	0.033(4)	1
O(1b)	4e	0.397(7)	0.372(10)	0.389(7)	0.012(3)	1
O(1d)	4e	0.094(7)	0.423(7)	0.107(10)	0.012(3)	1
O(1e)	4e	0.338(5)	0.700(10)	0.230(10)	0.012(3)	1
O(2b)	4e	0.208(6)	0.637(5)	0.303(10)	0.012(3)	1
O(2c)	4e	0.706(5)	0.916(10)	0.960(14)	0.012(3)	1
O(2f)	4e	0.805(5)	0.926(10)	0.547(14)	0.012(3)	1
O(1a)	4e	0.398(7)	0.319(2)	0.081(14)	0.012(3)	1
O(1c)	4e	0.104(7)	0.325(2)	0.478(10)	0.012(3)	1
O(1f)	4e	0.004(5)	0.085(10)	0.270(7)	0.012(3)	1
O(2a)	4e	0.506(5)	0.083(10)	0.240(7)	0.012(3)	1
O(2d)	4e	0.331(7)	0.614(10)	0.927(10)	0.012(3)	1
O(2e)	4e	0.167(6)	0.639(10)	0.582(7)	0.012(3)	1
Na(1a)	2a	0	0	0	0.090(13)	1 ^a
Na(1b)	2d	0.5	0	0.5	0.090(13)	0.98(8)
Na(2a₁)	4e	0.557 ^a	0.168ª	0.908°	0.090(13)	0.36(7)
Na(2a ₂)	4e	0.936	0.169	0.565	0.090(13)	O ^a
Na(2b)	4e	0.232(7)	0.140(14)	0.243(14)	0.090(13)	0.73(10)

Note that both monoclinic structural models for $Na_2V_2(PO_4)_3$ (P2/c and $P2_1/c$) have very similar cell parameters and can fully account for the existence of the (100) reflection at $2\theta = 3.85^{\circ}$. However, subtle differences to distinguish between the two space groups are convoluted in the possible existence of [(0k0), k=2n+1] reflections for P2/c while they are forbidden for $P2_1/c$. A very low-intensity peak at ~5.5° (of the SXRPD pattern) could be assigned to the (010) reflection in the space group P2/c, although the same was also observed in $Na_3V_2(PO_4)_3$ and $Na_1V_2(PO_4)_3$ phases with the same intensity. This evidence suggests this peak may not originate from the phase reflection of $Na_xV_2(PO_4)_3$ but it is rather a noisy background (**Figure S9**). For this reason, we believe that the $P2_1/c$ model (Model 1) is more suitable, although the P2/c one (Model 2) cannot be completely excluded.

To shed light on the thermodynamic stability of the intermediate $Na_2V_2(PO_4)_3$ phase, detected with our SXRPD diffraction, we performed dedicated DFT calculations. **Figure 5** shows the thermodynamic properties of $Na_xV_2(PO_4)_3$ in the region of x = 1 - 3 at 0 K, as computed by DFT. **Figure 5a** shows the DFT mixing enthalpies (H_{mixing} in **eq. 2**) for all Na/vacancy orderings of the $Na_xV_2(PO_4)_3$ compositions. Using a convex hull minimization algorithm, all the ground-state configurations were obtained. It can be concluded that besides the endmembers $Na_1V_2(PO_4)_3$ and $Na_3V_2(PO_4)_3$, which are assigned to rhombohedral and monoclinic symmetry, respectively, a new phase $Na_2V_2(PO_4)_3$ appears as a stable configuration. However, $Na_2V_2(PO_4)_3$ shows a relatively low mixing enthalpy (ca. -23 meV/f.u.) with respect to $Na_1V_2(PO_4)_3$ and $Na_3V_2(PO_4)_3$, and this suggests that the intermediate phase may be metastable at room temperature.

Table 2. Unit cell parameters, Na occupancy factors, and average of V-O distances of Na₂V₂(PO₄)₃ obtained by DFT calculations.

	s.g.	а	b	с	α	β	γ	V/Z	Na(1) /f.u.	Na(2) /f.u.	Total Na /f.u.	Avg. V-O (Å)
Na ₂ V ₂ (PO ₄) ₃	P 1	8.712	8.667	8.629	59.729	58.858	59.602	227.159	1	1	2	1.964

Table 2 presents unit cell parameters, sodium occupancy factors, and the average of V-O distances of the $Na_2V_2(PO_4)_3$ structure obtained by DFT calculations. The computed

structure of Na₂V₂(PO₄)₃ shows a similar cell volume with the experimentally observed one, and this calculated phase is assigned to a triclinic symmetry P1 with distinguished V4+ and V³⁺ states, and with fully ordered Na(1) and Na(2) sites. Higher temperatures will enable other Na-vacancy ordering to be stable, with intrinsic symmetries maybe similar to what was found experimentally. Therefore, the structures extracted from the synchrotron measurements can be assumed with a superposition of several Na-vacancy orderings. A closer look to the local arrangement of Na ions in the DFT structure of Na₂V₂(PO₄)₃ shows that fully occupied Na(1) site is surrounded by two fully occupied Na(2) sites and four vacancies.⁴⁹ Consequently, we could observe unique Na⁺ sites of the Na₂V₂(PO₄)₃ groundstate predicted by DFT split into a larger number of distinct Wyckoff positions compared to what elaborated by our experimental Model 1 and 2. However, our room-temperature synchrotron data of the intermediate Na₂V₂(PO₄)₃ structure detected under non-equilibrium conditions will likely incorporate several possible Na-vacancy configurations, averaging out the Na ions among the available Na(1) and Na(2) sites, which can be the origin of the observed fractional occupancies from SXRPD. 44,50 Furthermore, our DFT calculations suggest a specific vanadium charge orderings within the ground-state Na₂V₂(PO₄)₃, which may be disrupted by temperature effects. Ongoing synthesis efforts to obtain Na₂V₂(PO₄)₃ chemically as a pure phase will further clarify the discrepancies between the DFT data and our experimental models.

Figure 5b depicts the DFT-derived voltage profile in the region of $Na_1V_2(PO_4)_3$ to $Na_3V_2(PO_4)_3$. By identifying the $Na_2V_2(PO_4)_3$ phase, we could realize two voltage plateaus while Na^+ intercalation via biphasic reaction mechanisms, namely 3.29 V vs. Na^+/Na between $Na_1V_2(PO_4)_3$ and $Na_2V_2(PO_4)_3$, and 3.24 V vs. Na^+/Na between $Na_2V_2(PO_4)_3$ and $Na_3V_2(PO_4)_3$. Notably, the Na ordering of $Na_2V_2(PO_4)_3$ give rise to a small voltage step (~50 mV).

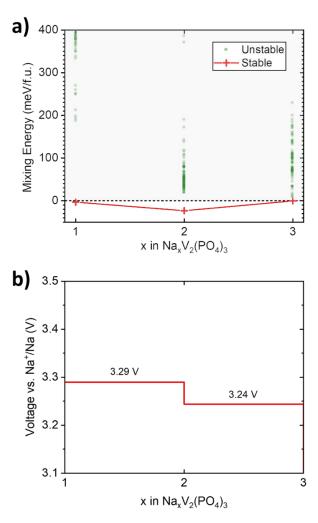


Figure 5. a) DFT-derived phase diagram in the composition range (1 ≤ x ≤ 3) for Na_xV₂(PO₄)₃ at 0 K, in terms of Na mixing enthalpies. The stable ground-state configurations, namely Na₁V₂(PO₄)₃, Na₁V₂(PO₄)₃ and Na₃V₂(PO₄)₃, and the unstable configurations are represented by red cross and green dots, respectively.
 b) The computed voltage profile from Na₁V₂(PO₄)₃ to Na₃V₂(PO₄)₃.

Having the crystal structures of the new $Na_2V_2(PO_4)_3$ phase determined (with the space group $P2_1/c$), the *operando* SXRPD data (shown in **Figure 2**) were analyzed by Rietveld refinements including the evolutions of phase transitions, cell volumes, and phase weights as shown in **Figure 6**. Five different regions can be distinguished during the charge and discharge processes (labeled from I to V) in **Figure 6**. In region I (solid solution part), only $Na_{3-\delta}V_2(PO_4)_3$ is present and its unit cell volume (V/Z) slightly decreases from 239.687(6) Å³ to 239.384(8) Å³. Region II (plateau at 3.4 V vs. Na^+/Na) can be divided into two sub-regions (II' and II''). The Na^+ extraction mechanism occurs first through an out-of-equilibrium "three-phase" reaction, where the amount of $Na_3V_2(PO_4)_3$ phase decreases while those of

 $Na_1V_2(PO_4)_3$ and $Na_2V_2(PO_4)_3$ phases increase concomitantly up to mid-charge (region II'). This can be rationalized as the overlap of two biphasic reactions of $Na_3V_2(PO_4)_3$ – $Na_2V_2(PO_4)_3$ and $Na_2V_2(PO_4)_3$ – $Na_1V_2(PO_4)_3$. We note that the two reactions tend to separate more when higher current densities are furnished (**Figure S6**). After that (in region II'' of **Figure 6**), the quantities of $Na_2V_2(PO_4)_3$ and $Na_3V_2(PO_4)_3$ phases diminish, while the $Na_1V_2(PO_4)_3$ content keeps increasing until the end of charge at ~3.75 V vs. Na^+/Na . The discharge process down to ~2 V vs. Na^+/Na appears rather different (region III). On the plateau, the main reaction seems to occur between $Na_1V_2(PO_4)_3$ and $Na_2V_2(PO_4)_3$ via a two-phase reaction. At this stage, the amount of $Na_3V_2(PO_4)_3$ remains low (< 10 wt%). Afterwards, in region IV, the phase transition from $Na_2V_2(PO_4)_3$ to $Na_3V_2(PO_4)_3$ occurred rapidly. Finally, in region V (reduction down to 1 V vs. Na^+/Na), a biphasic reaction between $Na_3V_2(PO_4)_3$ and $Na_4V_2(PO_4)_3$ is observed.

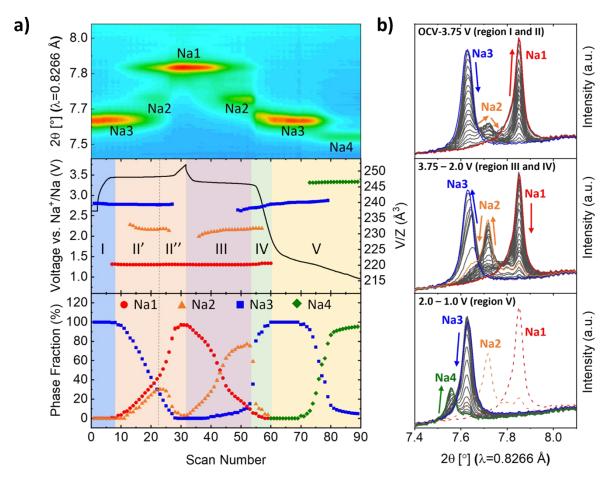


Figure 6. a) Counter plot of o*perando* SXRPD patterns in the 7.46-8.03° angular range (top). Voltage profile of $Na_3V_2(PO_4)_3$ during the first cycle and V/Z evolution of the $Na_xV_2(PO_4)_3$ (x = 1, 2, 3, and 4) phases (middle). The corresponding phase weights (bottom). **b)** Details of the SXRPD patterns, upon

Na⁺ extraction from Na₃V₂(PO₄)₃ to Na₁V₂(PO₄)₃, (top), upon Na⁺ re-insertion from Na₁V₂(PO₄)₃ to Na₃V₂(PO₄)₃ (middle), and upon one additional Na⁺ insertion from Na₃V₂(PO₄)₃ to Na₄V₂(PO₄)₃ (bottom). Na_x (x = 1, 2, 3, and 4) refers to Na_xV₂(PO₄)₃.

When the pristine $Na_3V_2(PO_4)_3$ phase re-appears during discharge, the reaction mainly occurs through a two-phase reaction mechanism but a slight peak-shift to lower angles (**Figure 6b**) and an increase of V/Z were observed, which indicates that a partial solid solution mechanism is also involved. This behavior is typically observed in $Na_3V_2(PO_4)_3^{17-22}$ and other electrode materials, such as, $Na_3Al_{0.5}V_{1.5}(PO_4)_3$, $Na_4MnCr(PO_4)_3$, $Na_2TiV(PO_4)_3$, $Na_2TiV(PO_4)_3$, and $Na_2TiV(PO_4)_3$, which involve a two-phase reaction mechanism upon cycling. When multiple phase boundaries are possibly observed between two end-members, leading to strains, slight changes in cell parameters can occur as a signature of these strains. $Na_2V_2(PO_4)_3$ is maintained after the re-sodiation, implying that the overall electrochemical reaction is highly reversible.

From the phase fraction analysis, it is clear that the $Na_2V_2(PO_4)_3$ phase could not be observed as completely isolated but rather coexisting together with the $Na_1V_2(PO_4)_3$ and $Na_3V_2(PO_4)_3$ ones. The maximum phase fraction of the $Na_2V_2(PO_4)_3$ phase observed during charge was of 30.1(8) wt% while it reached 77(1) wt% during discharge. The asymmetric behaviors in the appearance of the intermediate phase during charge and discharge were also observed in other studies of $Na_3V_2(PO_4)_3^{18-20}$ and of LiFePO $_4^{30,32,35,36}$. The intermediate phases of $Na_xV_2(PO_4)_3$ and Li_xFePO_4 are more visible during charge in some cases $^{18-20,30,36}$ and during discharge in other cases 20,32,35 . Zakharkin *et al.* investigated three different synthesis routes for preparing $Na_3V_2(PO_4)_3$ with different precursors resulting in different intensities of the XRD reflections of the $Na_2V_2(PO_4)_3$ intermediate phase. 20 Depending on the synthesis procedures, the $Na_2V_2(PO_4)_3$ phase was either not observed, or observed only during charge, or observed during both charge and discharge. 20 These observations may suggest that the intermediate phase could be metastable/transient. Further investigations are required to understand the origin of the asymmetric behavior of the $Na_2V_2(PO_4)_3$ intermediate phase in the $Na_3V_2(PO_4)_3 - Na_1V_2(PO_4)_3$ system.

A global overview of cell parameters, Na site occupancies, and average of V-O bond lengths of Na_xV₂(PO₄)₃ (x = 1, 2, 3, and 4) is summarized in **Table 3**. For the monoclinic phases, Na₃V₂(PO₄)₃ and Na₂V₂(PO₄)₃, the a, b, and c parameters decrease by ~1.1, 1.38, and 0.97 %, respectively, and a slight increase in the θ angle (0.14 %) is noticed from x = 3 to 2 in Na_xV₂(PO₄)₃. The two end members (Na₄V₂(PO₄)₃ and Na₁V₂(PO₄)₃) crystalize in the same space group R3c. From the Na-rich phase, Na₄V₂(PO₄)₃, to the Na-poor one, Na₁V₂(PO₄)₃, the a parameter dramatically decreases from 8.94302(10) to 8.42631(12) Å ($\Delta a/a$ = -5.81 %) while the c parameter slightly increases from 21.3609(4) to 21.4772(6) Å ($\Delta c/c$ = 0.54 %). This noticeable anisotropy in the change of cell parameters is closely linked to the occupancies of the Na(1) and Na(2) sites.

Table 3. Unit cell parameters, Na occupancy factors, and average V-O distances for the compositions $Na_xV_2(PO_4)_3$, (x = 1, 2, 3, and 4) obtained by Rietveld refinement. See the profiles of the Rietveld refinements for $Na_xV_2(PO_4)_3$ (x = 1, 3, and 4) in **Figures S10-S12**, and the details of their structural information in **Table S4-S6**.

5	S.G.	а	В	С	β	V/Z	Na(1) /f.u.	Na(2) /f.u.	Total Na /f.u.	Avg. V-O (Å)
Na ₄ V ₂ (PO ₄) ₃	R3c 8	.94302(10)	8.94302(10)	21.3609(4)	120	246.585(7)	0.97(4)	2.77(7)	3.74(11)	2.078(14)
Na ₃ V ₂ (PO ₄) ₃ (C2/c 1	15.4065(3)	8.7288(2)	8.8243(2)	126.1091(16)	239.682(10)	0.679(14)	2.27(8)	2.9(1)	2.02(4)
Na ₂ V ₂ (PO ₄) ₃ P	2 ₁ /c 1	15.2377(5)	8.6082(5)	8.7391(4)	126.281(3)	231.02(2)	0.98(4)	1.2(3)	2.2(3)	1.99(9)
Na ₁ V ₂ (PO ₄) ₃	R3c 8	.42631(12)	8.42631(12)	21.4772(6)	120	220.105(8)	0.96(4)	0	0.96(4)	1.91(2)

Generally, Na⁺ insertion in the NASICON structure increases the a parameter and decreases the c parameter (in hexagonal axes). When the Na(1) site is depopulated, the c parameter increases mainly due to an increasing repulsion between parallel O₃ triangular faces of the MO₆ octahedra through the Na(1) site, as less screened by the Na⁺ ions. ^{15,52,55–57}

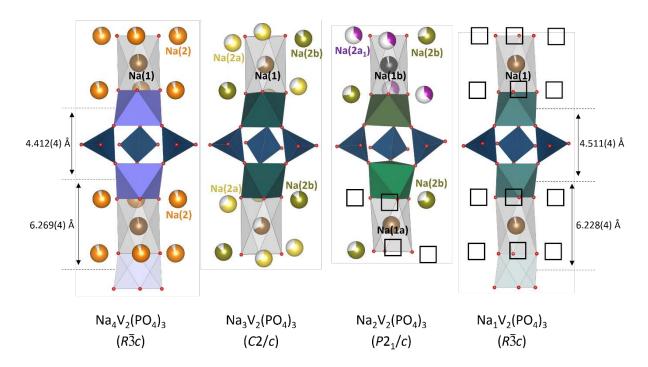


Figure 7. Illustration of the lantern units with adjacent Na ions of the compositions $Na_xV_2(PO_4)_3$ (x = 1, 2, 3, and 4). Black squares represent Na vacancies. The distances shown in $Na_4V_2(PO_4)_3$ and $Na_1V_2(PO_4)_3$ indicate V–V distances either through the Na(1) site or within the lantern unit.

In the case of Na_xV₂(PO₄)₃, the distances between adjacent VO₆ octahedra through the Na(1) site along [001]_{hexagonal} remain nearly constant, 6.269(4) Å in Na₄V₂(PO₄)₃ and 6.228(4) Å in Na₁V₂(PO₄)₃, (**Figure 7**), as the Na(1) site stays fully occupied (0.96(4) \rightarrow 0.97(4) when x varies from 4 to 1 in Na_xV₂(PO₄)₃). As a consequence, the c parameter undergoes no significant variation. The main reason for the slight increase in the c parameter may be the stronger repulsion of neighboring between VO₆ octahedra within the lantern unit when vanadium is oxidized from V^{2.5+} to V⁴⁺. Therefore, the V-V distances within the lantern unit themselves increase from 4.412(4) to 4.511(4) Å (**Figure 7**). Similar evolutions of the a and c cell parameters were found in other NASICON positive electrode materials but with a more pronounced increase of the c parameter: $\Delta a/a = -6.1$ % and $\Delta c/c = 2.4$ % in Na_xMnV(PO₄)₃, ¹⁵ and $\Delta a/a = -4.9$ % and $\Delta c/c = 2.2$ % in Na_xMnCr(PO₄)₃, ⁵² when x varies from 4 to 1. Unlike the case of Na_xV₂(PO₄)₃, a much depopulated Na(1) site is observed in Na_xMnV(PO₄)₃ (from 1 to 0.49(1) when x varies from 4 to 1) inducing stronger repulsions between the (Mn,V)O₆ octahedra through the Na(1) site, and thus a remarkable increase of the c parameter. ^{15,55}

Overall, the value of V/Z gradually decreases with a decreasing number of Na⁺ ions in the structure (driving a progressive oxidation of vanadium), from 246.585(7), 239.682(10), 231.02(2), and to 220.105(8) Å³ when x varies from 4 to 1 in Na_xV₂(PO₄)₃. The lattice mismatch in the phase transition between Na₃V₂(PO₄)₃ and Na₁V₂(PO₄)₃ ($\Delta V/V = 8.2$ %) is noticeably reduced when Na₂V₂(PO₄)₃ is invoked ($\Delta V/V = 3.6$, and 4.7 %, for Na₃V₂(PO₄)₃ \rightarrow Na₂V₂(PO₄)₃, and Na₂V₂(PO₄)₃ \rightarrow Na₁V₂(PO₄)₃, respectively). The reduced lattice mismatch enables a rapid phase transition between Na₃V₂(PO₄)₃ and Na₁V₂(PO₄)₃ via Na₂V₂(PO₄)₃ by lowering their nucleation energies.³⁰

The average V-O bond distances consequently show a gradual decrease from 2.076(14), to 2.02(4), to 1.99(9), and to 1.91(2) Å when x in Na_xV₂(PO₄)₃ changes from 4 to 1. The details of (not average but individual) V-O bond distances in Na_xV₂(PO₄)₃ are shown in **Table S2**. Also, the volumes of the VO₆ octahedra decrease in parallel from 11.69, to 10.73, to 10.16, and to 9.15 Å³, respectively ($\Delta V_{\text{oct}}/V_{\text{oct}}$ = 21.7 %). As a comparison, the volume of the (Mn,V)O₆ octahedra decreases about 23.8 % when x varies from 4 to 1 in Na_xMnV(PO₄)₃. ¹⁵ Furthermore, as x in Na_xV₂(PO₄)₃ decreases from 4 to 1, the average oxidation states of vanadium obtained by BVS calculation are 2.44(4), 2.92(11), 3.3(3) and 3.87(8), respectively, showing a good agreement with the average vanadium oxidation states expected for each composition (i.e., 2.5, 3, 3.5, and 4, respectively).

When it comes to the number of Na⁺ in the Na(1) and Na(2) sites per formula unit (**Table 3**), our findings establish that the Na(1) site is almost fully occupied in all compositions except for Na₃V₂(PO₄)₃ as the occupancy factor of Na(1) site is 0.679(14). For the Na(2) site, when the Na⁺ content changes from x=4 to 1 in Na_xV₂(PO₄)₃, the occupancy factor gradually decreases from almost 100 % down to \sim 0 %. This evidence appears in good agreement with the computational analysis on Na(1) and Na(2) sites at room temperature.⁴⁹ Other NASICON-type materials also show similar trends, i.e. the Na(1) site tends to keep its high occupancies while the Na(2) site is populated or depopulated depending on the compositions.^{8,9,14–16} Overall, the refined total number of Na⁺ per formula unit shows very good agreement with the expected compositions.

The detailed evolution on the Na⁺ distributions around the lantern units of the four compositions ($Na_xV_2(PO_4)_3$, with x=1, 2, 3, and 4) is illustrated in **Figure 7**. The Na(2) site in $Na_4V_2(PO_4)_3$ (R3c) splits into the two Na(2) positions, Na(2a) and Na(2b), in $Na_3V_2(PO_4)_3$ (C2/c). Then, from Na₃V₂(PO₄)₃ to Na₂V₂(PO₄)₃ $(P2_1/c)$, the Na(1) site splits into the Na(1a) and Na(1b) positions that are almost fully occupied in Na₂V₂(PO₄)₃. The Na(2a) position also further splits into Na($2a_1$) and Na($2a_2$) in Na₂V₂(PO₄)₃, but the Na($2a_2$) is found to be empty. Finally, from $Na_2V_2(PO_4)_3$ to $Na_1V_2(PO_4)_3$, the structure is back to rhombohedral unit cell (R3c), having the Na(2) site fully emptied. It is interesting that from Na₄V₂(PO₄)₃ to Na₂V₂(PO₄)₃, the Na(2b) position tends to be more occupied than the Na(2a) positions. This may be related to different connectivities of Na(2a) and Na(2b) with the Na(1) site. Figure 8 shows the polyhedra constructed from Na and O atoms in Na₃V₂(PO₄)₃ or Na₂V₂(PO₄)₃. The connectivity between Na(2a) and Na(1) forms distinct 2D Na⁺ diffusion paths parallel to the (100) plane, while the connectivity between Na(2b) and Na(1) results in 1D Na⁺ diffusion chains along the [101] direction. This suggests that Na⁺ ions in Na(2a) position may show easier migration than those in Na(2b) position, and therefore explaining the lower occupancy factor observed for Na(2a) than Na(2b).

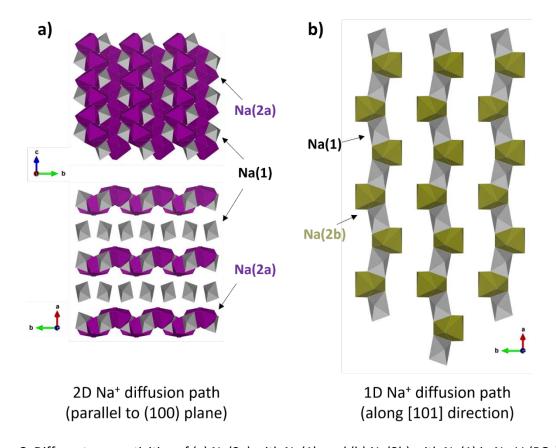


Figure 8. Different connectivities of (a) Na(2a) with Na(1), and (b) Na(2b) with Na(1) in Na₃V₂(PO₄)₃ or Na₂V₂(PO₄)₃. The polyhedra are constructed from Na and O atoms.

Conclusions

In this study, we report for the first time the crystal chemistry of the new intermediate $Na_2V_2(PO_4)_3$ composition as well as the electrochemical reaction mechanisms of $Na_xV_2(PO_4)_3$ ($1 \le x \le 4$) including the intermediate phase. The appearance of the $Na_2V_2(PO_4)_3$ phase occurs in a non-equilibrium battery operation and it is better observed with a higher current density (i.e., non-equilibrium state). The results of Rietveld refinement suggest that the crystal structure of $Na_2V_2(PO_4)_3$ crystalizes in a primitive (monoclinic) cell with the possible space groups of $P2_1/c$ (Model 1) or P2/c (Model 2) rather than rhombohedral (R3c) or monoclinic (C2/c) cells of other $Na_xV_2(PO_4)_3$ (x = 1, 3, and 4) compositions. The main difference between the two structure models proposed for $Na_2V_2(PO_4)_3$ is ascribed to different vanadium environments. As a symmetry is reduced in the $Na_2V_2(PO_4)_3$, the vanadium site splits into two Wyckoff positions. The structure with the space group $P2_1/c$

(Model 1) contains a single lantern unit with a random distribution of V³⁺ and V⁴⁺ types over two vanadium positions. The structure with the space group P2/c (Model 2) contains two different lantern units, each vanadium position forming its own lantern unit, with a possible charge ordering between V3+ and V4+. For the sodium sites, the Na(1) site is almost fully occupied for both structure models. The Na(2) site splits into several positions, in which one of the splitting Na(2) position [Na(2a₂)] is found to be a vacancy in the structure Model 1 whereas the four splitting Na(2) positions are all partially filled in the structure Model 2. The structure independently predicted by our DFT simulations at 0 K also shows a vanadium charge ordering as well as a full Na⁺/vacancy ordering. A fully ordered Na⁺ at 0 K becomes partially ordered at room temperature. These different Na⁺ distributions suggest that the Na₂V₂(PO₄)₃ phase can have possible phase transitions versus temperature due to Na⁺ order/disorder phenomena. Furthermore, Na⁺ ions in Na(2a) position can diffuse more easily than those in Na(2b) position due to different connectivities with Na(1) site. The intermediate Na₂V₂(PO₄)₃ phase appears by reducing the lattice mismatch between Na₃V₂(PO₄)₃ and Na₁V₂(PO₄)₃ phases lowering their nucleation energy thus beneficial for a high-rate performance. This study opens the door to a better understanding of the behavior of Na₃V₂(PO₄)₃ electrode upon cycling when the intermediate phase is involved. We believe our findings in this work will encourage researchers to further investigate the nature of the new $Na_2V_2(PO_4)_3$ phase.

Supporting Information

SEM images, TGA, synchrotron powder XRD patterns, *operando* XRD data, and detailed crystallographic information

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References

- (1) Masquelier, C.; Croguennec, L. Polyanionic (Phosphates, Silicates, Sulfates) Frameworks as Electrode Materials for Rechargeable Li (or Na) Batteries. *Chem. Rev.* **2013**, *113* (8), 6552–6591. https://doi.org/10.1021/cr3001862.
- (2) Hasa, I.; Mariyappan, S.; Saurel, D.; Adelhelm, P.; Koposov, A. Y.; Masquelier, C.; Croguennec, L.; Casas-Cabanas, M. Challenges of Today for Na-Based Batteries of the Future: From Materials to Cell Metrics. *J. Power Sources* **2021**, *482* (August 2020), 228872. https://doi.org/10.1016/j.jpowsour.2020.228872.
- (3) Jian, Z.; Hu, Y. S.; Ji, X.; Chen, W. NASICON-Structured Materials for Energy Storage. *Adv. Mater.* **2017**, *29* (20), 1–16. https://doi.org/10.1002/adma.201601925.
- (4) Chen, S.; Wu, C.; Shen, L.; Zhu, C.; Huang, Y.; Xi, K.; Maier, J.; Yu, Y. Challenges and Perspectives for NASICON-Type Electrode Materials for Advanced Sodium-Ion Batteries. *Adv. Mater.* **2017**, *29* (48), 1–21. https://doi.org/10.1002/adma.201700431.
- (5) Rajagopalan, R.; Zhang, Z.; Tang, Y.; Jia, C.; Ji, X.; Wang, H. Understanding Crystal Structures, Ion Diffusion Mechanisms and Sodium Storage Behaviors of NASICON Materials. *Energy Storage Mater.* 2021, 34 (May 2020), 171–193. https://doi.org/10.1016/j.ensm.2020.09.007.
- (6) Singh, B.; Wang, Z.; Park, S.; Gautam, G. S.; Chotard, J. N.; Croguennec, L.; Carlier, D.; Cheetham, A. K.; Masquelier, C.; Canepa, P. A Chemical Map of NaSICON Electrode Materials for Sodium-Ion Batteries. *J. Mater. Chem. A* 2021, 9 (1), 281–292. https://doi.org/10.1039/d0ta10688g.
- (7) Zhang, B.; Ma, K.; Lv, X.; Shi, K.; Wang, Y.; Nian, Z.; Li, Y.; Wang, L.; Dai, L.; He, Z. Recent Advances of NASICON-Na₃V₂(PO₄)₃ as Cathode for Sodium-Ion Batteries: Synthesis, Modifications, and Perspectives. *J. Alloys Compd.* **2021**, *867*, 159060. https://doi.org/10.1016/j.jallcom.2021.159060.
- (8) Bui, K. M.; Dinh, V. A.; Okada, S.; Ohno, T. Hybrid Functional Study of the NASICON-Type Na₃V₂(PO₄)₃: Crystal and Electronic Structures, and Polaron-Na Vacancy Complex Diffusion. *Phys. Chem. Chem. Phys.* **2015**, *17* (45), 30433–30439. https://doi.org/10.1039/c5cp05323d.
- (9) Song, W.; Cao, X.; Wu, Z.; Chen, J.; Huangfu, K.; Wang, X.; Huang, Y.; Ji, X. A Study into

- the Extracted Ion Number for NASICON Structured $Na_3V_2(PO_4)_3$ in Sodium-Ion Batteries. *Phys. Chem. Chem. Phys.* **2014**, *16* (33), 17681–17687. https://doi.org/10.1039/c4cp01821d.
- (10) Saravanan, K.; Mason, C. W.; Rudola, A.; Wong, K. H.; Balaya, P. The First Report on Excellent Cycling Stability and Superior Rate Capability of Na₃V₂(PO₄)₃ for Sodium Ion Batteries. *Adv. Energy Mater.* **2013**, *3* (4), 444–450. https://doi.org/10.1002/aenm.201200803.
- (11) Zheng, Q.; Yi, H.; Li, X.; Zhang, H. Progress and Prospect for NASICON-Type Na₃V₂(PO₄)₃ for Electrochemical Energy Storage. *J. Energy Chem.* **2018**, *27* (6), 1597–1617. https://doi.org/10.1016/j.jechem.2018.05.001.
- (12) Zhang, X.; Rui, X.; Chen, D.; Tan, H.; Yang, D.; Huang, S.; Yu, Y. Na₃V₂(PO₄)₃: An Advanced Cathode for Sodium-Ion Batteries. *Nanoscale* **2019**, *11* (6), 2556–2576. https://doi.org/10.1039/c8nr09391a.
- (13) Lim, S. Y.; Kim, H.; Shakoor, R. A.; Jung, Y.; Choi, J. W. Electrochemical and Thermal Properties of NASICON Structured Na₃V₂(PO₄)₃ as a Sodium Rechargeable Battery Cathode: A Combined Experimental and Theoretical Study . *J. Electrochem. Soc.* **2012**, 159 (9), A1393–A1397. https://doi.org/10.1149/2.015209jes.
- (14) Kabbour, H.; Coillot, D.; Colmont, M.; Masquelier, C.; Mentré, O. α-Na₃M₂(PO₄)₃ (M = Ti, Fe): Absolute Cationic Ordering in NASICON-Type Phases. *J. Am. Chem. Soc.* **2011**, 133 (31), 11900–11903. https://doi.org/10.1021/ja204321y.
- (15) Chen, F.; Kovrugin, V. M.; David, R.; Mentré, O.; Fauth, F.; Chotard, J.-N.; Masquelier,
 C. A NASICON-Type Positive Electrode for Na Batteries with High Energy Density:
 Na₄MnV(PO₄)₃ . Small Methods 2018, 1800218, 1800218.
 https://doi.org/10.1002/smtd.201800218.
- (16) Wang, Q.; Zhang, M.; Zhou, C.; Chen, Y. Concerted Ion-Exchange Mechanism for Sodium Diffusion and Its Promotion in Na₃V₂(PO₄)₃ Framework. *J. Phys. Chem. C* 2018, 122 (29), 16649–16654. https://doi.org/10.1021/acs.jpcc.8b06120.
- (17) Zhang, G.; Xiong, T.; Yan, M.; Xu, Y.; Ren, W.; Xu, X.; Wei, Q.; Mai, L. In Operando Probing of Sodium-Incorporation in NASICON Nanomaterial: Asymmetric Reaction and Electrochemical Phase Diagram. *Chem. Mater.* **2017**, *29* (19), 8057–8064.

- https://doi.org/10.1021/acs.chemmater.7b00957.
- (18) Yao, X.; Zhu, Z.; Li, Q.; Wang, X.; Xu, X.; Meng, J.; Ren, W.; Zhang, X.; Huang, Y.; Mai, L. 3.0 v High Energy Density Symmetric Sodium-Ion Battery: Na₄V₂(PO₄)₃ II Na₃V₂(PO₄)₃. ACS Appl. Mater. Interfaces 2018, 10 (12), 10022–10028. https://doi.org/10.1021/acsami.7b16901.
- (19) Wei, C.; Luo, F.; Zhang, C.; Gao, H.; Niu, J.; Ma, W.; Bai, Y.; Zhang, Z. Voltage Window-Dependent Electrochemical Performance and Reaction Mechanisms of Na₃V₂(PO₄)₃ Cathode for High-Capacity Sodium Ion Batteries. *Ionics (Kiel).* **2020**, *26* (5), 2343–2351. https://doi.org/10.1007/s11581-019-03363-0.
- (20) Zakharkin, M. V; Drozhzhin, O. A.; Ryazantsev, S. V; Chernyshov, D.; Kirsanova, M. A.; Mikheev, I. V; Pazhetnov, E. M.; Antipov, E. V; Stevenson, K. J. Electrochemical Properties and Evolution of the Phase Transformation Behavior in the NASICON-type Na_{3+x}Mn_xV_{2-x}(PO₄)₃ (0≤x≤1) Cathodes for Na-Ion Batteries. *J. Power Sources* 2020, 470 (February), 228231. https://doi.org/10.1016/j.jpowsour.2020.228231.
- (21) Jian, Z.; Han, W.; Lu, X.; Yang, H.; Hu, Y. S.; Zhou, J.; Zhou, Z.; Li, J.; Chen, W.; Chen, D.; et al. Superior Electrochemical Performance and Storage Mechanism of Na₃V₂(PO₄)₃ Cathode for Room-Temperature Sodium-Ion Batteries. *Adv. Energy Mater.* **2013**, *3* (2), 156–160. https://doi.org/10.1002/aenm.201200558.
- (22) Mirza, S.; Song, Z.; Zhang, H.; Hussain, A.; Zhang, H.; Li, X. A Simple Pre-Sodiation Strategy to Improve the Performance and Energy Density of Sodium Ion Batteries with Na₃V₂(PO₄)₃ as the Cathode Material. *J. Mater. Chem. A* **2020**, *8* (44), 23368–23375. https://doi.org/10.1039/d0ta08186h.
- (23) UEBOU, Y.; KIYABU, T.; OKADA, S.; YAMAKI, J. Electrochemical Sodium Insertion into the 3D-Framework of Na₃M₂(PO₄)₃ (M=Fe, V). *reports Inst. Adv. Mater. Study Kyushu Univ.* **2002**, *16*, 1–5.
- (24) Li, G.; Jiang, D.; Wang, H.; Lan, X.; Zhong, H.; Jiang, Y. Glucose-Assisted Synthesis of Na₃V₂(PO₄)₃/C Composite as an Electrode Material for High-Performance Sodium-Ion Batteries. *J. Power Sources* **2014**, *265*, 325–334. https://doi.org/10.1016/j.jpowsour.2014.04.054.

- (25) Lim, S. J.; Han, D. W.; Nam, D. H.; Hong, K. S.; Eom, J. Y.; Ryu, W. H.; Kwon, H. S. Structural Enhancement of Na₃V₂(PO₄)₃/C Composite Cathode Materials by Pillar Ion Doping for High Power and Long Cycle Life Sodium-Ion Batteries. *J. Mater. Chem. A* **2014**, *2* (46), 19623–19632. https://doi.org/10.1039/c4ta03948c.
- (26) Jian, Z.; Sun, Y.; Ji, X. A New Low-Voltage Plateau of Na₃V₂(PO₄)₃ as an Anode for Nalon Batteries. *Chem. Commun.* **2015**, *51* (29), 6381–6383. https://doi.org/10.1039/c5cc00944h.
- (27) Jian, Z.; Zhao, L.; Pan, H.; Hu, Y. S.; Li, H.; Chen, W.; Chen, L. Carbon Coated Na₃V₂(PO₄)₃ as Novel Electrode Material for Sodium Ion Batteries. *Electrochem. commun.* **2012**, *14* (1), 86–89. https://doi.org/10.1016/j.elecom.2011.11.009.
- (28) Delacourt, C.; Poizot, P.; Tarascon, J. M.; Masquelier, C. The Existence of a Temperature-Driven Solid Solution in Li_x FePO₄ for $0 \le x \le 1$. *Nat. Mater.* **2005**, *4* (3), 254–260. https://doi.org/10.1038/nmat1335.
- (29) Malik, R.; Zhou, F.; Ceder, G. Kinetics of Non-Equilibrium Lithium Incorporation in LiFePO₄. *Nat. Mater.* **2011**, *10* (8), 587–590. https://doi.org/10.1038/nmat3065.
- (30) Orikasa, Y.; Maeda, T.; Koyama, Y.; Murayama, H.; Fukuda, K.; Tanida, H.; Arai, H.; Matsubara, E.; Uchimoto, Y.; Ogumi, Z. Direct Observation of a Metastable Crystal Phase of Li_xFePO₄ under Electrochemical Phase Transition. *J. Am. Chem. Soc.* **2013**, *135* (15), 5497–5500. https://doi.org/10.1021/ja312527x.
- (31) Orikasa, Y.; Maeda, T.; Koyama, Y.; Murayama, H.; Fukuda, K.; Tanida, H.; Arai, H.; Matsubara, E.; Uchimoto, Y.; Ogumi, Z. Transient Phase Change in Two Phase Reaction between LiFePO₄ and FePO₄ under Battery Operation. *Chem. Mater.* **2013**, 25 (7), 1032–1039. https://doi.org/10.1021/cm303411t.
- (32) Hao Liu, Fiona C. Strobridge, Olaf J. Borkiewicz, Kamila M. Wiaderek, Karena W. Chapman, Peter J. Chupas, C. P. G. Capturing Metastable Structures during High-Rate Cycling of LiFePO₄ Nanoparticle Electrodes. *Science (80-.).* **2014**, *344* (6191), 1451–1452. https://doi.org/10.1126/science.1255819.
- (33) Nishimura, S. I.; Natsui, R.; Yamada, A. Superstructure in the Metastable Intermediate-Phase Li_{2/3}FePO₄ Accelerating the Lithium Battery Cathode Reaction.

 Angew. Chemie Int. Ed. 2015, 54 (31), 8939–8942.

- https://doi.org/10.1002/anie.201501165.
- (34) Lu, J.; Oyama, G.; Nishimura, S. I.; Yamada, A. Increased Conductivity in the Metastable Intermediate in Li_xFePO₄ Electrode. *Chem. Mater.* **2016**, *28* (4), 1101–1106. https://doi.org/10.1021/acs.chemmater.5b04508.
- (35) Takahashi, I.; Mori, T.; Yoshinari, T.; Orikasa, Y.; Koyama, Y.; Murayama, H.; Fukuda, K.; Hatano, M.; Arai, H.; Uchimoto, Y.; et al. Irreversible Phase Transition between LiFePO₄ and FePO₄ during High-Rate Charge-Discharge Reaction by Operando X-Ray Diffraction. *J. Power Sources* **2016**, *309*, 122–126. https://doi.org/10.1016/j.jpowsour.2016.01.077.
- (36) Yoshinari, T.; Mori, T.; Otani, K.; Munesada, T.; Yamamoto, K.; Uchiyama, T.; Fukuda, K.; Koyama, Y.; Hagiwara, R.; Orikasa, Y.; et al. Quantitative Elucidation of the Non-Equilibrium Phase Transition in LiFePO₄ via the Intermediate Phase. *Chem. Mater.* **2019**, *31* (18), 7160–7166. https://doi.org/10.1021/acs.chemmater.9b00834.
- (37) Fauth, F.; Peral, I.; Popescu, C.; Knapp, M. The New Material Science Powder Diffraction Beamline at ALBA Synchrotron. *Powder Diffr.* **2013**, *28* (September), S360–S370.
- (38) Herklotz, M.; Weiß, J.; Ahrens, E.; Yavuz, M.; Mereacre, L.; Kiziltas-Yavuz, N.; Dräger, C.; Ehrenberg, H.; Eckert, J.; Fauth, F.; et al. A Novel High-Throughput Setup for in Situ Powder Diffraction on Coin Cell Batteries. *J. Appl. Crystallogr.* **2016**, *49*, 340–345. https://doi.org/10.1107/S1600576715022165.
- (39) Kresse, G.; Furthmüller, J. Efficiency of Ab-Initio Total Energy Calculations for Metals and Semiconductors Using a Plane-Wave Basis Set. *Comput. Mater. Sci.* **1996**, *6* (1), 15–50. https://doi.org/10.1016/0927-0256(96)00008-0.
- (40) Vargas-Hernández, R. A. Bayesian Optimization for Calibrating and Selecting Hybrid-Density Functional Models. *J. Phys. Chem. A* **2020**, *124* (20), 4053–4061. https://doi.org/10.1021/acs.jpca.0c01375.
- (41) Sun, J.; Ruzsinszky, A.; Perdew, J. Strongly Constrained and Appropriately Normed Semilocal Density Functional. *Phys. Rev. Lett.* **2015**, *115* (3). https://doi.org/10.1103/PhysRevLett.115.036402.
- (42) Long, O. Y.; Sai Gautam, G.; Carter, E. A. Evaluating Optimal U for 3d Transition-Metal

- Oxides within the SCAN+ U Framework. *Phys. Rev. Mater.* **2020**, *4* (4), 1–15. https://doi.org/10.1103/PhysRevMaterials.4.045401.
- (43) Joubert, D. From Ultrasoft Pseudopotentials to the Projector Augmented-Wave Method. *Phys. Rev. B Condens. Matter Mater. Phys.* **1999**, *59* (3), 1758–1775. https://doi.org/10.1103/PhysRevB.59.1758.
- (44) Chotard, J.-N.; Rousse, G.; David, R.; Mentré, O.; Courty, M.; Masquelier, C. Discovery of a Sodium-Ordered Form of Na₃V₂(PO₄)₃ below Ambient Temperature . *Chem. Mater.* **2015**, *27* (17), 5982–5987. https://doi.org/10.1021/acs.chemmater.5b02092.
- (45) Saurel, D.; Pendashteh, A.; Jáuregui, M.; Reynaud, M.; Fehse, M.; Galceran, M.; Casas-Cabanas, M. Experimental Considerations for Operando Metal-Ion Battery Monitoring Using X-ray Techniques . *Chemistry–Methods* 2021, 1 (6), 249–260. https://doi.org/10.1002/cmtd.202100009.
- (46) Boultif, A.; Louër, D. Powder Pattern Indexing with the Dichotomy Method. *J. Appl. Crystallogr.* **2004**, *37* (5), 724–731. https://doi.org/10.1107/S0021889804014876.
- (47) Laugier, J. and Bochu, B. CHEKCELL. "LMGP-Suite Suite of Programs for the interpretation of X-ray. Experiments," (ENSP/ Laboratoire des Matériaux et du Génie Physique, BP 46. 38042, Saint Martin d'Hères, France). 2002, http://www.inpg.fr/LMGP and http://www.ccp14.ac.uk/tutorial/lmgp/
- (48) Kraus, W.; Nolze, G. POWDER CELL A Program for the Representation and Manipulation of Crystal Structures and Calculation of the Resulting X-Ray Powder Patterns. J. Appl. Crystallogr. 1996, 29 (3), 301–303. https://doi.org/10.1107/S0021889895014920.
- (49) Wang, Z.; Park, S.; Deng, Z.; Carlier, D.; Chotard, J.-N.; Croguennec, L.; Gautam, G. S.; Cheetham, A. K.; Masquelier, C.; Canepa, P. Phase Stability and Sodium-Vacancy Orderings in a NaSICON Electrode. **2021**.
- (50) Park, S.; Chotard, J. N.; Carlier, D.; Moog, I.; Courty, M.; Duttine, M.; Fauth, F.; Iadecola, A.; Croguennec, L.; Masquelier, C. Crystal Structures and Local Environments of NASICON-Type Na₃FeV(PO₄)₃ and Na₄FeV(PO₄)₃ positive Electrode Materials for Nalon Batteries. *Chem. Mater.* **2021**, *33* (13), 5355–5367. https://doi.org/10.1021/acs.chemmater.1c01457.

- (51) Lalère, F.; Seznec, V.; Courty, M.; David, R.; Chotard, J. N.; Masquelier, C. Improving the Energy Density of Na₃V₂(PO₄)₃-Based Positive Electrodes through V/Al Substitution. *J. Mater. Chem. A* **2015**, *3* (31), 16198–16205. https://doi.org/10.1039/c5ta03528g.
- (52) Wang, J.; Wang, Y.; Seo, D. H.; Shi, T.; Chen, S.; Tian, Y.; Kim, H.; Ceder, G. A High-Energy NASICON-Type Cathode Material for Na-Ion Batteries-Supporiting. *Adv. Energy Mater.* **2020**, *10* (10). https://doi.org/10.1002/aenm.201903968.
- (53) Lalère, F.; Seznec, V.; Courty, M.; Chotard, J. N.; Masquelier, C. Coupled X-Ray Diffraction and Electrochemical Studies of the Mixed Ti/V-Containing NASICON: Na₂TiV(PO₄)₃. *J. Mater. Chem. A* **2018**, *6* (15), 6654–6659. https://doi.org/10.1039/c7ta10689k.
- (54) Bianchini, M.; Ateba-Mba, J. M.; Dagault, P.; Bogdan, E.; Carlier, D.; Suard, E.; Masquelier, C.; Croguennec, L. Multiple Phases in the ε-VPO₄O-LiVPO₄O-Li₂VPO₄O System: A Combined Solid State Electrochemistry and Diffraction Structural Study. *J. Mater. Chem. A* **2014**, *2* (26), 10182–10192. https://doi.org/10.1039/c4ta01518e.
- (55) Masquelier, C.; Wurm, C.; Rodríguez-Carvajal, J.; Gaubicher, J.; Nazar, L. A Powder Neutron Diffraction Investigation of the Two Rhombohedral NASICON Analogues: γ-Na₃Fe₂(PO₄)₃ and Li₃Fe₂(PO₄)₃. *Chem. Mater.* **2000**, *12* (2), 525–532. https://doi.org/10.1021/cm991138n.
- (56) Liu, R.; Xu, G.; Li, Q.; Zheng, S.; Zheng, G.; Gong, Z.; Li, Y.; Kruskop, E.; Fu, R.; Chen, Z.; et al. Exploring Highly Reversible 1.5-Electron Reactions (V³⁺ /V⁴⁺ /V⁵⁺) in Na₃VCr(PO₄)₃ Cathode for Sodium-Ion Batteries . *ACS Appl. Mater. Interfaces* **2017**, *9* (50), 43632–43639. https://doi.org/10.1021/acsami.7b13018.
- (57) Gaubicher, J.; Wurm, C.; Goward, G.; Masquelier, C.; Nazar, L. Rhombohedral Form of Li₃V₂(PO₄)₃ as a Cathode in Li-Ion Batteries. *Chem. Mater.* **2000**, *12* (11), 3240–3242. https://doi.org/10.1021/cm000345g.

Supplementary Information

Crystal Structure of the Intermediate $Na_2V_2(PO_4)_3$ Phase and Electrochemical Reaction Mechanisms in $Na_xV_2(PO_4)_3$ (1 \leq x \leq 4) System

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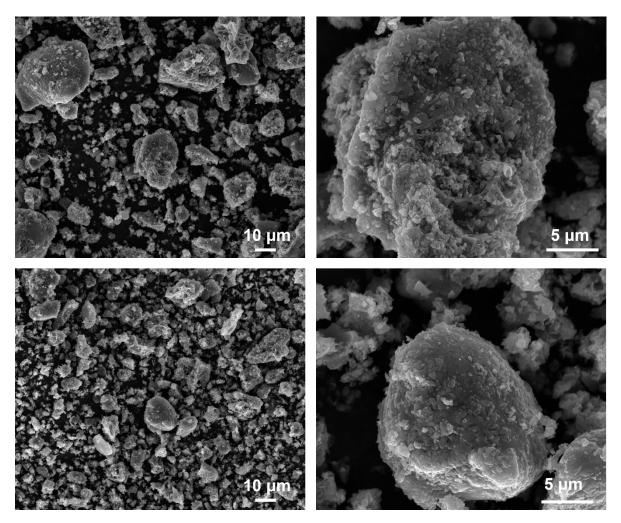


Figure S1. SEM images of the as-synthesized $Na_3V_2(PO_4)_3$ powder.

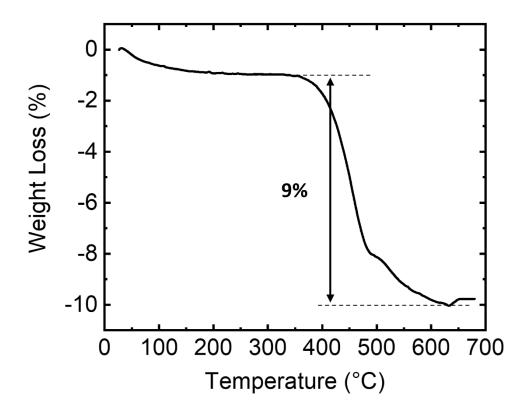


Figure S2. TGA data of the as-synthesized $Na_3V_2(PO_4)_3$ powder.

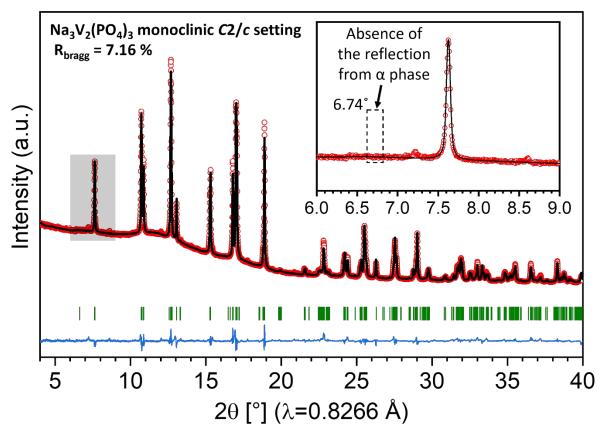


Figure S3. Rietveld refinement results of the as-synthesized $Na_3V_2(PO_4)_3$ powder at 298 K, highlighting that the α phase structure can be excluded here as reflection at 6.74° (a clear signature from the α phase) was not observed.

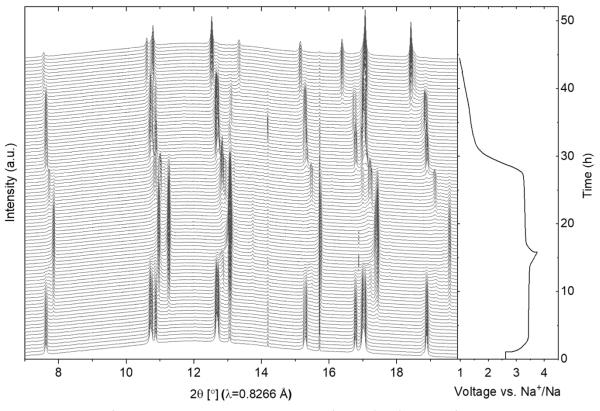


Figure S4. Wider 2θ ranged operando SPXRD patterns of $Na_3V_2(PO_4)_3$ during first cycle with a voltage window of 1.0-3.75 V vs. Na^+/Na at the C-rate of 0.11 C (=1 Na^+ in 9 h). The same data with the counter plot with the narrower 2θ range of $7.4-8.0^\circ$ is shown in Figure 2.

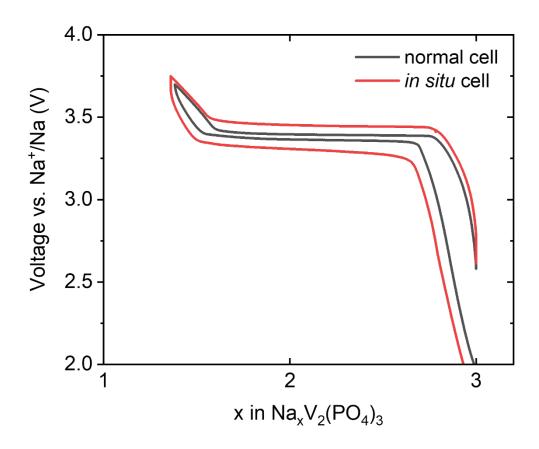


Figure S5. Comparison of a polarization between the first *in situ* cell (shown in Figure 2) and a normal coin cell cycled with the same C-rate of 0.11 C. The assembly of the normal coin cell is done with the same way as the *in situ* coin cell. The polarization of the *in situ* coin cell is about 150 mV while that of the normal coin cell is about 30 mV.

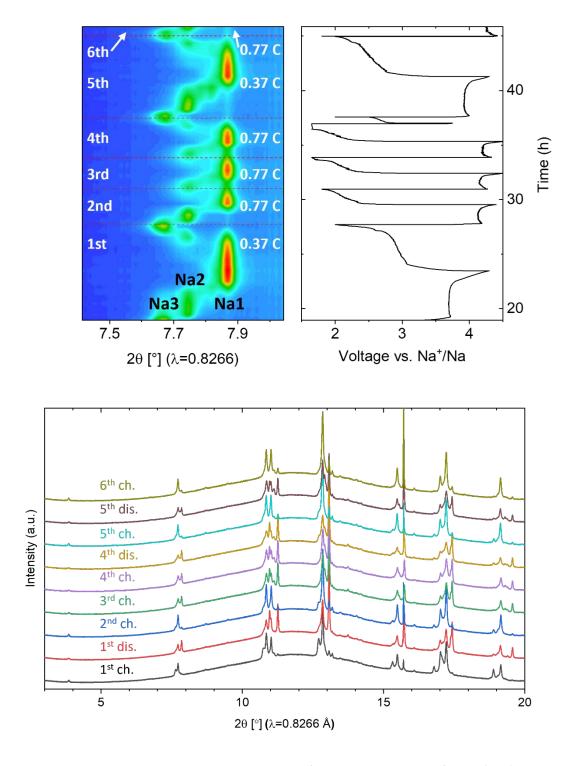


Figure S6 Top: *Operando* SPXRD measurements performed upon cycling of $Na_3V_2(PO_4)_3$ as positive electrode material in a half-cell versus Na metal, during six cycles at C-rates of 0.37 or 0.77 C. The voltage windows of each cycle are given in details in Table S2. Bottom: the SPXRD patterns containing the most $Na_2V_2(PO_4)_3$ phase during each cycle. Note that the $Na_3V_2(PO_4)_3$ phase during 2^{nd} and 3^{rd} discharge was not observed as data point missing (fewer data points) due to higher C-rate.

Table S1. Changes in voltage windows and C-rates during *operando* XRD measurements performed upon cycling of the second cell (**Figure S5**). The measurement was stopped in the middle of charge during the sixth cycle.

Cycle number	C-rate	Lower cut-off (V)	Upper cut-off (V)
1	0.37 C	2	4.3
2	0.77 C	1.8	4.4
3	0.77 C	1.65	4.5
4	0.77 C	1.65	4.5
5	0.37 C	2	4.3
6*	0.77 C	1.65	4.5

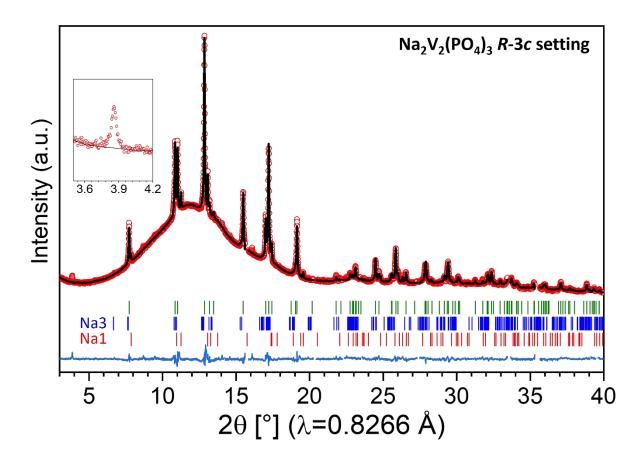


Figure S7. Rietveld refinement results of $Na_2V_2(PO_4)_3$ with the space group R3c. The reflection at 3.85° is not explained with the current structural model.

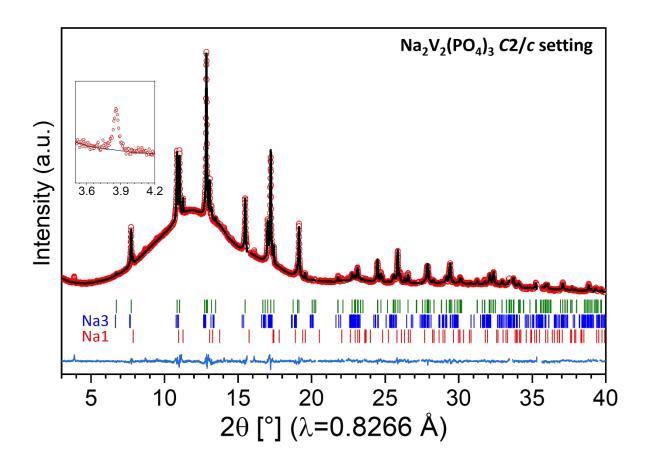


Figure S8. Rietveld refinement results of $Na_2V_2(PO_4)_3$ with the space group C2/c. The reflection at 3.85° is not explained with the current structural model.

Table S2. V-O bond distances obtained from Rietveld refinement of the four compositions $Na_xV_2(PO_4)_3$ (x = 1, 2, 3, and 4).

	Na ₄ V	2(PO ₄) ₃	Na	a₃V₂(I	PO ₄) ₃	N	a ₂ V ₂ (P	O ₄) ₃	Na	a ₂ V ₂ (P	O ₄) ₃		Na₁V	2(PO ₄) ₃
	R3c C		C2/	c	P2 ₁ /c (Model 1)		<i>P</i> 2/ <i>c</i> (Model 2)			R3c				
V(1)	O(1)	2.065(14) x 3	V(1)	O(1)	1.89(3)	V(1a)	O(1b)	2.05(9)	V(1a)	O(1b)	1.98(9)	V(1)	O(1)	1.931(16) x 3
	O(2)	2.087(14) x 3		O(2)	2.00(4)		O(1d)	1.70(10)		O(1d)	1.62(9)		O(2)	1.88(2) x 3
				O(3)	2.01(3)		O(1e)	1.93(7)		O(1e)	1.87(6)			
				O(4)	2.04(4)		O(2b)	2.17(10)		O(2b)	2.18(10)			
				O(5)	2.09(3)		O(2c)	2.03(8)		O(2c)	1.801(5)			
				O(6)	2.06(4)		O(2f)	2.06(9)		O(2f)	2.06(8)			
						avg. V	(1a)-O	1.99(9)	avg. V	(1a)–O	1.92(8)			
						V(1b)	O(1a)	2.04(9)	V(1b)	O(1a)	2.10(8)			
							O(1c)	1.85(10)		O(1c)	1.91(10)			
							O(1f)	2.17(7)		O(1f)	2.24(5)			
							O(2a)	2.01(10)		O(2a)	2.04(8)			
							O(2d)	1.82(8)		O(2d)	1.95(7)			
							O(2e)	2.08(11)		O(2e)	1.99(8)			
						avg. V	(1b)–O	1.99(9)	avg. V	(1b)–O	2.04(8)			
Avg.		2.076(14)			2.02(4)			1.99(9)			1.98(8)			1.91(2)

Table S3. Refined structural parameters of the intermediate phase $Na_2V_2(PO_4)_3$ using the space group P2/c (Model 2). ^aRefined and fixed at the last stages of refinement.

$Na_2V_2(PO_4)_3$

Space group: P2/c (#13); Z=4

a =15.2380(5) Å; b = 8.6090(5) Å; c = 8.7390(4); θ = 126.289(5)

V= 924.05(7) Å³; V/Z= 231.01(2) Å³

 $R_{\rm wp}$ = 12.8 %; $R_{\rm p}$ = 18.0 %; $R_{\rm bragg}$ = 7.50 %

Atom	Wyckoff position	x/a	y/b	z/c	Uiso, Ų	Occ.
V(1a)	4g	0.600(2)	0.243(4)	0.649(4)	0.026(3)	1
V(1b)	4g	0.108(2)	0.741(4)	0.645(4)	0.026(3)	1
P(1a)	4g	0.8498(10)	0.113(2)	0.932(2)	0.029(3)	1
P(1b)	4g	0.3569(10)	0.605(2)	0.958(2)	0.029(3)	1
P(2a)	2e	0	0.534(2)	0.25	0.029(3)	1
P(2b)	2f	0.5	0.021(2)	0.25	0.029(3)	1
O(1a)	4g	0.143(6)	0.149(10)	0.389(7)	0.012(3)	1
O(1b)	4g	0.660(7)	0.643(10)	0.389(10)	0.012(3)	1
O(2a)	4g	0.072(6)	0.451(10)	0.204(10)	0.012(3)	1
O(2b)	4g	0.553(6)	0.888(5)	0.214(10)	0.012(3)	1
O(3a)	4g	0.458(4)	0.678(10)	0.990(10)	0.012(3)	1
O(3b)	4g	0.937(4)	0.184(7)	0.919(10)	0.012(3)	1
O(4a)	4g	0.157(7)	0.064(2)	0.082(10)	0.012(3)	1
O(4b)	4g	0.635(7)	0.573(2)	0.020(4)	0.012(3)	1
O(5a)	4g	0.734(3)	0.840(10)	0.265(7)	0.012(3)	1
O(5b)	4g	0.259(5)	0.325(10)	0.273(7)	0.012(3)	1
O(6a)	4g	0.085(6)	0.364(10)	0.920(7)	0.012(3)	1
O(6b)	4g	0.581(6)	0.882(10)	0.929(7)	0.012(3)	1
Na(1)	4g	0.275(4)	0.280(7)	0.050(7)	0.030(13)	0.98(3)
Na(2a ₁)	4g	0.695ª	0.937 ^a	0.603ª	0.030(13)	0.17(7)
Na(2a ₂)	4g	0.172 ^a	0.446 ^a	0.570 ^a	0.030(13)	0.21(7)
Na(2b ₁)	2e	0	0.916(10)	0.25	0.030(13)	0.63(11)
Na(2b ₂)	2f	0.5	0.362(13)	0.25	0.030(13)	0.68(11)

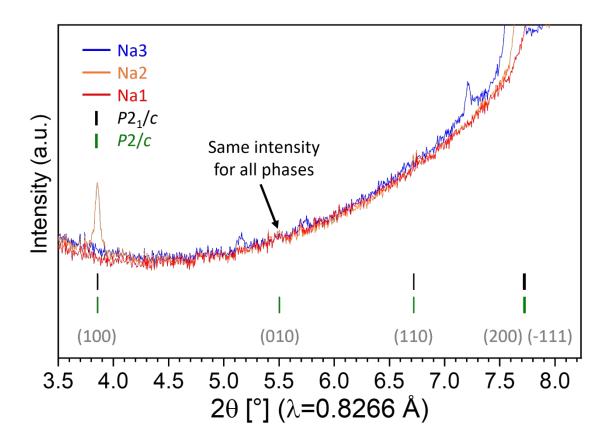


Figure S9. Comparison of the space group $P2_1/c$ and P2/c for the structural determination of $Na_2V_2(PO_4)_3$ phase. The same intensity for the possible (010) reflection (from the P2/c structural model) was observed in the XRD patterns of $Na_3V_2(PO_4)_3$, $Na_2V_2(PO_4)_3$, and $Na_1V_2(PO_4)_3$, suggesting it is not a peak but noisy background.

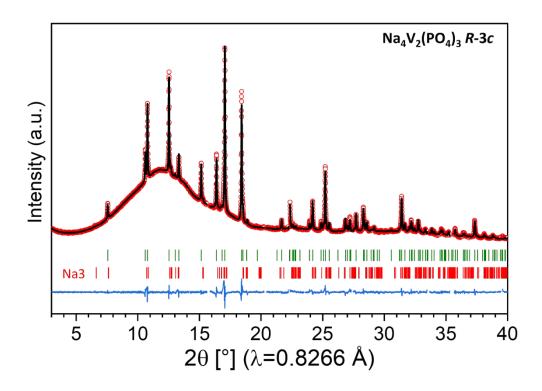


Figure S10. Rietveld refinement results of Na₄V₂(PO₄)₃. The XRD pattern was obtained from *operando* measurements. The contributions from Na metal and Al foil are removed

Table S4. Refined structural parameters of the $Na_4V_2(PO_4)_3$ using the space group R3c.

$Na_4V_2(PO_4)_3$

Space group: R3c (#167); Z=6 a = 8.94302(10) Å; c = 21.3609(4) Å; c/a = 2.389 V= 1479.51(4) Å³; V/Z=246.585(7) Å³ $R_{wp} = 14.1$ %; $R_p = 19.5$ %; $R_{bragg} = 4.2$ %

Atom	Wyckoff position	x/a	y/b	z/c	Uiso, Ų	Occ.
V(1)	12c	0	0	0.1467(3)	0.014(2)	1
P(1)	18e	0.2970(11)	0	0.25	0.021(4)	1
Na(1)	6b	0	0	0	0.031(9)	0.97(4)
Na(2)	18e	0.6461(14)	0	0.25	0.021(8)	0.92(2)
O(1)	36f	0.013(2)	0.2099(14)	0.1921(5)	0.020(5)	1
O(2)	36f	0.1827(14)	0.1713(14)	0.0833(7)	0.024(4)	1

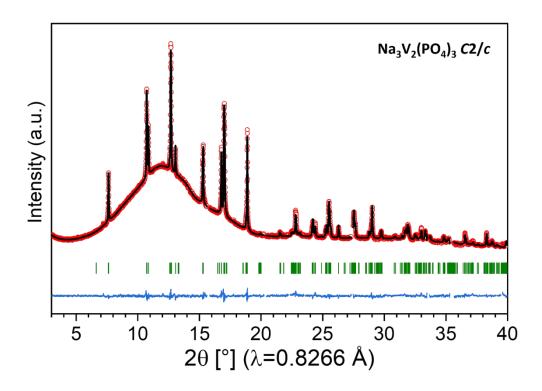


Figure S11. Rietveld refinement results of $Na_3V_2(PO_4)_3$. The XRD pattern was obtained from *operando* measurements. The contributions from Na metal and Al foil are removed

Table S5. Refined structural parameters of the intermediate phase $Na_3V_2(PO_4)_3$ using the space group C2/c. The XRD pattern was obtained from *operando* measurements.

$Na_3V_2(PO_4)_3$

Space group: C2/c (#15); Z=4 a =15.4065(3) Å; b=8.7288(2) Å; c=8.8243(2); $\theta=126.1091(16)$ V= 958.73(4) ų; V/Z= 239.682(10) ų $R_{wp}=11.2$ %; $R_p=17.5$ %; $R_{bragg}=7.17$ %

Atom	Wyckoff position	x/a	y/b	z/c	Uiso, Ų	Occ.
V(1)	8f	0.6029(6)	0.253(3)	0.6500(14)	0.015(2)	1
P(1)	8f	0.8514(11)	0.0999(14)	0.9620(14)	0.021(3)	1
P(2)	4e	0	0.532(2)	0.25	0.021(3)	1
O(1)	8f	0.138(2)	0.126(4)	0.357(3)	0.011(2)	1
O(2)	8f	0.0763(18)	0.450(3)	0.221(3)	0.011(2)	1
O(3)	8f	0.4510(18)	0.670(3)	0.987(4)	0.011(2)	1
O(4)	8f	0.156(2)	0.076(2)	0.066(4)	0.011(2)	1
O(5)	8f	0.7587(18)	0.828(4)	0.275(3)	0.011(2)	1
O(6)	8f	0.073(2)	0.361(3)	0.919(3)	0.011(2)	1
Na(1)	4c	0.25	0.25	0	0.059(9)	0.679(14)
Na(2a)	8f	0.665(2)	0.927(5)	0.634(5)	0.059(9)	0.70(3)
Na(2b)	4e	0	0.877(6)	0.25	0.059(9)	0.87(2)

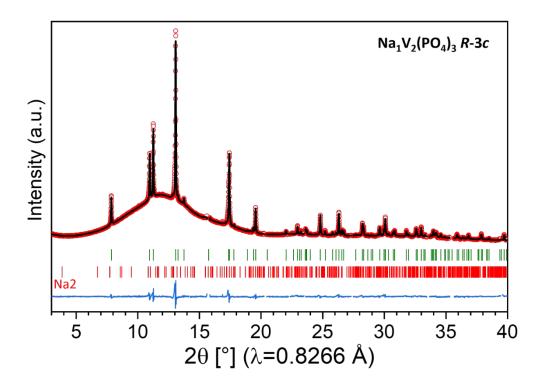


Figure S12. Rietveld refinement results of $Na_1V_2(PO_4)_3$. The XRD pattern was obtained from *operando* measurements. The contributions from Na metal and Al foil are removed.

Table S6. Refined structural parameters of the $Na_4V_2(PO_4)_3$ using the space group R3c.

$Na_1V_2(PO_4)_3$

Space group: R3c (#167); Z = 6 a = 8.42631(12) Å; c = 21.4772(6) Å; c/a = 2.549 V = 1320.63(5) Å³; V/Z = 220.105(8) Å³ $R_{wp} = 15.8$ %; $R_p = 24.3$ %; $R_{bragg} = 7.69$ %

Atom	Wyckoff position	x/a	y/b	z/c	Uiso, Ų	Occ.
V(1)	12c	0	0	0.1450(4)	0.024(3)	1
P(1)	18e	0.285(1)	0	0.25	0.023(4)	1
Na(1)	6b	0	0	0	0.034(0)	0.96(4)
O(1)	36f	0.187(2)	0.160(2)	0.087(1)	0.017(5)	1
O(2)	36f	0.023(3)	0.198(2)	0.192(1)	0.014(5)	1