Understanding the effect of doping on the charging performance of the Li-O₂ battery: the role of hole polarons and lithium vacancies

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Abstract

In this work, we perform DFT calculations using the hybrid functional HSE to properly describe the insulating nature of lithium peroxide and study its more energetically favourable surfaces [0001], [1100] and [1120]. We then analyse how the insulating character and the correct description of the hole polarons at the Li₂O₂ surfaces affect the electrochemical steps of Li₂O₂ decomposition in the charging process of the Li-O₂ battery. We then study the effect of doping and propose possible scenarios in which
the ions as Na\(^+\) or K\(^+\) dissolved in the electrolyte can dope and promote Li vacancies generation in the Li\(_2\)O\(_2\) that, in turn, reduce the energy barrier of the limiting steps of the Li\(_2\)O\(_2\) decomposition. The origin of this reduction are the lattice distortions associated with doping that weaken the surface binding.

**Introduction**

The Li-O\(_2\) battery (LOB) is a promising energy storage system due to its exceptionally high theoretical energy density (\(\sim 3500\) Whkg\(^{-1}\)).\(^1\),\(^2\) However, the LOBs technology is still facing important challenges and limitations that have to be sorted out. Among them, there are the high charging potential that leads to low discharge/charge cycle efficiency, the reduced capacity at high discharge rates and the poor cathode and electrolyte stability.\(^2\),\(^3\)

The main discharge product of the LOB is Li\(_2\)O\(_2\) whose insulating character deeply affects various aspect of the battery.\(^2\),\(^4\),\(^5\) The dominant reversible reaction that takes place at the cathode of a non-aqueous Li-O\(_2\) cell is

\[
2\text{Li}^+ + 2e^- + O_2 \rightleftharpoons \text{Li}_2\text{O}_2. \tag{1}
\]

During the discharge of the battery, the oxygen from the air is reduced at the cathode and combines with a Li ion to form solid Li\(_2\)O\(_2\). During the recharge, the reverse decomposition of Li\(_2\)O\(_2\) occurs. The overpotential needed to recharge the battery determines its efficiency and depends on several factors that can have different origin. The source of the energy barriers originates in the intrinsic reversible reaction but also is affected by the morphology of the discharge product\(^2\),\(^6\) or the presence of side-reaction secondary phases.\(^5\),\(^7\)

A profound knowledge of the electronic and transport properties of Li\(_2\)O\(_2\) both in bulk and at the surface is crucial to understand the reversible reaction of Eq. 1 and to propose new routes to circumvent the above mentioned difficulties.

The charge transport through the bulk of Li\(_2\)O\(_2\) has been studied extensively by ex-
periments and theoretical calculations.\textsuperscript{8–13} Particularly, Gerbig \textit{et al.} observed the Li\textsubscript{2}O\textsubscript{2} insulating nature by impedance spectroscopy and DC conductivity measurements, showing that ionic lithium defects are the majority carriers while electronic conductivity is two order of magnitude smaller and of hole type. These results were confirmed later by Dunst \textit{et al.} by means of nuclear magnetic resonance spectroscopy.\textsuperscript{9} Independently, Ceder and coworkers showed, using Density Functional Theory (DFT) calculations with the Heyd-Scuseria-Ernzerhof (HSE) screened hybrid functional, that holes can be self-trapped at the peroxide sites (O\textsubscript{2}\textsuperscript{−2}) forming small hole polarons (O\textsubscript{2}\textsuperscript{−1}). Furthermore, they noted that the nonpolaronic structure, which present metallic states, has significantly higher energy than the polaronic one.\textsuperscript{11} Afterwards, Radin and Siegel, employing the same hybrid functional, concluded that the dominant charge carriers in bulk Li\textsubscript{2}O\textsubscript{2} are the lithium vacancies (V\textsubscript{Li}) and hole polarons, and that the inclusion of exact exchange at some extent is essential for achieving their correct description.\textsuperscript{13}

Li\textsubscript{2}O\textsubscript{2} surfaces have also been object of study as possible conduction paths during the operation of the cell. Previous theoretical reports have shown that the more energetically favourable surface of Li\textsubscript{2}O\textsubscript{2} under ambient conditions is metallic.\textsuperscript{14} These results were based on DFT calculations using functionals in the General Gradient Approximation (GGA). A metallic behaviour of the Li\textsubscript{2}O\textsubscript{2} surface would have deep consequences in the performance of the LOB since it could mitigate the electrical passivation of the cathode. Furthermore, the important role played by the Li\textsubscript{2}O\textsubscript{2} surfaces in the oxygen evolution reaction (OER) occurring during the recharge of the battery has also motivated experimental and theoretical research.\textsuperscript{15–19} Resorting to DFT calculations in the GGA approximation, Mo \textit{et al.} studied the energetics and the OER for different surface orientations.\textsuperscript{16} Afterwards, Hummels\textphi{j \textit{et al.} investigated the electrochemical mechanism of growth and dissolution over the [1\textbar100] Li\textsubscript{2}O\textsubscript{2} facet, the more stable one using the revised PBE functional (RPBE), analysing possible origins of the overpotential. Based on these RPBE calculations where the intermediate lithium vacancies in the OER reaction give rise to surface metallic states, they conclude that
the electron transport through the Li$_2$O$_2$ may not be a problem at the high potentials.$^{17}$

In view of the well known self-interaction error of the GGA functional, the result of the surface metallicity was revisited$^{20}$ using the HSE correction and even the scGW method.$^{20}$ Interestingly, the metallic behaviour that was also obtained for these corrected functionals, arises as an artifact due to a finite size effect of a small 1x1 unit cell that does not allow for surface reconstruction. In fact, calculations done later for larger supercells and proper functionals confirm that all the Li$_2$O$_2$ surfaces are insulating and that the only charge carrier conduction path available is the diffusion of defects$^{21}$ or through tunnelling in the case of thin films.$^{22}$ Considering the very high computational cost of HSE, specially for simulating large supercells, the DFT+U technique$^{23}$ was also used as an alternative to correct the underestimation of the electronic correlation characteristic of local or semilocal functionals as GGA.$^{12}$

After this winding road towards understanding the formation and decomposition of Li$_2$O$_2$ in the LOB, there is still some confusion in the literature regarding these fundamental issues that hinders future efforts to make progress in this promising technology and a clarification is urging.

With respect to the high charging overpotential, several strategies were proposed. Recently, Byon and coworkers showed that the nanostructuring of one-dimensional and amorphous Li$_2$O$_2$ can get an improve of the round-trip efficiency of the LOB of $\sim$ 80%. DFT calculations reveal that the structural distortions of the amorphous structure lead to a weaker binding of LiO$_2$, a key intermediate in the reaction, yielding smaller overpotentials in the delithiation process.$^{24}$

On the other hand, the Li$_2$O$_2$ doping has been reported as another potential strategy to improve the efficiency of the LOB.$^{25-30}$ However, the mechanisms of how the incorporation of heteroatoms in the Li$_2$O$_2$ can affect performance of the battery is still unclear. Experimentally, barium (Ba) was one of the heteroatoms considered, achieving a significant reduction in the charging overpotential. The authors ascribed this effect to an improvement in the
charge transport as a consequence of Ba incorporation in Li$_2$O$_2$.\textsuperscript{28} Afterward, Chen and coworkers showed that a LOB with Na-doped Li$_2$O$_2$ as a discharge product also presents a lower charge overpotential as compared to the undoped system, since the Na$^+$ as the dopant induces lithium vacancies, which according their DFT calculations, lead to conducting states in Li$_2$O$_2$.\textsuperscript{29} Nevertheless, in view of the above mentioned problems of self-interaction errors, this theoretical interpretation needs to be revised.

Quite recently, Chen and coworkers synthesized K-doped Li$_2$O$_2$, detecting an increment of O$_2^-$ sites and Li vacancies. Compared to the pristine Li$_2$O$_2$, the as-prepared defective Li$_2$O$_2$ was also shown to give rise to lower overpotentials during the OER. Additionally, they showed that there is a strong correlation between the OER kinetics and the O$_2^-$ density in the discharge products and that those O$_2^-$ sites highly contribute to the decrease of charge overpotential.\textsuperscript{30}

The available reported values of the calculated overpotentials present considerable dispersion and they sometimes match with the ones experimentally observed and sometimes not. As said before, the absolute value of this quantity depends on many factors. Some of them have to do with variables that not always are considered in the theoretical calculations such as the characteristic of the electrolyte, the presence of complex extended defects, the presence of undesired secondary products or particular of the experimental setup. Other factors of technical origin are directly related to the particular model considered to describe the discharge product. For instance, the theoretical overpotential value strongly depends on the exchange and correlation functional, on the supercell size, on the calculation of the oxygen molecule chemical potential and the criteria to correct the well known overbinding error of GGA functionals. Despite this, if all these technicalities are properly taken into account, we believe that DFT can still provide deep understanding of the underlying mechanism of the Li$_2$O$_2$ formation and decomposition in the LOB and it is a powerful tool to propose new routes to face the limitations of this promising technology.

In this work, we provide an insightful description of the electronic and structural prop-
erties of the more energetically favourable Li$_2$O$_2$ surfaces obtained with the HSE functional, modeling the supercell that allow for the polaron formation not only for in non-stoichiometric surfaces but also during all the electrochemical steps involved in the recharge of the battery. We study the effect of the insulating nature of the surface in the lithium peroxide decomposition and how doping can induce lower energy barriers to decrease the charging overpotential.

**Computational methods**

First-principle calculations are performed with the generalized gradient corrected approximation (GGA) by Perdew, Burke and Ernzerhof (PBE), as well as the hybrid functional by Heyd, Scuseria and Ernzerhof (HSE06), as implemented in the Vienna ab initio simulation package. A mixing coefficient $\alpha = 0.48$ is used for the HSE hybrid calculation, in order to reproduce the bandgap obtained with more accurate techniques as $G_0W_0$ and self-consistent GW. DFT+$U$ corrections within the VASP code have also been considered and analysed.

The Kohn–Sham equations are solved employing the projected augmented wave (PAW) method. The Li (2s) and O (2s, 2p) valence electrons are treated with a plane wave cutoff of 400 eV. The k-point meshes with the Monkhorst–Pack scheme for the [0001], [1100] and [1200] surface supercells are 3x6x1, 2x6x1 and 4x3x1, respectively.

The ionic relaxations of the internal positions of the slabs are performed for fixed lattice constants\(^1\) until residual forces are below 0.02 eV/Å, with a total energy precision of $10^{-6}$ eV.

The surfaces are simulated using a slab geometry of Li$_2$O$_2$ separated by a vacuum layer of 10 Å in the [0001], [1100], and [1120] directions. In some cases, it is necessary to duplicate the cell in one direction of the surface plane and remove selected lithium or oxygen atoms in order to attain different surface stoichiometries such as the oxygen rich (O-rich) and stoichiometric one (ST). The lithium rich stoichiometry is not considered in the present work because it is

\(^1\)The lattice parameters are obtained from a full cell relaxation using GGA with a cutoff of 600 eV, getting $a=3.16$ Å and $c=7.69$ Å in good agreement with previous calculations and experimental results.\(^{14,31}\)
more energetically unstable.\textsuperscript{21}

The surface energy, for \( T = 300 \text{ K} \) and \( P = 1 \text{ atm} \), can be calculated as:

\[
\gamma(T, P) = \frac{1}{2A} \left[ G^{\text{slab}}(T, P, N_{Li}, N_{O}) - \frac{1}{2} N_{Li} g_{\text{Li}_2\text{O}_2}^{\text{bulk}}(T, P) + (N_{Li} - N_{O})\mu_{O}(T, P) \right],
\]

(2)

where \( G^{\text{slab}} \) is the free energy of the surface supercell, \( A \) is the area of the exposed surface, \( N_{Li} \) and \( N_{O} \) are the numbers of Li and O atoms present in the slab, \( g_{\text{Li}_2\text{O}_2}^{\text{bulk}}(T, P) \) is the free energy per formula unit of bulk \( \text{Li}_2\text{O}_2 \) and \( \mu_{O}(T, P) \) are the chemical potentials of O in bulk \( \text{Li}_2\text{O}_2 \). We neglect vibrational contributions to the free energy of the condensed phases and approximate the free energies \( G^{\text{slab}} \) and \( g_{\text{Li}_2\text{O}_2}^{\text{bulk}}(T, P) \) with the DFT ground-state total energies \( E^{\text{slab}} \) and \( E_{\text{Li}_2\text{O}_2} \), respectively. The chemical potential of oxygen is set by assuming equilibrium with \( \text{O}_2 \) gas at ambient conditions. To correct the well known oxygen overbinding error, the same approach as in Ref. 13 was employed, obtaining a correction of 740 meV and 630 meV using GGA and HSE(\( \alpha = 0.48 \)), respectively.

We calculate the free energy of each electrochemical intermediate step during the recharge process of the battery, following the approach as outline in Ref. 17. It is assumed that the couple (\( \text{Li}^+ + e^- \)) is in equilibrium with bulk metallic Li; that the \( \text{O}_2 \) molecule in solution is in equilibrium with both, \( \text{O}_2 \) in the gas phase and \( \text{O}_2 \) adsorbed at the surface; that during the desorption of \( \text{Li}^+ \) ion at the cathode there is a coordinated \( \text{Li}^+ + e^- \) charge transfer and that the interactions of the surface species with the electrolyte can be ignored. Furthermore, we consider that the \( \text{Li}_2\text{O}_2 \) dissolution occurs mainly on the \( \text{Li}_2\text{O}_2 \) surface rather than near the cathode.

The free energy change between reaction steps is given by:

\[
\Delta G_n = [E_n - E_{n-1} + \Delta N_{Li}(\mu_{Li} - eU) + \Delta N_{O_2}\mu_{O_2}],
\]

(3)

where \( n \) represents an intermediate reaction step, \( E_n \) is the total energy of the configuration at the step \( n \), \( \Delta N_{Li} \) and \( \Delta N_{O_2} \) are the number of Li and O\(_2\) atoms that are removed from
the surface in the step $n$ respect to the step $(n - 1)$, and $eU$ is electron energy under the applied charging potential $U$.

**Results and discussion**

**Surface energy and electronic structure**

First, we calculate the surface energy and the electronic structure of the [0001], [1100] and [1120] facets with different stoichiometries, which were previously reported as the most stable ones.\textsuperscript{14,18,21} Figure 1 shows the crystal structure of the studied surfaces for the stoichiometric and oxygen rich situations (ST and O-rich) obtained with HSE. The formation of polarons occurs for the non-stoichiometric cases within HSE. Precisely, the lacking charge at the oxygen rich surfaces takes the form of hole polarons at certain dimers, that are sketched as purple bonded O$_2$ in Figure 1.

It can be observed that all the O-rich orientations calculated using HSE exhibit hole polarons at their surface layers. The non-compensated charge due to the missing Li atoms gets self-trapped at the surface O$_2$ dimers. On the other hand, the ST ones do not show this effect.

Table 1 presents the calculated surface energies corresponding to the cases shown in Figure 1, obtained for $T=300$ K and $P=1$ atm, using both GGA and HSE. The $\gamma$ energies are in good agreement with previous reports.\textsuperscript{14,21}

Table 1: Surface energies $\gamma$ of Li$_2$O$_2$ at 300 K and 1 atm, the * denoted the lowest surface energy within each method.

<table>
<thead>
<tr>
<th>Orientation</th>
<th>Termination</th>
<th>$\gamma^{GGA}$ [meV/Å$^2$]</th>
<th>$\gamma^{HSE}$ [meV/Å$^2$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>[0001]</td>
<td>O-rich-1</td>
<td>17.0*</td>
<td>50.8</td>
</tr>
<tr>
<td></td>
<td>ST-4</td>
<td>47.8</td>
<td>44.2</td>
</tr>
<tr>
<td>[1100]</td>
<td>O-rich-2</td>
<td>31.5</td>
<td>43.7</td>
</tr>
<tr>
<td></td>
<td>ST-3</td>
<td>33.5</td>
<td>37.5*</td>
</tr>
<tr>
<td>[1120]</td>
<td>O-rich-1</td>
<td>40.4</td>
<td>49.4</td>
</tr>
<tr>
<td></td>
<td>O-rich-2</td>
<td>34.3</td>
<td>50.4</td>
</tr>
</tbody>
</table>
From Table 1, it can be seen how GGA and HSE provide a qualitatively different thermodynamic description of the trend in the stability of the surfaces. Within GGA the most stable orientation is the [0001] O-rich-1 while within HSE it is the [1\bar{1}00] ST-3 one. The discrepancy between GGA and HSE arises from the fact that GGA is not able to correctly describe the localization of the non-compensated charge (the hole polarons) due to the intrinsic self-interaction error. The functional HSE partially corrects this error by adding a fraction of exact exchange and it is able to achieve the formation of hole polarons. These polarons have an elastic cost which rises the surface energy $\gamma$, therefore, it is expected that
the O-rich facets have higher $\gamma$ than the ST ones within HSE.

Figure 2: (Left) DOS calculated using GGA (black line) and HSE (solid red) projected to the whole 1st and 2nd layers of the surface [0001] O-rich-1, top and bottom panels, respectively. (Right) Crystal structure of the corresponding surface calculated within HSE.

Figure 2 shows the DOS calculated using GGA (black line) and HSE (solid red line) projected on the atoms of the 1st and 2nd layers of the [0001] O-rich-1 surface, top and bottom panels, respectively. As can be observed in the figure, according to GGA, this O-rich surface turns out to be metallic and with spin polarized oxygen $p$-states in the 1st layer. The same happens for the rest of the O-rich facets studied. This is a consequence of the tendency of the GGA functional to spuriously delocalize the charge, being in this case holes, since the number of O atoms is greater than the number of Li ones. On the other hand, the 2nd layer remains insulating with a band-gap similar to the obtained for the bulk.\textsuperscript{11,20,27} Conversely, the same surface calculated within HSE turns out to be insulating. In this case the holes get localized in the form of polarons, which structurally is evidenced by the reduction of bond-length in one of the surface dimer from $d_{o-o} = 1.47$ Å that is the bond-length for $O_2^-$ to $d_{o-o} = 1.31$ Å for $O_2^-$. The corresponding projected DOS shows that the polaron states lye in the band-gap of the 1st layer (solid red in Figure 2).

The polaron formation at the O-rich surface emerges as a consequence of a surface reconstruction, which in Ref. 14 was blocked by using a 1x1 supercell. Breaking the symmetry
using a 2x1 unit cell, the reconstruction is now possible and the polaron is stabilized being 30.3 meV/Å² more stable than the delocalized configuration. The same effect occurs for Li₂O₂ bulk, where the extra charge also prefers to be localized at the oxygen dimers.¹¹,¹³,²⁷

On the other hand, Figure 3 presents the DOS calculated within GGA (black line) and HSE (solid red) for the whole 1st and 2nd layers of the [1100] ST-3 surface, the one with the lowest γ using HSE. Unlike the O-rich surfaces, in the ST ones there are not extra charge that can be self-trapped to produce polarons. In this case, it can be observed an insulating behavior with both methods (GGA and HSE), and the same happens to all stoichiometric situations.

Non of the studied surfaces are metallic within HSE. These results confirm the strong insulating character of Li₂O₂, that is one of the main drawbacks of the LOB.

Figure 3: (Left) DOS calculated with GGA (black line) and HSE (solid red) of the whole 1st and 2nd layers of the surface [1100] ST-3. (Right) Crystal structure of the corresponding surface calculated with HSE.

**DFT+U corrections applied to Li₂O₂**

The DFT+U technique has been also used to study Li₂O₂ as a less computationally demanding method to correct the well known problems of the GGA functionals.

Previously, it has been reported that DFT+U calculations as implemented in the GPAW
code, are able to describe the stabilization of hole polarons in Li$_2$O$_2$ for physically relevant values of the Hubbard U parameter. However, as mentioned later in Ref. 34, care should be taken when applying DFT+U techniques to extended orbitals as the $p$ states. For instance, in the VASP code, the implemented DFT+U formalism is sensitive to the PAW augmentation radius that it might be smaller than the spatial extension of the orbital that one intends to correct. On the other hand, the GPAW implementation of the DFT+U reduces the effect of the augmentation radius dependence by normalizing the integral of the projected atomic orbitals within the augmentation sphere, scaling the corresponding overlaps accordingly.

In this work, we aim to assess the effect of the DFT+U correction as implemented in the widely used VASP code when applied to extended $p$-states as the ones present in Li$_2$O$_2$. For this, we vary the U parameter between 0 and 16 eV in order to observe the effect of the Hubbard correction on the crystalline and electronic structure for Li$_2$O$_2$ bulk and its more stable surfaces.

Since the final conclusion of this assessment is that applying the U correction to the extended $p$-states of lithium peroxide gives rise to unrealistic situations, we present the whole analysis in the Supplementary Information (SI) material and summarise here the main findings.

From the bulk calculation, it is observed that the DFT+U correction is not able to reproduce the band-gap value of other more precise calculation techniques such as HSE or scGW. Furthermore, it is shown that a minimum value of U = 8 eV is necessary to stabilize the hole polarons and avoid spurious metallic solutions. In turn, these unphysical large values of U affect dramatically the formation energy and migrations barriers of the intrinsic defects, which could lead to wrong interpretations of the charge transport in the Li$_2$O$_2$. Regarding the calculations of the Li$_2$O$_2$ surface energies, the thermodynamic description obtained with DFT+U is different from that obtained with both GGA and HSE. This difference could be ascribed to the artificial reconstructions induced by the high U required to stabilize the polaron.
From a technical point of view, our calculations indicate that the DFT+U correction as implemented in the VASP code, is not appropriate for correcting GGA deficiencies in Li$_2$O$_2$. From now on, we continue presenting the results obtained with HSE in comparison with GGA.

**Li$_2$O$_2$ decomposition during the charging process**

Now we discuss the reaction energy profile of the OER for the surface with the lowest $\gamma$ according to HSE, the [1100] ST-3. The reaction free energy was calculated using Eq. 3. Figure 4 shows the results obtained for a potential $U=0$V, using the GGA (black line) and HSE (red line) functionals. First of all, at $U=0$V, as expected, the whole reaction is endothermic. In both methods, the initial step in the reaction path is the formation of a lithium vacancy ($V_{Li}$). Within GGA the extra charge left behind by $V_{Li}$ is wide spread along the surface, the surface turns metallic in this step. See the corresponding DOS in Figure S5 in the SI file. On the contrary, a hole gets trapped at a surface O$_2$ dimer within HSE, forming a polaron. This step has a higher energy barrier within HSE than within GGA, since the former functional leads to an extra elastic cost. The polarons are again schematized as purple bonded O$_2$ dimers in the insets of Figure 4. The second step is the formation of a second $V_{Li}$ that gives rise to another polaron within HSE whereas within GGA more metallic states are generated (see Figure S5 in the in SI file). In general, the second $V_{Li}$ has a lower formation energy than the first one because the surface structure was already distorted by the first vacancy; the system is less bound. The subsequent two reaction steps are the liberation of two LiO$_2$. It is important to remark that these steps present a higher energy barrier for the functional GGA. The reason for this is that the energy cost is comparatively larger within GGA due to the overbinding energy of the delocalized charge. On the other hand, within HSE the system gets rid of the elastic cost of one polaron in each of the last two steps so that the final reaction free energy turns out to be smaller than within GGA.
Figure 4: Reaction free energy diagram during OER calculated with GGA (black line) and HSE (red line), at U= 0V. Lithium in dark gray (bulk) and light green (to be removed); oxygen dimer in bulk (dark gray), to be removed (light red) and the O$_2^-$ (light purple).

In particular, the last step is the limiting one and will determine the value of the overpotential. In the present work, we do not aim to obtain an absolute value of the overpotential because we are not considering other complex details such as the role of the solvent, the Li and O$_2$ diffusion and charge transport through the Li$_2$O$_2$, among others. The main message of this section is that some care should be taken when describing the recharge process within GGA because the energy cost of the limiting step is overestimated.

Effect of doping in the Li$_2$O$_2$ decomposition

In the previous section we have clarified the electronic structure and the energetics of the Li$_2$O$_2$ surface and its mechanism for the delithiation in the recharge process of the LOB. We used a proper functional for the exchange and correlation potential as HSE that corrects the self-interaction error introduced by the standard GGA. In the present section, we proceed to study the effect of Na doping in the OER. As mentioned in the Introduction, Chen and coworkers showed a decrease in the charging overpotential when Na$^+$ ions were dissolved in the electrolyte, doping the formed Li$_2$O$_2$ in the LOB. The explanation of this desired effect
was ascribed to the generation of more lithium vacancies in the presence of Na\(^+\) that supposedly gives rise to metallic states as described by their DFT calculations. These calculations were performed using HSE with \(\alpha=0.207\) for which the obtained insulating band gap of \(\sim 4\) eV is still lower than the one calculated with \(\alpha=0.48\) and the more accurate formalism GW (\(\sim 6\) eV), indicating that the theoretical metallic states obtained in the presence of lithium vacancies with \(\alpha=0.207\) are an artifact because the self-interaction correction is not completely accomplished.

In this work, we study the effect of Na\(^+\) doping in the electronic structure and the OER of the more stable Li\(_2\)O\(_2\) surface using HSE with \(\alpha=0.48\). The experiment performed by Chen and coworkers shows that the increased amount of Na\(^+\) doping produces higher oxidation states of oxygen indicating a transition tendency from O\(^-\)\(_2\) to O\(^-\) associated to the presence of more lithium vacancies in the Li\(_2\)O\(_2\) deposit.

That the Na\(^+\) doping promotes the generation of lithium vacancies can be first checked by comparing the V\(_{Li}\) formation energy obtained with and without Na\(^+\) for the [1\(\overline{1}00\)] ST-3 surface. We explore different Li\(^+\) substitutional sites for Na doping (see Figure S6 and Table S2 in the SI material). For the more energetically stable Na-doping site, we calculate the lithium vacancy energy formation for different remaining Li\(^+\) sites (see Figure S7 and Table S3 in the SI file). In line with the experimental observation, the formation energy in the presence of Na\(^+\) for the more favorable vacancy site is 150 meV smaller than for the pristine surface (see Table S3 in the SI file).

There is another scenario in which dissolved Na\(^+\) can promoted lithium vacancies. If an electrolyte with high donor number is used in the experiment, as was the case of Ref. 29, the solution mechanism of Li\(_2\)O\(_2\) formation in the LOB is more likely.\(^{35}\)

Considering the solution mechanism, two LiO\(_2\) dissolved in the electrolyte disproportionate to form Li\(_2\)O\(_2\) releasing one O\(_2\) molecule. As mentioned before, the doping with K\(^+\) has also been probed to promote the tendency to O\(^-\)\(_2\) and the generation of lithium vacancies.\(^{30}\)

In general, when a cation X is dissolved in the electrolyte, the following disproportionation
is expected $\text{XO}_2 + \text{LiO}_2 \rightarrow \text{LiXO}_2 + \text{O}_2$.

We first calculate the energetics of the disproportionation when $X$ is equal to Li, Na and K for comparison. The corresponding disproportionation energy reads:

$$E_{\text{dis}} = (E_{\text{LiXO}_2} + E_{\text{O}_2}) - (E_{\text{LiO}_2} + E_{\text{XO}_2})$$  \hspace{1cm} (4)

In Figure 5, we show the three cases studied and their calculated $E_{\text{dis}}(X)$. We obtain $E_{\text{dis}}(\text{Li}) < E_{\text{dis}}(\text{Na}) < E_{\text{dis}}(\text{K})$. So that we conclude that the disproportionation of LiO$_2$ with NaO$_2$ and KO$_2$ are less energetically favorable than with LiO$_2$. In this scenario, the eventual non-disproportionated NaO$_2$ and KO$_2$ might get trapped in the Li$_2$O$_2$ deposits where Na$^{+}$ or K$^{+}$ occupy a Li$^{+}$ crystal site next to an associated O$^{2-}$. This frustrated disproportionation of NaO$_2$ or KO$_2$ concomitantly generates a V$_{\text{Li}}$ nearby.

Figure 5: Schema and disproportion energies $E_{\text{dis}}$ of LiO$_2$ with LiO$_2$, NaO$_2$ and KO$_2$.

Figure 6 shows the calculated reaction free energy of the OER process at $U=0$ V for the
Na-doped Li$_2$O$_2$ surface (blue line) in comparison with the corresponding for the pristine Li$_2$O$_2$ (red line). We can see that the energy cost of taking out the Li in the first step is considerable smaller in the Na-doped surface. The reason for this is that the doped case presents an initial level of distortion that makes this surface less bound. Similar arguments are valid for the following steps of the OER process. The main results of this study is that the more limiting step of the OER, that is, the last LiO$_2$ removal, presents a sensible reduction (266 meV for the simulated supercell) for the doped case as compared to the pristine surface. It is important to remark that the reduction of the energy barriers is not a consequence of the emerging metallic states as it has been claimed in the literature. We confirm that the poor electronic conductivity of lithium peroxide even at its surfaces is one of the main limitations for the operation of the LOBs. The effect of Na-doping induces structural distortions by promoting lithium vacancies and will also improve the electronic conductivity mediated by polarons as suggested in Refs. 36,37 for amorphous Li$_2$O$_2$, both effects turning beneficial for the Li$_2$O$_2$ decomposition during the recharge process.

Interestingly, similar conclusions pointing to the decrease in the overpotential as a consequence of a decrease in the binding energy of the intermediate LiO$_2$ have been reported for one-dimensional nanostructured amorphous Li$_2$O$_2$.}$^{24}$
In this line, our results suggest that K-doping will be even more effective in reducing the overpotential since more lithium vacancies and more structural distortions are expected for this heavier heteroatom.

It is worth mentioning that when these calculations of the OER are performed with GGA, we also obtain an improvement of the OER barrier (731 meV for the simulated supercell) for the Na-doped surface as compared to the pristine one. However, this energy gain is strongly overestimated as a consequence of the GGA overbinding of the pristine Li$_2$O$_2$ surface.

**Conclusions**

In this work, we have studied the electronic structure of different Li$_2$O$_2$ surfaces using the hybrid functional HSE that is capable of adequately describing the electronic structure and modeling the localization of hole polarons. The insulating nature of the all studied surfaces has been confirmed. In the non-stoichiometric terminations with low-coordinated surface oxygen atoms, we have also confirmed a similar charge self-trapping behaviour as found in Li$_2$O$_2$ bulk. Then, we have examined the Li$_2$O$_2$ decomposition that occurs during the
recharge process using HSE to take into account the presence of the surface polarons in the electrochemical intermediate steps. These results have been compared with the ones obtained using the GGA functional, which tend to delocalize the excess of charge carriers. We have shown that the free energy variation of the limiting step is overestimated within GGA when there are spurious metallic states instead of hole polarons.

Finally, we have investigated the Na-doping effect on the lithium vacancy generation and on the Li$_2$O$_2$ surface decomposition. On the one hand, it is found that Na dopant reduces the lithium vacancy formation energy compared to the value for pristine surface, promoting the vacancy generation in agreement with experimental results. On the other hand, we have presented a plausible scenario to enhance lithium vacancies when the formation of the lithium peroxide occurs via a solution mechanism and Na$^+$ or K$^+$ ions are dissolved in the electrolyte. Based on the analysis of the energetics for different superoxide disproportionations, we have proposed that NaO$_2$ formed in the electrolyte can get trapped on the discharge product, concomitantly with the formation of a lithium vacancy. We have also predicted that K-doping should be even more efficient in reducing the overpotential than Na-doping.

At last, the Na-doped Li$_2$O$_2$ decomposition has been studied. The removal of the second LiO$_2$ intermediate is found to be the limiting step during charge, in both Na-doped and pristine Li$_2$O$_2$ surfaces. We have found that Na-doping decreases the energy barrier of the limiting step, contributing to a reduction of the charging overpotential, in line with the experimental results. Our calculations indicate that the origin of this decrease are the lattice distortions associated with doping that weaken the LiO$_2$ binding, and not the emergence of surface metallic states as previously reported.

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Supporting Information Available

In the Supplementary information file we include:

- Detailed results of the DFT+U calculations performed with the VASP code.
- DOS plot of each electrochemical step of the Li$_2$O$_2$ decomposition reaction calculated with GGA and HSE ($\alpha=0.48$).
- The crystal structure of with the different sites evaluated for the dopants and lithium vacancies and their corresponding energy of formation.

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