Amphiphile Conformation Impacts Aggregate Morphology and Solution Structure Across Multiple Lengthscales

Michael J. Servis,^{α *,†} Biswajit Sadhu,^{b*,†,‡} L. Soderholm,[¶] and Aurora E. Clark^{*,†,§,||}

†Department of Chemistry, Washington State University, Pullman, WA 99164 ‡Health Physics Division, Bhabha Atomic Research Centre, Mumbai, India

¶Chemical Sciences and Engineering Division, Argonne National Laboratory, Argonne, IL

60439

§ Voiland School of Chemical Engineering and Bioengineering, Washington State University, Pullman, WA 99164

||Pacific Northwest National Laboratory, Richland, WA 99354

E-mail: mservis@anl.gov; biswajit.sadhu@wsu.edu; auclark@wsu.edu

^bco-first author

1

 $[^]a\mathrm{Current}$ address: Chemical Sciences and Engineering Division, Argonne National Laboratory, Argonne, IL 60439; co-first author

2

Abstract

Although the self-assembly of amphiphiles is well-studied in aqueous solutions, 3 much less is understood about the fundamental driving forces and structure property Δ relationships in non-polar media. In recent work [Journal of Physical Chemistry B, 5 2020, 124, 10822.] the authors have studied a series of malonomide-based amphiphiles 6 that are relevant to liquid-liquid extraction. That work demonstrated that aggregation 7 is largely driven by local dipole-dipole interactions between molecules. Here, we build 8 upon this observation to develop a more detailed understanding of how the balance q of dipole-dipole interactions (controlled by conformation) and molecular architecture 10 influences the morphology of the aggregates across lengthscale. Using constrained 11 molecular dynamics about key degrees of freedom, we demonstrate that the conforma-12 tion of N,N-dimethyl,N,N-dioctylhexylethoxy malonamide (DMDOHEMA) and N,N-13 dimethyl,N,N-dibutyltetradecyl malonamide (DMDBTDMA) has a significant impact 14 upon self-association - where appropriate conformational sampling is essential. To 15 quantify the aggregate morphology, several graph theoretic and persistent homology 16 based properties are determined. The former examines the patterns of intermolecu-17 lar interactions within clusters, while the latter examines the 3-dimensional spatial 18 distribution across lengthscales. Based upon these analyses, we find that the mor-19 phology of aggregates, particularly at higher malonamide concentration, depends on a 20 balance of dipole alignment and alkyl tail sterics. Dipole alignment encourages linear 21 patterns of the intermolecular interactions within aggregates, while the alkyl tail 22 steric interactions between the malonamide result in noticeably less linear aggregates 23 for DMDOHEMA than DMDBTDMA. This is reflected in the spatial distribution, 24 where more holes or voids exist between extractants within the DMDOHEMA that 25 distribute within the solution in more of a "swiss cheese" arrangement as opposed 26 to the more filamentous distribution of DMBDTDMA. This study links conformation 27 and molecular structure to the morphology of amphiphile assemblies, and serves as a 28 basis for ongoing study of multicomponent amphiphile solutions with polar and other 29 solutes, and how these impact aggregation phenomena. 30

31 **Introduction**

Supramolecular assembly of amphiphilic molecules supports a breadth of soft matter appli-32 cations¹ - from catalysis² to drug delivery³ to nano-devices.⁴ Aqueous assembly has been 33 the subject of significant study, where many of the fundamental driving forces and struc-34 ture property relationships have been identified.^{5,6} In comparison, organic phase amphiphile 35 assembly is less understood, despite important consequences to several technologies - includ-36 ing liquid-liquid extraction. Liquid-liquid extraction (LLE) is an industrial and analytical 37 process for the selective partitioning of solutes between immiscible liquid phases.⁷ Solutes 38 are distributed between low and high dielectric phases by their relative solubilities. This 39 free energy-driven process is controlled, therefore, by solute speciation: for example, target 40 aqueous solutes complex with amphiphilic "extractant" molecules to solubilize the resulting 41 complexes in the low dielectric organic phase. The free energy differences which drive ef-42 fective separations are often small, including on the order of thermal energy. As a result, 43 relatively minor free energy contributions are essential to understand and model LLE. Among 44 these small free energy contributions is the organic phase aggregation of the extractant and 45 extracted solutes, which imparts mesoscale structure to that phase.⁸ 46

Organic phase aggregation is driven by intermolecular interactions across different energy 47 and length scales. The nanoscopic lengths over which the organization is manifested evades 48 characterization by many experimental techniques: it is too large to probe with techniques in-49 cluding extended X-ray adsorption fine structure (EXAFS). IR or Raman spectroscopy which 50 are sensitive only to local environments while also being too small to effectively interpret 51 using NMR diffusion⁹ or small angle scattering data $^{10-19}$ fitted with colloidal models. For 52 this reason, a common approach to understanding organic phase aggregation is to combine 53 molecular dynamics (MD) simulation with experimental techniques including small angle X-54 ray scattering (SAXS).^{18,20,21} This provides the benefit of validating the simulation organic 55 phase structure with the experimental data while not relying on ill-suited colloidal models 56 to interpret that data.²² Instead, validated simulation structure can then be investigated in 57

⁵⁸ detail to bridge atomic and mesoscopic length scales.

In this study, we consider two malonamide extractants commonly applied to f-element 59 separations:²³ N,N'-dimethyl,N,N'-dioctylhexylethoxy malonamide (DMDOHEMA) and N,N'-60 dimethyl,N,N'-dibutyltetradecyl malonamide (DMDBTDMA), illustrated in Figure 1. To 61 isolate the contributions to organic phase organization from the differences in molecular 62 structure between DMDOHEMA and DMDBTDMA, we consider a simple organic phase: 63 the extractant/solvent mixture in the absence of extracted polar solutes. This system will 64 also serve a baseline from which the impact of extracted solutes can be understood. First, 65 we investigate the impact of extractant conformation and alkyl tail molecular structure 66 on extractant self-association. Then, we apply a graph theoretic and persistent homol-67 ogy approach to quantify both the malonamide aggregate morphology and their associated 68 conformations. The former method provides a detailed understanding of the patterns of 69 intermolecular interactions within and between aggregates, and has been used with much 70 success to characterize complex solutions. The latter provides new and additional insight 71 into the resultant spatial arrangement across lengthscales and represents a powerful emerging 72 tool to connect intermolecular forces and geometric structure. In combination these analyt-73 ical tools clearly demonstrate that two predominant forces impact aggregate structure for 74 malonomide systems - namely dipole alignment and alkyl tail sterics. Modulation of either 75 of these features influence the interconnectdness of intermolecular interactions within ag-76 gregates, inter-aggregate interactions and the resulting geometric arrangement at local and 77 extended lengthscales. This study provides insight into the fundamental drivers of organic 78 phase aggregation and serves as a framework to interpret the effects of chemical structure 79 and composition upon self-assembly and solution organization across lengthscales. 80

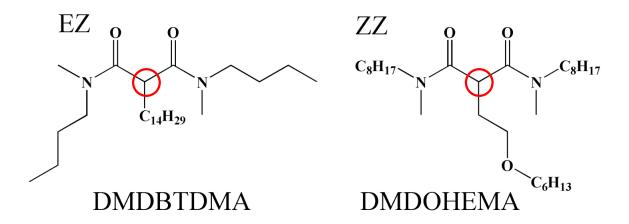


Figure 1: Molecular structures of the two malonamides considered in this study, with the central carbon, "CC," atoms highlighted with red circles. For DMDBTDMA, the two possible amide group conformational isomers are illustrated: E corresponds to the methyl group in the *gauche* configuration while Z refers to the methyl group in the *trans* configuration. For DMDOHEMA, the molecule is drawn with both amide groups in the Z configuration.

⁸¹ 2 Simulation and Analysis Methodology

82 2.1 Molecular Dynamics Simulations

Molecular dynamics simulations employed the GROMACS 2016.2 software package.²⁴ We 83 previously reported the GAFF-based²⁵ simulation potentials that are used in this study.²⁶ 84 Compositions for each system are given in Table 1. Packmol was used to generate random 85 initial configurations for the periodic cell, followed by energy minimization using a steepest 86 descent algorithm. Equations of motion were propagated with a leap-frog Verlet integra-87 tor²⁷ with a 2 fs time step. Hydrogen-containing bonds were constrained with the LINCS 88 algorithm.²⁸ A 15 Å cutoff was applied for Lennard-Jones interactions and short range elec-89 trostatics, with Particle-Mesh Ewald summation used for long-range electrostatics.²⁹ Systems 90 were equilibrated in the NPT ensemble for 5 ns with a temperature set to 300 K using the 91 velocity rescale thermostat³⁰ having a 0.2 ps coupling time and pressure set to 1 bar using 92 the Berendsen barostat³⁰ with a 2 ps coupling time. This was followed by 20, 50 or 100 ns 93 (for 0.5 M, 1.1 M and 1.5 M malonamide systems, respectively) of NVT equilibration with 94

temperature set to 300 K using the Nosé-Hoover thermostat³¹ and a 0.2 ps coupling time. Finally, a 50 ns NVT production trajectory was generated and sampled at 100 ps intervals. The equilibration of the conformational sampling was established through analysis of the time-dependent fluctuations on clustering and spatial distributions as described below and demonstrated in the Supplementary Information (*vide infra*).

Table 1: Molecular compositions and periodic cubic box sizes for the MD simulations. Simulation box dimensions are given in nm and concentrations in mol/L.

DMDOHEMA		DMDBTDMA		Solvent		Simulation box	
conc.	num.	conc.	num.	molecule num.		length (nm)	
0.5	301			n-dodecane	1941	9.890	
1.1	662			n-dodecane	1088	9.911	
1.5	903		—	n-dodecane	518	9.921	
		0.5	301	n-dodecane	2005	9.890	
		1.1	662	n-dodecane	1230	9.934	
		1.5	903	n-dodecane	713	9.957	

¹⁰⁰ 2.2 Topological Analyses

Graph Theory Analysis of Intermolecular Interactions. Non-covalent, or supramolec-101 ular, self-assembly is driven by local intermolecular interactions that may be represented in 102 a network or graph formalism. This approach is a valuable tool to quantify and characterize 103 the underlying patterns of interactions that govern the morphology of the self-assembled 104 species. Each individual malonamide molecule represents a single node. Edges are drawn 105 between nodes if the positions of the carbon atom bridging the amide groups—referred to 106 here as CC, highlighted in Figure 1—of those two malonamide molecules are within 1.0 107 nm. The choice of distance cutoff is taken from the CC-CC radial distribution functions 108 (RDF), vide infra. The cutoff is consistent between concentrations and the two malonamide 109 molecules. 110

Once the unweighted, undirected graph defining the malonamide connectivity is constructed, clusters are determined. Clusters are defined as disconnected subgraphs of the

total graph in which all nodes are connected to all other nodes through some path, but are 113 not connected through any path to any other node in a different subgraph. The cluster size 114 is the number of nodes within each subgraph. Within the clusters, several topological prop-115 erties of their intermolecular interactions are reported as a function of cluster size: global 116 clustering coefficient, average shortest path and maximum shortest path.³² The global clus-117 tering coefficient is defined as the fraction of all triplets within a cluster which are closed, 118 i.e., all three nodes in the triplet are connected to each other. The shortest path between a 119 pair of unique $(i \neq j)$ nodes i and j, d(i, j), sometimes referred to as the geodesic, is defined 120 as the length of the path on the graph with the fewest number of edges which connects i121 and j. The shortest path is computed for all pairs of nodes within each cluster C_n of size n 122 and the average shortest path, a, is defined as 123

$$a = \frac{1}{n(n-1)} \sum_{i,j \in C_n} d(i,j).$$
 (1)

¹²⁴ Similarly, the maximum shortest path for a given cluster C_n of size n is defined as

$$m = \max_{i,j \in C_n} d(i,j).$$
⁽²⁾

Topology of Spatial Organization. Complementing the topological characteristics of intermolecular interactions that comprise the amphiphile aggregates, the shape of the aggregates as well as the longer-range spatial organization has been examined. A traditional shape metric, is the radius of gyration, R_g , that is defined as the average root mean squared distance (r_i) of each CC position of node *i* and the center-of-mass position of all CC atoms in the identified C_n cluster.

$$\mathbf{R}_{\mathbf{g}}^2 = \frac{1}{n} \sum_{i \in C_n} r_i^2,\tag{3}$$

As with the geodesic properties, the radius of gyration is reported as a function of cluster size, n, with its value averaged over all instances of clusters of size n.

A more refined description of aggregate shape can be obtained using computational topol-133 ogy, specifically persistent homology (PH), which describes the 3-dimensional arrangement 134 of point cloud data. Over the last decade there has been tremendous growth of applied 135 mathematics methods that have combined the concepts of algebraic topology and computa-136 tion with the aim of characterizing the global shape of data.^{33,34} Broadly called topological 137 data analysis, persistent homology is a technique that produces a compact summary of the 138 global shape of sets of points in the form of a barcode and has been recently employed to 139 study ion aggregation in aqueous electrolytes.^{35,36} Given a collection of point cloud data (in 140 this case the position of the CC nodes), persistent homology provides an objective way to 141 quantify and compare global shapes of the data sets.³⁷ 142

We begin by constructing a sequence of growing simplicial complexes, where each sim-143 plicial complex is a collection of vertices, edges, triangles, and higher order simplices glued 144 together "nicely".³⁸ To create the growing simplicial complexes, a ball of diameter d is cen-145 tered at each CC node and the diameter systematically grown (Figure 2). As the diameter 146 grow, balls centered at CC nodes that are close to each other will intersect before those 147 centered at CC nodes that are farther apart. As d is increased, the intersection of a pair of 148 balls is captured by adding the edge connecting the points. Triangles, tetrahedra, and higher 149 order simplices are added to capture higher order intersections of balls. The small connected 150 components merge into bigger connected components that form the triangles and other sim-151 plices, while holes appear and disappear. The intersections of these balls over the entire 152 range of values of d capture all information about the global shape of the malonomide aggre-153 gates, initially at the local level, then the aggregates as a whole, then aggregate-aggregate 154 interactions, until the entire space of the simulation box is filled. The number of connected 155 components in the object or space is monitored by the β_0 number (which relates to the orig-156 inal homology of the space), while the β_1 counts the number of holes present. The changes 157

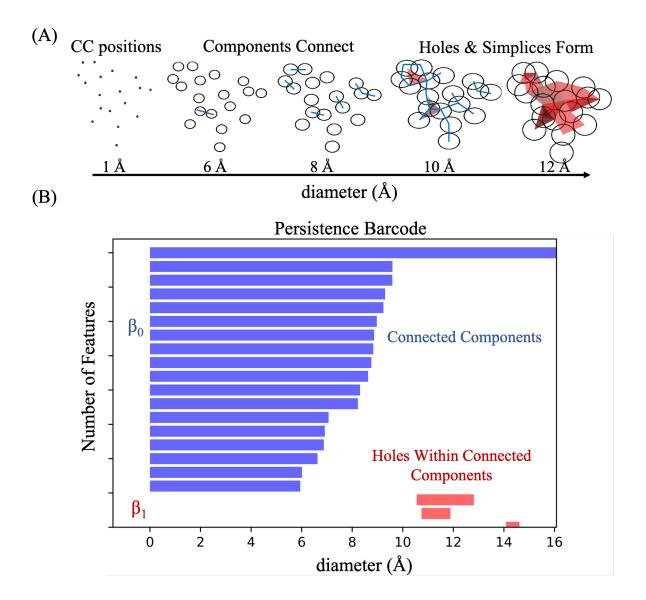


Figure 2: Construction of the persistent homology (PH) barcode from point cloud data based upon the CC positions of amphiphilic extractants. (A) Spheres centered on the CC positions have their diameter systematically increased, where individual spheres (components) merge to become connected and holes and voids form in 3-dimensional space and triangles and tetrahedra form simplicial complexes. (B) The number of connected components are counted (β_0) and the number of holes between amongst connected components are measured (β_1) as a function of sphere diameter to create the PH barcode.

to β_0 and β_1 values are tracked as d increases, and and this information is presented in a 158 compact form as a barcode as illustrated in Figure 2. Persistence barcodes are obtained over 159 a 50 ns trajectory at a sampling interval of 100 ps (1 barcode/frame of data). The persistent 160 topological features are extracted by computing the persistent betti number, defined as the 161 sum of all persistent kth dimensional features within a specified interval of the ball diameter. 162 The emergence (or birth) and disappearance (or death, caused by merging of features) of β_0 163 and β_1 along the d axis is tracked to identify the topologically relevant important lengthscales 164 of spatial organization. 165

¹⁶⁶ 3 Results and Discussion

Malonamide self-association and solution structure is driven by a balance between dipoledipole and steric interactions. By constraining malonamides to specific conformational isomers, we demonstrate a clear link between malonamide conformations that feature larger molecular dipoles and stronger self-association. Then, we investigate unconstrained malonamide solutions structures and demonstrate that, at higher concentrations, malonamidemalonamide steric contributions become relevant and influence both the patterns of intermolecular interactions as well as spatial distribution within and between aggregates.

3.1 Fixed Conformation Simulations

¹⁷⁵ Characteristics of the Constrained Systems. Malonamide conformation is an essen-¹⁷⁶ tial aspect of its ability to coordiante metal ions^{39–41} and has been correlated with changes ¹⁷⁷ in organic phase aggregation.⁴² There are two primary degrees of freedom that define the ¹⁷⁸ conformation and modulate the molecular dipole: the relative orientation of the carbonyl ¹⁷⁹ C=O bond vectors^{21,39–41,43} and the amide stereoisomerization.⁴² As the former is a pseudo-¹⁸⁰ dihedral, we define it as the angle between the C=O bond vectors. The latter is defined by ¹⁸¹ the O-C-N-Me dihedral angle. The relative C=O orientation is classified as either *gauche* (angles less than 120°) or *trans* (angles greater than 120°), as justified by the probability distribution of the angle between C=O vectors (Figure S1).^{21,43} For the O-C-N-Me dihedral angle, each amide group is defined as Z or E,⁴² as illustrated in Figure 1, with the O-C-N-Me angle cutoff between the E (methyl group in *gauche* position) and Z (methyl group in *trans* position) stereoisomers of 90°.

Table 2: The average molecular dipole values are given here for each combination of constrained relative C=0 vector orientation and conformational isomerization simulations.

	DMDOHEMA			DMDBTDMA			
	dipole (debye)			dipole (debye)			
	All	All	Not	All	All	Not	
	gauche	trans	constrained	gauche	trans	constrained	
All E	6.75	2.90		7.28	2.05		
All Z		3.04			2.15		
2:1 Z:E	6.05	2.96		6.70	2.15		
Not constrained			3.84			2.03	

At a concentration of 0.5 M, five combinations of C=O orientation and amide conforma-187 tional isomerization were considered: *qauche* C=O vectors with a) all E and, b) a 2:1 Z:E 188 ratio, and trans C=O vectors with c) all Z, d) all E and e) a 2:1 Z:E ratio. The 2:1 ratio 189 is the approximate distribution expected based on NMR spectroscopy.⁴² Constraints were 190 imposed by increasing the O-C-N-Me torsion barrier to 400 kJ/mol, which also fixed the 191 C=O orientation (see Table S1 for the fraction of trans C=O vectors for each constrained 192 system). Initial malonamide configurations were changed to match the fixed geometry of 193 interest; for the 2:1 Z:E ratio, Z and E conformations were generated randomly assuming 194 that conformational isomerization of amide groups within the same molecule are statistically 195 independent.⁴² The time evolution of the spatial distribution of the system, as analyzed by 196 the persistent homology, is shown in Figure S2 to demonstrate adequate equilibration of 197 the solution structure. The molecular dipole moments, calculated as the ensemble average 198 values of the sum of the distances of every atom site from the malonamide center of mass and 199 weighted by the atomic charge, are presented in Table 2 within each set of constrained sim-200

²⁰¹ ulations. The relative malonamide orientation is defined as the angle between two vectors: ²⁰² the bisector of the O-CC-O angle for each molecule, where the O atoms sites are the O-atoms ²⁰³ of the two amide groups. The probability density function of the angle, $P(\theta)$, normalized by ²⁰⁴ sin(θ), are plotted in Figure S3 for all fixed internal geometry 0.5 M simulations. Notably, ²⁰⁵ within constrained geometry simulations orientational preferences of the molecular dipoles ²⁰⁶ are observed, when in the *gauche* C=O vector conformation DMDBTDMA strongly prefers ²⁰⁷ parallel dipole alignment while DMDOHEMA does not.

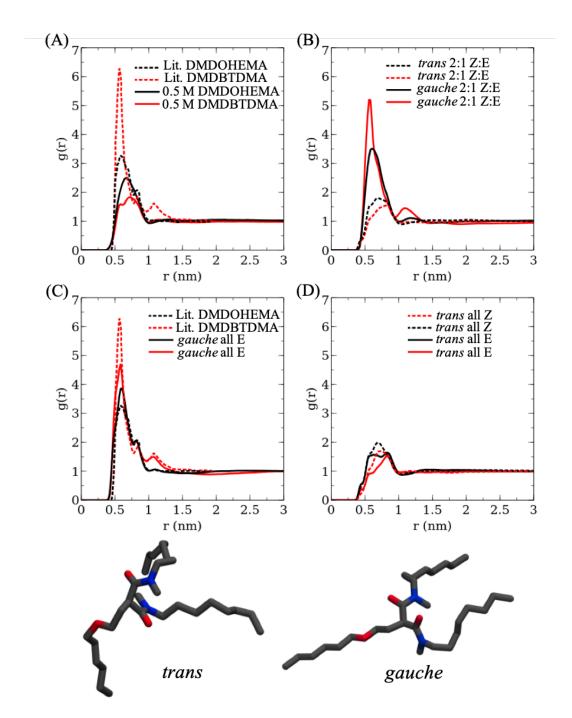


Figure 3: Comparison of RDFs for the 0.5 M solutions. (A) The unconstrained CC-CC RDFs from this study overlayed with those prior literature¹⁹ (using the OPLS force field in n-heptane). (B) the CC-CC RDFs for the constrained geometries having fixed 2:1 Z:E ratios for both *trans* and *gauche* C=O vectors. (C) Comparison of the prior literature RDFs with the constrained *gauche* C=O vectors having all E conformational isomerization, (D) CC-CC RDFs at the constrained *trans* conformations with all E or all Z.

The relative malonamide orientations are correlated with the primary and secondary 208 peaks of the CC-CC RDFs,²⁶ and their respective heights are used as an initial indication of 209 self-association (Figure 3). Importantly, both descriptors of internal malonamide geometry 210 impact self-association The *qauche* conformation of C=O vectors dramatically increase the 211 height of the first correlation peak for both malonamides. In the absence of the strong first 212 peak, the impact of the Z:E ratio on the peak heights of the weaker, secondary correlations at 213 larger CC-CC distances is also apparent. Overall, these results substantiate the conclusion 214 that the largest impact on molecular dipole—and self-association that derives from dipole 215 interactions—originates from the relative C=O vector orientation. 216

Intermolecular Networks and Spatial Organization. These data are further exam-217 ined using cluster analysis of the intermolecular interaction networks and persistent homol-218 ogy so as to understand the role of the molecular conformation upon the aggregate size 219 distribution and spatial organization. A detailed comparison is presented for the gauche 220 2:1 Z:E simulation versus the unconstrained simulation data. As observed in Figures 4A -221 4B, imposing the constraint clearly increases the average cluster size, with a more signif-222 icant affect being observed for DMDBTDMA, consistent with the larger molecular dipole 223 of DMDBTDMA and smaller alkyl chain lengths (presumably with reduced alkyl sterics). 224 Figure S4 presents a log-scale plot up to the largest, rare, clusters observed with sizes in 225 the several hundred. Graph analysis of the intermolecular interaction network within each 226 cluster further reveal longer network pathways within those clusters in the constrained sim-227 ulations (Figure S5). Such information can reflect changes to internal connectivity as well 228 as associated spatial distributions. To delve deeper into this topic, the number of connected 229 components β_0 as a function of distance was first examined (Figure 4C). For all systems, a 230 rapid drop in β_0 is observed immediately preceding 0.5 nm that is commensurate with the 231 growth of intermolecular interactions between CC nodes that cause components to merge 232 and the formation of the intermolecular network used to define self-association and cluster-233

ing. The merger of connected components rapidly continues from 0.5 nm to 1 nm, where the constrained systems have steeper slopes than the unconstrained analogues consistent with self-assembly. Interestingly, analysis of the β_1 holes reveals that cycles/holes of CC nodes do not form until ~ 0.7 nm. The constrained simulations have a larger increase in β_1 holes as the diameter of the CC nodes intersect to form cycles at lower distance relative to the unconstrained simulations, which supports increased self-association defined by more densely packed molecular assemblies within the constrained simulations.

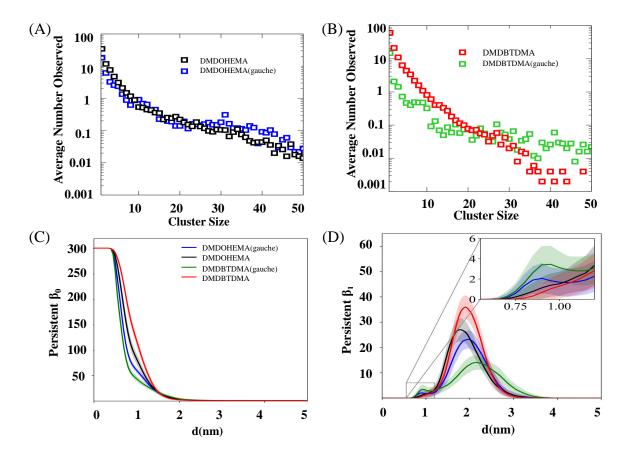


Figure 4: Comparison of cluster distributions and persistent homology betti numbers at 0.5 M DMDOHEMA or DMDBTDMA under constrained gauche 2:1 Z:E conformation and unconstrained conditions. (A) The cluster size distribution of DMDOHEMA. (B) The cluster size distribution of DMDBTDMA. (C) The variation of average persistent β_0 betti number (and β_1) with the increasing filtration value for 0.5 M DMDBTDMA and DMDOHEMA with and without the applied constraints. (D) The variation of average persistent β_1 betti number with the increasing filtration value for 0.5 M DMDBTDMA and DMDOHEMA with and without the applied constraints. Note that the error bar in the plot indicates the standard deviation of persistent betti numbers of all the frames within the window of 0.5 Å.

Interestingly, the steepness of the slope of the β_0 distribution exhibits a distinct change 241 at approximately 1 nm that is most pronounced for the constrained simulations; this is 242 complemented by a bimodal distribution in the β_1 values that is only observed within the 243 constrained simulations. Together, these data indicate two characteristic length scales associ-244 ated of organization when self-assembly is enhanced. The local spatial topology of CC nodes 245 is somewhat different for the constrained variants of DMDOHEMA and DMDBTDMA, as 246 indicated by the different shapes of the β_1 distribution (Figure 4D). Under 1 nm, the con-247 strained DMDBTDMA forms a larger number of 1D holes (higher peak in the distribution) 248 within the connected components relative to the constrained DMDOHEMA. Noticeably, the 240 presence of a minimum after the peak at ~ 1.2 nm indicates that the empty space between 250 the molecular nodes gets rapidly filled with the growth of the diameter centered on the CC 251 position. This indicates enhanced local intermolecular association of constrained DMDBT-252 DMA when compared with constrained DMDOHEMA within a distance of 1 nm. Beyond a 253 diameter of 1.2 nm, new growth of β_1 values indicates inter-aggregate hole formation caused 254 by aggregate-aggregate interactions. Comparison of the constrained simulations indicates 255 that variations in the local aggregation also impact longer-distance solution structure. The 256 DMDOHEMA is less able to form longer-range inter-aggregate associations (less holes in the 257 blue β_1 distribution at longer distance) relative to DMDBTDMA (the green β_1 distribution). 258 Further, there is a relationship between the extent of local aggregation, local aggregate size, 259 and longer-range solution structure. These are illustrated by comparing the blue and black 260 curves in the β_1 distribution in Figure 4D, while for DMDTDMA the green vs. red curves 261 are relevant. More clusters of larger size (in the case of DMDBTDMA) form extended spa-262 tial aggregate-aggregate interactions that are manifested in the formation of holes at longer 263 distances (relative to DMDOHEMA). 264

²⁶⁵ 3.2 Equilibrium Aggregation Behavior

Conformational Distributions. Equilibrium unconstrained simulations explore the mal-266 onamide conformational ensembles observed under realistic conditions and support an ex-267 panded view of how conformation is related to phase phenomena. Despite its importance, as 268 demonstrated above, the impact of malonamide conformation has not been discussed in the 269 malonamide simulation literature.^{18–20,44–49} The goal of the current discussion is to link the 270 equilibrium malonamide chemical structure to changes in self-association and then describe 271 how those changes lead to differences in the cluster size distribution, the characteristics of 272 the intermolecular interactions within an aggregate, and aggregate shape. 273

We begin by discussing the predicted and experimental solution structural features with 274 consideration of the ensemble distribution of equilibrium conformations. The unconstrained 275 malonamide conformation simulations allow the malonamide molecules to interconvert be-276 tween relative C=O orientations and Z/E conformational isomers. The time evolution of 277 the spatial distribution of molecules, demonstrating equilibration of resulting solution struc-278 ture across scale is presented in Figure S6. Electronic structure calculations show that the 279 gas phase electronic energy of the trans conformation is about 3 kcal/mol more favorable 280 than the gauche conformation. $^{39-41}$ For condensed phase simulations with dipole-dipole self-281 associating malonamides, we expect the *gauche* conformation to be more favorable than in 282 the gas phase.³⁹ As shown in Table 3, the fraction of malonamides in the *trans* conformation 283 in the equilibrium simulations is consistent with this expectation. Similarly, the fraction of Z 284 conformational isomers is consistent with the approximately 2:1 ratio from NMR for similar 285 systems.⁴² 286

In prior work we have described how organic phase structure—as observed in small angle scattering—stems from electron density heterogeneities introduced by dipole-dipole association, even in the absence of a reverse micellar structure as presumed in the literature.²⁶ The simulations in this work are consistent with the concentration dependent solution structure

Table 3: Thermophysical and conformational properties for each equilibrated system. The total density of each system is reported. For malonamides, their concentration, average molecular dipole, self-diffusion coefficient and configurational descriptors are given.

Malonamide	Conc.	Dipole	Density	D	Fraction	Fraction
type	[mol/L]	(debye)	(g/cm^3)	$(\times 10^{-6} {\rm cm}^2 {\rm /s})$	Z	trans
DMDOHEMA	0.5	3.84	816.5	0.28	0.75	0.72
DMDOHEMA	1.1	3.57	861.0	0.10	0.76	0.81
DMDOHEMA	1.5	3.46	889.9	0.05	0.76	0.85
DMDBTDMA	0.5	2.03	810.9	0.39	0.80	0.99
DMDBTDMA	1.1	2.32	846.5	0.12	0.78	0.94
DMDBTDMA	1.5	2.79	870.2	0.06	0.79	0.85

measured with SAXS: experimental SAXS data are compared to the SAXS profiles computed from the simulation trajectories in Figure S7, with details on experimental methodology and simulation-calculated scattering profiles provided in Servis et al.²⁶. Correlation peak positions and relative intensities are all well reproduced.

The CC-CC RDF has been reported from prior simulations of DMDOHEMA and DMDBT-295 DMA (in n-heptane),¹⁹ but the relative peak positions are substantially different from those 296 reported here, as shown with that data plotted with data from this study in Figure 3. This 297 differences in CC-CC RDFs between the unconstrained simulations in this work and the 298 prior RDFs can be entirely explained by differences in conformation. Despite being modeled 299 with the OPLS force field (versus GAFF used here), the prior simulation the malonamide 300 were fixed in the *qauche* C=O vector configuration with all E conformational isomerization. 301 Presumably, the larger O–C–N–Me torsion barrier in the OPLS force field implemented 302 in the prior study¹⁹ fixed the internal geometry of the malonamide molecules to the initial 303 uniform conformation and did not allow for equilibration of the conformational isomers. This 304 is consistent with visual inspection of snapshots provided by Qiao et al.¹⁹. Visual inspec-305 tion of other reported MD simulations which do not provide diagnostic data, such as the 306 CC-CC RDF or molecular dipole, also indicate the same conformation for all malonamide 307 molecules.^{18–20,44–49} Importantly, the restricted sampling of conformational isomers also im-308 pacts other characterization probes of solution structure, like SAXS. As observed in Figures 309

S8-S9, in comparison to experiment, the constrained simulation of the *gauche* all E conformational isomers have a demonstrable variation whereas the equilibrium simulations are in much better agreement.

This important observation points to the necessity of testing the energetic characteristics 313 of intramolecular potentials of the relevant conformational degrees of freedom in structurally 314 complex amphiphiles so as to ensure proper ergodic sampling. The fact that the malonamides 315 in this study are able to interconvert over simulation-accessible length scales, and therefore 316 sample more than the single initial configuration, lends confidence to the molecular model em-317 ployed. Given that we demonstrate the strong sensitivity of self-association to malonamide 318 conformation and the response of malonamide conformation to its local environment—as 319 demonstrated by its concentration dependence—future simulation studies should treat mal-320 onamide conformation carefully to avoid generating configurational ensembles which simply 321 reproduce the initial configuration. 322

Moving on to a more detailed study of the equilibrium distribution of conformations 323 as a function of concentration (Table 3), we first consider the relative orientation of asso-324 ciating malonamides. The probability density function of the angle, $P(\theta)$, normalized by 325 $\sin(\theta)$, are plotted in Figure 5 at each concentration. At 0.5 M, neither malonamide shows 326 a strong orientational preference: the large fraction of trans C=O vectors for DMDBTDMA 327 reduces the molecular dipole driver for strong orientational preference while DMDOHEMA 328 sterics—discussed below—prevent their strong alignment. At higher concentration, where 329 more *qauche* conformations are present for DMDBTDMA, a noticeable orientational prefer-330 ence emerges for *qauche* alignment, corresponding to values of θ near 0°. While it is intuitive 331 that dipole alignment is weak for the low-dipole trans C=O conformation, this does not ex-332 plain why only DMDBTDMA shows dipole alignment at high concentration—DMDOHEMA 333 has a larger molecular dipole and the same fraction of trans C=O vectors at 1.5 M. The 334 impact of the relative C=O orientation on molecular dipole is clear: the approximately 335 qauche configuration, where the carbonyl dipoles are more aligned compared to the trans 336

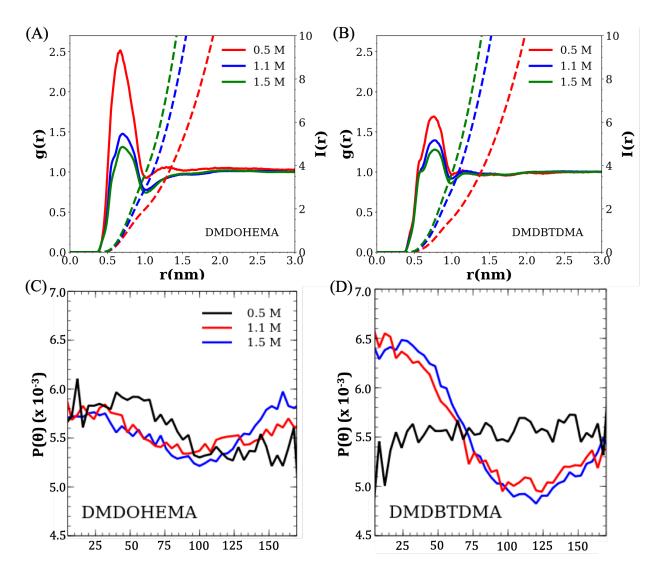


Figure 5: The CC-CC radial distribution functions are plotted for (A) DMDOHEMA and (B) DMDBTDMA for all systems. Line color corresponds to malonamide concentration. Probability distribution of the angle θ between molecular dipoles under constrained simulation conditions for (C) DMDOHEMA and (D) DMDBTDMA. The relative malonamide orientation is defined as the angle between two vectors: the bisector of the O-CC-O angle for each molecule, where the O atoms sites are the O-atoms of the two amide groups. The probability density function of the angle, P(θ), is normalized by sin(θ).

³³⁷ configuration, results in a larger average molecular dipole.

Relating this to the CC-CC RDFs, clearly points to a correlation of the aligned dipoles 338 with increased malonamide self-association. At low concentration, DMDOHEMA shows 339 higher self-association than DMDBTDMA, which is largely explained by the increased propen-340 sity of DMDOHEMA for the *qauche* configuration. The conformational isomerization has, 341 as expected, a smaller impact on the molecular dipole. The fraction of amide groups in the 342 Z conformation is largely constant between malonamides and the concentrations and are 343 close to the experimentally determined value of approximately two thirds.⁴² The difference 344 in association, as indicated by the RDFs decreases with increasing concentration. This trend 345 is explained by the difference in molecular dipole between the two molecules and between 346 concentrations, as shown in Table 3. At low concentration, the difference in dipole between 347 DMDOHEMA and DMDBTDMA is largest (3.84 vs. 2.03 debye, respectively), while at 348 higher concentrations the difference is reduced. 349

Cluster Characteristics. Given the impact of chemical structure on the relative orienta-350 tion of associating malonamides, the effect of that orientation on aggregate size, connectivity 351 of intermolecular interactions, and shape is investigated. First, aggregates are quantified by 352 clustering analysis. As we previously reported for different concentrations and malonamide 353 types, and evidenced by the malonamide cluster size distributions in Figure 6, there is no 354 characteristic size for aggregate formation at 0.5 M: the cluster sizes follow an approximately 355 power law distribution. At higher concentrations, most malonamide molecules belong to a 356 single system-spanning cluster.²⁶ As one might anticipate from studying the number of con-357 nected components β_0 within the persistent homology, increasing the concentration of the 358 malonomides causes sharper decreases to β_0 as a function of the diameter, consistent with 359 the formation of a system spanning cluster. At a diameter of 1 nm within the 0.5 M solu-360 tions, 28 % of all connected components remain for DMDOHEMA, whereas 40 % remain for 361 DMDBTDMA. Yet at 1.5 M concentration only 2 - 3 % of all components remain for both 362

malonomides. More than 99 % of the original number of components have been merged into
a single simplicial complex at 1.2 nm for both systems.

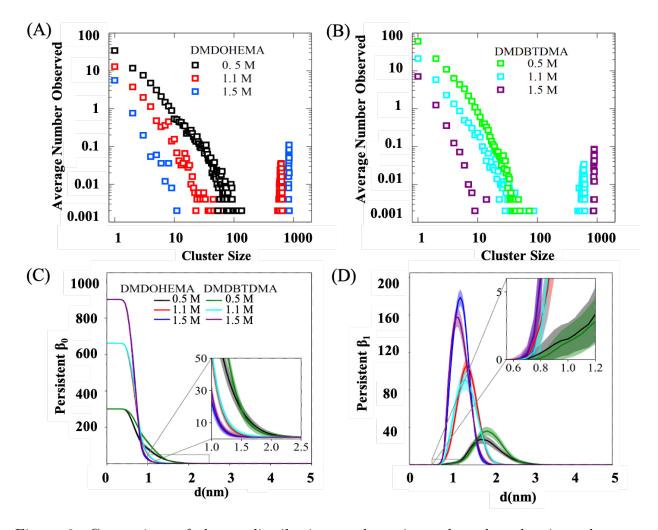


Figure 6: Comparison of cluster distributions and persistent homology betti numbers at 0.5, 1.1, and 1.5 M DMDOHEMA or DMDBTDMA. (A) The cluster size distributions of DMDOHEMA. (B) The cluster size distribution of DMDBTDMA. (C) The variation of average persistent β_0 betti number (and β_1) with the increasing filtration value as a function of concentration of DMDBTDMA and DMDOHEMA ligands. (D) The variation of average persistent β_1 betti number with the increasing filtration value as a function of DMDBTDMA and DMDOHEMA. Note that the error bar in the plot indicates the standard deviation of persistent betti numbers of all the frames within the window of 0.5 Å.

Relationships Between Intermolecular Interactions and Spatial Distribution. The organization within aggregates was quantified both in terms of the intermolecular interactions as well as spatial distribution. First, we quantify the topology of the intermolecular

network of interactions using the global clustering coefficient, which is averaged over all 368 clusters of a given size, plotted in Figure 7. Snapshots in Figure S5 show example 5-mer 369 clusters for DMDOHEMA and DMDBTDMA with global clustering coefficients of 1/3 and 370 1/5, respectively. First, we note that the clustering coefficient is largely consistent across 371 the range of observed cluster sizes for each system. This is consistent with the observed lack 372 of characteristic aggregate size: there is no fundamental, dramatic change in the topology 373 of the intermolecular network of interactions across different discrete cluster sizes and, sim-374 ilarly, no fundamental difference in network structure between the discrete clusters and the 375 dense, spanning clusters. 376

For each system, for all cluster sizes, the global clustering coefficient is lower for DMDBT-377 DMA than DMDOHEMA. This indicates that the network of individual DMDOHEMA 378 interactions more readily forms branch points within clusters, leading to more highly inter-379 connected aggregates. The clustering coefficients, averaged from cluster sizes from 3 to 50 380 (monomers and dimers do not contain triplets) with error reported as the standard deviation 381 between those cluster sizes, are 0.34 ± 0.02 for DMDOHEMA and 0.25 ± 0.03 for DMDBT-382 DMA. The trends in clustering coefficients are independent of edge definition. Choosing 383 a 0.77 nm CC-CC cutoff distance for malonamide connectivity (corresponding only to the 384 shoulder rather than the entire nearest neighbor peak) yields the same trend in clustering 385 coefficient, with average values of 0.13 ± 0.015 for DMDOHEMA and 0.091 ± 0.027 for 386 DMDBTDMA. These values are averaged are over 3- to 15-mers, given the lower overall 387 clustering with the smaller cutoff, and the magnitude of the values are similarly reduced due 388 to the reduction in the total number of edges. This trend is observed for the constrained 389 *gauche* simulations as well, with 0.41 ± 0.03 and 0.35 ± 0.05 for the constrained *gauche* DM-390 DOHEMA and DMDBTDMA, respectively. Therefore, the clustering coefficient is sensitive 391 to the different tail structures of the two malonamides regardless of conformation. It should 392 also be noted that the clustering coefficient is not simply the result of linear orientation, but 393 is naturally increased by more overall association: the constrained *qauche* simulations, hav-394

³⁹⁵ ing overall higher molecular dipoles and more malonamide self-association, as seen in Figure ³⁹⁶ 3, show larger clustering coefficients. Therefore, the differences in clustering coefficient from ³⁹⁷ tail structure should not be conflated with the differences from overall increased associated ³⁹⁸ from conformation. Indeed, the difference between unconstrained and constrained *gauche* ³⁹⁹ DMDBTDMA is roughly the same as the difference between unconstrained DMDBTDMA ⁴⁰⁰ and unconstrained DMDOHEMA. This highlights the sensitivity, and therefore utility, of the ⁴⁰¹ clustering coefficient to distinguish both conformational and alkyl tail structural differences.

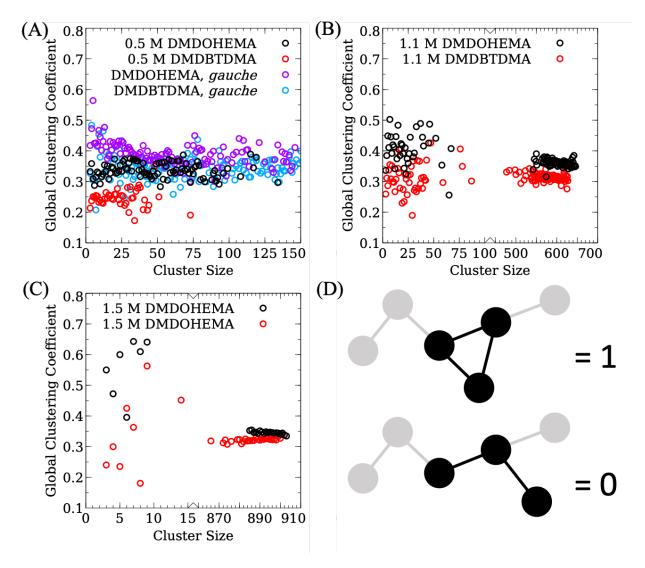


Figure 7: The global clustering coefficient is plotted as a function of cluster size for both malonamides for each concentration: (A) 0.5 M, (B) 1.1 M and (C) 1.5 M. (D) Illustration of two triplets within 6-mer clusters shows the contribution of those triplets to the global clustering coefficient.

Complementary to the clustering coefficient is the geodesic length of the intermolecular 402 interactions within an aggregate, which contains information about how extended the struc-403 ture is of the aggregate networks. This feature is quantified by the maximum shortest path 404 (or maximum geodesic). The maximum geodesic is averaged over all clusters of a given size, 405 and plotted in Figure 8 as a function of cluster size. The maximum shortest path lengths 406 for the constrained *qauche* simulations are plotted in Figure S10. Due to the relatively small 407 total path length differences between malonamides, the difference between path length val-408 ues is plotted for the 0.5 M simulations. For the 0.5 M simulations, DMDBTMDA show, on 409 average, larger maximum path lengths compared to DMDOHEMA. 410

The relationship between intermolecular network topology and spatial distribution is not 411 always straightforward. As a metric of overall size of aggregates, the difference in cluster 412 radius of gyration, R_g, is plotted in Figure S11 to quantify the difference in real space com-413 pactness of DMDBTDMA versus DMDOHEMA aggregates. The maximum geodesic and R_g 414 difference between DMDOHEMA and DMDBTDMA track closely over the range of cluster 415 sizes, which indicates that in this system the differences between malonamides in geodesic 416 distance are reflective of analogous differences in the overall spatial extent of an aggregate: 417 longer topological path lengths correspond to larger distances in real space. At high malon-418 amide concentration, where a system-spanning cluster dominates, the maximum path length 419 of that spanning cluster—while dependent on system size and malonamide concentration, 420 both of which are fixed here—is smaller for DMDOHEMA than DMDBTDMA. Therefore, 421 the dipole and steric influences that create the more linear DMDBTDMA clusters are lower 422 concentration also determine the structure of the densely packed malonamide network at 423 high concentration. Complementing this perspective, the β_1 distribution reflects the spatial 424 distribution and presence of holes or voids amongst groups of components across lengthscale 425 (Figure 4). At 0.5 M, the β_1 number distribution retains some of the bimodal characteristics 426 apparent within the constrained simulations, where the higher average dipole moment of 427 DMDOHEMA (3.84 D) than DMDBTDMA (2.03 D) correlates with the growth of β_1 holes 428

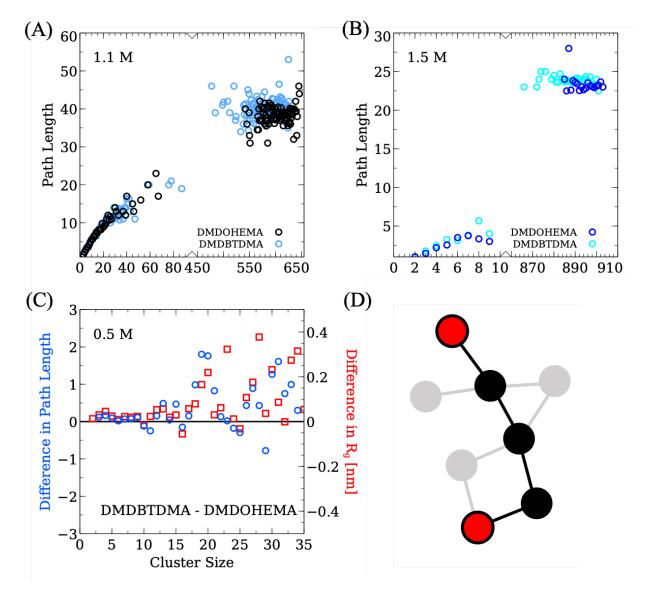


Figure 8: The average value of the maximum shortest path is plotted as a function of cluster size for (A) 1.1 and (B) 1.5 M malonamide simulations. (C) The difference between maximum shortest path lengths for the 0.5 M DMDBTDMA and DMDOHEMA systems is plotted (blue circles, left axis) along with the difference in cluster radius of gyration, R_g (red squares, right axis). (D) One of the possible maximum shortest paths (between red nodes, connected by black lines and black nodes) for an example cluster.

at smaller distances. However as the concentration is increased the distribution becomes 429 unimodal. Concomitant to the smaller differences of dipole moments between the ligands 430 at higher concentration, the growth of β_1 holes becomes more and more similar for both 431 the ligands. Further, with higher concentration β_1 distribution peak gets shifted to smaller 432 distance as a results of the dense packing of molecules that partially overcomes the steric 433 factors observed at 0.5 M (where holes form at larger distances). Another distinct feature of 434 these β_1 distributions is the associated peak height: at higher concentration DMDOHEMA 435 has larger peak height when compared with DMDBTDMA, suggesting generation of more 436 number of 1D holes for the former. This essentially reflects more organized circular order-437 ing or "swiss cheese" structures in case of DMDOHEMA, and therefore nicely corroborates 438 with the finding of geodesic analysis that suggested a more linearly connected DMDBTDMA 439 aggregates as compared to DMDOHEMA. 440

441 4 Conclusions

Amphiphile self-association in non-polar media is of significant importance to a number of 442 applications, not the least of which is liquid-liquid extraction. A significant opportunity 443 exists to understand how molecular-scale conformation and architecture influences not only 444 aggregate size distributions, but also morphology across scale-from local aggregation to the 445 aggregate-aggregate interactions that occur at high concentrations. Using representative 446 DMDOHEMA and DMDBTDMA malonomide extractants (commonly applied to f-element 447 separations), this work clearly demonstrates that self-association and multiscale solution or-448 ganization are driven by a balance between dipole alignment and alkyl tail sterics. Those 449 forces are significantly impacted by malonamide conformation and alkyl tail molecular struc-450 ture. This is the first simulation study to compare and contrast the impact of malonamide 451 conformation and, to the best of our knowledge, the first to use potentials which do not 452 incidentally constrain malonamides to their initial conformation. 453

The self-association driven by strong dipole alignment informs the resulting aggregation 454 topology, as evidenced from detailed graph theoretical and persistent homology analyses. 455 The lower clustering coefficients and larger geodesic path lengths for DMDBTDMA ag-456 gregates relative to DMDOHEMA show that DMDBTDMA forms more linear, less highly 457 interconnected clusters than DMDOHEMA; this in turn influences longer range solution 458 structure as measured by the β_0 and β_1 distributions from persistent homology. While the 459 linearity of DMDBTDMA aggregation compared to DMDOHEMA has been inferred from 460 small angle scattering in the literature,¹⁹ this graph theoretic and persistent homology ap-461 proach provides a molecular basis for the emergent self-assembly organization. Importantly, 462 the linearity of DMDBTDMA aggregates relative to DMDOHEMA is solely due to self-463 association in the absence of any extracted aqueous solutes or micellization. Therefore, this 464 property is inherent to the malonamide/alkane mixture and not necessarily a reflection of 465 micelle morphology. Having explained the underlying dipole alignment and steric balance 466 that underpins the morphology of malonamide aggregates and aggregate-aggregate interac-467 tions, we have provided a direct link between the conformation and molecular structure of 468 the malonamide to its resulting solution mesostructure. 469

470 5 Acknowledgments

⁴⁷¹ This work was supported by the U.S. Department of Energy (DOE), Basic Energy Sci⁴⁷² ences, Chemical Sciences, Geosciences, and Biosciences Division under contract DEAC02⁴⁷³ 06CH11357. This research used resources from the Center for Institutional Research Com⁴⁷⁴ puting at Washington State University.

475 References

(1) Zhang, X.; Wang, C. Supramolecular amphiphiles. *Chemical Society Reviews* 2011, 40,
94–101.

- (2) Yamada, Y. M.; Sarkar, S. M.; Uozumi, Y. Amphiphilic self-assembled polymeric copper
 catalyst to parts per million levels: click chemistry. *Journal of the American Chemical Society* 2012, *134*, 9285–9290.
- (3) Kabanov, A. V.; Kabanov, V. A. Interpolyelectrolyte and block ionomer complexes for
 gene delivery: physico-chemical aspects. Advanced Drug Delivery Reviews 1998, 30,
 483 49–60.
- (4) Shimizu, T.; Masuda, M.; Minamikawa, H. Supramolecular nanotube architectures
 based on amphiphilic molecules. *Chemical Reviews* 2005, 105, 1401–1444.
- (5) Wang, Y.; Xu, H.; Zhang, X. Tuning the amphiphilicity of building blocks: controlled
 self-assembly and disassembly for functional supramolecular materials. Advanced Ma *terials* 2009, 21, 2849–2864.
- (6) Molla, M. R.; Ghosh, S. Aqueous self-assembly of chromophore-conjugated amphiphiles.
 Physical Chemistry Chemical Physics 2014, *16*, 26672–26683.
- (7) Rydberg, J.; Cox, M.; Musikas, C.; Choppin, G. Solvent Extraction Principles and
 Practices, 2nd ed.; Marcel Dekker: New York, 2004.
- (8) Bourgeois, D.; El Maangar, A.; Dourdain, S. Importance of weak interactions in the
 formulation of organic phases for efficient L/L extraction of metals. *Current Opinion in Colloid & Interface Science* 2020,
- (9) Dozol, H.; Berthon, C. Characterisation of the supramolecular structure of malonamides
 by application of pulsed field gradients in NMR spectroscopy. *Physical Chemistry Chem- ical Physics* 2007, 9, 5162–5170.
- (10) Meridiano, Y.; Berthon, L.; Crozes, X.; Sorel, C.; Dannus, P.; Antonio, M. R.;
 Chiarizia, R.; Zemb, T. Aggregation in Organic Solutions of Malonamides: Consequences for Water Extraction. *Solvent Extraction and Ion Exchange* 2009, *27*, 607–637.

29

(11) Erlinger, C.; Gazeau, D.; Zemb, T.; Madic, C.; Lefrancois, L.; Hebrant, M.; Tondre, C. Effect of nitric acid extraction on phase behavior, microstructure and interactions between primary aggregates in the system dimethyldibutyltetradecylmalonamide
(DMDBTDMA)/n-dodecane/water: A phase analysis and small angle X-ray scattering (SAXS) characterisation study. *Solvent Extraction and Ion Exchange* 1998, *16*, 707–738.

- (12) Erlinger, C.; Belloni, L.; Zemb, T.; Madic, C. Attractive interactions between reverse ag gregates and phase separation in concentrated malonamide extractant solutions. *Lang- muir* 1999, 15, 2290–2300.
- (13) Dozol, H.; Berthon, C. Characterisation of the supramolecular structure of malonamides
 by application of pulsed field gradients in NMR spectroscopy. *Phys. Chem. Chem. Phys.* **2007**, *9*, 5162–5170.
- (14) Bauduin, P.; Testard, F.; Berthon, L.; Zemb, T. Relation between the hydrophile/hydrophobe ratio of malonamide extractants and the stability of the organic
 phase: Investigation at high extractant concentrations. *Physical Chemistry Chemical Physics* 2007, 9, 3776–3785.
- (15) Abécassis, B.; Testard, F.; Zemb, T.; Berthon, L.; Madic, C. Effect of n-octanol on
 the structure at the supramolecular scale of concentrated dimethyldioctylhexylethoxymalonamide extractant solutions. *Langmuir* 2003, 19, 6638–6644.
- (16) Ellis, R. J.; D'Amico, L.; Chiarizia, R.; Antonio, M. R. Solvent Extraction of
 Cerium(III) Using an Aliphatic Malonamide: The Role of Acid in Organic Phase Be haviors. Separation Science and Technology 2012, 47, 2007–2014.
- (17) Ellis, R. Critical Exponents for Solvent Extraction Resolved Using SAXS. Journal of
 Physical Chemistry B 2014, 118, 315–322.

- (18) Ferru, G.; Rodrigues, D.; Berthon, L.; Diat, O.; Bauduin, P.; Guilbaud, P. Elucidation
 of the Structure of Organic Solutions in Solvent Extraction by Combining Molecular
 Dynamics and X-ray Scattering. Angewandte Chemie 2014, 53, 5346–5350.
- (19) Qiao, B.; Littrell, K. C.; Ellis, R. J. Liquid worm-like and proto-micelles: water solubilization in amphiphileoil solutions. *Physical Chemistry Chemical Physics* 2018, 20, 12908–12915.
- Guilbaud, P.; Zemb, T. Depletion of water-in-oil aggregates from poor solvents: Transition from weak aggregates towards reverse micelles. *Current Opinion in Colloid & Interface Science* 2015, 20, 71–77.
- Servis, M. J.; Piechowicz, M.; Soderholm, L. Impact of Water Extraction on Mal onamide Aggregation: A Molecular Dynamics and Graph Theoretic Approach. *The Journal of Physical Chemistry B* 2021, *125*, 6629–6638.
- (22) Baldwin, A.; Servis, M.; Yang, Y.; Bridges, N.; Wu, D.; Shafer, J. The Structure of
 Tributyl Phosphate Solutions: Nitric Acid, Uranium (VI), and Zirconium (IV). Journal
 of Molecular Liquids 2017, 246, 225–235.
- (23) Nash, K.; Braley, J. Advanced Separation Techniques for Nuclear Fuel Reprocessing
 Waste Treatment; Woodhead Publishing Series in Energy: Cambridge, UK, 2011;
 Chapter Chemistry of Radioactive Materials in the Nuclear Fuel Cycle, pp 3–22.
- ⁵⁴⁴ (24) Abraham, M.; Murtol, T.; Schulz, R.; Pall, S.; Smith, J.; Hess, B.; Lindhal, E. GRO ⁵⁴⁵ MACS: High performance molecular simulations through multi-level parallelism from
 ⁵⁴⁶ laptops to supercomputers. SoftwareX 2015, 1-2, 19–25.
- ⁵⁴⁷ (25) Wang, J.; Wolf, R.; Caldwell, J.; Kollman, P.; Case, D. Development and testing of a
 ⁵⁴⁸ general amber force field. *Journal of Computational Chemistry* 2004, 25, 1157–1174.

- (26) Servis, M. J.; Piechowicz, M.; Shkrob, I. A.; Soderholm, L.; Clark, A. E. Amphiphile
 Organization in Organic Solutions: An Alternative Explanation for Small-Angle X-ray
 Scattering Features in Malonamide/Alkane Mixtures. *The Journal of Physical Chem*-*istry B* 2020, *124*, 10822–10831, PMID: 33200612.
- ⁵⁵³ (27) Hockney, R. W.; Goel, S. P.; Eastwood, J. Quiet High Resolution Computer Models of
 ⁵⁵⁴ a Plasma. Journal of Computational Physics 1974, 148–158.
- (28) Hess, B.; Bekker, H.; Berendsen, H.; Fraaije, J. LINCS: A constrained solver for molecular simulations. *Journal of Computational Chemistry* 1997, 18, 1463–1472.
- ⁵⁵⁷ (29) Darden, T.; York, D.; Pedersen, L. An N·log(N) method for Ewald sums in large sys⁵⁵⁸ tems. Journal of Chemical Physics 1993, 10089–10092.
- (30) Berendsen, H.; Postma, J.; van Gunsteren, W.; DiNola, A.; Haak, J. Molecular dynamics with coupling to an external bath. *Journal of Chemical Physics* 1984, *81*, 3684.
- (31) Hoover, W. Canonical dynamics: Equilibrium phase-space distributions. *Physical Re- view A* 1985, *31*, 1695–1697.
- ⁵⁶³ (32) Wilson, R. J. Introduction to Graph Theory; Oliver and Boyd, Edinburgh, 1972.
- (33) Carlsson, G. Topology and data. Bulletin of the American Mathematical Society 2009,
 46, 255–308.
- ⁵⁶⁶ (34) Edelsbrunner, H.; Harer, J. L. Computational Topology An Introduction; American
 ⁵⁶⁷ Mathematical Society, 2009.
- (35) Ghrist, R. Barcodes: The persistent topology of data. Bulletin of the American Math *ematical Society* 2008, 45, 61–75.
- (36) Xia, K. Persistent homology analysis of ion aggregations and hydrogen-bonding net works. *Physical Chemistry Chemical Physics* 2018, 20, 13448–13460.

32

- ⁵⁷² (37) Edelsbrunner, H.; Letscher, D.; Zomorodian, A. Topological persistence and simplifica⁵⁷³ tion. Discrete and Computational Geometry 2002, 28, 511–533.
- (38) Munkres, J. R. *Elements of Algebraic Topology*; Addison–Wesley Publishing Company:
 Menlo Park, 1984; pp ix+454.
- (39) Diss, R.; Wipff, G. Lanthanide cation extraction by malonamide ligands: from liquid–
 liquid interfaces to microemulsions. A molecular dynamics study. *Physical Chemistry Chemical Physics* 2005, 7, 264–272.
- (40) Sandrone, G.; Dixon, D. A.; Hay, B. P. Conformational Analysis of Malonamide, N,
 N -Dimethylmalonamide, and N, N, N , N -Tetramethylmalonamide. *The Journal of Physical Chemistry A* 1999, *103*, 3554–3561.
- (41) Lumetta, G. J.; Rapko, B. M.; Garza, P. A.; Hay, B. P.; Gilbertson, R. D.; Weakley, T. J.; Hutchison, J. E. Deliberate design of ligand architecture yields dramatic
 enhancement of metal ion affinity. *Journal of the American Chemical Society* 2002, *124*, 5644–5645.
- (42) Lefrançois, L.; Delpuech, J. J.; Hébrant, M.; Chrisment, J.; Tondre, C. Aggregation
 and protonation phenomena in third phase formation: An NMR study of the quaternary malonamide/dodecane/nitric acid/water system. *Journal of Physical Chemistry B* 2001, 105, 2551–2564.
- (43) Servis, M. J.; Piechowicz, M.; Skanthakumar, S.; Soderholm, L. Molecular-scale origins
 of solution nanostructure and excess thermodynamic properties in a water/amphiphile
 mixture. *Physical Chemistry Chemical Physics* 2021, 23, 8880–8890.
- (44) Qiao, B.; Demars, T.; Olvera de la Cruz, M.; Ellis, R. J. How hydrogen bonds affect
 the growth of reverse micelles around coordinating metal ions. *The Journal of Physical Chemistry Letters* 2014, 5, 1440–1444.

- ⁵⁹⁶ (45) Ellis, R.; Meridiano, Y.; Muller, J.; Berthon, L.; Guilbaud, P.; Zorz, N.; Antonio, M.;
 ⁵⁹⁷ Demars, T.; Zemb, T. Complexation-Induced Supramolecular Assembly Drives Metal⁵⁹⁸ Ion Extraction. *Chemistry: A European Journal* 2014, 20, 12796–12807.
- (46) Chen, Y.; Duvail, M.; Guilbaud, P.; Dufrêche, J.-F. Stability of reverse micelles in rare earth separation: a chemical model based on a molecular approach. *Physical Chemistry Chemical Physics* 2017, 19, 7094–7100.
- (47) Duvail, M.; van Damme, S.; Guilbaud, P.; Chen, Y.; Zemb, T.; Dufrêche, J. The
 role of curvature effects in liquid-liquid extraction: assessing organic phase mesoscopic
 properties from MD simulations. Soft Matter 2017, 13, 5518–5526.
- (48) Qiao, B.; Ferru, G.; Ellis, R. J. Complexation Enhancement Drives Water-to-Oil Ion
 Transport: A Simulation Study. *Chemistry-A European Journal* 2017, 23, 427–436.
- (49) Duvail, M.; Dumas, T.; Paquet, A.; Coste, A.; Berthon, L.; Guilbaud, P. UO₂²⁺ structure
 in solvent extraction phases resolved at molecular and supramolecular scales: a combined molecular dynamics, EXAFS and SWAXS approach. *Physical Chemistry Chem- ical Physics* 2019, *21*, 7894–7906.