Maximizing TADF via Conformational Optimization

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Abstract

We investigate a new strategy to enhance thermally activated delayed fluorescence (TADF) in organic light-emitting diodes (OLEDs). Given that the TADF rate of a molecule depends on its conformation, we hypothesize that there exists a conformation that maximizes the TADF rate. In order to test this idea, we use time-dependent density functional theory (TDDFT) to simulate the TADF rates of several TADF emitters, while shifting their geometries towards higher TADF rates in a select subspace of internal coordinates. We find that geometric changes in this subspace can increase the TADF rate up to three orders of magnitude with respect to the minimum energy conformation, and the simulated TADF rate can even be brought into the submicrosecond timescales under the right conditions. Furthermore, the TADF rate enhancement can be maintained with a conformational energy that might be within the reach of modern synthetic chemistry. Analyzing the maximum TADF conformation, we extract a number of structural motifs that might provide a useful handle on the TADF rate of a donor-acceptor (DA) system. The incorporation of conformational engineering into the TADF technology could usher in a new paradigm of OLEDs.
Introduction

Organic light-emitting diodes (OLEDs) are a promising solution in digital displays and lighting applications. Since Tang and Van Slyke demonstrated the first practical OLED device in 1987,1 OLEDs have attracted widespread research and development (R&D) efforts in both the academia and industry. OLED displays exhibit supremacy in energy efficiency, image quality, response time, and compactness over conventional technologies, such as liquid crystal displays (LCDs).2–4 In addition, OLEDs are expected to help reduce global energy consumption5,6 and yield new commercial products, such as transparent lighting panels and flexible displays.7,8

A key issue in developing more efficient OLEDs is overcoming the disadvantageous spin statistics. When electrons and holes are injected into the organic layer, they recombine in one of the four possible spin states with equal likelihoods: one singlet state and three triplet states. Whereas the singlet excitons can emit a photon and decay to the likewise singlet ground state, radiative decay of the triplet excitons is spin-forbidden. Most of the exitons are dissipated as heat, and the external quantum efficiency (EQE) of fluorescent OLEDs cannot exceed 25%. As a way to harvest the triplet excitons, Baldo et al. introduced phosphorescent OLEDs (PhOLEDs), which activate the otherwise forbidden transition between the triplet excited state and the singlet ground state.9 Using the strong spin-orbit coupling (SOC) in heavy metal complexes, the rate of phosphorescence can be brought into the useful microsecond timescale.7,10 However, in spite of the commercial success of red and green PhOLEDs, an efficient and stable blue PhOLED remains out of reach,4,11 and the rarity and toxicity of heavy metals are also problematic.

Thermally activated delayed fluorescence (TADF) is an alternative approach of converting the non-emissive triplet excitons to emissive singlet excitons.12,13 In typical organic molecules, electron exchange stabilizes the first triplet excited state (T1) with respect to the first singlet excited state (S1). However, if the singlet-triplet (ST) energy gap is less than few k_BT, thermal fluctuations can drive the reverse intersystem crossing (RISC) of the T1 population
into the $S_1$ state. Modulation of the exchange energy can be accomplished by tuning the spatial overlap between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO). In the first metal-free TADF OLED, Adachi et al. employed a donor-acceptor (DA) architecture to localize the HOMO and the LUMO on orthogonal moieties, creating $S_1$ and $T_1$ states of charge transfer (CT) character.$^{14,15}$ Since then, a large number of TADF emitters have been designed on the same principle,$^{16-20}$ and high-throughput screening approaches with the aid of machine learning techniques have been employed to give extensive surveys of the relevant chemical space.$^{21,22}$ As a culmination of the R&D efforts, TADF OLEDs are becoming competitive with commercial PhOLEDs.$^{23-26}$

Unfortunately, spatial separation of the HOMO and the LUMO also diminishes the transition dipole moment (TDM) between the $S_1$ state and the ground state ($S_0$). A decrease in the TDM entails a decrease in both the prompt and delayed fluorescence rates. The trade-off between a small ST gap and a large TDM is manifest even in the outcomes of high-throughput screening studies.$^{21,22}$ In addition, the identical CT character of the $S_1$ and $T_1$ states is expected to lead to a vanishing SOC according to El-Sayed’s rule$^{27}$ and hence a vanishing RISC rate. However, the trade-off might not be an intrinsic limitation of TADF, but an artifact of the design principles based on an oversimplified model. Indeed, recent studies have demonstrated that the $T_1$ state of many TADF molecules have significant contributions of local excitation (LE)$^{19,28,29}$ and that higher triplet states might also have an important role in the RISC step.$^{28,30,31}$ The two-state model of TADF does not provide the requisite insight to guide the development of trend-breaking emitters.

Recently, a four-state model of TADF has been proposed that might provide a way to overcome the trade-off.$^{32}$ According to the four-state model, the ST gap contains additional terms that can counter the effects of electron exchange, enabling the coexistence of a small ST gap and a large TDM in the same molecule. Furthermore, the adiabatic $S_1$ and $T_1$ wavefunctions contain different fractions of diabatic CT and LE wavefunctions, enabling the coexistence of a vanishing ST gap and a non-vanishing SOC. Although the mathematical forms
of the $S_1$ and $T_1$ energies and wavefunctions do not render themselves to straight-forward interpretation, exploring the conformation space of TADF emitters has been proposed as a practical approach to discover new design principles. Using molecular dynamics (MD) to sample the conformation space and time-dependent density functional theory (TDDFT) to simulate the electronic excitations, de Silva et al. showed that a DA complex can achieve upto an 800-fold enhancement of the TADF rate with respect to the minimum energy conformation. Indeed, a number of theoretical studies have shown that the conformation of a molecule can modulate the excitation energies and state-to-state couplings that contribute to the TADF rate. It would be reasonable to believe that the TADF rate has a strong dependence on the conformation.

In this work, we take the idea of conformational dependence to the next step and examine the potential of direct optimization to maximize the TADF rate. Using a number of known TADF emitters, we show that the TADF rate can be enhanced up to three orders of magnitude and can even be brought into the submicrosecond timescales via suitable changes of conformation. The maximum TADF conformation is free of thermal fluctuations that plague MD snapshot geometries, and one can extract specific hints, as well as general principles that can boost the performance of TADF OLEDs. Furthermore, we find that taking a small subset of the conformational variables suffices to gain substantial control over the TADF rate, and the relevant variables seem to overlap with degrees of freedom (DOFs) that might be tunable via steric hindrance or mechanical strain. Hence, conformational optimization appears to herald a new paradigm of TADF OLEDs.

**Methods**

The TADF rate was estimated using the formulation of Adachi et al. First, the rate of TADF is understood to mean the quasi-steady state rate at which the excited states are
depopulated via fluorescence

\[ k_{\text{TADF}} \equiv \frac{k_F[S_1]}{[S_1] + [T_1] + [T_2]} \]  

(1)

where we have assumed that internal conversion (IC) is fast enough that only the \( S_1, T_1, \) and \( T_2 \) states have significant populations. In our experience, omission of the \( T_2 \) state can lead to an overestimation of the TADF rate when the \( T_2 \) energy is below the \( S_1 \) energy. Assuming that the forward and reverse intersystem crossing (ISC and RISC) are fast compared to the radiative and non-radiative decay processes, the formula reduces to

\[ k_{\text{TADF}} = \frac{k_F}{1 + K_1 + K_2} \]  

(2)

where \( K_n \) is the equilibrium constant between the \( S_1 \) state and the \( T_n \) state

\[ K_n = 3 \exp \left( \frac{\Delta E_{S_1-T_n}}{k_B T} \right) \]  

(3)

The fluorescence rate is estimated by the Einstein coefficients\textsuperscript{37}

\[ k_F = \frac{e^2 \omega_{10}^2}{2 \pi \epsilon_0 m_e c^3} f_{10} \]  

(4)

where \( e \) and \( m_e \) are the electron charge and mass, respectively; \( c \) is the speed of light; and \( \omega_{10} \) and \( f_{10} \) are the \( S_1 \rightarrow S_0 \) energy gap and oscillator strength, respectively. In the final objective function, we added a penalty to damp the increase in the conformational energy (the DFT energy with respect to the energy minimum) and byproduct features that might arise in the optimization

\[ \Phi = k_{\text{TADF}} - \Lambda \Delta E_{\text{DFT}} \]  

(5)

where \( \Lambda \) is a tunable parameter and \( \Delta E_{\text{DFT}} \) is the change in the DFT energy with respect to the minimum energy conformation. We chose the tunable parameter to be on the order
\[ \Lambda \sim 1 \mu s^{-1} E_h^{-1} . \]

We need to emphasize a couple of points regarding the objective function. First, Equation 2 attempts to describe a single conformer of definite geometry. There are theories that enable the inclusion of geometric relaxation (or reorganization)\textsuperscript{38,39} and vibrational effects\textsuperscript{40} in estimating the rates of RISC and fluorescence, and these would be the proper way to describe a dynamical ensemble of conformers.\textsuperscript{41–43} However, the TADF rate maximization is a geometry optimization where we maximize the TADF rate instead of minimizing the energy, which necessitates the evaluation of the TADF rate at a definite geometry. Hence, consideration of nuclear dynamics is incompatible with the present investigation.

Second, Equation 2 represents an upper bound on the TADF rate. In the real universe, non-radiative decay and a finite RISC rate would entail a slowdown in addition to the fluorescence rate and the thermodynamic cap on the S\textsubscript{1} population. Nonetheless, the formula appeals to our purposes in a number of ways. In the first place, we are only interested in good TADF emitters, where TADF dominates over non-radiative decay, so it makes sense to compute the TADF rate by itself and verify after the fact that TADF proceeds on a feasible timescale. Moreover, Brédas et al. calculated the RISC rates of several TADF emitters and found that RISC rates on the microsecond timescale are not uncommon.\textsuperscript{28} We expect that RISC would not be a severe bottleneck in most cases and that the formula would provide a tight upper bound on the TADF rate. Indeed, we found that the RISC only makes quantitative corrections and does not alter the qualitative trends in our model systems. The computational details and numerical results have been provided in the SI.

The electronic structure calculations were performed using the B3LYP exchange-correlation functional\textsuperscript{44–49} and the 6-31+G* basis set\textsuperscript{50–53} as implemented in the Q-Chem 5.1 software package.\textsuperscript{54} The geometries were visualized in Avogadro 1.2.0,\textsuperscript{55} and the natural transition orbitals (NTOs)\textsuperscript{56} were visualized in MacMolPlt 7.7.\textsuperscript{57} Standard hybrid functionals are known to underestimate the excitation energy and overestimate the CT character of CT-like states.\textsuperscript{58,59} We are also neglecting the dielectric environment, which is known to stabilize
the CT-like states,\(^{42}\) and the dielectric stabilization is not in principle equivalent to the CT error.\(^{41}\) However, our objective was not to make quantitative predictions of TADF rates, but to extract qualitative trends that can guide the design of TADF emitters. Since analytical derivatives of the TDM are not available, the TADF rate maximization entails much higher computational costs than the usual energy minimization. Thus, it was desirable to use a functional that can reproduce the qualitative trends at minimal costs.

In order to establish that conformational dependence is not an artifact of B3LYP, the electronic structures at the key geometries were recalculated using PBE0,\(^{60-62}\) M06-2X,\(^{63}\) and LRC-\(\omega^*\)PBE.\(^{64-66}\) The asterisk indicates IPEA-tuning of the range-separation parameter, which we did at the minimum energy conformation in vacuum. Solvent effects were examined in the cases of M06-2X and LRC-\(\omega^*\)PBE, using the integral equation formalism polarizable continuum model (IEF-PCM)\(^{67-69}\) and first order, perturbative state-specific (ptSS)\(^{70}\) treatment of the excited states. We used the dielectric constant and optical dielectric constant of toluene at room temperature: \(\varepsilon = 2.379\) and \(\varepsilon_\infty = 2.232.\(^{71}\)

The TADF rate maximization was performed using a variation of the Nelder-Mead simplex method.\(^{72,73}\) Since there are multiple versions of the method, we have outlined our algorithm in the SI. The geometries of the molecules were represented in the Z-matrix coordinates. We have included the Z-matrices of the model systems at the key geometries in the SI. In order to reduce the computational costs and contain the geometric changes in the meaningful regions of the conformation space, a subset of the bond lengths, bond angles, and dihedral angles were chosen to be varied, while the others were constrained to the values at the minimum energy conformation. Since peripheral hydrogens should not have strong effects on the electronic structure and aromatic ring systems should be resistant to distortions, we chose the geometries of the single bonds that connect the aromatic ring systems as the variables. For a complete range of motion, six DOFs are required per bond: one bond length, two bond angles, and three dihedral angles. Hence, the number of variables in each of the model systems could be reduced to 30 or fewer Z-matrix coordinates. In order
to assess the extent to which our choices of variables were justified, a constrained energy
minimization was performed at the end of the TADF rate maximization, where we relaxed
the bond lengths and angles that had been fixed in the TADF rate maximization.

Results and Discussion

![Figure 1: Skeletal structures of DCzTrz, Cz2BP, Ac-MPM, and SpiroAC-TRZ. The
donor and acceptor groups are indicated in red and blue, respectively. Shown in green are
the single bonds whose geometries were varied in the TADF rate maximization.]

As model systems, we chose a number of TADF emitters that have been reported to
exhibit high EQE in blue: DCzTrz, Cz2BP, Ac-MPM, and SpiroAC-TRZ. The
skeletal structures of the model systems are shown in Figure 1. We are going to examine
the case of DCzTrz in detail and use the other emitters to assess the extent to which the
results can be generalized.

DCzTrz

Table 1 summarizes the energetics of DCzTrz at the maximum TADF geometries with
various energy penalties. Between the energy minimum ($\Lambda = \infty$) and the TADF maximum
with no energy penalty ($\Lambda = 0$), the TADF rate increases over two orders of magnitude
from $9.4\, \text{ms}^{-1}$ to $1.07\, \mu\text{s}^{-1}$. Moreover, the enhancement is not a result of trade-off between
Table 1: Conformational energies, excitation energies, oscillator strengths, and TADF rates of DCzTrz at the maximum TADF geometries with various energy penalties. The case of $\Lambda = \infty$ corresponds to the energy minimum, and the case of $\Lambda = 0$ corresponds to the TADF maximum with no energy penalty.

<table>
<thead>
<tr>
<th>$\Lambda$ ($\mu s^{-1}E_h^{-1}$)</th>
<th>$\Delta E_{\text{DFT}}$ (kJ mol$^{-1}$)</th>
<th>EE (eV)</th>
<th>$k_{\text{TADF}}$ ($\mu s^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\infty$</td>
<td>0</td>
<td>2.84 / 2.71 / 2.74</td>
<td>0.017 / 0.0094</td>
</tr>
<tr>
<td>8.0</td>
<td>211</td>
<td>2.86 / 2.83 / 2.93</td>
<td>0.026 / 0.88</td>
</tr>
<tr>
<td>4.0</td>
<td>278</td>
<td>2.94 / 2.91 / 3.00</td>
<td>0.029 / 1.06</td>
</tr>
<tr>
<td>2.0</td>
<td>409</td>
<td>2.86 / 2.84 / 2.95</td>
<td>0.026 / 1.08</td>
</tr>
<tr>
<td>0.0</td>
<td>594</td>
<td>2.79 / 2.77 / 2.90</td>
<td>0.028 / 1.07</td>
</tr>
</tbody>
</table>

a small ST gap and a large TDM: the $S_1$-$T_1$ gap decreases from 0.13 eV to 0.02 eV, and $f_{10}$ increases from 0.017 to 0.028. The simultaneous improvement of what are supposed to be contraindicated properties confirms that conformational optimization has achieved more than modulation of the HOMO-LUMO overlap. Although the conformational energy also undergoes a gigantic increase of 594 kJ mol$^{-1}$, the results with energy penalty reveal that much of the energy is irrelevant to improving the TADF rate. Using $\Lambda = 4.0 \mu s^{-1}E_h^{-1}$, the conformational energy can be halved with negligible loss in the TADF rate. Using $\Lambda = 8.0 \mu s^{-1}E_h^{-1}$, further damping to 211 kJ mol$^{-1}$ is possible with less than 20% loss of the TADF rate enhancement. The stability of the TADF rate against an energy penalty affirms that the maximum TADF conformation is not an absurdity, but its essential features are ones that one may hope to reproduce using suitable techniques in the real universe.

Figure 2a shows the minimum energy conformation with arrows indicating the DOFs that participate in the TADF rate maximization. It is obvious that the TADF maximum in Figure 2b is a strained conformation. The carbazole (Cz, donor) groups have popped above and below the plane of the 2,4,6-triphenyl-1,3,5-triazine (Trz, acceptor) group by $-33.4^\circ$ (left) and $+3.7^\circ$ (right), respectively. To be precise, two of the phenyl rings have twisted with respect to the triazine ring, so the Trz group is no longer planar, so these angles are with respect to the phenyl ring that bridges the Cz groups to the rest of the Trz group. Also, the Cz groups have rotated to become more orthogonal to the Trz group. The Cz groups are
Figure 2: Geometries of DCzTrz at (a) the energy minimum ($\Lambda = \infty$); (b) the TADF maximum with no energy penalty ($\Lambda = 0$); (c) the donor-acceptor bond (maginfied view); and (d) the TADF maximum with energy penalty ($\Lambda = 8.0 \text{ns}^{-1} E_h^{-1}$). Also, the dominant NTO pairs of the $S_1$ state at (e) the energy minimum ($\Lambda = \infty$) and (f) the TADF maximum with no energy penalty ($\Lambda = 0$). The arrows in (a) indicate the DOFs that are the most active in the TADF rate maximization, and the translucent geometries in the background of (b-d) are the minimum energy conformation. In (e-f), the hole orbitals are shown in red and orange, and the electron orbitals are shown in sky blue and indigo. Contour value: 0.025.
92.7° (left) and 79.8° (right) to the Trz group, respectively, in contrast to 57.3° (left) and 56.5° (right) at the energy minimum. Increasing the dihedral angle between the donor and acceptor moieties is a known strategy to reduce the HOMO-LUMO overlap and hence the ST gap. The fact that the same motif appears at the TADF maximum of DCzTrz is an encouraging sign that useful design principles can be extracted.

Indeed, a strange feature comes to attention. After popping above and below the plane of the Trz group, the Cz groups tilt back towards the Trz group, as shown in Figure 2c. The lower and upper Cz-Cz-C-Trz angles at each Cz group differ by +17.7° (left) and −19.5° (right), respectively, whereas the Cz-N-C-Trz angles at the energy minimum are the same 125.7° ± 0.2°. Though the differences in the angles change to +23.8° (left) and −6.5° (right), the gooseneck persists even with an energy penalty of Λ = 8.0 µs⁻¹Eₜ⁻¹. Hence, the gooseneck cannot be a side product of the optimization, but a feature relevant to TADF. Though the physical intuition is unclear, it might be associated with the additional terms in the four-state model or the dissimilar forms of the integrands in the exchange integral ⟨r₁₂⁻¹⟩ and the transition dipole integral ⟨r₁⟩. After all, the ST gap and the TDM should depend not only on the overlap, but also on the orientation of the HOMO and the LUMO.

Meanwhile, the twist in the Trz group tends to dissipate with energy penalty. As shown in Figure 2d, the phenyl rings return to a more coplanar arrangement to the triazine ring in what appears to be a concerted manner. However, the planarity of the Trz group remains quite disturbed even with an energy penalty of Λ = 8.0 µs⁻¹Eₜ⁻¹. The phenyl rings to the front center and the back left are 30.2° and 30.6° to the triazine ring, respectively, which are 41.6° and 61.3° in the absence of energy penalty. We conjecture that the twist in the Trz group controls the distribution of the LUMO so that it gets neither too close to nor too far away from to the HOMO. Comparing the dominant NTO pairs of the S₁ state at the energy minimum (Figure 2e) and the TADF maximum (Figure 2f), the distribution of the S₁ hole is indeed impacted. The NTOs of the T₁ state are similar (Figure S4). This would
also explains why the twist appears to unroll in a concerted manner as energy penalties are imposed. Overall, the twist in the Trz group appears to help enhance the TADF rate, but a balance must be struck with the conformational energy.

Other Model Systems

Table 2: Conformational energies, excitation energies, oscillator strengths, and TADF rates of Cz2BP, Ac-MPM, and SpiroAC-TRZ at the maximum TADF geometries with various energy penalties. The case of \( \Lambda = \infty \) corresponds to the energy minimum, and the case of \( \Lambda = 0 \) corresponds to the TADF maximum with no energy penalty.

<table>
<thead>
<tr>
<th>( \Lambda ) (( \mu s^{-1} E_h^{-1} ))</th>
<th>( \Delta E_{\text{DFT}} ) (kJ mol(^{-1}))</th>
<th>EE (eV)</th>
<th>( k_{\text{TADF}} ) (( \mu s^{-1} ))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cz2BP</td>
<td>inf</td>
<td>0</td>
<td>2.99 / 2.67 / 2.78</td>
</tr>
<tr>
<td></td>
<td>8.0</td>
<td>162</td>
<td>2.67 / 2.63 / 2.64</td>
</tr>
<tr>
<td></td>
<td>4.0</td>
<td>181</td>
<td>2.66 / 2.62 / 2.62</td>
</tr>
<tr>
<td></td>
<td>0.0</td>
<td>193</td>
<td>2.64 / 2.60 / 2.61</td>
</tr>
<tr>
<td>Ac-MPM</td>
<td>inf</td>
<td>0</td>
<td>2.47 / 2.46 / 2.47</td>
</tr>
<tr>
<td></td>
<td>8.0</td>
<td>51</td>
<td>2.51 / 2.49 / 2.49</td>
</tr>
<tr>
<td></td>
<td>4.0</td>
<td>365</td>
<td>2.54 / 2.51 / 2.67</td>
</tr>
<tr>
<td></td>
<td>0.0</td>
<td>420</td>
<td>2.55 / 2.52 / 2.61</td>
</tr>
<tr>
<td>SpiroAC-TRZ</td>
<td>inf</td>
<td>0</td>
<td>2.41 / 2.41 / 2.66</td>
</tr>
<tr>
<td></td>
<td>8.0</td>
<td>104</td>
<td>2.56 / 2.54 / 2.75</td>
</tr>
<tr>
<td></td>
<td>4.0</td>
<td>294</td>
<td>2.48 / 2.46 / 2.75</td>
</tr>
<tr>
<td></td>
<td>0.0</td>
<td>475</td>
<td>2.50 / 2.48 / 2.67</td>
</tr>
</tbody>
</table>

Table 2 summarizes the energetics of Cz2BP, Ac-MPM, and SpiroAC-TRZ. The TADF rates start in the millisecond timescale at the energy minimum and end in the microsecond timescale at the TADF maximum, suggesting that TADF rate enhancements over two to three orders of magnitude might be typical in the conformational optimization of TADF emitters. Cz2BP undergoes the largest enhancement in the TADF rate, a factor of 3000. However, the improvement is a result of trade-off between a small ST gap and a large TDM: the \( S_1-T_1 \) gap and \( f_{10} \) both decrease from 0.32 eV to 0.04 eV and from 0.345 to 0.060, respectively. The cases of Ac-MPM and SpiroAC-TRZ might be more complicated. Whereas the increases in the \( S_1-T_1 \) gaps of 0.02 eV are comparable to the uncertainty, the increases in the \( f_{10} \) of Ac-MPM and SpiroAC-TRZ span three orders of magnitude.
from $3.4 \times 10^{-5}$ to 0.028 and from $7.9 \times 10^{-6}$ to 0.019, respectively. The disproportionate trade-off suggests that conformational optimization might have had a non-trivial impact on the electronic structure. In any case, simultaneous improvement of the ST gap and the TDM might be a rare occurrence, which might also explain why DCzTrz was the only model system whose TADF rate reached the submicrosecond regime.

Notice that the minimum energy conformations of Ac-MPM and SpiroAC-TRZ have a tiny ST gap. In particular, the ST gap of SpiroAC-TRZ is near vanishing. The two-state model would suggest that the SOC must vanish, since both the $S_1$ and $T_1$ states must be CT states. Surprisingly, the RISC step does not appear to be the most severe bottleneck. The $f_{10}$ and SOC are $7.9 \times 10^{-6}$ and 0.0063 cm$^{-1}$, respectively, which correspond to a fluorescence rate of 2.0 ms$^{-1}$ and a RISC rate of 2.9 ms$^{-1}$ (Table S1). This makes sense in light of the four-state model. The $S_1$ and $T_1$ states contain different fractions of the diabatic CT and LE states, and the electron exchange favors the $S_1$ state as the more CT-like state. Hence, the fluorescence step can end up slower than the RISC step. We refer interested readers to the work of de Silva et al. In each of the model systems, a suitable energy penalty can reduce the conformational energy with minimal loss in the TADF rate. Even with no energy penalty, the TADF maximum of Cz2BP has a conformational energy of 194 kJ mol$^{-1}$, less than half of the other model systems. With an energy penalty of $\Lambda = 8.0 \mu s^{-1} E_h^{-1}$, Ac-MPM and SpiroAC-TRZ reduce their conformational energies to 53 kJ mol$^{-1}$ and 102 kJ mol$^{-1}$, respectively, while retaining more than 90% and 80% of the TADF rates. Though these conformational energies might seem daunting, synthetic chemists have created and stabilized molecules with strain energies over 300 kJ mol$^{-1}$. For certain TADF emitters, the maximum TADF conformation might be synthesizable using suitable modifications in the real universe.

Figure 3 shows the geometries of Cz2BP, Ac-MPM, and SpiroAC-TRZ at the TADF maximum with no energy penalty ($\Lambda = 0$). The maximum TADF geometries with energy penalties and a detailed discussion of their relations to the energetics can be found in the
SI. Here, we summarize the key results. First, the dihedral angles between the donor and acceptor groups increase in Cz2BP (Figure 3a), while they decrease in Ac-MPM (Figure 3b) and SpiroAC-TRZ (Figure 3c). The dihedral angle changes are consistent with the outcome that the ST gap and the TDM both decrease in Cz2BP and increase in Ac-MPM and SpiroAC-TRZ. Second, SpiroAC-TRZ is the only model system that does not develop a gooseneck. The donor groups of Cz2BP (Figure 3d) and Ac-MPM (Figure 3e) both pop above and below the plane of the acceptor group and then tilt back towards the acceptor group. Third, the acceptor groups of Cz2BP and Ac-MPM become twisted, albeit in different ways from both DCzTrz and each other. In Cz2BP, the phenyl rings become more orthogonal to each other. In Ac-MPM, one of the phenyl rings twists out of plane, while the other maintains a moderate angle to the pyrimidine ring. The gooseneck and the twist in the acceptor group tend to persist even with energy penalties.

Remarkably, three out of the four model systems developed a gooseneck at the DA bond and a twist in the acceptor group. We suspect that these motifs might provide a useful
handle on the TADF rate in general DA systems. Unfortunately, there is want of theoretical intuition and experimental evidence at this point. Inspite of abundant efforts to manipulate the DA dihedral angles, we are not aware of prior studies that have considered out-of-plane displacement of the donor and the acceptor moieties. As discussed earlier, the gooseneck might be associated with the mathematical forms of the integrals that enter the TADF rate, but it is unclear which integrals are affected in what way.

The twist in the acceptor group is also obscure. While it is not hard to rationalize how the twist might change the distribution of the LUMO, it is not always clear why a particular distribution should be more conducive to TADF than another, nor does there appear to be a pattern in how the acceptor groups become distorted. For example, Ac-MPM appears to push the LUMO towards just one of the donor groups, while Cz2BP remains much more symmetric. The dominant NTO pairs of the S\(_1\) and T\(_1\) states can be found in the SI. Perhaps, the absence of a trend is due to the small number of model systems. The twist might not be a single motif, but a collection of motifs that concern specific families of emitters.

On the other hand, the lack of physical intuition attests to the true value of conformational optimization: discovery of design principles that do not render themselves to deduction.

**Choice of Density Functional**

In order to assess the functional dependence of the results, we took the maximum TADF geometries optimized using B3LYP and recalculated the electronic structures using PBE0, M06-2X, and LRC-\(\omega^*\)PBE. To our surprise, the generalized gradient approximation (GGA) global hybrid, the meta-GGA global hybrid, and the range-separated hybrid (RSH) exhibited similar patterns. Since tuned RSHs have been shown to be effective at predicting the excited state properties of TADF emitters, we focus on LRC-\(\omega^*\)PBE as the primary subject of comparison. The complete set of results can be found in the SI.

Table 3 summarizes the LRC-\(\omega^*\)PBE energetics of DCzTrz at the B3LYP geometries.
Table 3: Conformational energies, excitation energies, oscillator strengths, and TADF rates of DCzTrz and Ac-MPM recomputed using LRC-ω*PBE/IEF-PCM at the maximum TADF geometries optimized using B3LYP. The case of Λ = ∞ corresponds to the energy minimum, and the case of Λ = 0 corresponds to the TADF maximum with no energy penalty.

<table>
<thead>
<tr>
<th></th>
<th>Λ (µs⁻¹Eₕ⁻¹)</th>
<th>ΔE_{DFT} (kJ mol⁻¹)</th>
<th>EE (eV)</th>
<th>f₁₀</th>
<th>k_{TADF} (µs⁻¹)</th>
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<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>S₁ / T₁ / T₂</td>
<td></td>
<td></td>
</tr>
<tr>
<td>DCzTrz (vacuum)</td>
<td>inf</td>
<td>0</td>
<td>3.39 / 3.07 / 3.14</td>
<td>0.0310</td>
<td>1.5 × 10⁻⁵</td>
</tr>
<tr>
<td></td>
<td>8.0</td>
<td>202</td>
<td>3.49 / 3.27 / 3.29</td>
<td>0.0133</td>
<td>2.8 × 10⁻⁴</td>
</tr>
<tr>
<td></td>
<td>4.0</td>
<td>267</td>
<td>3.49 / 3.26 / 3.27</td>
<td>0.0018</td>
<td>2.4 × 10⁻⁵</td>
</tr>
<tr>
<td></td>
<td>2.0</td>
<td>394</td>
<td>3.37 / 3.15 / 3.20</td>
<td>3.5 × 10⁻⁴</td>
<td>7.1 × 10⁻⁶</td>
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<tr>
<td></td>
<td>0.0</td>
<td>573</td>
<td>3.33 / 2.93 / 3.11</td>
<td>3.9 × 10⁻⁴</td>
<td>1.1 × 10⁻⁸</td>
</tr>
<tr>
<td>DCzTrz (toluene)</td>
<td>inf</td>
<td>0</td>
<td>3.30 / 3.07 / 3.08</td>
<td>0.0312</td>
<td>3.1 × 10⁻⁴</td>
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<tr>
<td></td>
<td>8.0</td>
<td>199</td>
<td>3.37 / 3.27 / 3.27</td>
<td>0.0146</td>
<td>0.024</td>
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<tr>
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<td>0.0021</td>
<td>0.0019</td>
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<tr>
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<td>4.2 × 10⁻⁴</td>
<td>2.5 × 10⁻⁴</td>
</tr>
<tr>
<td></td>
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<td>568</td>
<td>3.24 / 2.93 / 3.12</td>
<td>3.4 × 10⁻⁴</td>
<td>2.7 × 10⁻⁷</td>
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<tr>
<td>Ac-MPM (toluene)</td>
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<td>3.04 / 3.09 / 3.06</td>
<td>5.0 × 10⁻⁵</td>
<td>0.0073</td>
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<td>2.97 / 2.98 / 3.07</td>
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<tr>
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<td>0.034</td>
<td>0.026</td>
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<tr>
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<td>393</td>
<td>3.08 / 2.82 / 3.08</td>
<td>0.0059</td>
<td>3.4 × 10⁻⁵</td>
</tr>
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</table>

Interestingly, the TADF rates in LRC-ω*PBE seem to increase with the energy penalty at small values of Λ. The TADF rate reduces to 0.011 s⁻¹ at the geometry optimized with no energy penalty (Λ = 0), which is smaller than 15 s⁻¹ at the energy minimum. On the other hand, the maximum TADF rate is 280 s⁻¹ at the geometry optimized with Λ = 8.0 µs⁻¹Eₕ⁻¹, which is an order of magnitude greater. A toluene-like environment stabilizes the S₁ state by 0.1 eV to 0.2 eV, increasing the maximum TADF rate to 24 ms⁻¹ at the geometry optimized with Λ = 8.0 µs⁻¹Eₕ⁻¹, which is now two orders of magnitude greater than 0.31 ms⁻¹ at the energy minimum. The other molecules exhibit similar trends, as shown in Tables S4 and S6.

Remarkably, LRC-ω*PBE predicts much more favorable TADF properties in Ac-MPM and SpiroAC-TRZ. Table 3 shows the energetics of Ac-MPM in a toluene-like environment as computed using LRC-ω*PBE/IEF-PCM. Notice that Ac-MPM exhibits a simultaneous improvement of the ST gap and TDM and a TADF rate in the submicrosecond timescales at the geometry optimized with Λ = 8.0 µs⁻¹Eₕ⁻¹. As shown in Table S6, SpiroAC-TRZ also exhibits a simultaneous improvement at Λ = 4.0 µs⁻¹Eₕ⁻¹, though
the TADF rate is the greatest at $\Lambda = 8.0 \mu s^{-1} E_h^{-1}$. The TADF rates of Ac-MPM and SpiroAC-TRZ are $3.8 \mu s^{-1}$ and $2.9 \mu s^{-1}$ at the respective geometries optimized with $\Lambda = 8.0 \mu s^{-1} E_h^{-1}$. Again, we emphasize that we have not re-optimized the geometries using LRC-\(\omega\)*PBE/IEF-PCM. It stands to reason that we could have gotten even more drastic enhancements if we had.

Hence, various functionals corroborate the enhancement of TADF rates in the B3LYP geometries, provided that the objective function contained sufficient energy penalty. We suspect that the TADF rate maximization had a propensity to exploit the quirks of the B3LYP universe and that the energy penalty helped the optimizer to remain in the safe region of the conformation space. The existence of such quirks is not surprising, since B3LYP is just an approximation to the exact density functional. However, B3LYP is not special in this regard. In fact, we might have encountered the same issue even if we had optimized the geometries using a different functional. Suppose that we had done the TADF rate maximization using LRC-\(\omega\)*PBE/IEF-PCM. We would have obtained drastic enhancements, only to have those results be brought into question by the other functionals. For practical purposes, it would make sense to perform the TADF rate maximization using an inexpensive method and verify the improvements using more sophisticated methods.

We recapitulate the noteworthy commonalities in the energetics predicted by B3LYP and the other functionals. First, there exists a conformation where the TADF rate is orders of magnitude greater than at the minimum energy conformation. Moreover, the maximum TADF conformation in B3LYP and in the other functionals cannot be too far apart, considering that a moderate energy penalty is sufficient to arrive at a geometry that exhibits TADF rate enhancement in all of the functionals. These observations reaffirm that the maximum TADF conformation not only exists, but also can be determined to a reasonable precision. Second, one or more of the model systems exhibit a simultaneous improvement of the ST gap and TDM. These are DCzTrz in B3LYP and PBE0 and Ac-MPM and SpiroAC-TRZ in M06-2X/IEF-PCM and LRC-\(\omega\)*PBE/IEF-PCM. When a simultaneous improvement of the
ST gap and TDM occurs, the maximum TADF rate can be impressive. The TADF rate of DCzTrz in B3LYP and the TADF rates of Ac-MPM and SpiroAC-TRZ in M06-2X/IEF-PCM and LRC-ω*PBE/IEF-PCM reach the submicrosecond timescales. It is possible but difficult to think that the simultaneous improvement is just a quirk in each of the functionals, given that the last two methods predicted simultaneous improvement in geometries optimized using a different functional. The results cast a serious doubt on the conventional wisdom that the trade-off is an inherent property of TADF emitters.

Choice of Conformational Variables

So far, we have assumed that the variables in the TADF rate maximization corresponded to the most flexible DOFs in the model systems. While the assumption does not affect the existence of conformations that maximize the TADF rate, it does affect the extent to which we can expect the maximum TADF conformation to be reproducible in the real universe. If our choice of conformational variables were appropriate, then the changes in the geometry and the consequent changes in the TADF rate would be minimal even if we relaxed the complementary DOFs. Hence, we took the maximum TADF geometries and performed a constrained energy minimization to relax the hydrogen atoms and the aromatic ring systems, which had been fixed in the TADF rate maximization.

Figure 4 summarizes the energetics of the maximum TADF geometries before and after the constrained energy minimization. The effects of the relaxation depend on the system. For example, DCzTrz undergoes an order-of-magnitude decrease in the TADF rate from 1.07 µs⁻¹ to 0.14 µs⁻¹, and a noticeable decrease in the DFT energy from 594 kJ mol⁻¹ to 472 kJ mol⁻¹, as shown in Figures 4a and Figure 4b, respectively. It appears that our choice of variables included too many rigid DOFs, or the geometric changes might have been severe enough to obscure the distinction of flexible and rigid DOFs. Figure 2c reveals that the constrained energy minimization causes distortions in the phenyl and the triazine rings that tend to restore the planarity of the Trz group. These changes agree with the conjecture that
Figure 4: (a) TADF rates and (b) DFT energies of DCzTrz, Cz2BP, Ac-MPM, and SprioAC-TRZ at the energy minimum, at the TADF maximum (\( \Lambda = 0 \)), and after the relaxation of the hydrogen atoms and the aromatic ring systems. (c) Geometry of DCzTrz at the TADF maximum (\( \Lambda = 0 \)) after the relaxation of the hydrogen atoms and the aromatic ring systems.

The twist in the acceptor group imparts a considerable strain on DCzTrz. Also, it makes sense that unrolling the twist in the acceptor group in an unconcerted manner would be detrimental to the TADF rate, since the distortion controls the distribution of the LUMO.

With the exception of DCzTrz, the TADF rate enhancement is quite stable against the relaxation of the hydrogen atoms and the aromatic ring systems. Cz2BP shows minimal changes in both the TADF rate and the DFT energy, meaning that our choice of variables captured both the most flexible DOFs and the DOFs that are the most relevant to the TADF rate. In the cases of Ac-MPM and SprioAC-TRZ, the conformational energies are halved, but the TADF rates remain at 0.52\( \mu \text{s}^{-1} \) and 0.49\( \mu \text{s}^{-1} \), respectively. The geometries of Cz2BP, Ac-MPM, and SprioAC-TRZ after the constrained energy minimization have been provided in the SI. In addition to affirming our choice of variables, the stability of the TADF rate suggests a substantial overlap between the most flexible DOFs and the DOFs that determine the TADF rate in the model systems. The outcome is consistent with our proposition that the essential features of the maximum TADF conformation might be
synthesizable using suitable modifications in the real universe.

How to synthesize the maximum TADF conformers is beyond the scope of this work, but we can suggest some basic examples. The textbook chemist’s approach would be to attach bulky groups that constrain the rotation of certain bonds – the same approach has been used to modulate the donor-acceptor dihedral angles in TADF emitters.\textsuperscript{76–78} We can also imagine placing the organic layer under mechanical stress or pressure to crowd the molecules together. In the first place, it is not necessary to have every OLED molecule in the maximum TADF conformation. For most practical purposes, it would suffice to increase the population of molecules that have higher TADF rate than the equilibrium ensemble of the original emitter. We expect that a myriad of techniques in enzyme design might prove applicable to the conformational engineering of TADF OLEDs.

**Conclusions**

In order to demonstrate the potential of conformational optimization to assist the development of trend-breaking TADF OLEDs, we studied direct maximization of the TADF rate in the conformation spaces of several TADF emitters. As desired, one of the model systems achieved a simultaneous improvement of the ST gap and the TDM, and its simulated TADF rate could be brought into the submicrosecond timescales (\textbf{DCzTrz}). Even model systems that exhibited trade-off between a small ST gap and a large TDM were found to undergo TADF rate enhancements by two to three orders of magnitude. The conformational energy required to maximize the TADF rate can be as small as 193 kJ mol\textsuperscript{-1} even in the absence of energy penalty (\textbf{Cz2BP}), and the conformational energy can be as small as 51 kJ mol\textsuperscript{-1} with minimal loss in the TADF rate enhancement (\textbf{Ac-MPM}). Furthermore, the maximum TADF conformations of the model systems shared a number of structural motifs, such as the gooseneck at the DA bond and the concerted rotation of the aromatic rings in the acceptor group. Although the physical intuition behind these motifs remain obscure, the opacity itself
demonstrates the true value of conformational optimization: discovery of design principles that do not render themselves to deduction.

The conformational dependence of the TADF rate motivates the incorporation of conformational engineering into the TADF technology. Based on the results of TADF rate maximization with energy penalties and constrained energy minimization, the maximum TADF conformation of certain molecules, or another conformation that contains its essential features, might be synthesizable, given the high levels of strain that are within the reach of modern synthetic chemistry. Since the minimum energy conformation is not the best geometry in terms of the TADF rate, it would be desirable to manipulate the conformation in a way that enhances the TADF rate. Although the proposition might seem unorthodox in physical or organic chemistry, changing the properties of a molecule by changing its conformation is a standard in fields such as enzyme design. In the future, we hope to connect conformational optimization with experimental efforts and demonstrate that the electronic structures of TADF emitters can be improved in the real universe.

Acknowledgement

This work was supported by a grant from the U.S. Department of Energy Office of Basic Energy Sciences (DE-FG02-07ER46474).

Supporting Information Available

Our version of the Nelder-Mead simplex method; calculation of the RISC rate and evaluation of its effects on the TADF rate; recalculation of the electronic structures using PBE0, M06-2X, LRC-ω*PBE, M06-2X/IEF-PCM and LRC-ω*PBE/IEF-PCM; geometries of Cz2BP, Ac-MPM, and SprioAC-TRZ at the TADF maximum with various energy penalties, and after the relaxation of DOFs that had been fixed in the TADF rate maximization; dominant NTO pairs of DCzTrz, Cz2BP, Ac-MPM, and SprioAC-TRZ in the S1 and T1 states;
Z-matrices thereof.

References


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TOC Graphic

Conformational Optimization

\[ \Delta E_{ST} \downarrow \]
\[ \text{TDM} \uparrow \]
\[ \text{SOC} \uparrow \]

\[ \text{TADF Rate} \times 10^3 \]

+ New Design Principles