
Cooperative single-atom active centers for attenuating linear scaling effect in nitrogen reduction reaction

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ABSTRACT: Cooperative effects of adjacent active centers are critical for single-atom catalysts (SACs) as active site density matters. Yet how it affects scaling relationships in many important reactions like nitrogen reduction reaction (NRR) is underexplored. Herein we elucidate how the cooperation of two active centers can attenuate the linear scaling effect in NRR, through the first-principle study on 39 SACs comprised of two adjacent (~4 Å apart) four N-coordinated metal centers (MN₄ duo) embedded in graphene. Bridge-on adsorption of dinitrogen-containing species appreciably tilts the balance of adsorption of N₂H and NH₂ towards N₂H and thus substantially loosens the restraint of scaling relations in NRR, achieving low onset potential (V) and direct N≡N cleavage (Mo, Re) at room temperature, respectively. The potential of MN₄ duo in NRR casts new insight into circumventing limitations of scaling relations in heterogeneous catalysis.

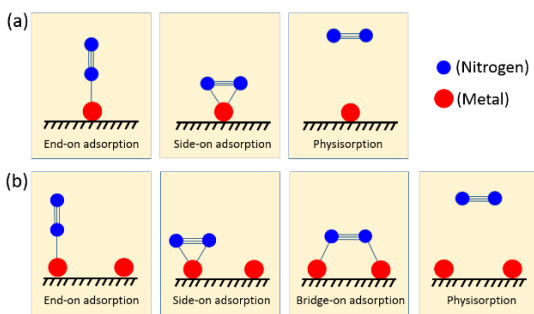
Heterogeneous catalysis lies at the heart of the chemical industry.¹ The ideal scenario for heterogeneous catalysis, as illustrated by the Sabatier principle, seeks a delicate balance between the activation of reactants and the desorption of products.² Yet for most reactions involving multiple intermediates, scaling relationships between adsorption strengths of different intermediates make such a balance difficult to achieve, limiting optimization of catalysts.³ Breaking scaling relations is crucial for heterogeneous catalyst design. Nørskov and co-workers have suggested using multiple active centers to achieve it based on the first-principle calculations⁴, which is supported by two recent experimental studies.⁵⁻⁶ However, the ambiguity, and complexity of structures of active centers in heterogeneous catalysis make it difficult to gain a straightforward and precise understanding on how catalysts could work around the restraint of scaling relations posed to reactions. A simpler catalyst model with a well-defined structure of the active center would be helpful to decipher it.

The emerging single-atom catalysts (SACs) combining the merits of both homogeneous and heterogeneous catalysts have demonstrated excellent performances in a number of different reactions.⁷⁻¹¹ Because SACs possess simple and unified active centers with well-defined composition and coordination

environments, they are deemed an ideal type of catalysts model to provide mechanistic insight into heterogeneous catalysis. Particularly, the advent of high-density SACs due to the rapid advance of synthetic technologies¹²⁻¹⁸ and precise control of inter-site distance¹⁹⁻²¹ would facilitate the study of cooperative effects of multiple active centers. The synergetic effects between adjacent active sites on heterogeneous catalysis have drawn increasing attention in experimental work.^{5, 22-26} In parallel, the computational approach plays an indispensable role in dissecting mechanisms and structure-property relationships associated with SACs.²⁷ Previously, we have conducted a first-principle study on cooperative communications between two neighboring active centers, and impacts of active site density on oxygen reduction reaction (ORR) and nitrogen reduction reaction (NRR) respectively.²⁸⁻³⁰, which has prompted ourselves to continue the exploration of cooperative single-atom active centers.

In the present work, we employed high-density SACs as model systems to systematically investigate impacts of multiple active centers on scaling relationships between adsorption strengths of different reaction intermediates in electrocatalytic nitrogen reduction reaction (eNRR).^{4, 31} eNRR has been inspired by enzymatic catalysis of nitrogenase at mild conditions and regarded as a promising solution of energy-saving nitrogen

fixation.³¹ Unfortunately, it is hampered by the challenge of realizing optimal activation energy (E_a) of N_2 and adsorption energy (ΔE_{ads}) of nitrogen-containing intermediate species simultaneously due to the scaling relations that couple favorable (unfavorable) E_a and unfavorable (favorable) ΔE_{ads} together. For eNRR, based on the Bell-Evans-Polanyi principle, the strong coupling between adsorption strength of $*NH_2$ and $*N_2H$ ($*$ denotes adsorbed species) is in the center of scaling relations that undermine catalytic activities.⁴ To surpass this limitation, it requires a decoupling mechanism to allow them to be optimized independently.



Scheme 1. Various adsorption configurations of N_2 on (a) MN_4/G and (b) MN_4 duo/ G .

Well-established eNRR mechanisms, however, resolve around associative pathways (Figure S1)³² assuming single active center, which adsorbs dinitrogen via either end-on or side-on manners (Scheme 1). Meanwhile, alternative adsorption mode of N_2 via ensemble active centers³³ has largely been underexplored. Previously, we found an alternative reaction path based on cooperative bridge-on adsorption of N_2 (Scheme 1) by two closely arranged (~ 6 Å) Mo-N-C sites.²⁹ This discovery naturally raised the question that whether the bridge-on manner might initiate a game-changing strategy of NRR.³⁴ It then motivated us to explore in this work how the scaling relations evolve from single active center to two cooperative active centers as the bridge-on adsorption pattern of N_2 and other nitrogen species are adopted.

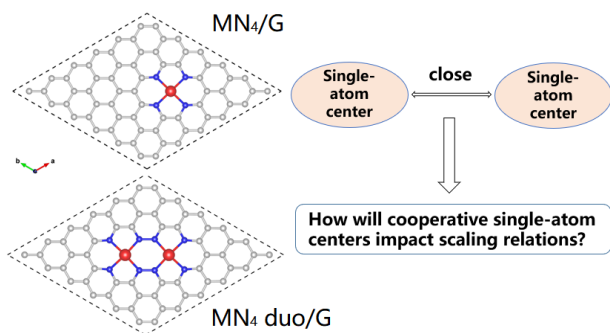


Figure 1. Top view of MN_4/G and MN_4 duo/ G models used in this work, with the annotation of the philosophy of building them.

A single metal center coordinated with four nitrogen atoms (shorted as MN_4) constitutes the essential moiety of many

excellent molecular catalysts derived from metal porphyrins and metal phthalocyanines.³⁵⁻³⁷ The marriage of MN_4 active center and two-dimensional carbon support (shorted as MN_4/C) benefits from the ease of synthesis¹³⁻¹⁸, which has generated quite a few promising SACs, including NRR catalysts³⁸⁻⁴³. As shown in Figure 1, we placed two adjacent MN_4 within graphene (shorted as MN_4 duo/ G) as a prototype model of high-density MN_4 SACs to investigate how the cooperation of single-atom centers will impact scaling relations in NRR. Note that our MN_4 duo model is different from other dual-atom M-N-C models⁴⁴⁻⁴⁸ (Figure S2) in two aspects: (1) our model consists of two well-separated MN_4 centers while others either have a metal-metal bond (essentially dimer) or share coordinating atoms; (2) our model focuses on cooperation between two individual active centers while others emphasize one active center with two interconnecting metal atoms.

The results and discussion are organized into two parts. In the first part, we surveyed the scaling relationship between adsorption strength of $*NH_2$ and $*N_2H$ in NRR occurring on 39 different MN_4/G and MN_4 duo/ G (Figure S3), represented by their respective Gibbs adsorption free energies ($\Delta G^*_{NH_2}$ and $\Delta G^*_{N_2H}$), and showed how it appreciably shifts as the adsorption mode of $*N_2$ and $*N_2H$ varies from end-on to side-on to bridge-on. Equivalently, the significant changes of scaling relations for bridge-on mode were demonstrated in the form of a favorable shift of the volcano plot. In the second part, under the guidance of altered scaling relations, we investigated several potential NRR catalysts, and achieved low onset potential (V) and direct $N\equiv N$ cleavage (Mo, Re) at room temperature (energy barrier < 0.85 eV), respectively. Our results demonstrate the importance of cooperation of monodispersed active centers, which casts new insight into the rational design of SACs for NRR at mild conditions.

RESULTS AND DISCUSSION

After building two different sets of MN_4 -type SACs: MN_4/G and MN_4 duo/ G (M =transition metals and main group IIIA-VA metals), we first examined their stabilities in terms of thermodynamic stability represented by formation energy (E_f) and electrochemical stability represented by dissolution potential (U_{diss}). The majority of them are found to be thermodynamically stable (See Figure S4, Table S1, and associated text in Supporting Information). Since we used the atomic energy in bulk metal as the reference state of the metal, the assignment of “unstable” in the sense of formation energy does not mean it would decompose or undergo aggregation. We expected a large energy barrier for metal migration from one site to another will prevent them from clustering.²⁹ Further, as we explore the scaling relationship of adsorption of different intermediates of NRR, these seemingly “unstable” MN_4 duo models are all valuable data points that can help sketch the whole picture we need.

All possible adsorption patterns of N_2 as illustrated in Scheme 1 were investigated for all MN_4 and MN_4 duo models. The main group metals of interest could not effectively activate

adsorbed N_2 , because they invoke physisorption or very weak chemisorption. Transition metals develop five different scenarios for the adsorption of N_2 (Table S2). In the rest of presentation, only MN_4 and MN_4 duo enabling substantial chemisorption of N_2 will be examined in the study of scaling relations of NRR intermediates.

For associative NRR pathways, the first ($*N_2 + H^+ + e^- \rightarrow *N_2H$) and sixth ($*NH_2 + H^+ + e^- \rightarrow *NH_3$) reductive hydrogenation steps are the most likely potential-limiting steps.³⁴ Their respective free energy changes (ΔG_1 and ΔG_6) are coupled through an inversely proportional relationship. Since ΔG_1 and ΔG_6 scale well with ΔG^*N_2H for better ΔG^*NH_2 respectively (Figure S5), the key scaling relations in NRR eventually fall onto ΔG^*N_2H and ΔG^*NH_2 .

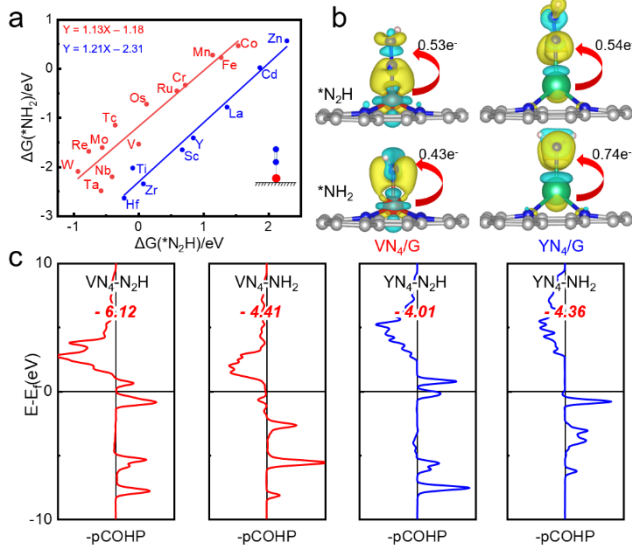


Figure 2. (a) The scaling relationship between ΔG^*NH_2 and ΔG^*N_2H for end-on adsorption mode on MN_4/G . (b) The differential charge density profiles of end-on $*N_2H$ and $*NH_2$ by VN_4/G and YN_4/G with an isosurface value of $5 \times 10^{-3} e \text{ \AA}^{-3}$. Yellow and blue bubbles represent charge accumulation and depletion, respectively. (c) Projected crystal orbital Hamilton population (pCOHP) between the metal centers (V and Y) and the nitrogen adatom. The values of integrated COHP (ICOHP) are shown in red bold italics.

On MN_4/G , as expected, the adsorption of NH_2 scales well with N_2H in end-on mode (Figure 2a), in line with their scaling relationship established on pure metals surfaces.⁴ The transition metals can be divided into two groups based on two respective fitting lines. Group 1 (labels in blue) includes the elements in groups IB-IVB, while group 2 (labels in red) contains those in groups VB-VIIIB. (Figure S6) Note that the balance between adsorption of N_2H and NH_2 shifts towards N_2H from group 1 to group 2, which can be interpreted by the amount of charge transfer from metal to nitrogen species (Figure 2b) based on Bader charge profile and the bonding strength between them (Figure 2c) using the integrated crystal orbital Hamilton population (ICOHP)⁴⁹⁻⁵² values (more negative value indicates

stronger bonding). Take V and Y for example, more negative charges transfer from V to N_2H than to NH_2 , while less from Y to N_2H than NH_2 ; the M-N bonding interaction is appreciably stronger in MN_4-N_2H than in MN_4-NH_2 for V, while it's weaker in the former than the latter for Y. The same distinction between group 1 and 2 can be found on all types of adsorption mode on both MN_4/G and MN_4 duo/G (Figure S7). Since preferable enhancing the adsorption of N_2H over NH_2 is favorable to mitigate the uphill energetics of activating the adsorbed N_2 and producing NH_3 from NH_2 , we then focus on the study of transition metals in group 2 in the rest of work.

From MN_4/G to MN_4 duo/G, the scaling relationships between ΔG^*N_2H and ΔG^*NH_2 in end-on and side-on adsorption modes do not change significantly (Figure 3), as only one metal center bonds with adsorbates. However, bridge-on adsorption of N_2H on MN_4 duo/G appreciably alters the landscape of scaling relations (Figure 3a). As Figure 3a shows, bridge-on mode appreciably reduces the slope and shifts up the intercept of scaling line relative to end-on mode while side-on mode reduces slope at the cost of shifting down the intercept. Note that smaller slope and higher intercept values enable strengthening adsorption of N_2H much more than NH_2 , which facilitates dinitrogen activation without impeding the final reductive hydrogenation producing ammonia. Again, the strengthening of N_2H in bridge-on mode relative to end-on and side-on is demonstrated using Bader charge and ICOHP profiles (Figure 3b). Compared to end-on and side-on modes where only one metal center bond with N_2H , bridge-on mode has two collaborative metal centers binding to N_2H , which increases electrons transferred to anti-bonding orbitals of N_2H and overall metal-nitrogen bonding strength.

In addition, ΔG_1 barely scales with ΔG^*N_2H (Figure 3c) for bridge-on mode, which is in sharp contrast to the well scaling between the two in end-on and side-on modes. Here the internal energy part plays a dominant role while the entropy factor has negligible contribution (Table S3). The change of dependence of ΔG_1 on ΔG^*N_2H can be explained by the change of binding strength from $*N_2$ to $*N_2H$. The integral of partial density of states (pDOS) of nitrogen atoms from -3 eV to 0 eV (Fermi level is reset to 0) is an indicator of effective number of electrons involved in the bonding interaction between nitrogen and metal atoms. Thus, the difference of this integral between $*N_2$ and $*N_2H$ roughly reflects the difference of their binding strength to metal centers. Clearly, bridge-on mode has the smallest difference while end-on and side-on bear comparable changes (Figure 3d). As two cooperative metal centers accommodate dinitrogen-containing species together, they not only bind them stronger but also mitigate the uphill energetics of first dinitrogen hydrogenation. Consequently, in bridge-on associated NRR pathways, ΔG_1 and ΔG_6 are decoupled (Figure S8), creating room for substantial improvement of overall catalytic activity, as seen in the volcano plots of NRR occurring on MN_4 duo (Figure 4).

Based on the volcano plot associated with bridge-on adsorption mode (Figure 4c), we have identified four selected MN_4 duo/G models ($M = Mo, Re, V, Os$) as potential NRR catalysts. Although Tc appears to be the closest element to the

vertex of volcano curve, it has to be excluded because it is radioactive. Then, for OsN_4 duo/G, initial N_2 adsorption adopts an end-on rather than bridge-on mode (Table S4). Thus, we skipped Os as well. In the rest of presentation, we mainly discussed Mo, Re, and V. Intriguingly, V, Mo, and Re are in one diagonal line in the periodic table, which may account for

their similar catalytic activities in NRR. In addition to homonuclear MN_4 duo/G models, we have also considered heteronuclear MN_4 duo/G models in the form of hybrid MN_4 duo. Therefore, we have a total of six MN_4 duo/G models, including VN_4 duo, MoN_4 duo, ReN_4 duo, VN_4 - MoN_4 , MoN_4 - ReV_4 , and ReV_4 - VN_4 .

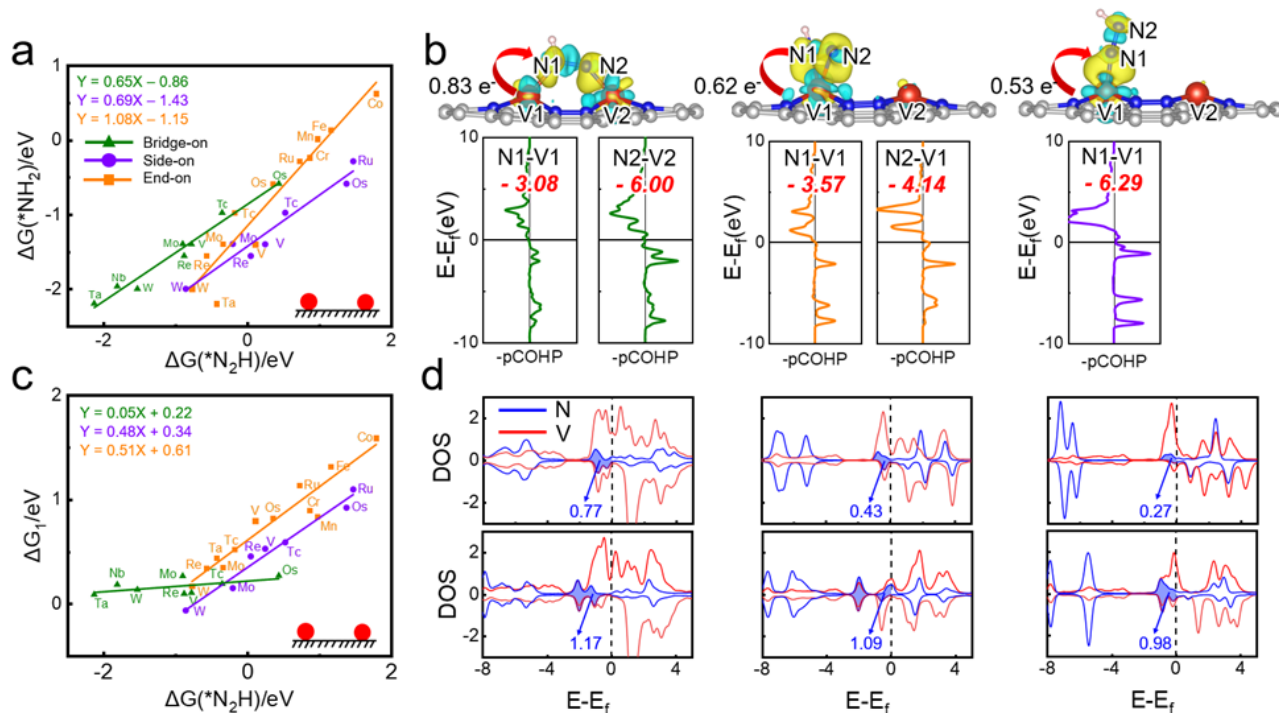


Figure 3. (a) The scaling relationships between $\Delta G^*\text{NH}_2$ and $\Delta G^*\text{N}_2\text{H}$ as N_2H is adsorbed on MN_4 duo/G via end-on, side-on, and bridge-on modes, respectively. (b) The differential charge densities of $^*\text{N}_2\text{H}$ in bridge-on, side-on, and end-on (from left to right) adsorption modes by VN_4 duo/G with an isosurface value of $5 \times 10^{-3} \text{ e } \text{\AA}^{-3}$, and their respective pCOHP between two V atoms and the nitrogen adatoms. Yellow and blue bubbles represent charge accumulation and depletion, respectively. The values of ICOHP are shown in red bold italics. (c) The scaling relationships between $\Delta G^*\text{N}_2\text{H}$ and ΔG_1 as both N_2 and N_2H are adsorbed on VN_4 duo/G via, respectively. (d) Electronic densities of states of $^*\text{N}_2$ (up) and $^*\text{N}_2\text{H}$ (down) adsorbed via end-on, side-on, and bridge-on modes on VN_4 duo/G, respectively.

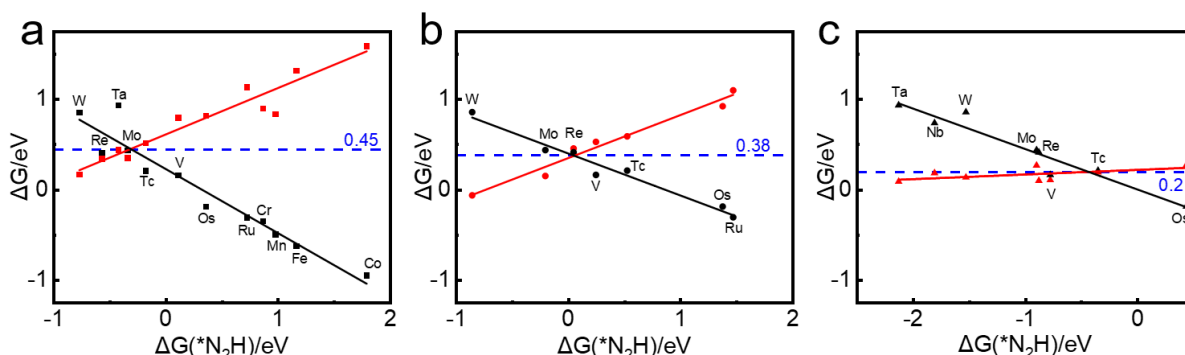


Figure 4. The scaling relationships between ΔG_1 and $\Delta G^*\text{NH}_2$ (red line) and between ΔG_6 and $\Delta G^*\text{N}_2\text{H}$ (black line) for end-on, side-on, and bridge-on (from left to right) adsorption modes of $^*\text{N}_2$ and $^*\text{N}_2\text{H}$. The blue dash line in each panel indicates the theoretical lower bound of energetics of presumable potential-limiting steps of NRR in respective adsorption mode.

Using these models, we calculated the full NRR pathways starting from bridge-on adsorption and obtained the onset potential of NRR that signifies the activity of the catalyst of interest. We first examined the adsorption energies of bridge-on adsorbed N_2 , associated charge redistribution, and geometric changes of reactant-active center complexes. As shown in Table S5, the computed binding energies are between -1.46 and -1.82 eV for bridge-on adsorption, accompanied by substantial charge

transfer (0.59 ~ 0.93 |e| by Bader charge analysis) from both two MN_4 sites to N_2 . The corresponding charge distribution is also demonstrated by the differential charge densities of N_2 - MN_4 duo binding complexes (Figure S9), which illustrates electron gain in the antibonding orbital of N_2 . As a result, the adsorbed N_2 is activated, with an appreciable stretching of N-N bond from 1.11 Å (free N_2 in the gas phase) to 1.18 ~ 1.23 Å.

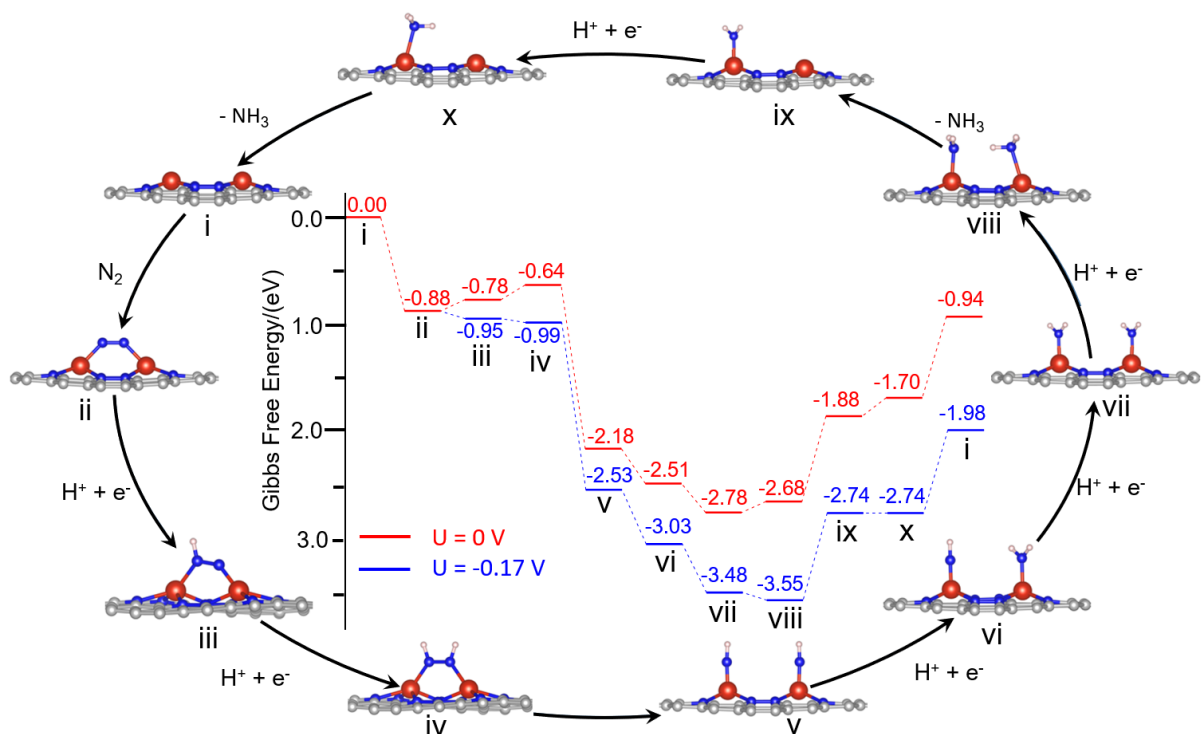


Figure 5. The reaction profile of the bridge-on adsorption initiated NRR pathway on VN4 duo/G model. Roman numbers denote all reaction species along the pathway.

Then we investigated the $N\equiv N$ bond dissociation following the bridge-on adsorption. The transition state structures are showing in Figure S10. Remarkably, 3 out of 6 selected models, including MoN_4 duo, ReN_4 duo, and MoN_4 - ReN_4 , enable direct $N\equiv N$ bond breaking with a reaction barrier below 0.91 eV (Table S6), a well-documented threshold for chemical reactions available at room temperature.⁵³ This unusual phenomenon suggests a dissociative NRR mechanism, in sharp contrast to common $N\equiv N$ bond dissociation aided by reductive hydrogenation seen in associative NRR pathways. Intriguingly, this pathway will avoid the formation of $*N_2H$, one of two key intermediate species in NRR, suggesting the possibility of circumventing the well-established scaling relationship for NRR by direct $N\equiv N$ bond dissociation through the joint effort of two adjacent active centers.

To understand it, we adopted the N-N distance as the reaction coordinate to understand the trend of energy barriers of N-N dissociation. Intriguingly, the barriers are positively correlated with the distances (Figure S11-a), because a smaller difference

of N-N distance between the transition state (TS) and initial state will result in a smaller barrier for N-N bond dissociation. This is typical for an early TS, whose structure is close to the corresponding initial state. Then we examined the relationship between the stabilities of all six models and the corresponding energy barrier of TS and found that the lower stability of the catalyst results in a smaller energy barrier (Figure S11-b). Since the ReN_4 duo is the least stable one among these six models, it has the lowest direct N_2 dissociation barrier. Similarly, MoN_4 duo and MoN_4 - ReN_4 enables direct N_2 dissociation at room temperature for their relative lability. The direct $N\equiv N$ breaking aided by bridge-on adsorption may open a new possibility of breaking scaling relationships applied on NRR, which will be investigated in the future. In contrast, as the stabilities increase, which are the cases of VN_4 duo, VN_4 - MoN_4 , and VN_4 - ReN_4 , the dissociative pathway is unfavorable at room temperature; thus, NRR will proceed via associative mechanisms in which $N\equiv N$ breaking takes place after one or two steps of reductive hydrogenation. Their bridge-on adsorption initiated NRR pathways is similar to the one occurring on MoN_3 duo

embedded in graphene.²⁹ The balance between stability and lability of these catalysts may be a key factor for determining the preferred reaction pathways of NRR occurring on them.

The full reaction coordinates of NRR with all six of these models are collected in Figure S12 through Figure S17. Based on the Gibbs free energy data therein, we found that VN₄ duo/G possesses the lowest limiting potential (0.18 V) and thus bears the highest theoretical activity. The reaction coordinates are shown in Figure 5. For the strong adsorption, the $\Delta G^{\ast}\text{N}_2 \rightarrow \ast\text{N}_2\text{H}$ for bridge-on $\ast\text{N}_2$ is 0.11 eV and the N–N distance is stretched to 1.31 Å. The second reductive hydrogenation ($\ast\text{NNH} \rightarrow \ast\text{HNNH}$) is endothermic ($\Delta G^{\ast}\text{N}_2\text{H} \rightarrow \ast\text{HNNH} = 0.16$ eV), with the N–N distance of 1.37 Å. Intriguingly, this bridge-on $\ast\text{HNNH}$ resembles the bridging “diazene” species found in nitrogenase.^{54–55} Then $\ast\text{HNNH}$ dissociates and produces two $\ast\text{NH}$, each of which is attached to one V atom. The energy barrier (0.78 eV) for this N≡N bond breaking can be easily overcome at room temperature. Then the two $\ast\text{NH}$ alternately undergo reductive hydrogenation steps, producing two $\ast\text{NH}_2$. Both reductive hydrogenation of $\ast\text{NH}_2$ and desorption of NH_3 from $\ast\text{NH}_3$ are thermodynamically uphill. The electrochemical step can be promoted only by applying an external potential. At $U = -0.17$ V, $\Delta G^{\ast}\text{NH}_2 \rightarrow \ast\text{NH}_3$ becomes zero, and the uphill energetics is substantially mitigated (Figure 5). This remarkably low limiting potential benefits from the cooperation of two adjacent VN₄ sites that help breaking the scaling relationship of NRR by properly balancing the adsorption energies of $\ast\text{N}_2\text{H}$ and $\ast\text{NH}_2$. For the endergonic (~ 0.7 eV) desorption of ammonia, we expect that the solvation of ammonia can mitigate the unfavorable energetics because it will stabilize the desorbed ammonia.^{4, 39, 43, 56–57} Thus, NH_3 desorption may not be a main obstacle in NRR and, hence, is not considered in detail here.

CONCLUSION

In this work, we have conducted a systematic first-principle study on impacts of bridge-on N₂ adsorption by two adjacent MN₄ sites on scaling relationships within electrocatalytic NRR and found the key to attenuate the scaling relations is to create inhomogeneous adsorption between dinitrogen-containing species and nitrogen-containing species.

We confirmed that the scaling relationship between adsorption of N_2H and NH_2 hold for NRR occurring on single active center, regardless of MN₄ or MN₄ duo. Since the room of improvement of NRR activity associated with one active center is limited, we have to go beyond conventional end-on and side-on adsorption modes. Intriguingly, the side-on fashion benefits from different metal-nitrogen bonding patterns for $\ast\text{N}_2\text{H}$ and $\ast\text{NH}_2$, hinting a path for the evolution of NRR catalysts.^{43–44, 58} The bridge-on adsorption mode can be viewed as a two-center version of “side-on”. It further widens the gap of metal-nitrogen bonding strengths between $\ast\text{N}_2\text{H}$ and $\ast\text{NH}_2$, enabling us to decouple the optimization of ($\ast\text{N}_2 + \text{e}^- + \text{H}^+ \rightarrow \ast\text{N}_2\text{H}$) and ($\ast\text{NH}_2 + \text{e}^- + \text{H}^+ \rightarrow \ast\text{NH}_3$). Thus, it shows the potential of making substantial progress towards breaking scaling relations in NRR. Importantly, the bridge-on pattern relies on the

proximity of two metal active sites, which could well explain other reported promising NRR catalytic systems invoking bridge-on like activation of N₂ by multiple active centers.^{59–61}

Based on the survey, we then identified VN₄ duo and ReN₄ duo as promising NRR catalysts through associative mechanisms and dissociative mechanisms, respectively. For VN₄ duo, the remarkably low onset potential (0.18 eV) indicates the level of excellent activity of NRR that can be achieved by high-density SACs. For ReN₄ duo, the most appealing feature is the low energy barrier (0.52 eV) of direct N≡N bond dissociation enabling a dissociative mechanism for NRR at room temperature, which for sure will inspire more mechanistic study on dissociative pathways with multiple concerted active centers. We also expect it motivates more exploration on how the delicate balance between stability and lability of active centers would affect the dynamics of N₂ activation process.

In summary, through a comprehensive understanding of scaling relationships for NRR in MN₄-type single-atom catalysts, we found cooperation of two adjacent single-atom active centers can attenuate scaling relation effect and facilitate nitrogen fixation. Although our computational models are based on ideal reaction conditions, we expect our work casting new light on NRR mechanisms with collective active centers will be helpful for the rational design of high-density SACs and prompting mechanistic study on breaking scaling relationships existing in other reactions (e.g. CO₂ reduction⁶² and oxygen reduction reaction) aided by cooperative multiple active centers. We will also continue the investigation of cooperative single-atom active centers under more realistic reaction conditions in the future work.

COMPUTATIONAL DETAILS

All spin-polarized density functional theory (DFT) calculations were performed using the Perdew-Burke-Ernzerhof (PBE)⁶³ functional in conjunction with plane-wave projected augmented wave (PAW)⁶⁴ method as implemented in Vienna ab initio simulation program (VASP)^{65–66}. The kinetic cutoff energy for the plane-wave basis set was set to be 480 eV. The Gaussian smearing method was adopted with a width of 0.1 eV to describe partial occupancies of each orbital. The first Brillouin zone was sampled by a Monkhorst–Pack scheme with a $3 \times 3 \times 1$ k -point grid. To avoid the interaction between two periodic units, a vacuum space exceeds 15 Å was employed. Structures were fully relaxed until the forces were converged to less than 0.02 eV Å^{−1}. The Grimme’s D3 dispersion correction scheme was used to describe the van der Waals interaction. The solvent effect on scaling relations are not taken into account as a previous study showed that no significant change that can alter the scaling relations has been found as solvent effect was incorporated.⁶⁷ More details regarding adopted computational models, calculation of various energy values and selection of energetic descriptors are given in the Supporting Information.

ASSOCIATED CONTENT

Supporting Information

Computational detail, geometrical structures and stability validation of MN₄ and MN₄ duo models, the adsorption energies of N₂, differential charge densities, various scaling relationships and Gibbs free energy diagrams for NRR occurring on selected MN₄ duo models.

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Note

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