TMtopo Dataset — Quantum Geometries and Density Topology for 1.1k Transition Metal Complexes

Filipe Teixeira,* Edgar Silva-Santos, and M. Natália D. S. Cordeiro*

LAQV-REQUIMTE, Faculty of Sciences of the University of Porto, Rua do Campo Alegre, 4169-007 Porto, Portugal

E-mail: filipe.teixeira@fc.up.pt; ncordeir@fc.up.pt

Abstract

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The chemistry of transition metal (TM) complexes is a hugely diverse field where 2 commonly accepted chemistry concepts are routinely challenged, hindering the de-3 velopment of predictive models of TM complex chemistry. In this work, we report 4 the TM topo data set containing optimized geometries, quantum calculated proper-5 ties, and quantum topological descriptors for 1110 first row TM complexes. Properties 6 were computed at the TPSSh/Def2-TZVP level of theory and the quantum topological 7 descriptors were collected under the framework of the Quantum Theory of Atoms in 8 Molecules (QTAIM), including a systematic topological survey of the Laplacian of the 9 electron density, $\nabla^2 \rho(\mathbf{r})$. This survey yielded novel insights on the proliferation of inner 10 Valence Shell Charge Concentrations (iVSCCs, local minima of $\nabla^2 \rho(\mathbf{r})$) in the metal 11 center, suggesting that their number is determinant for the stabilization of the metal 12 center in a more intense manner than their arrangement opposing each of the metal's 13 ligands (Inorg. Chem. 2016, 55, 3653). Pairwise representation of the collected prop-14 erties revealed overall low correlation, although some structure could be perceived in 15

the data (specially when considering the topological features of $\nabla^2 \rho(\mathbf{r})$). This suggests that the TMtopo data set could be usefully exploited in the data-driven discovery of new TM complexes with interesting properties for applications in as catalysis, optoelectronics and sustainable energy production and storage. TMtopo is an open data set that can be accessed free of charge from https://github.com/teixeirafilipe/TMtopo.

²¹ 1 Introduction

Machine Learning (ML) is playing an important role in chemical research $^{1-6}$. ML algorithms 22 generate predictive models mapping a set of descriptors (features) into one or more properties 23 (targets) by minimizing the error relative to reference training data⁷. In order to accomplish 24 this, ML techniques such as Artificial Neural Networks^{8,9}, Kernel Ridge Regression², Sup-25 port Vector Machines⁵, and Random Forests^{10,11} rely on highly flexible algorithms with a 26 myriad of internal parameters, and thus require big data sets for their training, as well as to 27 access their predictive capabilities regarding new data^{11,12}. This poses an important hurdle 28 when applying ML to chemical research, as reference experimental data is usually small and 29 limited in the exploration of the chemical space. In order to circumvent this obstacle, ML 30 models started to be trained with data generated from first-principles Quantum Mechanical 31 (QM) calculations, giving rise to quantum-based ML (QML)^{2,12–16}. QML models are used to 32 predict energies and nuclear gradients (enabling ML-accelerated molecular dynamics simula-33 tions)^{14,17,18}, but also other properties such as the energies of the frontier molecular orbitals, 34 dipole moments, polarizabilities, band structure, and other quantum properties^{19,20}. Similar 35 to their experimentally-rooted counterparts, these QML models also require large and com-36 prehensive data sets to avoid biasing and overfitting issues. Examples of such data sets are 37 the Materials Project²¹ and PubChemQC²², which cover significant parts of the chemical 38 space for solid state and general (mainly main-group) chemistry, respectively. Quantum data 39 sets devoted to transition metal (TM) complexes have been known to cover either small²³ 40 or very specific regions²⁴ of the chemical space. Recently, Balcells and Skjelstad²⁵ published 41 the tmQM dataset containing geometries of about 86 000 TM complexes, as well as a few 42 QM-calculated properties, such as the total energy, HOMO and LUMO energies, Natural 43 charge of the metal center, norm of the dipole momentum and polarizability. 44

One important aspect of TM chemistry is the relatively large diversity of molecular geometries attainable even by compounds with relatively simple molecular formula (i.e., low coordination number and mono-atomic ligands). Often, the most stable geometry of these

complexes does not conform to the predictions made by well established models such as 48 VSEPR, ligand field, crystal field, or ligand-repulsion models²⁶. In this regard, Gillespie and 49 co-workers noticed that the Electron Localization Function (ELF) of several TM fluorides, 50 oxofluorides, hydrides and methanides has some interesting characteristics, namely the ab-51 sence of Electron Localization Basins (ELB) at the spatial region where the metal's valence 52 shell is expected, as well as the appearance of ELB's in the region of the outermost core 53 shell and located opposite to each ligand $2^{7,28}$. These results where confirmed by analysing 54 the Laplacian of the electron density, $\nabla^2 \rho(\mathbf{r})$, which shows local maxima ((3,+3) critical 55 points) in the same spacial region and geometrical arrangement²⁹. These observations had 56 lead to the conclusion that the penultimate shell (usually referred to as the inner-Valence 57 Shell, iVS) of the metal center of a TM complex is not isotropic and that the molecular 58 geometry in these complexes is dictated by the lowering of the repulsion among these iVS 59 Charge Concentrations (iVSCC) that lie opposite to each ligand.^{26–28} 60

More recently, a detailed analysis of several vanadium-acetate complexes under the more 61 framework of the Quantum Theory of Atoms in Molecules (QTAIM) has revealed some im-62 portant exceptions of Gillespie's observations³⁰. Although vanadium-acetate complexes in 63 which acetate behaved as a mono-dentate ligand usually conformed to Gillespie's observa-64 tions, the ones with at least one bidentate acetate ligand did not. What is more, when 65 partitioning the molecular energy by the individual atomic basins under the QTAIM frame-66 work, the former complexes show a lower energy for the metal center, whereas the latter 67 show a stabilization of the atoms in the acetate moiety, due to the electron delocalization 68 along the V-O-C-O ring³⁰. These results lead to the hypothesis that QTAIM properties 69 derived from the analysis of both the electron density, $\rho(\mathbf{r})$, as well as $\nabla^2 \rho(\mathbf{r})$ could be useful 70 for creating novel ML models predicting molecular geometries, as well as other important 71 aspects of TM-complexes. 72

⁷³ We herein report the TM topological database (TMtopo)³¹, which contains a curated ⁷⁴ collection of first-row TM complexes containing O, F and F. The following sections describe ⁷⁵ the computational methodology used to generate the data, the architecture of the database,
⁷⁶ as well as a statistical overview of the data contained in TMtopo. The results and data are
⁷⁷ shared in the hope of nurturing the development of novel data-driven (including ML) models
⁷⁸ for the advancement of TM complex chemistry and their application.

79 2 Methodology

⁸⁰ 2.1 Exploration of the Chemical Subspace

The TM topo data comprises the equilibrium geometries of all fluoride, chloride and oxygen (oxo-) complexes of first-row TMs (Sc to Zn), with a general formula $MO_iCl_jF_k$. The chemical subspace includes all common oxidation states for each of the metals, from +1 (Cu and Sc) to +6 (Cr, Mn, Fe and Co), as well as the lowest lying states of the spin multiplicities accessible for each complex, given the formal occupation of the 3*d* shell: hexaplet for d^5 ; quintuplet for d^4 and d^6 ; quadruplet for d^3 , d^5 , and d^7 ; triplet for d^2 , d^4 , d^6 , and d^8 ; doublet for d^1 , d^3 , d^5 , d^7 , and d^9 ; and singlet for d^0 , d^2 , d^4 , d^6 , d^8 , and d^{10} metal centers.

In order to generate all possible geometries, the following procedure was implemented 88 using an in-house developed Python script. Given the metal and the number of oxygen, 89 fluoride and chloride atoms, the metal center was placed at the origin of the Cartesian 90 coordinates. Then, all possible arrangements of the ligand atoms were generated by placing 91 each ligand atom on different vertices of a virtual octahedron centerd at the origin and 92 oriented so that the vertices lie on the xx, yy and zz axes, at a distance of 1.6 Å from the 93 center. Following that, all redundant geometries were discarded, the metal-chloride bonds 94 were stretched to 2.2 Å, and the structure was saved as an initial guess for the subsequent 95 geometry optimization step. It should be noted that this strategy is unable to yield trigonal 96 planar or trigonal bipyramidal guesses when the coordination number (n_{coord}) is 3 or 5, 97 respectively. Because of this, a similar procedure was carried out for the TM complexes with 98 3 or 5 ligands, starting from an idealized triangular bipyramid, and the redundant structures 99

(mainly T-shaped molecules) were discarded. At the end of these procedures, 1649 guess
 structures were generated (considering variations in spin multiplicity).

¹⁰² 2.2 Quantum Geometries and Properties

Each guess structure was subjected to geometry optimization using Density Functional The-103 ory (DFT) calculations at the TPSSh approximation^{32,33}, given the good performance it 104 attained in several benchmarks using TM complexes^{33–36}. The Def2-TZVP basis set from 105 Ahlrichs³⁷ was used for all atoms. Vibrational analysis of the equilibrium geometries allowed 106 the selection of geometries representing true minima of the Potential Energy Surface (PES), 107 for which all vibrational frequencies are positive. All DFT calculations were carried out using 108 version 4.0.1.2 of the Orca program package³⁸. The resulting geometries were then grouped 109 by molecular formula and spin multiplicity, and each group was scanned for redundant equi-110 librium geometries, taking into account all bond lengths, all valence angles centerd on the 111 metal atom as well as the out-of-plane angles in complexes for which $n_{coord} > 2$, taking the 112 plane defined by the metal center and the first two ligands as reference. 113

After discarding all non-equilibrium and redundant structures, the resulting set of 1110 TM complexes was further analysed under the QTAIM framework, using the AIMAll software, version 16.08.17³⁹. For each structure, relevant information on the topology of $\rho(\mathbf{r})$ and $\nabla^2 \rho(\mathbf{r})$ was collected, as well as atomic basin populations, effective atomic charges, and energy decomposition analysis over the atomic basins.

The data was collected in structured text files (one file per compound), containing a description of the TM complex and the level of theory used, equilibrium geometry, vibrational and thermochemistry data, as well as several QTAIM data pertaining to the Bond Critical Points (BCPs) found, properties of the atomic basins, as well as information on the minima of $\nabla^2 \rho(\mathbf{r})$ (points of local charge concentration). A detailed overview of the structure of these entries is given in the Supporting Information (SI), as on the Github page hosting the data base: https://github.com/teixeirafilipe/TMtopo.

126 2.3 Data Availability

¹²⁷ The TMtopo database is an open data set freely available at GitHub³¹, comprising DFT-¹²⁸ optimized geometries and quantum properties calculated at the TPSSh/Def2-TZVP level of ¹²⁹ theory, as well as an assortment of quantum topological descriptors derived from the analysis ¹³⁰ of $\rho(\mathbf{r})$ and $\nabla^2 \rho(\mathbf{r})$. In addition to this, database specifications and example code for handling ¹³¹ the data is also provided in GitHub (https://github.com/teixeirafilipe/TMtopo), and in the ¹³² SI.

3 Results and Discussion

The TM topo database comprises calculated geometries and quantum properties for 1110 134 TM complexes with oxygen (oxo-), fluoride and chloride. The distribution of the entries 135 in the data along the first-row transition metals depends heavily on the oxidation states 136 available for each metal, as shown in Figure 1a. At the same time, the composition of the 137 data also reflects the fact that metals in higher oxidation states are able to form a more 138 diverse set of complexes (at least in theory), given the limited number of ligands considered 139 in this work. Although some TM complexes of high spin multiplicity were discarded due to 140 poor convergence of the self-consistent field calculations, or due to the presence of at least 141 one negative (imaginary) vibrational frequency in their predicted infra-red spectrum, the 142 distribution along the different spin multiplicities reflects the availability of each spin state 143 given the formal occupation of the 3d shell of each metal, at each oxidation state, as shown 144 in Figure 1b. 145

Figure 1c depicts the representation of the different molecular geometries in the data, and the relative proportion of each metal center within each geometry. Again, the representation of a given molecular geometry appears to be limited only by the availability of the underlying coordination number(s), which in turn depends on the distribution of the complexes by metal and oxidation state. The distribution depicted in Figure 1c suggests that the geometry



Figure 1: Distribution of the entries in the data: (a) distribution by metal center and its formal oxidation state; (b) distribution by metal center and spin multiplicity; (c) distribution by molecular geometry and by metal center. The height of the bars shows the cumulative number of entries in each of the categories shown in the horizontal axis.

¹⁵¹ optimization procedure was able to locate different minima of the PES, depending on the ¹⁵² initial guess geometry. This is well illustrated by the relatively high frequency of T-shaped ¹⁵³ TM complexes ($n_{coord} = 3$), as well as square planar ($n_{coord} = 4$), and square pyramidal ¹⁵⁴ $n_{coord} = 5$ TM complexes. However, it must be stressed that the single criteria for inclusion ¹⁵⁵ of a given TM complex in the database is being a minima in the PES at a given spin ¹⁵⁶ multiplicity, and does not endorse a particular form of a TM complex as being neither the ¹⁵⁷ most stable one, nor synthetically available.

On the other hand, the TM topo database allows one to evaluate and correlate quantum 158 properties of TM complexes, in the prospect of training predictive ML models for evaluating 159 these properties in larger or more complex compounds. The database was designed to address 160 the possibility of training predictive models of interesting quantum properties from data 161 concerning $\rho(\mathbf{r})$ and $\nabla^2 \rho(\mathbf{r})$, and in particular the configuration and characteristics of the 162 iVSCCs on the metal center. Thus, an overview regarding the distribution of these data 163 is in order. For each metal, the iVS is located in a region of space between 0.25 Å and 164 0.45 A from the TM nucleus. As shown in Figure 2a, the location of the iVS mainly reflects 165 the increase in nuclear charge, with the distribution of the iVS radius (r_{iVS}) being mostly 166

¹⁶⁷ mono-modal for each metal. An important exception to this is provided by Ti, which shows ¹⁶⁸ a bi-modal distribution. A closer inspection of the data for the Ti complexes highlighted ¹⁶⁹ some factors that may contribute to a more contracted iVS layer, such has a triplet state ¹⁷⁰ for Ti(II), or the presence of chloride ligands. However, the data does not allow for a clear ¹⁷¹ ruling regarding these observations, and one may postulate that the lower effective nuclear ¹⁷² charge in Ti makes the iVS more sensitive to the atom's chemical environment.

Three to eight iVSCC were found in within the QTAIM atomic basin of the metal center 173 of each TM complex. In the case of ScO, 18 additional minima of $\nabla^2 \rho(\mathbf{r})$ were found further 174 away from the nucleus, at about 1.9 Å. These points were discarded as numerical artefacts, 175 given the very low value of $\rho(\mathbf{r})$ in that region. As shown in Figure 2b, Sc, Ti and V mostly 176 exhibit four or five iVSCCs, whereas Cr, Mn, Fe and Co show a stronger tendency to present 177 six iVSCCs. In the case of the latter metals (Ni, Cu and Zn), the tendency seems to show 178 eight iVSCCs. Overall, the data depicted in Figure 2b shows a distinct tendency to exhibit 179 a larger number of iVSCCs when progressing along the first TM series. What is more, 180 the number of iVSCCs does not appear to vary considerably with n_{coord} , as illustrated in 181 Figure 2c. Indeed, Figure 2c shows a dominance of complexes with $n_{coord} = 4$, but also 182 the preference for the number of iVSCCs (n_{iVSCC}) equal to six, irrespective of n_{coord} . This 183 preference for $n_{\rm iVSCC} = 6$ is also observed irrespective of the geometry of the TM complex, 184 as illustrated in Figure 2d, with the notable exception of trigonal planar complexes, which 185 apparently prefer $n_{\rm iVSCC} = 5$. 186

The data collected in this work appears to contradict the observations made by Gillespie and co-workers^{27–29} regarding the preference for an iVSCC configuration where each iVSCC lies opposite to a ligand. According to such observations, the spacial arrangement of the iVSCC should match that of the TM geometry. As illustrated in Figure 3, this is only observed for a small portion of the TM complexes in the TMtopo database. Indeed, the iVSCCs can achieve a large variety of spacial arrangements, which do not appear to be clearly related to the geometry of the TM complex. Nevertheless, it is important to notice



Molecular Geometry

Figure 2: Distribution of the data regarding the characteristics of the metal's inner Valence Shell (iVS) in TMtopo: (a) kernel density distribution of the iVS radius (r_{iVS}) by metal; (b) number of iVSCCs (n_{iVSCC}) by metal center; (c) cross-distribution of n_{iVSCC} and n_{coord} ; (d) distribution of n_{iVSCC} along the different observed molecular geometries.

that tetrahedral arrangements of the iVSCCs are usually found in tetrahedral TM complexes.
What is more, square pyramidal complexes are quite likely to also have a square pyramidal
arrangement of the iVSCCs. Trigonal bipyramidal complexes also appear to follow Gillespie's
observations and prefer a trigonal bipyramidal arrangement of the iVSCCs.



Figure 3: Distribution of the data regarding the spacial of the iVSCC and the geometry of the TM-complexes in the TM topo database.

Further observation of the topology of $\nabla^2 \rho(\mathbf{r})$ has shown that at least some iVSCCs 198 could be found in a location opposite to a ligand, even if not all iVSCCs in a particular 199 complexes follows that rule. This is unavoidable when $n_{iVSCC} > n_{coord}$, which accounts 200 for a large portion of such cases. More rarely, one would notice that the arrangement of 201 the iVSCCs follows Gillespie's rule for some but not all ligands, even if $n_{iVSCC} = n_{coord}$. 202 These observations raised the need to quantify how much a given TM complex deviates from 203 Gillespie's rule. For this purpose, each iVSCC was classified as being gillespian if and only if 204 a Metal–Ligand BCP was found along the line that connects the iVSCC to the metal nucleus 205 (with a tolerance of 10° to accommodate eventual numerical noise when searching for the 206 critical points of $\nabla^2 \rho(\mathbf{r})$). This allows the definition of two index measuring adherence to 207

²⁰⁸ Gillespie's rule:

$$G_1 = \frac{n_g}{n_{\rm iVSCC}} \tag{1}$$

209 and,

$$G_2 = \frac{n_g}{n_{coord}} \tag{2}$$

where n_g is the number of gillespian iVSCCs found in the complex. Figure 4 depicts the 210 relative abundance of each $(G_1, G_2 \text{ combination in the data, showing that most species in the}$ 211 database do not follow Gillespie's observations at all (i.e. $G_1 = 0.0$, and $G_2 = 0.0$, accounting 212 for 695 entries), and only 54 compounds are completely gillespian (i.e. $G_1 = G_2 = 1.0$). More 213 interesting, 361 TM-metals have intermediary values of either indexes. Within this latter 214 group, two tendencies are perceptible in Figure 4: some compounds do appear to have extra 215 iVSCCs than was is expected from the TM-geometry ($G_1 \leq 0.0$, but $G_2 = 1.0$), while other 216 complexes appear to follow Gillespie's observations only with respect to some of its ligands. 217 Also worth noting, is the absence of cases where $(G_1 = 1.0, \text{ but } G_2 < 1.0)$, which would 218 correspond to all iVSCCs being opposed to a ligand, but not all ligands being meet with an 219 opposing iVSCC. Such an absence leads to the conclusion that the cases where arrangement 220 of the iVSCCs follows Gillespie's rule for some but not all ligands (mentioned above) is never 221 observed due to a lack of iVSCCs in the metal basin. 222

These observations might reflect the tendency for attaining certain values of n_{iVSCC} , as shown in Figures 2c and 2d, which overcomes the preference for a gillespian arrangement of the iVSCCs. In order evaluate the importance of this trend, Figure 5a depicts the distribution of the total molecular energy per electron according to n_{iVSCC} . Despite the large overlapping between the different populations divided by their n_{iVSCC} , Figure 5a strongly suggests that complexes with $n_{iVSCC} = 5$ might be less stable than an isoelectronic complex with a different arrangement and count of iVSCCs.

The relatively large dispersion of $E_{\text{Mol}}/n_{\text{electrons}}$ shown in Figure 5a is justifiable by the relatively small impact the iVSCC should have on the potential felt by the electrons in the



Figure 4: Distribution of the G_1 and G_2 in the TM topo database.

atomic basins pertaining to the ligands of each TM complex. Although relying on a local 232 adherence to the virial theorem, the negative value of the electronic kinetic energy in the 233 metal basin, -K(M), is a suitable surrogate for contribution of the metal's population to the 234 electronic energy of the molecule, specially when considering general trends in the data 30,40 . 235 Figure 5b depicts -K(M) per electron in the metal's basin, which highlights the impact of 236 $n_{\rm iVSCC}$ on the stability of the metal center (and then to the contribution of the metal center 237 to the total energy). The energy distribution per electron shown in Figure 5b clearly suggest 238 that odd values of n_{iVSCC} are linked to higher electronic energy of the metal center, with 239 the case where $n_{\rm iVSCC} = 3$ being particularly penalizing. On the other hand, even values of 240 $n_{\rm iVSCC}$ are linked to lower energy per electron, especially when $n_{\rm iVSCC} = 8$ and $n_{\rm iVSCC} = 6$. 241 Hence, the data shows that the strong presence of these latter $n_{\rm iVSCC}$ values shown in Figure 242 2c reflects an underlying physical cause, possibly a lowering in the inter-electronic repulsion. 243 What is more, Figure 5b further suggests that the energetic penalty associated with an 244 odd $n_{\rm iVSCC}$ can range from 5 to 10 E_h per electron. This value is two to three orders of 245 magnitude higher than the energetic penalty observed for non-gillespian arrangements of 246 the iVSCC in vanadium-acetate complexes³⁰, suggesting a precedence of $n_{\rm iVSCC}$ over the 247 geometrical arrangement of the coordination sphere. 248



Figure 5: Kernel density estimates of the distribution of the total electronic energy per electron $(E_{\text{Mol}}/n_{\text{electrons}})$ (a), and of the distribution of the electronic kinetic energy per electron among the electrons within the metal's atomic basin (-K(M)/Pop(M)) (b). In both cases the data is subdivided by n_{iVSCC} .

Given our main objective of providing a database of quantum calculated properties and 249 topological features of $\rho(\mathbf{r})$ and $\nabla^2 \rho(\mathbf{r})$ for a large number of first-row TM complexes, the 250 remainder of this discussion will explore the nature of the data by representing commonly 251 used quantum property pairs in scatter plots. Figure 6a shows that the pairwise distribu-252 tion of the HOMO and LUMO energies has some structure, with some Fe, Co, Ni and Zn 253 complexes showing higher LUMO energies, yielding also large HOMO-LUMO gaps. These 254 abnormalities are also reflected in Figure 6b, which displays the polarizability versus the 255 HOMO-LUMO gap. Nonetheless, the correlation between the two properties appears to be 256 low. Each point in 6b is colored by the value of the G_1 , highlighting a concentration of 257 complexes with high G_1 in the region corresponding to a HOMO-LUMO gap between 3.0 258 and 6.0 eV. 259

In general, there is poor correlation between the QTAIM charge of the metal center, 260 q_{metal} , and the magnitude of the dipole moment ($|\mu_{\text{Dipole}}|$), as displayed in Figure 6c. Indeed, 261 the spread of the scatter plot displayed in Figure 6c closely resembles the scattering of the 262 same properties in the tmQM dataset, recently published by Balcells and Skjelstad²⁵. One 263 should notice, however, that the highest scores of the G_1 index, are concentrated amongst 264 the higher values of q_{metal} , providing some structure to these data. In a similar fashion, 265 q_{metal} also bears very low correlation with the isotropic polarizability, as shown in Figure 266 6d. Moreover, Figure 6b further suggests poor correlation between the G_2 index and either 267 properties. 268

Figure 7 further explores the relationship between G_1 , G_2 and some quantum calculated properties of interest: HOMO-LUMO gap, $|\mu_{\text{Dipole}}|$, and the isotropic polarizability and quadrupole. Overall, the representations displayed in Figure 7 demonstrate low correlation between these four important properties and either G_1 or G_2 , but do suggest some structure in the data, which might be worthy of further exploration. For example, Figure 7a suggests a region in the HOMO-LUMO gap between 4.0 and 6.0 eV that is mainly occupied by compounds with high G_1 and $G_2 = 1.0$. On the other hand, Figure 7b shows a tendency for



Figure 6: Pairwise representation of commonly used quantum properties: a) HOMO and LUMO energies, colored by metal; b) HOMO-LUMO gap *versus* the isotropic polarizability, colored by the value of the G_1 index; c) QTAIM charge of the metal (q_{metal}) versus the magnitude of the dipole moment $(|\mu_{Dipole}|)$, colored by G_1 , and; d) q_{metal} versus the isotropic polarizability, colored by the value of the G_2 index.

gillespian compounds to bear lower dipole moments, which may be due to a more symmetrical 276 arrangement of both the ligands and the iVSCCs. Figure 7c shows some ascending trend of 277 the isotropic polarizability with respect to G_1 , although strongly obfuscated by other factors. 278 Furthermore, Figure 7d reveals some interesting structure concerning the data for the 279 isotropic quadrupole: although both gillespian and completely non-gillespian (i.e. $G_1 =$ 280 $G_2 = 0$) compounds appear to fill the range available for this variable, TM complexes with 281 $G_2 = 1$ and intermediate values of G_1 prefer higher (less negative) values. TM complexes 282 with values of G_1 , but $G_2 = 1$ also show higher values of the isotropic quadrupole, but 283 lowering G_2 does increase the dispersion to a region almost as wide as the one observed for 284 $G_1 = G_2 = 0$. Because of this, the graphic displayed in Figure 7d shows a void region, 285 suggesting that compounds with $G_2 = 1$ do not present an isotropic quadrupole lower than 286 -50 a.u., unless G_1 is also 1. 287

In general, the G_1 and G_2 indexes convey some information on the properties of TM complexes in the TM topo database. The structured data suggested in Figure 7 is not easily discernible when considering other iVS descriptors, such as n_{iVSCC} and r_{iVS} , as depicted in Figure S1 of the SI. Indeed, r_{iVS} is clearly related to the atomic number of the metal center (Cf. Figure 2a), whereas n_{iVSCC} appears to follow a general trend towards eight iVSCCs arranged in an octahedral arrangement, as discussed above.

²⁹⁴ 4 Conclusions

This work presents the TMtopo data set, which provides geometries, quantum calculated quantities and quantum topological descriptors for over 1000 TM complexes containing one first-row transition metal center and any possible combination of fluoride, chloride and oxygen, in the form of the oxo ligand. The complexes were systematically generated in order to explore different possible molecular geometries and spin multiplicities, and optimized using well established DFT techniques. The data was then curated in order to exclude duplicated



Figure 7: Scatter plots of the HOMO-LUMO gap (a); $|\mu_{\text{Dipole}}|$ (b); isotropic polarizability (c), and isotropic quadrupole (d), against the G_1 index, and colored by the value of G_2 (common color code at the bottom of the Figure). Jitter with an amplitude of 0.1 were introduced along the xx coordinates (G_1 , adimensional) in order to aid visualization.

and non-equilibrium geometries. A total of 1110 unique entries were compiled upon curation.
 Quantum topological descriptors were then collected under the QTAIM framework.

Particular attention was given to the topological features of $\nabla^2 \rho(\mathbf{r})$ within the metal's 303 atomic basin, which allowed for an unprecedented systematic survey of the properties con-304 cerning the relationship between iVSCC and other molecular properties. Preliminary ob-305 servations reported in this work highlight that the number of iVSCCs is of paramount im-306 portance in lowering the electronic energy of the metal center, allowing for non-gillespian 307 arrangements of the iVSCCs to proliferate. Deviations to the gillespian arrangements were 308 quantified in the form of two indexes G_1 and G_2 , measuring excess of iVSCCs and their 300 misalignment with the ligands, respectively. 310

Pairwise representations of the data in TMtopo suggests a large number of poorly correlated descriptor/property, although some structure is noticeable in such representations, suggesting that further useful information may be gathered by advanced multivariate statistics and/or machine learning methods. We hope to report on the application of these methods for gathering further information in a subsequent publication.

³¹⁶ Supporting Information Available

Additional data (database specifications and additional figures) are available free of charge in the Electronic Supporting Information. This information is available free of charge via the Internet at http://pubs.acs.org.

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Graphical TOC Entry

