

Theoretical estimates of equilibrium carbon and hydrogen isotope effects in microbial methane production and anaerobic oxidation of methane

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Abstract

Microbial production and consumption of methane are widespread in natural and artificial environments, with important economic and climatic implications. Attempts to use the isotopic composition of methane to identify its sources are complicated by incomplete understanding of the mechanisms of variation in methane’s isotopic composition. Knowledge of the equilibrium isotope fractionations among the large organic intracellular intermediates in the microbial pathways of methane production and consumption must form the basis of any exploration of the mechanisms of isotopic variation, but estimates of these equilibrium isotope fractionations are currently unavailable. To address this gap, we calculated the equilibrium isotopic fractionation of carbon ($^{13}\text{C}/^{12}\text{C}$) and hydrogen (D/H) isotopes among compounds in the anaerobic methane metabolisms, as well as the abundance of double isotope substitutions (“clumping,” i.e., a single ^{13}C –D bond or two ^{12}C –D bonds) in these compounds. The density functional theory calculations are at the M06-L/def2-TZVP level of theory with the SMD implicit solvation model, which we have recently tested against measured equilibrium isotope fractionations. The computed $^{13}\beta$ and $^2\beta$ values decrease with decreasing average oxidation state of the carbon atom in the molecules, resulting in a preference for enrichment in ^{13}C and D of the molecules with more oxidized carbon. Using the computed β values, we calculated the equilibrium isotope fractionation factors in the prominent methanogenesis pathways (hydrogenotrophic, methylotrophic and acetoclastic) and in the pathway for anaerobic oxidation of methane (AOM) over a temperature range of 0-700 °C. Our

calculated equilibrium fractionation factors compare favorably with experimental constraints, where available, and we then used them to investigate the relation between the apparent isotope fractionation during methanogenesis or AOM and the thermodynamic drive for these reactions. We show that a detailed map of the equilibrium fractionation factors along these metabolic pathways allows for an evaluation of the contribution of equilibrium and kinetic isotope effects to apparent isotope fractionations observed in laboratory, natural and artificial settings. The comprehensive set of equilibrium isotope fractionation factors calculated in this study provides a firm basis for future explorations of isotope effects in methane metabolism.

1 INTRODUCTION

2 1.1 General

3 The isotopic distributions in thermodynamic equilibria can be predicted with quantum me-
4 chanical calculations. These theoretical predictions are invaluable in exploring isotope frac-
5 tionation systematics where experimental data are lacking or hard to obtain (e.g., Rustad
6 et al., 2008; Eldridge et al., 2016), such as for the intracellular components of biological
7 production and oxidation of methane (methanogenesis and methanotrophy, respectively).
8 Theoretical approaches, in particular density functional theory (DFT), have been widely
9 applied to small molecules (Li & Liu, 2011; Fujii et al., 2014), and recently also to large
10 organic molecules (Black et al., 2007; Rustad, 2009; Wang et al., 2009a,b, 2013; Moynier
11 & Fujii, 2017; Iron & Gropp, 2019) in the gas, aqueous and solid phases. The application
12 of DFT is of special interest in methanogenesis and methanotrophy since these processes
13 involve large organic molecules, which have received less attention than small molecules due
14 to issues of calculation cost and accuracy (Iron & Gropp, 2019). Consequently, studies to
15 date of the isotopic compositions in methanogenesis and methanotrophy have focused on the
16 extracellular substrates and products, mainly H₂, CO₂, CH₄ and H₂O, but have neglected
17 the intracellular components of these processes. To bridge this gap, we (*i*) provide a novel set
18 of constraints on the temperature-dependent carbon and hydrogen isotope equilibrium frac-
19 tionation factors (EFFs) among the intracellular molecules involved in the methanogenesis
20 and methanotrophy pathways, (*ii*) compare these results to previous reports, mostly of the
21 pathway end-members, and (*iii*) discuss the possible applications and the associated caveats
22 of these results in geochemical and bioisotopic models.

23 1.2 Methanogenesis and anaerobic methanotrophy

24 1.2.1 Physiology of methanogens and methanotrophs

25 Methanogenic organisms produce methane by fixing CO₂ in the hydrogenotrophic pathway
26 or by reducing methylated compounds, such as acetate (i.e., acetoclastic methanogenesis) or
27 methanol (i.e., methylotrophic methanogenesis), as described in the following net reactions:



28 These three metabolic pathways have been described in detail (Thauer et al., 2008) and
29 all are assumed to originate from a single, common ancestor that utilized a version of the

hydrogenotrophic pathway (Berghuis et al., 2019) (Fig. 1). In the hydrogenotrophic pathway (Eq. 1), CO_2 is reduced to methane in seven, consecutive enzymatic reactions, with four reduction steps, which are mediated by the electron carriers ferredoxin (Fd), coenzyme F_{420} (F_{420}) and coenzyme B (HS-CoB). In acetoclastic methanogenesis (Eq. 2), acetate (CH_3COO^-) is initially activated to acetyl-CoA ($\text{CH}_3\text{-COSCoA}$). The methyl group is then transferred to tetrahydromethanopterin (H_4MPT) and then into the classic hydrogenotrophic pathway (Welte & Deppenmeier, 2014), while the CoA-bound carbonyl carbon is oxidized to CO_2 . In the methylotrophic pathway (Eq. 3), the methyl group is transferred from methanol directly to HS-CoM to form methyl coenzyme M ($\text{CH}_3\text{-SCoM}$). The $\text{CH}_3\text{-SCoM}$ is then either oxidized to CO_2 in the oxidative direction of the methanogenesis pathway or reduced to methane. The reductive and oxidative branches of this pathway operate at a ratio of $\sim 3:1$, to balance the electrons needed for the reduction of $\text{CH}_3\text{-SCoM}$ (Vanwonterghem et al., 2016).

Anaerobic oxidation of methane (AOM) is an important process in mitigating the emission of methane from anoxic sediments to the atmosphere (Egger et al., 2018). More specifically, AOM is mediated by anaerobic methanotrophs (ANME) in a modified reverse-methanogenesis pathway, where the same enzymes of the hydrogenotrophic pathway catalyze methane oxidation. The oxidation is generally coupled to syntrophic sulfate, nitrate or ferric iron reduction (Scheller et al., 2010; Thauer, 2011; McGlynn, 2017; Scheller et al., 2017) or to nonsyntrophic formation of elemental sulfur (Milucka et al., 2012).

1.2.2 Isotopic composition of methane

The hydrogen (D/H) and carbon ($^{13}\text{C}/^{12}\text{C}$) isotope ratios of methane have been extensively used to distinguish among environmental methane sources (Whiticar, 1999), yet the sources often overlap in their characteristic isotopic compositions (e.g., Alstad & Whiticar, 2011), masking the source of methane. Recent developments in the precise measurement of the abundance of the doubly-substituted (“clumped”) isotopologues of methane (i.e., $^{13}\text{CH}_3\text{D}$ and $^{12}\text{CH}_2\text{D}_2$) further constrain the temperature of methane formation under equilibrium conditions (Stolper et al., 2014a; Ono et al., 2014; Stolper et al., 2015; Ash et al., 2019). However, disequilibrium clumped isotope compositions are common in laboratory and natural settings (Wang et al., 2015; Gruen et al., 2018; Young et al., 2017; Young, 2019; Ono et al., 2020), and the mechanisms that control these departures from equilibrium are not fully understood.

Bioisotopic models have the potential to reveal details of the elusive mechanisms that control such isotopic fingerprints. Such models have been successfully applied to microbial sulfate reduction by demonstrating how the sulfur isotope fractionations of individual steps in the pathway combine to control the net isotope fractionation (Wing & Halevy, 2014; Bradley et al., 2016; Zaarur et al., 2017; Wenk et al., 2017; Sim et al., 2019). A similar hypothesis

66 was suggested for carbon and hydrogen isotopes in methanogenesis (Valentine et al., 2004).
67 Previous applications of simplified isotope mass-balance models to the hydrogenotrophic
68 methanogenesis pathway assign EFFs of the intracellular intermediate reactions as free pa-
69 rameters without any theoretical or experimental constraints (Wang et al., 2015; Stolper
70 et al., 2015; Cao et al., 2019). To address this gap, to facilitate the application of bioisotopic
71 models to microbial production and consumption of methane, and to allow a better under-
72 standing of data from laboratory experiments and natural environments, we provide hydrogen
73 and carbon isotope and clumped isotopologue EFF values for the three main pathways of
74 methanogenesis and for ‘reverse-methanogenesis’ AOM.

75 **1.3 Calculating equilibrium isotope fractionation factors**

76 Experimentally-measured EFFs are the basis for understanding the distributions of isotopes
77 in many geochemical systems, but the scope of these methods is often limited by long equi-
78 libration times at low temperatures, potential isotope fractionation during the sampling
79 processes, and complex separation procedures of the reactants and products. Early studies
80 demonstrated that EFFs can be calculated from the observed molecular vibrational frequen-
81 cies using a simplified quantum mechanical model of the experimentally measured molecular
82 vibrations and rotations and expressed as a reduced partition function ratio (RPFR) (Urey,
83 1947; Bigeleisen & Mayer, 1947). Subsequently, computational methods such as Hartree–Fock
84 (HF) (Roothaan, 1951) and DFT (Hohenberg & Kohn, 1964; Kohn & Sham, 1965) provided
85 an independent means of estimating the vibrational frequencies. These approaches have
86 been extensively used to study several systems of geochemical interest, primarily for small
87 molecules in the gaseous and aqueous phases, including sulfur compounds (Otake et al., 2008;
88 Eldridge et al., 2016), metals (Domagal-Goldman & Kubicki, 2008; Fujii et al., 2014) and
89 crystalline solids (e.g., Méheut et al., 2007). The application to large organic molecules in
90 the aqueous phase has remained limited due to computational cost and inaccurate results.
91 Accordingly, in methanogenesis, experimental and theoretical work so far has focused on
92 the small gaseous end-members, namely the $\text{H}_2\text{O}\text{--}\text{H}_2$, $\text{CH}_4\text{--}\text{H}_2$ and $\text{CO}_2\text{--}\text{CH}_4$ systems (e.g.,
93 Suess, 1949; Bottinga, 1969; Horibe & Craig, 1995; Horita, 2001), and not on the intracellular
94 organic intermediates.

95 There have been attempts to calculate EFFs among large organic molecules for some
96 elements, such as Mg (Black et al., 2007; Moynier & Fujii, 2017), C (Rustad, 2009), Cu (Ten-
97 nant et al., 2017) and H (Wang et al., 2009a,b, 2013). Wang et al. (2009a; 2013) compared
98 experimental and DFT calculations (B3LYP/6-311G**) of hydrogen isotope EFFs of the C_α
99 positions in ketones finding a good overall agreement. The B3LYP functional is commonly
100 used in geochemical DFT calculations, and is the most commonly used functional in general.
101 However, there are more modern and cost-effective methods (Zhao et al., 2011; Mardirossian

102 et al., 2016), and until recently the accuracy of these and other functionals in predicting EFFs
103 of large organic molecules has not been systematically compared. We recently conducted a
104 thorough examination of various DFT functionals and basis sets to determine the uncertainty
105 associated with the prediction of EFFs of H, C, N and O stable isotopes among large soluble
106 organic molecules (Iron & Gropp, 2019). The mean unsigned error (MUE) of these calcula-
107 tions in predicting the hydrogen isotope fractionation in the C_α position of linear and cyclic
108 ketones is 20.8‰, comparable to the results of Wang et al. (2009a; 2013). For C, N and O
109 isotopes, there was an insignificant difference between the various methods, but the M06-L
110 functional with the def2-TZVP basis set and the SMD solvation model yielded the best fits,
111 with an MUE of 2.3‰ for carbon isotopes. In this study, we employed the best-fit DFT
112 model (M06-L functional, def2-TZVP basis set, SMD solvation model) to calculate a novel
113 set of carbon and hydrogen isotope equilibrium fractionation factors for the species involved
114 in the core methanogenesis and AOM pathways. These calculations can aid in the interpre-
115 tation of isotope fractionations during methanogenesis and anaerobic oxidation of methane,
116 in both laboratory cultures and natural environments. Moreover, these calculations elimi-
117 nate a degree of freedom from future bioisotopic models, which could potentially be used
118 to understand methane isotope compositions out-of-equilibrium and their physiological and
119 environmental implications. We will discuss the uncertainties in our predictions and their
120 implications for the observations of the isotopic composition of methane in various systems.

2 METHODS

2.1 Overview: the Bigeleisen–Mayer equation

The RPF_R is the equilibrium isotope fractionation factor of a given isotope pair in a given molecule:

$$\text{RPF}_R = \frac{\sigma}{\sigma^*} \prod_{i=1}^{3N-6(5)} \frac{u_i^*}{u_i} \cdot \frac{\exp(-u_i^*/2)}{\exp(-u_i/2)} \cdot \frac{1 - \exp(-u_i)}{1 - \exp(-u_i^*)} \quad (4)$$

where $u_i = hc\omega_i/k_B T$, h is the Planck constant, c is the speed of light, ω_i are the vibrational frequencies, k_B is the Boltzmann constant, T is the absolute temperature, σ is the molecular symmetry number (most large organic molecules lack any symmetry so this term is often unity), and the asterisk denotes the species with the heavy isotope(s). The product runs over the $3N - 5$ or $3N - 6$ vibrational frequencies of linear and nonlinear molecules, respectively, where N is the number of atoms in the molecule. The three ratios in the product are the classical factor accounting for rotational and translational energy, the zero-point energy (ZPE) contribution, and the excitation factor. The RPF_R is related to the β factor, which is the RPF_R of a compound and an ideal monoatomic gas. For single isotope substitutions, when the excess factors are ignored, $\beta = \text{RPF}_R$, and the (temperature-dependent) EFF between two species (α) that contain the rare isotope r is the ratio of the respective β s: ${}^r\alpha_{\text{A-B}}^{\text{eq}} = {}^r\beta_{\text{A}}/{}^r\beta_{\text{B}}$.

We also calculated the EFFs of doubly-substituted (clumped) isotopologues that contain a single ^{13}C – D bond or two ^{12}C – D bonds. The abundance of clumped isotopologues is commonly reported as the deviation from the expected stochastic distribution, $\Delta_i^{\text{eq}} \equiv (R_i^{\text{eq}}/R_i^* - 1)$ where i is the isotopologue of interest, R_i^{eq} is the abundance of the clumped isotopologue relative to the nonsubstituted isotopologue at equilibrium, and R_i^* is its abundance at a stochastic distribution of the rare isotopes. We calculated Δ_i^{eq} from RPF_Rs following Cao and Liu (2012), who suggested that Δ_i^{eq} of the clumped isotopologue $\text{V}'\text{Y}'\text{Y}_{n-1}$, where V' and Y' are the rare isotopes of atoms V and Y , respectively, and n is the number of Y atoms in the molecule VY_n , can be calculated by the general relation:

$$\Delta_{\text{V}'\text{Y}'\text{Y}_{n-1}} = \left(\frac{(\sigma^*/\sigma) \times {}^{\text{V}'\text{Y}'}\text{RPF}_{\text{V}'\text{Y}'\text{Y}_{n-1}}}{{}^{\text{V}'}\beta_{\text{V}'\text{Y}_n} \times {}^{\text{Y}'}\beta_{\text{V}'\text{Y}_n}} \right) \quad (5)$$

where ${}^{\text{V}'\text{Y}'}\text{RPF}_{\text{V}'\text{Y}'\text{Y}_{n-1}}$ is the RPF_R of the clumped isotopologue of interest. ${}^{\text{V}'}\beta_{\text{V}'\text{Y}_n}$ and ${}^{\text{Y}'}\beta_{\text{V}'\text{Y}_n}$ are approximately equal to the β values of single substitutions of V' and Y' in VY_n (Cao & Liu, 2012). In addition to the internal equilibrium distribution of V' – Y' bonds in the molecule VY_n (Eq. 5), we are interested in the distribution of V' – Y' bonds in large organic molecules of the general form $x\text{VY}_n$, where x denotes an arbitrary organic moiety. We calculated the EFFs of reactions that include a clumped isotopologue and distinguish between equilibrium

152 isotope effects in which a new V'-Y' bond is formed or broken:

$${}^{V'Y'}\alpha_{aV'Y,bVY'/cV'Y'} = {}^V\beta_{aV'Y} \times {}^{Y'}\beta_{bVY'}/{}^{V'Y'}\text{RPFR}_{cV'Y'} \quad (6)$$

153 and equilibrium isotope effects in which the original V'-Y' bond remains intact:

$${}^{V'Y'}\alpha_{aV'Y'/cV'Y'} = {}^{V'Y'}\text{RPFR}_{aV'Y'}/{}^{V'Y'}\text{RPFR}_{cV'Y'}. \quad (7)$$

154 By analogy to the terminology for kinetic isotope effects, we refer to these as primary and
155 secondary equilibrium isotopes effects. As suggested by Wang et al. (2015), the clumped
156 isotope fractionation factors can be expressed as ${}^{13,2}\alpha^{\text{eq}} = {}^{13}\alpha^{\text{eq}} \times {}^2\alpha^{\text{eq}} \times {}^{13,2}\gamma^{\text{eq}}$ and ${}^{2,2}\alpha^{\text{eq}} =$
157 ${}^2\alpha^{\text{eq}} \times {}^2\alpha^{\text{eq}} \times {}^{2,2}\gamma^{\text{eq}}$. The unitless ${}^{13,2}\gamma^{\text{eq}}$ and ${}^{2,2}\gamma^{\text{eq}}$ factors are a measure of the deviation
158 of the actual isotope fractionation factor from a simple product of the isotope fractionation
159 factors of the singly-substituted isotopologues. Though originally proposed for KFFs, the
160 γ^{eq} notation may be used to express similar deviations in EFFs, and we adopt it here for
161 consistency with the existing literature. By definition $\alpha^{\text{eq}} = \alpha^-/\alpha^+$, where α^- and α^+ are the
162 backwards and reverse kinetic isotope effects, respectively, and it can be shown that based
163 on this relation $\gamma^{\text{eq}} = \gamma^-/\gamma^+$, where γ^- and γ^+ are the backwards and forward kinetic γ
164 factors, respectively.

165 **2.2 Quantum mechanical calculations of partition coefficients for** 166 **large organic molecules**

167 All calculations were done with GAUSSIAN16 revisions A.03, B.01 and C.01 (Frisch et al.,
168 2016). Based on its performance in predicting EFFs in large organic molecules (Iron &
169 Gropp, 2019), we chose the M06-L DFT exchange-correlation functional and def2-TZVP
170 basis set (Andrae et al., 1990; Kaupp et al., 1991; Leininger et al., 1996; Metz et al., 2000;
171 Weigend & Ahlrichs, 2005). The use of scaling factors has been shown to provide more
172 accurate predictions of vibrational frequencies (see Kesharwani et al. (2016) and references
173 therein). As discussed in our benchmark study (Iron & Gropp, 2019), two scaling factors
174 were used in Eq. 4, one for the zero-point (vibrational) energy term (the second term in
175 product, specifically, $\lambda_{\text{ZPE}} = 0.9825$) and another for the harmonic frequencies in the other
176 two terms (specifically, $\lambda_{\text{harm}} = 0.9965$).

177 The original derivation of RPFR by Bigeleisen and Mayer suited molecules in a gas phase,
178 but biochemical reactions within the cells usually occur in the aqueous phase. Adding explicit
179 water molecules should, in principle, yield more accurate results for reactions in aqueous
180 solution, but this also increases the size of the system and associated calculation costs.
181 Implicit solvation models, which assume that the solvent effects can be described by the free
182 energy cost of solvation alone, thereby offering a substantial reduction in computational cost,

183 are a common solution to this issue (Tomasi et al., 2005). We generated the RPFRRs of the
184 end-member molecules in both the gaseous and aqueous phases. To account for the aqueous
185 phase, we used the SMD solvation model of Truhlar and coworkers (Marenich et al., 2009).

186 In this work, we use the singly substituted hydrogen isotopologues as a proxy for the bulk
187 D/H ratios of the compounds, which is a common practice for isotopologues with atoms in
188 equivalent positions (Galimov, 2006; Wang et al., 2009a; Liu et al., 2010). We perform our
189 DFT calculations for frozen-geometry molecules, which produce distinct RPFRR values for
190 substitution of D for H in the different positions of the methyl groups. The free rotation of
191 the methyl group makes the three C–H bonds equivalent and chemically indistinguishable,
192 and we therefore calculate the RPFRR of the deuterated molecule from the geometric mean
193 of RPFRR values determined from the distinct site-specific D/H-substitutions (Wang et al.,
194 2009a).

195 Liu et al. (2010) considered a number of corrections to the Bigeleisen–Mayer equation,
196 including anharmonic effects and vibrational–rotational couplings. However, they studied
197 small, triatomic molecules, where these corrections are small. In our previous study, where
198 we considered much larger molecules, it was found that these terms were actually detrimental
199 to the accuracy of the results (Iron & Gropp, 2019). We hypothesized that the degradation of
200 accuracy may result from the inclusion of these terms violating the underlying assumptions of
201 the Bigeleisen–Mayer equation, specifically, the assumptions of a rigid rotor and a harmonic
202 oscillator, which in turn allow the use of the Teller–Redlich product rule. As noted by Webb
203 & Miller (2014) in their study comparing path integral Monte Carlo (PIMC) methods
204 with the Urey-harmonic oscillator model, the latter takes advantage of substantial error
205 cancellation.

206 PIMC methods, which are based on potential energy surface fits to DFT or CCSD(T)
207 data, have recently been used to determine EFFs (e.g., Webb et al., 2017; Eldridge et al.,
208 2019). However, these methods are limited to very small molecules such as methane (Eldridge
209 et al., 2019) or ethane (Webb et al., 2017), and their application to the much larger organic
210 molecules studied here as part of the methanogenesis pathways would be a Herculean task
211 and beyond the scope of the current study. He et al. (2020) recently suggested that trun-
212 cating large organic molecules to ease the calculation cost may have a negligible effect on
213 $^{13}\alpha$ predictions when used with an implicit solvation model. We chose to model the entire
214 molecules, especially since none were too large for the available computer hardware. He et al.
215 used the more expensive Møller-Plesset (MP2) method, yet we found that reliable results can
216 be obtained using cheaper DFT methods and, in fact, MP2 is inferior to many DFT function-
217 als in predicting vibrational frequencies, which are the basis of the Bigeleisen-Mayer equation
218 (Eq. 4) (Iron & Gropp, 2019). In addition, in some cases long-range interactions, such as
219 hydrogen bonds, may affect the vibrational frequency of the primary site, and these effects

220 might be overlooked if truncations are applied without the appropriate considerations. A
221 careful truncation of molecules can be effective, but it does introduce a new potential source
222 of error.

223 3 RESULTS

224 We calculated the RPFs for position-specific single ^{13}C or D substitutions and double
 225 ^{13}C and D or D and D substitutions of the molecules that participate in anaerobic methane
 226 metabolisms at the M06-L/def2-TZVP level of theory at 0-700 °C (Full details in Section 2.2).
 227 The results of these calculations are presented in Tables 2–5, and Tables S.1 and S.2. The
 228 $^{13}\beta$ and $^2\beta$ values at 0-100 °C, the temperature range that is relevant for biological activity
 229 and the large organic molecules on which we focus, are presented in Fig. 2. In general, $^{13}\beta$
 230 and $^2\beta$ RPFs at 25 °C covary with the carbon oxidation state, with the exception of the
 231 $^{13}\beta$ values for the methyl and carbonyl groups in $\text{CH}_3\text{-COSCoA}$ and the $^{13}\beta$ for the methyl
 232 group in $\text{CH}_3\text{-COOH}$. The $^2\beta$ and $^{13,2}\text{RPF}$ values also covary with the carbon oxidation
 233 state, though only for oxidation states between zero and -4 .

234 We calculated the EFFs (α^{eq}) for the enzymatic reactions in the hydrogenotrophic, ace-
 235 toclastic and methylotrophic methanogenesis pathways. The full results at 25 °C, 50 °C and
 236 75 °C are provided in Tables 6, 8 and 9 and Figs. 3-4. For each reaction, we report α -values
 237 based on β and RPF values through the relation ${}^r\alpha_{\text{A-B}}^{\text{eq}} = \beta_{\text{A}}/\beta_{\text{B}}$, where we arbitrarily
 238 chose compound A to be upstream of compound B in the methanogenesis pathway. For
 239 convenience, we follow the convention of reporting EFFs as the natural logarithm of ${}^r\alpha_{\text{A-B}}^{\text{eq}}$
 240 in permil (‰) units ($1000\ln\alpha$). The isotope fractionations of reactions involving H_2O are
 241 reported relative to $\text{H}_2\text{O}_{(l)}$. As calculation of the RPF for liquid H_2O is notoriously chal-
 242 lenging, we chose to apply the approach used by Wang et al. (2009a) and calculate $^2\beta$ of
 243 $\text{H}_2\text{O}_{(g)}$ and use the ${}^2\alpha_{\text{H}_2\text{O}_{(l)}-\text{H}_2\text{O}_{(g)}}^{\text{eq}}$ reported for the range 0-374 °C (Horita & Wesolowski,
 244 1994), where ${}^2\beta_{\text{H}_2\text{O}_{(l)}} = {}^2\beta_{\text{H}_2\text{O}_{(g)}} \times {}^2\alpha_{\text{H}_2\text{O}_{(l)}-\text{H}_2\text{O}_{(g)}}^{\text{eq}}$.

245 Notably, the carbon isotope fractionations of the reactions in the hydrogenotrophic path-
 246 way, which add up to the net $\text{CO}_2\text{-CH}_4$ carbon isotope fractionation, distribute almost evenly
 247 among four steps in the pathway, three of which are carbon reduction reactions. The $\text{CO}_2\text{-}$
 248 CHO-MFR , $\text{CH}\equiv\text{H}_4\text{MPT}^+\text{-CH}_2=\text{H}_4\text{MPT}$, $\text{CH}_2=\text{H}_4\text{MPT-CH}_3\text{-H}_4\text{MPT}$ and $\text{CH}_3\text{-H}_4\text{MPT-}$
 249 $\text{CH}_3\text{-SCoM}$ carbon isotope fractionations are all between $\sim 15\text{‰}$ and $\sim 18\text{‰}$ at 25 °C, whereas
 250 the other reactions yield smaller positive or small negative isotope fractionations (Table 6).
 251 For hydrogen, primary equilibrium isotope effects, in which a C–H bond is broken or made,
 252 produce larger positive or negative hydrogen isotope fractionations than secondary equilib-
 253 rium isotope effects, in which C–H bonds remain intact, except for the reaction between
 254 F_420H_2 and $\text{CH}_3\text{-H}_4\text{MPT}$ that has a smaller primary EFF than its secondary EFFs (Fig. 4).

255 Using the $^{13}\beta$, $^2\beta$, ^2RPF and $^{13,2}\text{RPF}$ values of the intermediates in the methanogenic
 256 pathways, we calculated these metabolites’ equilibrium deviation of clumped isotopologue
 257 abundance from a stochastic distribution (Δ_i^{eq} , where i is the isotopologue of interest). The
 258 Δ_i^{eq} values for $^{13}\text{C}\text{-D}$ clumping increase with decreasing oxidation state, from $\Delta_{^{13}\text{CDO-H}_4\text{MPT}}^{\text{eq}}$
 259 $= 4.211\text{‰}$ to $\Delta_{^{13}\text{C}_3\text{H}_3\text{D}}^{\text{eq}} = 5.738\text{‰}$ at 25 °C, while Δ_i^{eq} values for D–D clumping are larger,

260 ranging from $\Delta_{12\text{CD}_2=\text{H}_4\text{MPT}}^{\text{eq}} = 13.38\text{‰}$ to $\Delta_{12\text{CH}_2\text{D}_2}^{\text{eq}} = 18.50\text{‰}$ at 25 °C, and they all depend
261 inversely on temperature (Fig. 5 and Table 7). We also calculated the clumped isotope
262 fractionations of reactions that involve doubly-substituted isotopologues ($^{13,2}\alpha^{\text{eq}}$ and $^{2,2}\alpha^{\text{eq}}$),
263 and the deviation of these values from the product of the $^{13}\alpha^{\text{eq}}$ and $^2\alpha^{\text{eq}}$ values ($^{13,2}\gamma^{\text{eq}}$ and
264 $^{2,2}\gamma^{\text{eq}}$). In general, the $^{13,2}\alpha^{\text{eq}}$ values are similar in magnitude, but not identical, to the
265 corresponding product of $^{13}\alpha^{\text{eq}}$ and $^2\alpha^{\text{eq}}$. For secondary equilibrium isotope effects, where
266 the $^{13}\text{C-D}$ or the $^{12}\text{C-D}$ bonds remain intact, $^{13,2}\gamma^{\text{eq}}$ and $^{2,2}\gamma^{\text{eq}}$ are very close to unity, with
267 a mean values of 0.9998 and 0.9994 at 25 °C, respectively. For primary equilibrium isotope
268 effects, where a $^{13}\text{C-D}$ or $^{12}\text{C-D}$ bond is formed or broken, $^{13,2}\gamma^{\text{eq}}$ and $^{2,2}\gamma^{\text{eq}}$ are larger, with
269 mean values of 0.9951 and 0.9849, respectively. A complete list of γ^{eq} values is in Tables S.5
270 and S.6.

4 DISCUSSION

4.1 Beta values

The principles of equilibrium isotope fractionation can explain the general trends observed in the calculated $^{13}\beta$ values. At a given temperature, these values decrease with the carbon oxidation state (from +4 in CO_2 to -4 in CH_4), which exerts first-order control over the carbon bonding environment. The correlation of the $^2\beta$, $^{13,2}\text{RPFR}$ and $^{2,2}\text{RPFR}$ values with the carbon oxidation state is less trivially understood, as the hydrogen's bonding environment is also affected by the S, N and O atoms to which the carbon is often bound and by the orbital hybridization of the molecules. Irrespective of the mechanism(s), similar correlations of β values and oxidation state were observed for S (Eldridge et al., 2016), Fe (Fujii et al., 2014), and Se (Li & Liu, 2011) isotope fractionations. A natural consequence of this correlation is that, in general, we may expect carbon reduction reactions to have carbon, hydrogen and clumped isotope EFFs larger than unity.

4.2 Uncertainties in calculated isotope fractionation factors

The uncertainties in our predicted EFFs would best be estimated by comparison with experimentally determined isotope fractionations. However, experimental evaluations of carbon, hydrogen and clumped isotope fractionations among the intermediate, intracellular metabolites of all three methanogenic pathways have not yet been reported, with the exception of one investigation of the carbon and hydrogen isotope fractionation among $\text{CH}_3\text{-SCoM}$, HS-CoB and CH_4 . Moreover, in the methylotrophic and acetoclastic pathways, even measurements of equilibrium isotope fractionations between the pathway end-members have not been reported. In the absence of experimental constraints on the isotope fractionation factors, we follow the approach taken in previous studies for assessing the accuracy of DFT calculations of EFFs of large organic molecules. The 95% confidence interval (CI95) associated with the comparison of calculated and experimental hydrogen EFFs was found to be $\pm 5\%$ to $\pm 10\%$ for linear ketones (Wang et al., 2009a) and $\pm 10\%$ to $\pm 30\%$ for cyclic ketones (Wang et al., 2013), at the B3LYP/6-311G** level of theory. More recently, we extended the evaluation to isotopes of C, N and O (Iron & Gropp, 2019). The associated CI95 for C, N and O isotopes is $\pm 2.5\%$. However, CI95 represents only the uncertainty in the parameters of the regression model, and the predictive power of our DFT calculations is more rigorously captured by the 95% prediction interval (PI95). The nonsimultaneous observation bounds of the PI95s are $\pm 30\%$ for hydrogen isotopes and $\pm 8\%$ for carbon isotopes. While the benchmark database on which these PI95 are based is limited in its coverage of different functional groups, we suggest that it is currently the most suitable alternative to experimental constraints when

305 attempting to determine the actual magnitude of the uncertainty.

306 **4.3 Comparisons with previous experimental and theoretical stud-** 307 **ies**

308 To validate our calculated EFFs, we compare our results with previous experimental obser-
309 vations and theoretical predictions of EFFs.

310 **4.3.1 isotope fractionation in the CO₂–CH₄–H₂O–H₂ system**

311 The small, volatile end-members of the hydrogenotrophic methanogenesis pathway have been
312 well characterized in both theoretical and experimental studies, and the efforts to better
313 constrain the isotope fractionations among them are ongoing. Four EFFs are of interest:
314 (*i*) the CO₂–CH₄ carbon isotope fractionation, (*ii*) the H₂O–H₂ hydrogen isotope fraction-
315 ation, (*iii*) the CH₄–H₂ hydrogen isotope fractionation, and (*iv*) the CH₄–H₂O hydrogen
316 isotope fractionation. For hydrogen isotopes, we also present here the results using the
317 HCTH/def2-TZVP level of theory. Overall, our predictions based on the M06-L/def2-TZVP
318 and HCTH/def2-TZVP levels of theory yield good agreement with previous estimates of the
319 isotope fractionation factors, as discussed below.

320 Our results for case (*i*) agree with $1000\ln^{13}\alpha_{\text{CO}_2\text{--CH}_4}^{\text{eq}}$ values calculated using measured
321 vibrational frequencies over a temperature range of 0-700 °C (Richet et al., 1977) and with ex-
322 perimental observations of $1000\ln^{13}\alpha_{\text{CO}_2\text{--CH}_4}^{\text{eq}}$ over a temperature range of 200-700 °C (Horita,
323 2001; Kueter et al., 2019) (Fig. 7A). To the best of our knowledge, CO₂–CH₄ carbon isotope
324 fractionations have not been experimentally measured below 200 °C, but the agreement of
325 our theoretical predictions with the available, high-temperature experimental data provides
326 confidence in our predictions at lower temperatures.

327 For case (*ii*), our $1000\ln^2\alpha_{\text{H}_2\text{O--H}_2}^{\text{eq}}$ values generally agree with previous experimental mea-
328 surements at low and high temperatures (Cerrai et al., 1954; Rolston et al., 1976) (Fig. 7B).
329 Rolston et al. (1976) measured isotope fractionation between H₂O_(l) and H_{2(g)}. Our H₂O–H₂
330 hydrogen isotope fractionations using M06-L are comparable but slightly higher than other
331 modeling studies based on spectroscopic data rather than DFT (Suess, 1949; Bardo & Wolfs-
332 berg, 1976). Our H₂O–H₂ hydrogen isotope fractionation based on the HCTH functional
333 produce a better fit to the observations, which is identical to the prediction of Bardo &
334 Wolfsberg (1976).

335 In case (*iii*), our $1000\ln^2\alpha_{\text{CH}_4\text{--H}_2}^{\text{eq}}$ values calculated at the M06-L level of theory are larger
336 by 40-45‰ than the values measured in the temperature range 200-500 °C (Horibe & Craig,
337 1995) (Fig. 7C), while the HCTH level of theory produces a better fit in this temperature
338 range (only 10-30‰ larger than the experimental values). At this range of temperatures,

339 there is disagreement between published theoretical estimates of the CH₄-H₂ equilibrium
 340 hydrogen isotope fractionation (Bottinga, 1969; Richet et al., 1977). Our results agree with
 341 those of Richet et al. (1977) and are smaller by 0-30‰ than the isotope fractionations calcu-
 342 lated by Bottinga (1969). Of all published theoretical estimates of the CH₄-H₂ equilibrium
 343 hydrogen isotope fractionation, our calculations at the HCTH level of theory are closest to
 344 the available high-temperature measurements. At temperatures below 100 °C, which are
 345 relevant for biological activity, there are no experimentally-determined CH₄-H₂ equilibrium
 346 hydrogen isotope fractionations. At these temperatures, there is an even larger discrepancy
 347 between all available theoretical predictions and a linear regression of ${}^2\alpha_{\text{CH}_4-\text{H}_2}^{\text{eq}}$ on $10^6/T$,
 348 extrapolated from experimental results at 200-500 °C (Horibe & Craig, 1995). Reconciling
 349 these discrepancies is beyond the scope of the current study, requiring experiments to de-
 350 termine the CH₄-H₂ equilibrium hydrogen isotope fractionations at temperatures below 200
 351 °C.

352 For case (*iv*), there are no direct measurements of the CH₄-H₂O equilibrium hydrogen
 353 isotope fractionation, $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}_{(l)}}^{\text{eq}}$, and a common practice is to combine available val-
 354 ues for $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2}^{\text{eq}}$ and $1000\ln^2\alpha_{\text{H}_2-\text{H}_2\text{O}_{(l)}}^{\text{eq}}$. As observed in a previous work (Wang et al.,
 355 2015), there is a striking disagreement among the different combinations of $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2}^{\text{eq}}$
 356 and $1000\ln^2\alpha_{\text{H}_2-\text{H}_2\text{O}_{(l)}}^{\text{eq}}$ values, with $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}_{(l)}}^{\text{eq}}$ ranging from -110 to -300‰ at 0 °C
 357 and from -85 to -210‰ at 60 °C (Fig. 8A). Most of this spread stems from the uncertainty
 358 in $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2}^{\text{eq}}$ values at low temperatures. To date, most interpretations of environ-
 359 mental $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}_{(l)}}^{\text{eq}}$ values rely on the extrapolation of the 200-500 °C experimental
 360 results (Horibe & Craig, 1995) to environmentally-relevant temperatures (e.g., Proskurowski
 361 et al., 2006; Wang et al., 2017). As noted above, this extrapolation does not agree with
 362 any method of theoretical calculation. To get a better understanding of this disparity, we
 363 compiled from the literature 165 environmental samples of biological origin, from marine
 364 sediments and gas reservoirs located below the sulfate-methane transition zone (Table S.11).
 365 We compared the measured CH₄-H₂O_(l) hydrogen isotope fractionation to the calculated
 366 temperature-dependent $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}_{(l)}}^{\text{eq}}$ (Fig. 8A-B). We also compiled 183 values of mea-
 367 sured CO₂-CH₄ carbon isotope fractionations from the same locations and their deviation
 368 from the expected temperature-dependent $1000\ln^3\alpha_{\text{CO}_2-\text{CH}_4}^{\text{eq}}$ (Fig. 8C). We found that the
 369 distribution of the deviations of the CO₂-CH₄ apparent carbon isotope fractionation from
 370 isotopic equilibrium has a distinct peak at zero, which we interpret as evidence of carbon
 371 isotope equilibration in the CO₂-CH₄ system. This may suggest that the hydrogen isotopes
 372 in the CH₄-H₂O system are also at (or close to) isotopic equilibrium. If this is the case,
 373 the distribution of compiled apparent hydrogen isotope fractionations from environmental
 374 samples may inform the choice of DFT theory and constrain the error on our calculated
 375 hydrogen isotope fractionation factors. The distribution of the deviation of the CH₄-H₂O_(l)

376 apparent hydrogen isotope fractionation from isotopic equilibrium calculated with the M06-L
377 functional has a distinct peak at zero, whereas with HCTH the distribution peaks at $\sim 20\%$,
378 suggesting that the former provides a more accurate prediction in this case.

379 **4.3.2 isotope fractionation between large organic molecules in the methanogen-** 380 **esis pathway**

381 To our knowledge, the equilibrium hydrogen isotope fractionation between $\text{CH}_3\text{-SCoM}$ and
382 CH_4 ($\ln^2\alpha_{\text{CH}_3\text{-SCoM}-\text{CH}_4}^{\text{eq}}$) is the only experimentally determined isotope fractionation between
383 intracellular intermediate metabolites in the methanogenesis pathway. Scheller et al. (2013)
384 investigated the kinetic isotope fractionation in the Mcr-catalyzed reaction, the final step
385 in methanogenesis. EFFs can be calculated from the kinetic isotope fractionation factors
386 (KFFs) of the reverse and forward reactions: $r\alpha_{\text{A}-\text{B}}^{\text{eq}} = r\alpha_{\text{B}\rightarrow\text{A}}^{\text{kin}}/r\alpha_{\text{A}\rightarrow\text{B}}^{\text{kin}}$, where $r\alpha_{\text{B}\rightarrow\text{A}}^{\text{kin}}$ and
387 $r\alpha_{\text{A}\rightarrow\text{B}}^{\text{kin}}$ are the reverse and forward KFFs, respectively. The KFF is defined as the ratio
388 of the rate constants for reaction of the heavy isotope to the light isotope (i.e., $^{13}k/^{12}k$ for
389 carbon isotopes and $^{\text{D}}k/^{\text{H}}k$ hydrogen isotopes). For a normal KFF, where the light isotope
390 reacts more rapidly than the heavy isotope, $r\alpha^{\text{kin}}$ is less than unity and its natural logarithm
391 is negative. While Scheller et al. (2013) did not explicitly report $1000\ln^2\alpha_{\text{CH}_3\text{-SCoM}-\text{CH}_4}^{\text{eq}}$, we
392 calculated a value of $17\pm 42\%$ at 60°C based on their measured $^2\alpha_{\text{CH}_3\text{-SCoM}\rightarrow\text{CH}_4}^{\text{kin}}$ (0.840 ± 0.01)
393 and $^2\alpha_{\text{CH}_4\rightarrow\text{CH}_3\text{-SCoM}}^{\text{kin}}$ (0.855 ± 0.05), taking into account error propagation. Our calculated
394 value of 40.4% at this temperature is within error of the experimental value.

395 **4.3.3 $\Delta_{^{13}\text{CH}_3\text{D}}^{\text{eq}}$ and $\Delta_{^{12}\text{CH}_2\text{D}_2}^{\text{eq}}$**

396 For methane, our predictions of $\Delta_{^{13}\text{CH}_3\text{D}}^{\text{eq}}$ in thermodynamic equilibrium agree well with previ-
397 ous theoretical and experimental estimates (Webb & Miller, 2014; Liu & Liu, 2016; Eldridge
398 et al., 2019) (Fig. 6A). Our predictions also agree with the theoretical and experimental
399 estimates of $\Delta_{^{12}\text{CH}_2\text{D}_2}^{\text{eq}}$ (Young et al., 2017; Eldridge et al., 2019), though in this case our pre-
400 dictions are systemically lower by $\sim 0.8\%$ in the temperature range of 0°C to 100°C (Fig.
401 6B). There are currently no available measurements of the intermediates in the methanogen-
402 esis pathway to which we can compare our results.

403 **4.4 Implications of predicted EFFs for methanogenesis and anaer-** 404 **obic oxidation of methane**

405 Methanogenesis is characterized by large and variable $\text{CO}_2\text{-CH}_4$ carbon isotope fractionations
406 (tens of permil) and $\text{CH}_4\text{-H}_2\text{O}$ hydrogen isotope fractionations (hundreds of permil). Varia-
407 tions within these ranges have been hypothesized to be controlled by the degree of reversibility
408 of the enzymatically-catalyzed reactions (Valentine et al., 2004; Wang et al., 2015; Stolper

et al., 2015). The net isotope fractionation of any individual biochemical reaction varies between the thermodynamic and kinetic end-members. The thermodynamic end-member is the product of a fully reversible reaction, and it gives rise to a substrate-product isotope fractionation equal to the EFF between these compounds. The kinetic end-member is well-defined for a single reaction as the isotope fractionation when that reaction is unidirectional, and it is equal to the ratio of the isotope-specific rate constants of the reaction. The kinetic end-member depends on the reaction mechanism, which depends on the structure of the enzyme catalyzing the reaction, and on the exact substrates participating in the reaction. Thus, the kinetic end-member may vary for different microbial strains and physiological conditions.

As a single reaction departs from equilibrium, for example in response to an increase in substrate concentration, its isotope fractionation will transition from the equilibrium to the kinetic isotope fractionation (DePaolo, 2011; Wing & Halevy, 2014). For the reaction $r \rightleftharpoons p$, the net isotope fractionation from metabolite pools r and p at steady state ($\alpha_{r-p}^{\text{net}}$) can be calculated from the EFF (α_{r-p}^{eq}), the forward KFF ($\alpha_{r \rightarrow p}^{\text{kin}}$) and the ratio of the backward and forward mass fluxes of the reaction ($f_{p,r}$):

$$\alpha_{r-p}^{\text{net}} = (\alpha_{r-p}^{\text{eq}} - \alpha_{r \rightarrow p}^{\text{kin}}) f_{p,r} + \alpha_{r \rightarrow p}^{\text{kin}}. \quad (8)$$

The thermodynamic end-member is expressed when the reaction is fully reversible ($f_{p,r} = 1$) and Eq. 8 reduces to $\alpha_{r-p}^{\text{net}} = \alpha_{r-p}^{\text{eq}}$. The kinetic end-member is expressed when the reaction is unidirectional ($f_{p,r} = 0$) and Eq. 8 reduces to $\alpha_{r-p}^{\text{net}} = \alpha_{r \rightarrow p}^{\text{kin}}$. In a linear reaction network with metabolite pools s , r and p such that $s \rightleftharpoons r \rightleftharpoons p$, different steps have isotope fractionations that have a differential departure from their individual thermodynamic equilibrium isotope fractionation end-members to give a range of disequilibrium isotope fractionations of the total reaction network (Wing & Halevy, 2014). The net isotope fractionation between s and p at a steady state can be calculated from the recursive expression:

$$\alpha_{s-p}^{\text{net}} = (\alpha_{r-p}^{\text{net}} \times \alpha_{s-r}^{\text{eq}} - \alpha_{s \rightarrow r}^{\text{kin}}) f_{r,s} + \alpha_{s \rightarrow r}^{\text{kin}} \quad (9)$$

(See Appendix A and Wing & Halevy (2014) for details). In this case, the thermodynamic end-member is expressed when both reactions are fully reversible ($f_{r,s} = f_{p,r} = 1$) and Eq. 9 reduces to $\alpha_{s-p}^{\text{net}} = \alpha_{r-p}^{\text{eq}} \times \alpha_{s-r}^{\text{eq}}$. The kinetic end-member is expressed when the most upstream reaction is unidirectional ($f_{r,s} = 0$) and Eq. 9 reduces to $\alpha_{s-p}^{\text{net}} = \alpha_{s \rightarrow r}^{\text{kin}}$. A range of disequilibrium net isotope fractionations between these values is expressed upon progressive departure from equilibrium (e.g., with increasingly negative ΔG_r), and the transition may not be monotonic due to the dependence on the reversibilities and KFFs of individual reactions. This approach is only applicable to linear metabolic networks, and we use it here to explore the possible effect of the ΔG_r (and rate) of hydrogenotrophic and acetoclastic methanogenesis and anaerobic methanotrophy on the carbon isotope fractionation (Sections 4.4.1, 4.4.4 and 4.4.5).

443 In some metabolic networks, the isotope exchange reaction involves three compounds
 444 rather than two, such as for hydrogen atoms in the hydrogenotrophic pathway. For example,
 445 in the reaction $aY_n + bY_m \rightleftharpoons cY_{n+m}$, where a , b and c are arbitrary organic moieties, Y is
 446 the atom of interest and n and m are the stoichiometric coefficients of Y . For brevity, we will
 447 denote this reaction as $r_1 + r_2 \rightleftharpoons p$, where r_1 is aY_n , r_2 is bY_m and p is cY_{n+m} . The change
 448 in the isotopic composition of compound p with time can be expressed as:

$$\frac{dR_p}{dt} = \frac{1}{[p]} \left[\phi_{rp} \left(n \cdot \alpha_{r_1 \rightarrow p}^{\text{kin}} R_{r_1} + m \cdot \alpha_{r_2 \rightarrow p}^{\text{kin}} R_{r_2} \right) - \phi_{pr} \cdot R_p \left(n \cdot \alpha_{p \rightarrow r_1}^{\text{kin}} + m \cdot \alpha_{p \rightarrow r_2}^{\text{kin}} \right) - R_p (m + n) (\phi_{rp} - \phi_{pr}) \right], \quad (10)$$

449 where ϕ_{rp} and ϕ_{pr} are the net forward and reverse mass fluxes, respectively, and R_{r_1} , R_{r_2}
 450 and R_p are the ratios of the rare and abundant isotopes in pools r_1 , r_2 and p , respectively.
 451 In the specific case of a chemical and isotopic steady state, the isotopic composition of p is
 452 constant, and $\frac{d}{dt} ([p] \cdot R_p) = 0$. Rearranging Eq. 10 yields an analytical solution for R_p at a
 453 steady state:

$$R_p = \frac{\phi_{rp} \left(n \cdot \alpha_{r_1 \rightarrow p}^{\text{kin}} R_{r_1} + m \cdot \alpha_{r_2 \rightarrow p}^{\text{kin}} R_{r_2} \right)}{\phi_{pr} \left(n \cdot \alpha_{p \rightarrow r_1}^{\text{kin}} + m \cdot \alpha_{p \rightarrow r_2}^{\text{kin}} \right) + (m + n) (\phi_{rp} - \phi_{pr})} \quad (11)$$

454 (see full derivation of Eqs. 10 and 11 in Appendix B.1). In a metabolic network with multiple
 455 sources of the atom of interest, extending Eq. 11 is impractical unless we impose constraints
 456 over the values of the mass fluxes and isotope effects (e.g., Cao et al., 2019). To avoid prior
 457 assumptions, the net isotope fractionations in such a system can be determined numerically
 458 by solving an isotopic mass balance, such as in Eq. 10, for each metabolite as a set of
 459 ordinary differential equations. The numerical solutions do not provide the same intuition
 460 as analytical expressions, but in some cases the systems can be simplified to produce an
 461 approximate analytical solution. We will discuss one such simplified analytical solution for
 462 the hydrogen isotope fractionation between CH_4 and H_2O in the hydrogenotrophic pathway
 463 (Section 4.4.2) and a numerical solution for carbon isotope fractionation in the methylotrophic
 464 pathway (Section 4.4.3). In both cases we discuss the isotope fractionations observed in
 465 laboratory cultures or environmental samples. These apparent isotope fractionations between
 466 compounds A and B are defined by ${}^r\alpha_{A-B} \equiv {}^rR_A/{}^rR_B$ and presented using the $1000\ln{}^r\alpha_{A-B}$
 467 notation. These isotope fractionations represent combinations of the equilibrium and kinetic
 468 isotope fractionations (Section 4.4) and should not be confused with the EFFs ($1000\ln{}^r\alpha_{A-B}^{\text{eq}}$)
 469 or KFFs ($1000\ln{}^r\alpha_{A \rightarrow B}^{\text{kin}}$).

470 4.4.1 Carbon isotopes in the hydrogenotrophic pathway

471 Fractionation of carbon isotopes in the hydrogenotrophic methanogenesis pathway ($1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$)
 472 ranges from $\sim 10\text{‰}$ to $\sim 90\text{‰}$ in laboratory cultures, and correlates with the net ΔG_r and

473 the cell-specific rate of methanogenesis (Valentine et al., 2004; Penning et al., 2005; Takai
 474 et al., 2008; Okumura et al., 2016; Topçuoğlu et al., 2019). Cocultures and enrichment ex-
 475 periments of methanogens grown at small negative ΔG_r (e.g., low concentrations of H_2) often
 476 have $1000\ln^{13}\alpha_{CO_2-CH_4}$ values larger than the equilibrium carbon isotope fractionation (the
 477 temperature-dependent EFF) (Valentine et al., 2004; Penning et al., 2005; Hattori et al.,
 478 2012; Topçuoğlu et al., 2019). We compiled the apparent $1000\ln^{13}\alpha_{CO_2-CH_4}$ values available
 479 in the literature for pure culture, coculture and enrichment experiments. Comparing these
 480 measurements with the calculated temperature-dependent EFFs, we found a bimodal dis-
 481 tribution with peaks at +10‰ and -20‰ (Fig. S.1). Most of the values larger than the
 482 corresponding temperature-dependent EFF are from batch culture experiments. However,
 483 we only considered data that was not affected by Rayleigh distillation, that is, experiments
 484 where the isotopic composition of the substrates was similar to the initial isotopic composition
 485 throughout the experiment.

486 Previous models of microbial methanogenesis suggested various scenarios in which the
 487 reversibility of the metabolic pathway shapes the relationship between $1000\ln^{13}\alpha_{CO_2-CH_4}$
 488 and ΔG_r or the cell-specific methanogenesis rate. In these models, the EFFs and f s for the
 489 various steps in the reaction network were treated as free parameters. We used our calculated
 490 EFFs at 25 °C and the mathematical framework for linear metabolic networks outlined in
 491 Section 4.4 to explore some of the previously suggested scenarios:

- 492 (i) gradual and uniform departure from equilibrium of all steps in the pathway (Wang
 493 et al., 2015).
- 494 (ii) isotopic equilibrium between CO_2 and CH_3-H_4MPT or CH_3-SCoM , and variable re-
 495 versibility of the Mtr- or Mcr-catalyzed reactions (Alperin & Hoehler, 2009; Stolper
 496 et al., 2015).
- 497 (iii) differential reversibility of the different reactions in the pathway (Cao et al., 2019).

498 For each scenario, we used some combination of f values in the recursive term in Eq. 9 to
 499 estimate $1000\ln^{13}\alpha_{CO_2-CH_4}$ (Table 10). We assigned $1000\ln^{13}\alpha^{kin}$ of -20‰ for all the reactions
 500 in the pathway, except for $1000\ln^{13}\alpha_{CH_3-SCoM\rightarrow CH_4}^{kin}$, which has been experimentally measured
 501 to be $\sim -40\%$ (Scheller et al., 2013). Though the KFFs other than $1000\ln^{13}\alpha_{CH_3-SCoM\rightarrow CH_4}^{kin}$
 502 are unknown and were treated here as free parameters, the findings and conclusions below
 503 are robust within a reasonable range of these KFFs between 0‰ and -50‰. Details of the
 504 calculations are in Appendix A.

505 In scenario (i) of uniform departure from reversibility, the minimal, kinetic end-member
 506 $1000\ln^{13}\alpha_{CO_2-CH_4}$ value (i.e., when $f = 0$) is -20‰, consistent with isotope fractionations
 507 measured at large negative ΔG_r . In this case, only the KFF of the most upstream, Fmd-
 508 catalyzed reaction ($\ln^{13}\alpha_{CO_2\rightarrow CHO-MFR}^{kin}$) is expressed, and the net isotope fractionations of the

509 other reactions in the network (in this case, all $^{13}\alpha^{\text{kin}}$ values, as $f = 0$) are not expressed (Eq.
510 9). The maximal $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ depends on the $^{13}\alpha^{\text{kin}}$ values assigned to the different
511 reactions. For $^{13}\alpha^{\text{kin}}$ values more positive than -60% , the maximal $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ is the
512 thermodynamic equilibrium carbon isotope fractionation of 69% . Larger-than-equilibrium
513 $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ values require $^{13}\alpha^{\text{kin}}$ values more negative than -60% . For example, a
514 $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ value of 75% at $25\text{ }^\circ\text{C}$ would require $^{13}\alpha^{\text{kin}}$ values of $\sim -80\%$ for the re-
515 actions catalyzed by Mtd, Mer and Mtr. Though we cannot rule them out, to the best of
516 our knowledge carbon isotope KFFs of such magnitude have not been measured. Within
517 the limits of observed carbon isotope KFFs, the assumption of a uniform departure from
518 equilibrium places a hard limit on the maximum value of $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$, which is smaller
519 than the observed net carbon isotope fractionation.

520 In scenario (*ii*), the reactions from CO_2 to $\text{CH}_3\text{-SCoM}$ are fully reversible (i.e., $f = 1$),
521 and only the most downstream, Mcr-catalyzed reaction departs from reversibility. When
522 implemented in the framework described above, the range of possible $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ is
523 $69\text{-}106\%$. The maximal $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ value is due to substitution of the small $\text{CH}_3\text{-}$
524 SCoM-CH_4 EFF (we calculated 1.6% at $25\text{ }^\circ\text{C}$) by the much larger KFF of the Mcr-catalyzed
525 step (-40% ; Scheller et al., 2013). In this scenario, $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ cannot be smaller than
526 69% , which is inconsistent with the large number of $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ measurements that
527 are smaller than this value, suggesting that the departure from equilibrium of the last steps
528 in the pathway cannot be the sole process responsible for the observed range of $\text{CO}_2\text{-CH}_4$
529 carbon isotope fractionation.

530 In scenario (*iii*), Cao et al. (2019) explored combinations of differential reversibility in
531 methanogenesis, focusing on clumped isotopologues. They suggested binary f values (either 0
532 or 1) for the reactions catalyzed by Fmd, Mtd, Mer and Mcr. Using our calculated EFFs, we
533 find that the binary scenarios yield $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ covering the range of observed values
534 ($20\text{-}106\%$). The largest $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ value is obtained, as in scenario (*ii*), when $f =$
535 0 for the Mcr-catalyzed reaction and $f = 1$ for all other reactions in the pathway. In this
536 case, a combination of the KFF of the Mcr-catalyzed reaction (-40%) with the equilibrium
537 $\text{CO}_2\text{-CH}_3\text{-SCoM}$ carbon isotope fractionation ($\sim 69\%$) leads to a net $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ of
538 109% . The smallest $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ is obtained, as in scenario (*i*), when $f = 0$ for the
539 Fmd-catalyzed reaction, leading to expression of only the KFF of that reaction (prescribed
540 to be -20%).

541 We conclude that both scenarios (*i*) and (*iii*) are capable of covering the entire range of
542 observed $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$. However, both scenarios invoke arbitrary combinations of the
543 reversibility of the steps in the pathway, and scenario (*i*) also requires unrealistic carbon
544 isotope KFFs. We note that in all models suggested to date, the reaction reversibilities
545 were assigned rather than calculated, and it seems that a more detailed metabolic model is

546 required to explain the nuances in the dependence of $1000\ln^{13}\alpha_{\text{CO}_2-\text{CH}_4}$ on ΔG_r .

547 4.4.2 Hydrogen isotopes in the hydrogenotrophic pathway

548 Fractionation of hydrogen isotopes during hydrogenotrophic methanogenesis in laboratory
549 cultures ranges from $\sim -100\text{‰}$ to -600‰ and displays a weaker dependence on ΔG_r than
550 the carbon isotope fractionation (Valentine et al., 2004; Stolper et al., 2015; Okumura et al.,
551 2016). Observed $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ values deviate significantly from the expected $\text{CH}_4-\text{H}_2\text{O}$
552 hydrogen isotope EFF (Fig. 7). For example, in two different experiments grown at 55°C and
553 low H_2 concentrations ($<10 \mu\text{M}$), one a coculture and the other a deep aquifer groundwa-
554 ter incubation, the $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ values of $-320\pm 12\text{‰}$ and $-393\pm 43\text{‰}$, respectively, are
555 significantly more negative than the temperature-dependent equilibrium isotope fractiona-
556 tion of -175‰ (Yoshioka et al., 2008; Hattori et al., 2012). Similar to carbon isotopes, such
557 deviations of $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ from the temperature-dependent hydrogen isotope EFF may
558 arise from variations in the reversibility of the metabolic pathway, depending on the ΔG_r .
559 In contrast to carbon isotopes, hydrogen isotope deviations from the EFF may also arise
560 from mixing of hydrogen atom sources through direct incorporation of hydrogen atoms from
561 H_2 in the Hmd-catalyzed reaction. There is ample evidence that this only occurs at high
562 H_2 pressure or during exponential cell growth (e.g., Kawagucci et al., 2014; Okumura et al.,
563 2016). Thus, it seems likely that the large, negative $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ values observed in cul-
564 tures grown at low H_2 concentrations are due to departure from equilibrium and expression
565 of KFFs, not incorporation of hydrogen from H_2 .

566 Hydrogenotrophic methanogenesis involves the stepwise addition of four hydrogen atoms
567 in four individual reactions (Fig. 1). Each of these additions is characterized by an in-
568 dividual net $\text{CH}_4-\text{H}_2\text{O}$ hydrogen isotope fractionation, which depends on the reaction re-
569 versibility and the equilibrium and kinetic end-member isotope fractionations. The overall
570 $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ value depends on these individual isotope fractionations in ways that may
571 not be intuitive. In the extreme case that all hydrogen addition reactions are unidirectional
572 (i.e., $f = 0$), for example at very large negative ΔG_r of the methanogenesis reaction, the
573 overall $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ value will be the average of the four KFFs associated with these
574 reactions. As primary hydrogen isotope KFFs are generally large (e.g., $1000^2\alpha_{\text{CH}_3-\text{SCoM}\rightarrow\text{CH}_4}^{\text{kin}}$
575 is $\sim -890\text{‰}$ at 60°C ; Scheller et al., 2013), the expectation in this case is a substantially
576 larger-than-equilibrium net $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$, as found in the majority of laboratory culture
577 experiments (Fig. S.1). This phenomenon is also apparent in non canonical methanogenic
578 pathways, such as the nitrogenase-catalyzed formation of methane by nitrogen fixers, where
579 $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ reaches -730‰ at ambient temperatures (Luxem et al., 2020).

580 Unlike carbon isotopes, for which the reaction network is linear, there are four distinct
581 steps in which exchange of hydrogen isotopes between methane and water may occur. The

582 exchange does not occur directly with intracellular water but through various intracellular
 583 metabolites with isotopic compositions that are related to that of the intracellular water.
 584 For example, in the Mcr-catalyzed reaction, one hydrogen atom is transferred from HS-
 585 CoB to CH₃-SCoM yielding methane with a net CH₄-H₂O hydrogen isotope fractionation
 586 that depends on the reversibility of this reaction. If the Mcr-catalyzed reaction fully departs
 587 from equilibrium ($f = 0$) to express its KFF, the total $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ will deviate from the
 588 calculated EFF, even if the other three hydrogen addition reactions result only in equilibrium
 589 isotope effects. In this case (See Appendix B.1 for full derivation), the net CH₄-H₂O hydrogen
 590 isotope fractionation at a steady state between HS-CoB and methane is:

$${}^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}^{\text{net}} = \frac{3}{4} \left({}^2\alpha_{\text{CH}_3-\text{SCoM}\rightarrow\text{CH}_4}^{\text{kin}} / {}^2\alpha_{\text{H}_2\text{O}-\text{CH}_3-\text{SCoM}}^{\text{eq}} \right) + \frac{1}{4} \left({}^2\alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{\text{kin}} / {}^2\alpha_{\text{H}_2\text{O}-\text{HS-CoB}}^{\text{eq}} \right). \quad (12)$$

591 In other words, even if three of the four hydrogen atoms in CH₄ reflect equilibrium between
 592 H₂O and an intracellular CH₃-S-CoM intermediate, departure of the last hydrogen addition
 593 reaction from equilibrium will result in a disequilibrium net $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$. Using our
 594 calculated EFFs at 25 °C and literature KFFs for this reaction (${}^2\alpha_{\text{CH}_3-\text{SCoM}\rightarrow\text{CH}_4}^{\text{kin}} = 0.85$
 595 and ${}^2\alpha_{\text{HSCoB}\rightarrow\text{CH}_4}^{\text{kin}} = 0.41$; Scheller et al., 2013), Eq. 12 yields a $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ value of
 596 -507% , compared to the calculated EFF of -195% . The standard ΔG_r (ΔG_r^0) of Mcr is
 597 $\sim -30 \text{ kJ mol}^{-1}$, and it has been suggested that during methanogenesis the last hydrogen
 598 addition reaction is effectively irreversible (Thauer, 2011). Eq. 12 demonstrates how the
 599 KFFs that are associated with Mcr are sufficient to drive deviations of the net CH₄-H₂O
 600 hydrogen isotope fractionation from equilibrium by more than 300%.

601 4.4.3 Methylo-trophic pathway

602 The methylo-trophic pathway is underrepresented in the literature compared to the hy-
 603 drogenotrophic pathway, and thus there is a smaller database with which to compare our
 604 results. Most of the data are from laboratory experiments, which are important as they are
 605 often used to assess the specific pathway of microbial methane production in the environ-
 606 ment (e.g., Zhuang et al., 2018). However, the main controls on carbon and hydrogen isotope
 607 fractionation in these pathways remain unclear, as do their dependencies on ΔG_r . Below, we
 608 discuss the implications of our predicted EFFs for the methylo-trophic pathway, focusing on
 609 carbon isotopes.

610 Net carbon isotope fractionation between methanol and methane $1000\ln^{13}\alpha_{\text{methanol}-\text{CH}_4}$
 611 during methylo-trophic methanogenesis in laboratory cultures spans a relatively narrow range
 612 of 67-83‰ (Krzycki et al., 1987; Londry et al., 2008; Penger et al., 2012, 2014), and methy-
 613 lotrophic enrichment cultures have carbon isotope fractionations of up to 90‰ (Rosenfeld
 614 & Silverman, 1959). It is unclear whether these limited observations cover the entire range
 615 of physiologically relevant conditions, but it is clear that the range of $1000\ln^{13}\alpha_{\text{methanol}-\text{CH}_4}$

616 values is much larger than our predicted EFFs that are 19.1-20.9‰ at 25-40 °C. Methanol
 617 conversion to methane is a disproportionation pathway, where methanol molecules are either
 618 fully oxidized to CO₂ or reduced to methane (Fig. 1). Assuming that all methanol is used
 619 to produce chemical energy and not to generate biomass, a 3:1 ratio of reduction:oxidation
 620 ($R_{r/o}$) is expected to account for cycling of the electron carriers. However, $R_{r/o}$ may vary if
 621 the cells utilize some of the methanol to generate biomass, which requires reducing equiva-
 622 lents. The reducing equivalents in this case are reduced coenzyme F₄₂₀ and ferredoxin, which
 623 are produced in the reverse methanogenesis pathway from CH₃-S-CoM to CO₂.

624 We explored the dependence of $1000\ln^{13}\alpha_{\text{methanol-CH}_4}$ and $1000\ln^{13}\alpha_{\text{methanol-CO}_2}$ on the
 625 reversibility of the pathway and on $R_{r/o}$, and to this end developed a simplified isotopic mass
 626 balance to find the isotope fractionation in the methyltrophic pathway at steady state (see
 627 Appendix B.2). We reduced the pathway to its three main branches: (1) from methanol to
 628 CH₃-S-CoM, (2) from CH₃-S-CoM to CH₄, and (3) from CH₃-S-CoM to CO₂. We assign
 629 KFFs in the range -30‰ to -50‰, assign a value to $R_{r/o}$, and use our calculated EFFs at
 630 25 °C. We assume 75% reversibility between CH₃-S-CoM and CO₂ ($f_3 = 0.75$), repeatedly
 631 ($N = 10,000$) pick random reversibility values for reactions 1 (f_1) and 2 (f_2) from a uniform
 632 distribution between 0 and 1, and calculate the possible range of $1000\ln^{13}\alpha_{\text{methanol-CH}_4}$ and
 633 $1000\ln^{13}\alpha_{\text{methanol-CO}_2}$ values (Table 10).

634 For $R_{r/o} = 3:1$, $1000\ln^{13}\alpha_{\text{methanol-CH}_4}$ is 55-70‰, covering the lower range of the experi-
 635 mental observations. At $R_{r/o} = 1:1$, the range of $1000\ln^{13}\alpha_{\text{methanol-CH}_4}$ shifts to 60-90‰ (Fig.
 636 9, left), closer to the observed range and suggesting that the ratio of methanol reduction
 637 to oxidation may, in some cases, be appreciably lower than 3:1 due to a biosynthetic shunt.
 638 At the theoretical extreme case of $R_{r/o} = 20:1$, there is almost no oxidation of methanol to
 639 CO₂, and the $1000\ln^{13}\alpha_{\text{methanol-CH}_4}$ range is 35-55‰. These small $1000\ln^{13}\alpha_{\text{methanol-CH}_4}$ val-
 640 ues indicate that the oxidation to CO₂ is required to generate the observed range of carbon
 641 isotope fractionation between methanol and CH₄. There are currently no known available
 642 measurements of methanol limitation conditions, and we have no indication whether at very
 643 low rates of methyltrophic methanogenesis $1000\ln^{13}\alpha_{\text{methanol-CH}_4}$ values approach the EFF.

644 In this study, we calculated an equilibrium methanol-CO₂ carbon isotope fractionation
 645 ($1000\ln^{13}\alpha_{\text{methanol-CO}_2}^{\text{eq}}$) of -47.8‰ at 25 °C, while at $R_{r/o} = 3:1$ our model predicts a range of
 646 net carbon isotope fractionations between -25‰ and 0‰ (Fig. 9, right). At $R_{r/o} = 1:1$, the
 647 range shifts to -20‰ to 20‰. The upper end of this range is similar to the ~20‰ isotope
 648 fractionations measured in a laboratory cultures (Penger et al., 2012). These values are
 649 complemented by the methanol-biomass and methanol-lipid carbon isotope fractionations,
 650 which are also large and positive (>30‰; Londry et al., 2008) and which stem from the same
 651 metabolic branch. In our model, the large, positive $1000\ln^{13}\alpha_{\text{methanol-CO}_2}$ values required that
 652 the reversibility of the CH₃-S-CoM to CO₂ branch be lower than 75%, because the calculated

653 EFF is large and negative. At low reversibility of the methanol oxidation reaction, the
654 net methanol–CO₂ isotope fractionation shifts from the large, negative EFF to the large,
655 positive KFF. Overall, this suggests a dominance of kinetic isotope effects in methylotrophic
656 methanogenesis, at least under the conditions explored in laboratory culture experiments.

657 4.4.4 Acetoclastic pathway

658 The isotope effects in the acetoclastic pathway, similar to the methylotrophic pathway,
659 are not well studied. During acetoclastic methanogenesis, acetate dissociates to a methyl
660 group (C₁), which is reduced to CH₃-H₄MPT and later released as CH₄, and to a car-
661 boxyl group (C₂), which is released as CO₂. The acetoclastic pathway has a smaller carbon
662 isotope fractionation between the substrate and CH₄ ($1000\ln^{13}\alpha_{\text{acetate}(C_1)-\text{CH}_4}$) than the hy-
663 drogenotrophic and methylotrophic pathways, with a range of 7-35‰ (Krzycki et al., 1987;
664 Gelwicks et al., 1994; Penning et al., 2006; Londry et al., 2008; Goevert & Conrad, 2009).
665 Published measurements of the isotope fractionation between the carboxyl group of acetate
666 and CO₂ ($1000\ln^{13}\alpha_{\text{acetate}(C_2)-\text{CO}_2}$) are in the range of 35-47‰ in laboratory experiments and
667 as low as 9‰ in a rice field soil incubation (Goevert & Conrad, 2009). We calculated the
668 acetate–CH₄ and acetate–CO₂ carbon isotope EFFs of 16.3‰ and –13.3‰, respectively, at 25
669 °C. The equilibrium carbon isotope fractionations between the C₁ atoms in acetate and those
670 in acetyl-CoA and CH₃-H₄MPT are –0.4‰ and –3.3‰, respectively. The largest equilibrium
671 carbon isotope fractionation in this pathway is associated with the methyl group transfer
672 between CH₃-H₄MPT and CH₃-S-CoM (17.9‰).

673 We explored the dependence of $1000\ln^{13}\alpha_{\text{acetate}(C_1)-\text{CH}_4}$ and $1000\ln^{13}\alpha_{\text{acetate}(C_2)-\text{CO}_2}$ on
674 the reversibility of reactions in the pathway using the recursive expression in Eq. 9 for lin-
675 ear metabolic networks (details in Appendix A). A scenario of full reversibility (i.e., iso-
676 topic equilibrium) in the steps before the Mcr-catalyzed reaction and variable expression
677 of $^{13}\alpha_{\text{CH}_3-\text{S-CoM}\rightarrow\text{CH}_4}^{\text{kin}}$ yields a $1000\ln^{13}\alpha_{\text{acetate}(C_1)-\text{CH}_4}$ value between 16‰ and 53‰ at 25 °C
678 depending on the reversibility of the Mcr-catalyzed reaction (Table 10). This calculated
679 range covers most of the range observed in laboratory experiments, but it also dictates that
680 $1000\ln^{13}\alpha_{\text{acetate}(C_2)-\text{CO}_2}$ is equal to the acetate–CO₂ carbon isotope EFF (–13‰), much lower
681 than the observed range. This suggests that the observed ranges of carbon isotope frac-
682 tionations between acetate and CO₂ or CH₄ are due to expression of kinetic isotope effects
683 not only in the Mcr-catalyzed reaction but also in the first two reactions in the acetoclastic
684 pathway (catalyzed by Ack/Pta and Cdh, Table 1).

685 4.4.5 Anaerobic methane oxidation

686 In reverse-methanogenesis AOM, the EFFs are the inverse of those in hydrogenotrophic
687 methanogenesis, with the expected $1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}^{\text{eq}}$ in the range of –50‰ to –70‰ depending

688 on temperature. To date, there are only a few measured $1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$ and $1000\ln^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$
689 values of AOM in laboratory cultures, with ranges of 12-38‰ and 103-274‰, respectively
690 (Holler et al., 2009). This enrichment of methane in ^{13}C and D contradicts the trends pre-
691 dicted by the EFFs for these reactions, suggesting that under the conditions of the available
692 experimental results, the kinetic isotope fractionation of carbon and hydrogen isotopes of
693 steps in the pathway contributed to the observed net isotope fractionations. There are lim-
694 ited observations at low sulfate availability (< 0.5 mM), in which methane is depleted in ^{13}C
695 during AOM activity (Yoshinaga et al., 2014; Chuang et al., 2018). More specifically, Chuang
696 et al. (2018) observed an apparent CH_4-CO_2 isotope fractionation of -54.3% in the sulfate-
697 methane transition zone (SMTZ), compared to the expected temperature-dependent EFF of
698 -76.1% at 5°C . In the case of AOM, a positive apparent $1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$ is indicative of
699 strong kinetic control over the system, whereas negative values, though not as negative as
700 the EFFs, are indicative of joint expression of equilibrium and kinetic isotope effects.

701 To explore the possible control of the reversibility on $1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$ during reverse-
702 methanogenesis AOM, we used the recursive expression in Eq. 9 for linear metabolic networks
703 (details in Appendix A). We applied the approach of Cao et al. (2019) for methanogenesis,
704 where we followed the carbon isotope reservoir effect of the seven reactions in the pathway
705 (Table 10). We used the EFFs calculated in the present study at 25°C , and calculated a
706 $1000\ln^{13}\alpha_{\text{CH}_4\rightarrow\text{CH}_3-\text{SCoM}}^{\text{kin}}$ value of -38% based on the measured $1000\ln^{13}\alpha_{\text{CH}_3-\text{SCoM}\rightarrow\text{CH}_4}^{\text{kin}}$ value
707 (-40% , Scheller et al., 2013) and our calculated $1000\ln^{13}\alpha_{\text{CH}_4-\text{CH}_3-\text{SCoM}}^{\text{eq}}$ (-2%). For the rest
708 of the pathway, we assumed arbitrary but reasonable $1000\ln^{13}\alpha^{\text{kin}}$ values of -5% or -40%
709 (Table 10).

710 We find that at steady state, a gradual expression of $1000\ln^{13}\alpha_{\text{CH}_4\rightarrow\text{CH}_3-\text{SCoM}}^{\text{kin}}$ (moving
711 from $f = 1$ to 0) yields the largest $1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$ range of -69% to 37% . The min-
712 imum value in this case is the calculated EFF, and the maximum value is the complete
713 expression of $1000\ln^{13}\alpha_{\text{CH}_4\rightarrow\text{CH}_3-\text{SCoM}}^{\text{kin}}$ blocking any expression of isotope effects downstream
714 of the reaction catalyzed by Mcr (Table 11). This covers the entire observed range of AOM
715 $1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$ in laboratory cultures (12-38‰). However, it is not clear whether this re-
716 action can actually be fully irreversible due to its large-positive ΔG_r^0 ($+30$ kJ mol $^{-1}$) (Thauer,
717 2011). Net forward reaction would likely require substantial adjustment of the intracellular
718 metabolite concentrations so that the actual ΔG_r is a small negative number (i.e., relatively
719 close to equilibrium). The observed range of AOM $1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$ can also be obtained if
720 the next downstream step, between CH_3-SCoM and $\text{CH}_3-\text{H}_4\text{MPT}$, imposes a reservoir effect
721 and assuming a $1000\ln^{13}\alpha_{\text{CH}_3-\text{SCoM}\rightarrow\text{CH}_3-\text{H}_4\text{MPT}}^{\text{kin}}$ of -40% , similar to the approach taken by
722 Alperin & Hoehler (2009). As the isotope reservoir effect occurs further downstream in the
723 AOM pathway, the range of net carbon isotope fractionation becomes smaller, until finally
724 the maximal $1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$ is between -50% and -15% , depending on the magnitude of

726 **4.4.6 Mixing and combinatorial effects in clumped isotopologues**

727 Recent years have seen a surge in measurements of the abundances of the clumped methane
728 isotopologues $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ from natural environments and laboratory cultures
729 (e.g., Stolper et al., 2014a; Wang et al., 2015; Douglas et al., 2016; Shuai et al., 2018; Ash
730 et al., 2019; Giunta et al., 2019). Further analytical advances have allowed measurements
731 of clumped-isotopologue abundances of other hydrocarbons (e.g., ethane; Clog et al., 2018),
732 but the application to other organic molecules has so far been limited. Natural samples of
733 methane from marine sediments, natural gas and methane hydrates often have equilibrium
734 $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ compositions (Stolper et al., 2014a; Giunta et al., 2019; Ash et al.,
735 2019). However, methane from laboratory cultures and some natural environments is mostly
736 at $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ disequilibrium (Stolper et al., 2015; Wang et al., 2015, 2016;
737 Douglas et al., 2016; Young et al., 2016, 2017; Giunta et al., 2019; Gruen et al., 2018; Douglas
738 et al., 2020). There is an ongoing effort to explain the mechanisms responsible for these
739 disequilibrium clumped-isotope compositions, and the current models invoke a dependence
740 on the rate of methanogenesis through expression of KIEs (Stolper et al., 2014b; Wang et al.,
741 2015; Douglas et al., 2020; Cao et al., 2019; Douglas et al., 2020), quantum tunneling (Young
742 et al., 2017; Young, 2019), mixing of methane sources (Young et al., 2016; Douglas et al.,
743 2016), and combinatorial effects, which are a specific case of mixing of hydrogen sources,
744 relevant mainly for D–D clumps (Yeung, 2016; Röckmann et al., 2016; Young et al., 2017;
745 Taenzer et al., 2020). Most of the modeling efforts require parameters such as the EFFs
746 and KFFs of the reactions in the methanogenesis and AOM pathways, and so far, there
747 have been only a few reports of these values (e.g., Wang et al., 2016; Whitehill et al., 2017;
748 Gruen et al., 2018; Ono et al., 2020). Furthermore, the available reports usually reflect
749 the net isotope fractionation (i.e., a combination of EFFs and KFFs associated with the
750 reaction network) rather than reaction-specific EFFs or KFFs, and in most cases they lump
751 together the primary and secondary KFFs. Our calculations of the EFFs may be useful when
752 implementing such models to explain disequilibrium methane clumped-isotope compositions.

753 Cao et al. (2019) explored the effects of the reversibility of the enzymatically-catalyzed
754 reactions in hydrogenotrophic methanogenesis on the $\Delta^{13}\text{CH}_3\text{D}$ – $\Delta^{12}\text{CH}_2\text{D}_2$ space (Section
755 4.4.1). They defined scenarios, denoted by binary reversibility (i.e., $f = 0$ or 1) vectors of
756 the four hydrogen addition reactions (e.g., [1,1,1,1] when all reactions are reversible, [0,0,0,0]
757 when all reactions are irreversible). They assumed an identical hydrogen isotope KFF for
758 each of the four reactions, an identical EFF for all four reactions, and hydrogen isotopic
759 equilibrium between the intracellular hydrogen pools (F_{420}H_2 , HS-CoB and H_2O). Drawing
760 from a wide distribution of KFF and EFF values, Cao et al. (2019) showed that the pre-

dicted range of $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ covers the entire range of laboratory and natural observations of microbial methane. Using a comparable conceptual framework and EFFs calculated for metal-catalyzed abiotic formation of methane, Young (2019) similarly found that the entire laboratory and environmental ranges of $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ could be reproduced. However, in the absence of EFFs relevant to the large organic molecules involved in hydrogenotrophic methanogenesis, both studies made assumptions (identical EFFs and KFFs), allowances (wide distributions of EFF and KFF values), and analogies (microbial methanogenesis versus metal-catalyzed radical reactions) that may not be appropriate.

We used the framework presented in Table 1 in Cao et al. (2019) to recalculate the $\Delta^{13}\text{CH}_3\text{D}$ – $\Delta^{12}\text{CH}_2\text{D}_2$ ranges using our calculated EFFs and Δ_i^{eq} values together with the forward and reverse KFFs of the Mcr-catalyzed reaction as measured by Scheller et al. (2013). As we currently do not have good estimates for the KFFs other than that of the Mcr-catalyzed reaction, we adopted the distributions used by Cao et al. (2019) for these KFFs. Under these conditions, the range of $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ values were significantly offset from those calculated by Cao et al. (2019) under all three reversibility scenarios (Fig. 10). Our calculated $\Delta^{12}\text{CH}_2\text{D}_2$ values in all three scenarios are more negative by ~ 20 – 100% than values typical of hydrogenotrophic methanogenesis, which are not lower than -20% (Giunta et al., 2019; Young et al., 2017). It is unlikely that the binary reversibility vectors are responsible for this significant $\Delta^{12}\text{CH}_2\text{D}_2$ ‘anti-clumping’, as these arbitrary, end-member scenarios should cover the possible range of $\Delta^{12}\text{CH}_2\text{D}_2$ values. Instead, these results may implicate the assumption of an equilibrium between the intracellular hydrogen pools as the cause of the mismatch between observed and calculated $\Delta^{12}\text{CH}_2\text{D}_2$ values. This theoretical exercise clearly highlights the importance of using robust EFFs and a more realistic description of the metabolic pathway to shed light on the possible determinants of methane clumped-isotope signatures.

5 CONCLUSIONS

This study provides a set of equilibrium carbon, hydrogen and clumped isotope fractionation factors associated with methanogenesis and anaerobic oxidation of methane, calculated by DFT at the M06-L/def2 TZVP level of theory with the SMD implicit solvation model. We compared our calculations to previous experimentally measured carbon and hydrogen isotope EFFs of the small, volatile end-members of these metabolic pathways (CO_2 , CH_4 , H_2O , H_2). Notably, we suggest that the CH_4 - H_2O hydrogen isotope EFF at low (biologically-relevant) temperatures is probably more positive than the values obtained from extrapolation from high-temperature (>200 °C) experimental results. Experimental results with which one would normally compare our calculated EFFs are mostly absent, and we based our computational pipeline on a previous exploration of the optimal method of calculating of EFFs for large organic molecules.

We used our calculated EFFs to probe the isotope fractionation among molecules in the most important metabolic pathways of anaerobic production and oxidation of methane—hydrogenotrophic, methylotrophic and acetoclastic methanogenesis—and anaerobic oxidation of methane. In these pathways, the net isotope fractionation between the reactants and products are determined by a combination of EFFs and KFFs, and the degree of expression of each depends on the metabolic state of the organisms. In extremely energy-limited environments, the extracellular reactants and products may be in isotopic equilibrium. In this case, the intracellular reactions will also be at or close to equilibrium, each expressing its respective EFF. If more energy is available, departure from equilibrium of some (but not necessarily all) of the intracellular reactions in the pathway results in net isotope fractionations that reflect a combination of their respective EFF and KFF, the contribution of which depends on the degree of departure of the reactions from equilibrium.

In the hydrogenotrophic methanogenesis pathway, we suggest that the large range of CO_2 - CH_4 carbon isotope fractionations is a product of differential departure from reversibility along the metabolic pathway rather than a uniform departure of all reactions or a departure of only one of the reactions from equilibrium. In the methylotrophic pathway, the calculated CH_3OH - CH_4 carbon isotope fractionation is smaller than the apparent isotope fractionations observed in environmental and laboratory culture samples by at least 50%. Using a numerical solution to a simplified model of the methylotrophic pathway, we suggest that the large observed carbon isotope fractionations are due to utilization of some of the electrons from methanol to fix biomass rather than to produce methane, resulting in a higher proportion of methanol oxidation to CO_2 than reaction stoichiometry would dictate in the absence of biomass fixation.

We also used our calculated EFFs to probe the clumped-isotope compositions of methane in the hydrogenotrophic pathway based on several scenarios for reaction reversibility. Using

823 a common assumption of isotopic equilibrium between H_2O and the intracellular hydrogen
824 donors, we found that the abundance of the $^{12}\text{CH}_2\text{D}_2$ clumped isotopologue of methane is lower
825 than observed in laboratory cultures. Mixing (combinatorial) effects of hydrogen transferred
826 to methane from intracellular hydrogen pools (F_{420}H_2 and HS-CoB) that are out of equilib-
827 rium with the intracellular water is a possible explanation for this mismatch. We suggest that
828 incorporating realistic EFFs and KFFs in future models and using more accurate descriptions
829 of the metabolic pathway will be critical in gaining a better understanding of the biochemi-
830 cal mechanisms that govern the clumped isotopic compositions of methane and other organic
831 molecules.

832 The EFF values we discussed in this work are universal among all organisms that utilize
833 similar organic compounds, irrespective of possible inter-species differences in the enzymes
834 that catalyze reactions among these compounds. In contrast, KFFs may often be strain-
835 specific, due to differences in the transition state of the reaction enforced by the enzyme
836 active site (Bradley et al., 2016). Moreover, theoretical predictions of KFFs are currently
837 considered harder to obtain than EFFs, and also often less accurate. To date, there is
838 an experimental estimate of only a single KFF in the methanogenesis pathway (for Mcr;
839 Scheller et al. 2013), from a single organism. Further studies of KFFs for the other enzymes
840 in the pathway, preferably from several organisms, are sorely needed to complement the EFFs
841 provided here.

842 The simplified examples discussed in this work provide a glimpse of the insights into
843 complex biological systems, made available by accurate determination of equilibrium isotope
844 fractionation factors. In the future, the comprehensive set of EFFs calculated here can be
845 used in investigations of biologically-induced isotope effects in methanogenesis and AOM, to
846 expand our understanding of the interaction between microorganisms and their environment,
847 and the way in which these interactions are recorded in the stable isotope composition of
848 natural materials.

849 **RESEARCH DATA**

850 All code and data for the models presented here are posted in a GitHub repository (<https://github.com/jagro>)

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Table 1: **Enzymes that are included in this report and the reactions they catalyze.** The hydrogen and carbon atoms of interest are shown in bold. Note that we include only the reactions that participate in carbon and hydrogen isotope exchange during methanogenesis and AOM.

#	Enzyme	Reactant	Product
1	Fmd*	$\text{CO}_2 + \text{Fd}_{\text{red}} + \text{MFR} + 2\text{H}^+$	$\rightleftharpoons \text{CHO-MFR} + \text{Fd}_{\text{ox}} + \text{H}_2\text{O}$
2	Ftr	$\text{CHO-MFR} + \text{H}_4\text{MPT}$	$\rightleftharpoons \text{CHO-H}_4\text{MPT} + \text{MFR}$
3	Mch	$\text{CHO-H}_4\text{MPT} + \text{H}^+$	$\rightleftharpoons \text{CH}\equiv\text{H}_4\text{MPT}^+ + \text{H}_2\text{O}$
4	Mtd	$\text{CH}\equiv\text{H}_4\text{MPT}^+ + \text{F}_{420}\text{H}_2$	$\rightleftharpoons \text{CH}_2=\text{H}_4\text{MPT} + \text{F}_{420} + \text{H}^+$
5	Hmd	$\text{CH}\equiv\text{H}_4\text{MPT}^+ + \text{H}_2$	$\rightleftharpoons \text{CH}_2=\text{H}_4\text{MPT}$
6	Mer	$\text{CH}_2=\text{H}_4\text{MPT} + \text{F}_{420}\text{H}_2$	$\rightleftharpoons \text{CH}_3\text{-H}_4\text{MPT} + \text{F}_{420}$
7	Mtr	$\text{CH}_3\text{-H}_4\text{MPT} + \text{HS-CoM}$	$\rightleftharpoons \text{CH}_3\text{-SCoM} + \text{H}_4\text{MPT}$
8	Mcr	$\text{CH}_3\text{-SCoM} + \text{HS-CoB}$	$\rightleftharpoons \text{CH}_4 + \text{CoM-S-S-CoB}$
9	Frh*	$\text{H}_2 + \text{F}_{420}$	$\rightleftharpoons \text{F}_{420}\text{H}_2$
10	Hdr*	$\text{H}_2 + \text{CoM-S-S-CoB} + \text{Fd}_{\text{ox}}$	$\rightleftharpoons \text{HS-CoB} + \text{HS-CoM} + \text{Fd}_{\text{red}} + 2\text{H}^+$
11	Mta	$\text{CH}_3\text{OH} + \text{HS-CoM}$	$\rightleftharpoons \text{CH}_3\text{-SCoM} + \text{H}_2\text{O}$
12	Ack/Pta	$\text{CH}_3\text{-COO}^- + \text{ATP} + \text{CoA-SH}$	$\rightleftharpoons \text{CH}_3\text{-COSCoA} + \text{ADP} + \text{HPO}_4^{2-}$
13	Cdh	$\text{CH}_3\text{-COSCoA} + \text{H}_4\text{MPT} + \text{Fd}_{\text{ox}}$	$\rightleftharpoons \text{CH}_3\text{-H}_4\text{MPT} + \text{CO}_2 + \text{CoA-SH} + \text{Fd}_{\text{red}}$

* In these reactions, the source of the hydrogen atom is a proton from H_2O , while H_2 is the electron donor of the reaction.

Abbreviations: Fmd - formyl-methanofuran dehydrogenase; Ftr - formyl transferase; Mch - methylene- H_4MPT cyclohydrolase; Mtd - F_{420} -dependent methylene- H_4MPT dehydrogenase; Hmd - H_2 -forming methylene dehydrogenase; Mer - methylene- H_4MPT reductase; Mtr - methyl transferase; Mcr - methyl-CoM reductase; Frh - F_{420} -reducing hydrogenase; Hdr - heterodisulfide reductase; Mta - methanol:coenzyme M methyltransferase; Ack - acetate kinase; Pta - phosphotransacetylase; Cdh - CO-dehydrogenase/acetyl-CoA synthase; MFR - methanofuran; H_4MPT - tetrahydromethanopterin; F_{420} - oxidized coenzyme F_{420} ; F_{420}H_2 - reduced coenzyme F_{420} ; Fd - ferredoxin; HS-CoM - Coenzyme M; HS-CoB - Coenzyme B; CoM-S-S-CoB - heterodisulfide; CoA-SH - coenzyme A.

Table 2: **Coefficients for the fourth-order polynomial fits to ${}^2\beta$ values.** Computed at the M06-L/def2-TZVP level of theory, between 273.15 and 973.15 K (0-700 °C). The fit to all values is of the form $A \times 10^{12}/T^4 + B \times 10^9/T^3 + C \times 10^6/T^2 + D \times 10^3/T + E$. For compounds with two or more inequivalent hydrogen atoms, the position-specific isotope substitutions are marked in bold font. For compounds with steric centers, we present the relevant stereoisomers (pro-R or pro-S). For a full list of the RPFR values see Tables S.1 and S.2.

Compound	$A \times 10^{-3}$	$B \times 10^{-2}$	$C \times 10^{-2}$	$D \times 10^{-2}$	E	${}^2\beta$ (25 °C)	C valence
CHO-MFR	167.555	-84.343	246.766	-219.067	1.879	11.6617	+2
CHO-H ₄ MPT	168.547	-85.518	249.729	-222.961	1.89616	11.5740	+2
CH≡H ₄ MPT ⁺	195.478	-101.046	288.642	-259.554	2.04363	12.4210	+2
CH ₂ =H ₄ MPT (pro-S)	230.033	-120.302	338.561	-317.557	2.27702	13.4320	0
CH ₂ =H ₄ MPT (pro-R)	230.714	-121.129	341.502	-322.530	2.30194	13.3951	0
CH ₃ -OH	182.591	-91.671	267.380	-238.241	1.95795	12.5648	-2
CH ₃ -H ₄ MPT	180.957	-91.660	267.497	-239.266	1.96388	12.3466	-2
CH ₃ -SCoM	164.319	-82.161	242.168	-210.262	1.84204	11.8269	-2
CH ₃ -COO ⁻	155.320	-77.350	230.683	-198.767	1.79846	11.5532	-3
CH ₃ -COSCoA	157.643	-78.365	232.909	-200.537	1.80484	11.6615	-3
CH ₄ (g)	130.627	-62.458	194.656	-158.370	1.63645	11.1873	-4
H ₂ O (g)	137.421	-64.383	204.176	-151.087	1.61410	12.6136	-
H ₂ (g)	4.783	-1.839	16.090	23.524	0.92746	3.4378	-
F ₄₂₀ H ₂ (pro-S)	184.583	-94.693	273.108	-247.161	1.99267	12.0564	-
HS-CoB	34.348	-14.865	63.062	-30.632	1.11648	5.9213	-

Table 3: **Coefficients for the fourth-order polynomial fits to $^{13}\beta$ values.** Computed at the M06-L/def2-TZVP level of theory, between 273.15 and 973.15 K (0-700 °C). The fit to all values is of the form $A \times 10^{12}/T^4 + B \times 10^9/T^3 + C \times 10^6/T^2 + D \times 10^3/T + E$. For compounds with two or more inequivalent carbon atoms, the position-specific isotope substitutions are marked in bold font. For a full list of the RPFRR values see Tables S.1 and S.2.

Compound	$A \times 10^{-6}$	$B \times 10^{-5}$	$C \times 10^{-4}$	$D \times 10^{-4}$	E	$^{13}\beta$ (25 °C)	C valence
CO ₂ (g)	337.660	-380.158	215.297	194.858	0.99085	1.1977	+4
CH ₃ -COO ⁻	376.418	-496.601	301.421	-55.714	1.00117	1.1818	+3
CH ₃ -COSCoA	220.645	-331.492	228.555	-3.505	0.99906	1.1578	+3
CHO-MFR	342.806	-451.468	266.672	16.754	0.998	1.1769	+2
CHO-H ₄ MPT	365.873	-466.108	272.013	-3.047	0.99925	1.1747	+2
CH≡H ₄ MPT ⁺	284.386	-389.139	249.574	32.095	0.99791	1.1786	+2
CH ₂ =H ₄ MPT	277.203	-354.319	223.792	20.167	0.99867	1.1586	0
CH ₃ -OH	234.470	-310.213	180.119	90.771	0.99613	1.1418	-2
CH ₃ -H ₄ MPT	243.089	-301.290	177.597	80.947	0.99658	1.1406	-2
CH ₃ -SCoM	152.839	-197.916	126.247	114.374	0.99526	1.1203	-2
CH ₃ -COOH	100.086	-177.146	136.586	125.940	0.99473	1.1364	-3
CH₃-COSCoA	202.747	-257.052	158.118	103.706	0.99558	1.1369	-3
CH ₄ (g)	96.945	-144.788	91.262	196.812	0.99193	1.1182	-4

Table 4: **Coefficients for the fourth-order polynomial fits to 13,2 RPFRR values.** Computed at the M06-L/def2-TZVP level of theory, between 273.15 and 973.15 K (0-700 °C). The fit to all values is of the form $A \times 10^{12}/T^4 + B \times 10^9/T^3 + C \times 10^6/T^2 + D \times 10^3/T + E$. For compounds with prochiral centers, we present the relevant stereoisomers (pro-R or pro-S). For a full list of the RPFRR values see Tables S.1 and S.2.

Compound	$A \times 10^{-3}$	$B \times 10^{-2}$	$C \times 10^{-2}$	$D \times 10^{-2}$	E	13,2 RPFRR (25 °C)	C valence
¹³ CDO-MFR	243.909	-128.453	359.899	-341.736	2.37839	13.786	+2
¹³ CDO-H ₄ MPT	244.502	-129.601	362.748	-345.432	2.39398	13.658	+2
¹³ CD≡H ₄ MPT ⁺	284.794	-153.837	424.386	-407.709	2.64816	14.711	+2
¹³ CHD=H ₄ MPT (pro-S)	324.191	-176.815	483.570	-477.038	2.93127	15.643	0
¹³ CHD=H ₄ MPT (pro-R)	324.277	-177.147	484.820	-479.472	2.94235	15.599	0
¹³ CH ₂ D-OH	249.049	-130.131	366.133	-344.898	2.39117	14.429	-2
¹³ CH ₂ D-H ₄ MPT	246.024	-129.336	364.234	-344.048	2.39097	14.161	-2
¹³ CH ₂ D-SCoM	216.035	-111.966	319.046	-293.357	2.18153	13.327	-2
¹³ CH ₂ D-COO ⁻	209.806	-108.220	309.711	-283.216	2.14019	13.201	-3
¹³ CH ₂ D-COSCoA	214.231	-110.773	316.256	-290.118	2.16833	13.330	-3
¹³ CH ₃ D (g)	168.779	-83.028	247.554	-213.261	1.85576	12.583	-4

Table 5: **Coefficients for the fourth-order polynomial fits to $^{2,2}\text{RPFR}$ values.** Computed at the M06-L/def2-TZVP level of theory, between 273.15 and 973.15 K (0-700 °C). The fit to all values is of the form $A \times 10^{12}/T^4 + B \times 10^9/T^3 + C \times 10^6/T^2 + D \times 10^3/T + E$. For a full list of the RPFR values see Tables S.1 and S.2.

Compound	$A \times 10^{-1}$	B	C	D	E	$^{2,2}\text{RPFR}$ (25 °C)	C valence
$^{12}\text{CD}_2=\text{H}_4\text{MPT}$	205.153	-143.588	381.662	-438.791	184.900	185.1934	0
$^{12}\text{CHD}_2\text{-OH}$	160.503	-110.846	293.114	-335.342	141.135	160.2113	-2
$^{12}\text{CHD}_2\text{-H}_4\text{MPT}$	156.170	-107.879	285.365	-326.515	137.466	158.4884	-2
$^{12}\text{CHD}_2\text{-SCoM}$	135.033	-92.796	245.092	-279.893	117.863	143.8200	-2
$^{12}\text{CHD}_2\text{-COO}^-$	125.327	-85.838	226.473	-258.318	108.785	135.5578	-3
$^{12}\text{CHD}_2\text{-COSCoA}$	128.799	-88.306	233.059	-265.928	111.982	138.0637	-3
$^{12}\text{CH}_2\text{D}_2$ (g)	106.778	-72.203	189.641	-215.319	90.609	128.7908	-4

Table 6: **Equilibrium carbon and hydrogen isotope fractionation factors at 25 °C, 50 °C and 75 °C.** Notations: (g) gas phase, (l) liquid phase, (S) is a D substitution in the pro-S face, and (R) is a D substitution in the pro-R face of molecules with a prochiral center. In the acetoclastic pathway, C₁ is the methyl-bound carbon atom, and C₂ is the carboxyl or CoA-bound carbon atom. The full reactions are listed in Table 1.

Enzyme	Reactant	Product	1000ln ¹³ α ^{eq} (‰)			1000ln ² α ^{eq} (‰)		
			25 °C	50 °C	75 °C	25 °C	50 °C	75 °C
Hydrogenotrophic pathway								
Net	CO _{2(g)} / H ₂ O _(l)	CH _{4(g)}	69.4	61.0	56.9	195.3	177.9	165.6
Fmd	CO _{2(g)} / H ₂ O _(l)	CHO-MFR	17.5	16.4	15.6	153.2	149.7	148.2
Ftr	CHO-MFR	CHO-H ₄ MPT	1.9	1.9	1.9	8.5	8.5	8.3
Mch	CHO-H ₄ MPT	CH≡H ₄ MPT ⁺	-3.3	-2.9	-2.7	-70.5	-65.2	-61.1
Mtd	F ₄₂₀ H ₂ (S)	CH ₂ =H ₄ MPT (R)	-	-	-	-105.2	-94.0	-84.3
Mtd	CH≡H ₄ MPT ⁺	CH ₂ =H ₄ MPT (S)	16.9	15.6	14.8	-78.2	-68.3	-59.5
Hmd	H ₂	CH ₂ =H ₄ MPT (R)	-	-	-	-1359.0	-1202.1	-1069.6
Mer	F ₄₂₀ H ₂ (S)	CH ₃ -H ₄ MPT	-	-	-	-23.9	-25.8	-27.0
Mer (s)	CH ₂ =H ₄ MPT (R)	CH ₃ -H ₄ MPT	15.8	13.2	12.0	81.3	68.2	57.3
Mer	CH ₂ =H ₄ MPT (S)	CH ₃ -H ₄ MPT	-	-	-	84.0	71.0	60.2
Mtr	CH ₃ -H ₄ MPT	CH ₃ -SCoM	18.1	15.9	14.9	42.9	38.2	34.1
Mcr	HS-CoB	CH _{4(g)}	-	-	-	-635.8	-580.0	-531.6
Mcr	CH ₃ -SCoM	CH _{4(g)}	2.1	0.8	0.2	55.4	44.2	35.3
Acetoclastic pathway								
Net	CH ₃ -COO ⁻ (C ₁)	CH _{4(g)}	15.7	13.5	12.1	31.9	23.6	17.2
Net	CH ₃ -COO ⁻ (C ₂)	CO _{2(g)} / H ₂ O _(l)	-13.3	-13.4	-13.5	-162.1	-153.7	-147.4
Ack/Pta	CH ₃ -COO ⁻ (C ₁)	CH ₃ -COSCoA (C ₁)	-0.4	-0.4	-0.3	-9.4	-8.5	-7.7
Cdh	CH ₃ -COSCoA (C ₁)	CH ₃ -H ₄ MPT	-3.2	-2.8	-2.6	-57.0	-50.2	-44.5
Methylotrophic pathway								
Net	CH ₃ OH	CH _{4(g)}	20.3	18.0	16.5	115.8	98.9	85.0
Net	CH ₃ OH	CO _{2(g)} / H ₂ O _(l)	-46.7	-42.9	-40.4	-79.3	-79.1	-81.0
Mta	CH ₃ OH	CH ₃ -SCoM	18.6	17.2	16.3	60.4	54.8	49.7
Electron cycling								
Frh	H ₂ O _(l)	F ₄₂₀ H ₂ (S)	-	-	-	120.9	121.4	123.2
Hdr	H ₂ O _(l)	HS-CoB	-	-	-	831.1	757.9	697.2

Table 7: **Doubly-substituted (“clumped”) isotopologue compositions in methanogenesis at 0 °C, 25 °C, 50 °C, 75 °C and 100 °C.** Computed at the M06-L/def2-TZVP level of theory. The deviation of the abundance of the ^{13}C -D and D-D clumped isotopologue from the stochastic distribution is expressed as $\Delta_i^{\text{eq}} = (R_i/R_i^*) - 1$, where R_i is the calculated ratio of the doubly-substituted isotopologue to the unsubstituted isotopologue, and R_i^* is this ratio at a stochastic distribution of the rare isotopes.

Compound	Δ_i^{eq} (‰)				
	0 °C	25 °C	50 °C	75 °C	100 °C
^{13}C-D					
$^{13}\text{CDO-MFR}$	5.197	4.482	3.898	3.412	3.002
$^{13}\text{CDO-H}_4\text{MPT}$	4.850	4.211	3.686	3.248	2.872
$^{13}\text{CD}\equiv\text{H}_4\text{MPT}^+$	5.159	4.560	4.060	3.644	3.286
$^{13}\text{CHD}=\text{H}_4\text{MPT}$ (pro-S)	5.382	4.692	4.119	3.636	3.217
$^{13}\text{CHD}=\text{H}_4\text{MPT}$ (pro-R)	5.533	4.826	4.239	3.745	3.316
$^{13}\text{CH}_2\text{D-OH}$	6.350	5.499	4.796	4.212	3.718
$^{13}\text{CH}_2\text{D-H}_4\text{MPT}$	5.989	5.219	4.582	4.039	3.581
$^{13}\text{CH}_2\text{D-SCoM}$	6.302	5.491	4.819	4.253	3.770
$^{13}\text{CH}_2\text{D-COO}^-$	5.959	5.206	4.581	4.052	3.599
$^{13}\text{CH}_2\text{D-COSCoA}$	5.971	5.218	4.589	4.065	3.615
$^{13}\text{CH}_3\text{D}$ (g)	6.606	5.738	5.017	4.413	3.896
D-D					
$^{12}\text{CD}_2=\text{H}_4\text{MPT}$	15.694	13.287	11.281	9.604	8.198
$^{12}\text{CHD}_2\text{-OH}$	19.577	16.141	13.372	11.128	9.303
$^{12}\text{CHD}_2\text{-H}_4\text{MPT}$	18.865	15.608	12.968	10.819	9.062
$^{12}\text{CHD}_2\text{-SCoM}$	18.876	15.606	12.958	10.804	9.043
$^{12}\text{CHD}_2\text{-COO}^-$	20.334	16.756	13.872	11.535	9.631
$^{12}\text{CHD}_2\text{-COSCoA}$	19.591	16.132	13.345	11.089	9.253
$^{12}\text{CH}_2\text{D}_2$ (g)	22.621	18.497	15.209	12.571	10.442

Table 8: **Equilibrium ^{13}C – D clumped isotopologue fractionation factors at 25 °C, 50 °C and 75 °C.** The deviation of the clumped isotopologue equilibrium fractionation factors (EFFs) from the product of the hydrogen and carbon EFFs is denoted by $^{13,2}\gamma^{\text{eq}}$ where $^{13,2}\gamma^{\text{eq}} = ^{13,2}\alpha^{\text{eq}} / (^{13}\alpha^{\text{eq}} \times ^2\alpha^{\text{eq}})$. Notation: (g) gas phase. The full reactions are listed in Table 1.

Enzyme	Reactant/s	Product	$1000\ln^{13,2}\alpha^{\text{eq}}$ (‰)			$^{13,2}\gamma^{\text{eq}}$		
			25 °C	50 °C	75 °C	25 °C	50 °C	75 °C
Hydrogenotrophic pathway								
Fmd	$^{13}\text{CO}_2 + \text{HDO}$	$^{13}\text{CDO-MFR}$	166.2	162.2	160.4	0.9955	0.9961	0.9966
Ftr	$^{13}\text{CDO-MFR}$	$^{13}\text{CDO-H}_4\text{MPT}$	10.6	10.6	10.4	1.0003	1.0002	1.0002
Mch	$^{13}\text{CDO-H}_4\text{MPT}$	$^{13}\text{CD-H}_4\text{MPT}$	-74.2	-68.5	-64.0	0.9997	0.9996	0.9996
Mtd	$^{13}\text{CH-H}_4\text{MPT} + \text{F}_{420}\text{HD}$	$^{13}\text{CHD-H}_4\text{MPT}^\dagger$	-92.6	-82.5	-73.7	0.9953	0.9959	0.9964
Mtd	$^{13}\text{CD-H}_4\text{MPT} + \text{F}_{420}\text{H}_2$	$^{13}\text{CHD-H}_4\text{MPT}^\ddagger$	-61.2	-52.9	-45.4	0.9997	0.9998	0.9999
Hmd	$^{13}\text{CH-H}_4\text{MPT} + \text{HD}$	$^{13}\text{CHD-H}_4\text{MPT}^\dagger$	-1346.4	-1190.6	-1059.0	0.9953	0.9959	0.9964
Mer	$^{13}\text{CH}_2\text{-H}_4\text{MPT} + \text{F}_{420}\text{HD}$	$^{13}\text{CH}_2\text{D-H}_4\text{MPT}$	-13.9	-17.6	-20.2	0.9948	0.9954	0.9960
Mer	$^{13}\text{CHD-H}_4\text{MPT}^\dagger + \text{F}_{420}\text{H}_2$	$^{13}\text{CH}_2\text{D-H}_4\text{MPT}$	96.0	80.5	67.8	0.9995	0.9995	0.9996
Mer	$^{13}\text{CHD-H}_4\text{MPT}^\ddagger + \text{F}_{420}\text{H}_2$	$^{13}\text{CH}_2\text{D-H}_4\text{MPT}$	98.8	83.5	70.8	0.9996	0.9997	0.9997
Mtr	$^{13}\text{CH}_2\text{D-H}_4\text{MPT}$	$^{13}\text{CH}_2\text{D-SCoM}$	61.0	54.2	48.4	0.9997	0.9998	0.9998
Mcr	$^{13}\text{CH}_3\text{-SCoM} + \text{DS-CoB}$	$^{13}\text{CH}_3\text{D(g)}$	-639.5	-584.2	-536.2	0.9943	0.9950	0.9956
Mcr	$^{13}\text{CH}_2\text{D-SCoM} + \text{HS-CoB}$	$^{13}\text{CH}_3\text{D(g)}$	57.1	44.7	35.0	0.9998	0.9998	0.9998
Acetoclastic pathway								
Ack/Pta	$^{13}\text{CH}_2\text{D-COO}^-$	$^{13}\text{CH}_2\text{D-COSCoA}$	-10.0	-9.0	-8.2	1.0000	1.0000	1.0000
Cdh	$^{13}\text{CH}_2\text{D-COSCoA}$	$^{13}\text{CH}_2\text{D-H}_4\text{MPT}$	-60.1	-52.9	-46.9	1.0000	1.0000	1.0000
Methylotrophic pathway								
Mta	$^{13}\text{CH}_2\text{D-OH}$	$^{13}\text{CH}_2\text{D-SCoM}$	79.6	72.2	65.6	1.0000	1.0000	1.0000

Notes: (\dagger) $^{13}\text{CHD-H}_4\text{MPT}$ with D in the pro-R face. (\ddagger) $^{13}\text{CHD-H}_4\text{MPT}$ with D in the pro-S face.

Table 9: **Equilibrium D–D clumped isotopologue fractionation factors at 25 °C, 50 °C and 75 °C.** The deviation of the clumped isotopologue equilibrium fractionation factors (EFFs) from the product of the hydrogen EFFs is denoted by $^{2,2}\gamma^{\text{eq}}$ where $^{2,2}\gamma^{\text{eq}} = ^{2,2}\alpha^{\text{eq}} / (^2\alpha^{\text{eq}} \times ^2\alpha^{\text{eq}})$. Notation: (g) gas phase. The full reactions are listed in Table 1.

Enzyme	Reactant/s	Product	$1000\ln^{2,2}\alpha^{\text{eq}}$ (‰)			$^{2,2}\gamma^{\text{eq}}$		
			25 °C	50 °C	75 °C	25 °C	50 °C	75 °C
Hydrogenotrophic pathway								
Mtd	$^{12}\text{CD-H}_4\text{MPT} + \text{F}_{420}\text{HD}$	$^{12}\text{CD}_2\text{-H}_4\text{MPT}$	-196.7	-173.6	-153.4	0.9868	0.9888	0.9904
Hmd	$^{12}\text{CD-H}_4\text{MPT} + \text{HD}$	$^{12}\text{CD}_2\text{-H}_4\text{MPT}$	-1450.5	-1281.7	-1138.8	0.9868	0.9888	0.9904
Mer	$^{12}\text{CHD-H}_4\text{MPT}^\dagger + \text{F}_{420}\text{HD}$	$^{12}\text{CHD}_2\text{-H}_4\text{MPT}$	44.7	32.3	22.4	0.9846	0.9872	0.9893
Mer	$^{12}\text{CD}_2\text{-H}_4\text{MPT} + \text{F}_{420}\text{H}_2$	$^{12}\text{CHD}_2\text{-H}_4\text{MPT}$	163.2	137.5	116.4	0.9978	0.9984	0.9988
Mtr	$^{12}\text{CHD}_2\text{-H}_4\text{MPT}$	$^{12}\text{CHD}_2\text{-SCoM}$	85.8	76.4	68.2	1.0000	1.0000	1.0000
Mcr	$^{12}\text{CH}_2\text{D-SCoM} + \text{DS-CoB}$	$^{12}\text{CH}_2\text{D}_2(\text{g})$	-598.7	-550.9	-508.8	0.9818	0.9850	0.9876
Mcr	$^{12}\text{CHD}_2\text{-SCoM} + \text{HS-CoB}$	$^{12}\text{CH}_2\text{D}_2(\text{g})$	107.9	86.1	68.9	0.9972	0.9978	0.9983
Acetoclastic pathway								
Ack/Pta	$^{12}\text{CH}_2\text{D-COO}^-$	$^{13}\text{CH}_2\text{D-COSCoA}$	-18.1	-16.4	-14.9	1.0006	1.0005	1.0004
Cdh	$^{12}\text{CH}_2\text{D-COSCoA}$	$^{13}\text{CH}_2\text{D-H}_4\text{MPT}$	-113.5	-100.1	-88.7	1.0005	1.0004	1.0003
Methylotrophic pathway								
Mta	$^{12}\text{CH}_2\text{D-OH}$	$^{13}\text{CH}_2\text{D-SCoM}$	121.4	110.0	99.7	1.0005	1.0004	1.0003

Notes: (†) $^{13}\text{CHD-H}_4\text{MPT}$ with D in the pro-S face.

Table 10: **Scenarios of reversibility control over the net carbon isotope fractionation in the considered pathways.** In all scenarios, the reversibility f (defined as the ratio of the backward and forward fluxes) of each enzymatically catalyzed reaction ranges from 1 (i.e., fully reversible) to 0 (i.e., irreversible). References are to previous reports that used the scenario.

Scenario description	Ref.	$1000\ln^{13}\alpha$
<i>Hydrogenotrophic pathway</i> (Section 4.4.1)		
(i) Uniform departure from equilibrium of all reactions ($f = 1 \rightarrow 0$).	1	20‰ to 69‰
(ii) Equilibrium between CO_2 and $\text{CH}_3\text{-SCoM}$ ($f = 1$), gradual departure from equilibrium of the Mcr-catalyzed reaction ($f = 1 \rightarrow 0$).	2, 3	69‰ to 106‰
(iii) Pathway reduced to four carbon reduction steps (Fmd, Mtd, Mer, Mcr), with f of either 0 or 1 for each.	4	20‰ to 106‰
<i>Methylotrophic pathway</i> (Section 4.4.3)		
Variable reversibility between CH_3OH and $\text{CH}_3\text{-SCoM}$, and between $\text{CH}_3\text{-SCoM}$ and CH_4 (f drawn from a uniform distribution between 0 and 1). Between $\text{CH}_3\text{-SCoM}$ and CO_2 f is set to 0.75.	–	Depends on $R_{r/o}$, the reduction:oxidation ratio of methanol
<i>Acetoclastic pathway</i> (Section 4.4.4)		
Equilibrium between $\text{CH}_3\text{-COO}^-$ and $\text{CH}_3\text{-SCoM}$ ($f = 1$), gradual departure from equilibrium of the Mcr-catalyzed reaction ($f = 1 \rightarrow 0$).	–	16‰ to 53‰
<i>AOM</i> (Section 4.4.5)		
All reactions are fully reversible ($f = 1$), with the exception of a single reaction that is irreversible ($f = 0$). The identity of the irreversible reaction is varied to produce the range.	2	–69‰ to 37‰

(1) Wang et al. (2015); (2) Alperin & Hoehler (2009); (3) Stolper et al. (2015); (4) Cao et al. (2019).

Table 11: **Carbon isotope fractionation during AOM.** The maximum net CH₄-CO₂ carbon isotope fractionation ($1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$) that can be obtained at a steady state when a single reaction is irreversible ($f = 0$) and all other reactions remain completely reversible ($f = 1$), using the framework outlined in Appendix A. We used the experimentally-determined KFF of Mcr ($1000\ln^{13}\alpha_{\text{CH}_4 \rightarrow \text{CH}_3\text{-SCoM}}^{\text{kin}} = -38\%$; Scheller et al., 2013). The KFFs of the other enzymes were uniformly assigned values of -5% or -40% .

Irreversible reaction	$1000\ln^{13}\alpha_{\text{CH}_4-\text{CO}_2}$	
	$1000\ln^{13}\alpha^{\text{kin}} = -5\%$	$1000\ln^{13}\alpha^{\text{kin}} = -40\%$
Mcr	37.9	37.9
Mtr	3.0	37.9
Mer	-14.0	20.0
Mtd	-30.6	4.4
Mch	-47.8	-12.7
Ftr	-44.4	-9.3
Fmd	-49.9	-14.8

856 **6** FIGURES

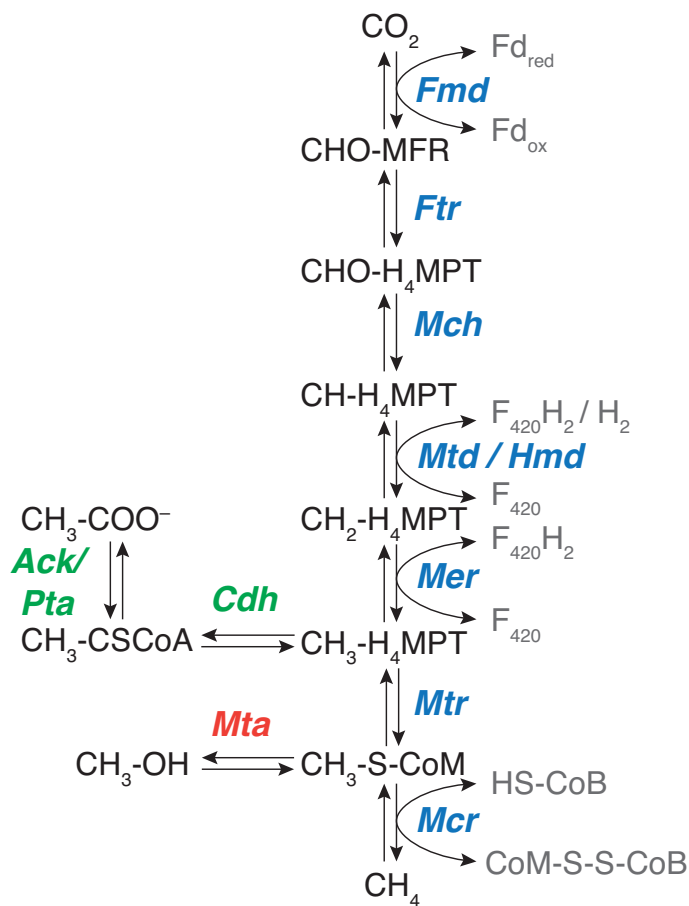


Figure 1: **Metabolic pathways of methanogenesis and anaerobic oxidation of methane (AOM)**. The metabolite names are in black, electron carriers in gray, and enzymes in bold-italicized colored fonts. The reactions that are unique to the acetoclastic and methylotrophic pathways are in green and red, respectively. The reactions in blue are the hydrogenotrophic and AOM pathways, and are common also with the acetoclastic and methylotrophic pathways. All the reactions are assumed to have the potential for full reversibility.

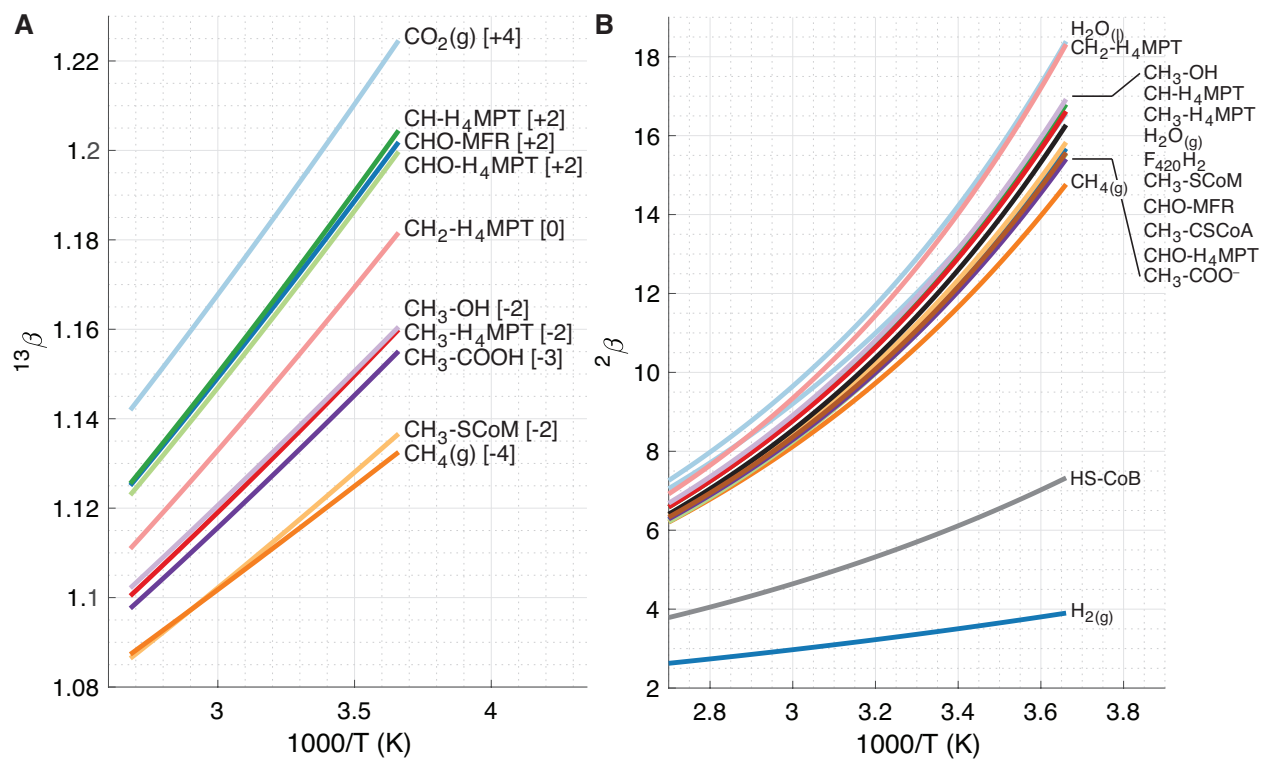


Figure 2: **Calculated carbon (A) and hydrogen (B) β values.** The carbon oxidation state is given in square brackets. The β values, including the clumped isotopologues (not plotted here), are listed in Tables 2-4.

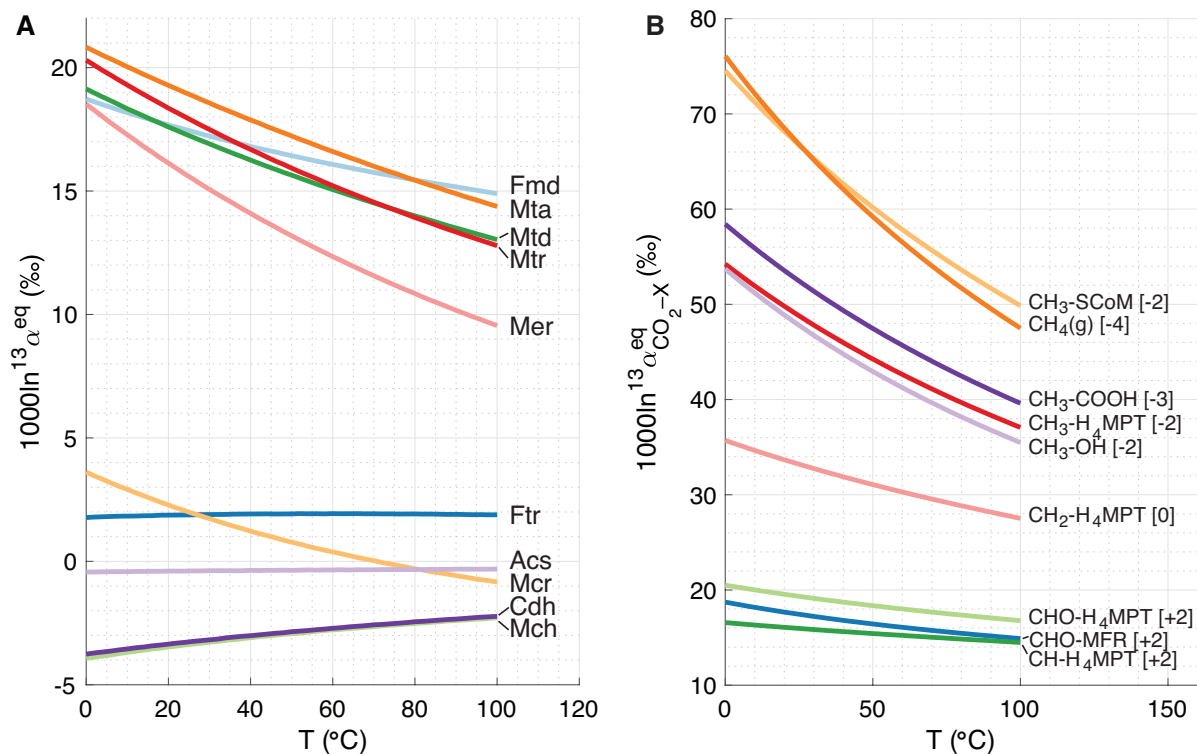


Figure 3: **Temperature dependence of the calculated equilibrium carbon isotope fractionation factors (EFFs) for the organic compounds involved in methanogenesis.** (A) The EFFs of the reactions catalyzed by the enzymes shown next to the corresponding lines and listed in Table 1. (B) The carbon isotopic EFFs between gas-phase CO_2 and the compounds in the methanogenesis pathways ($1000 \ln^{13}\alpha_{\text{CO}_2\text{-X}}^{\text{eq}}$, where ‘X’ denotes the intracellular compounds). The carbon oxidation state is given in square brackets.

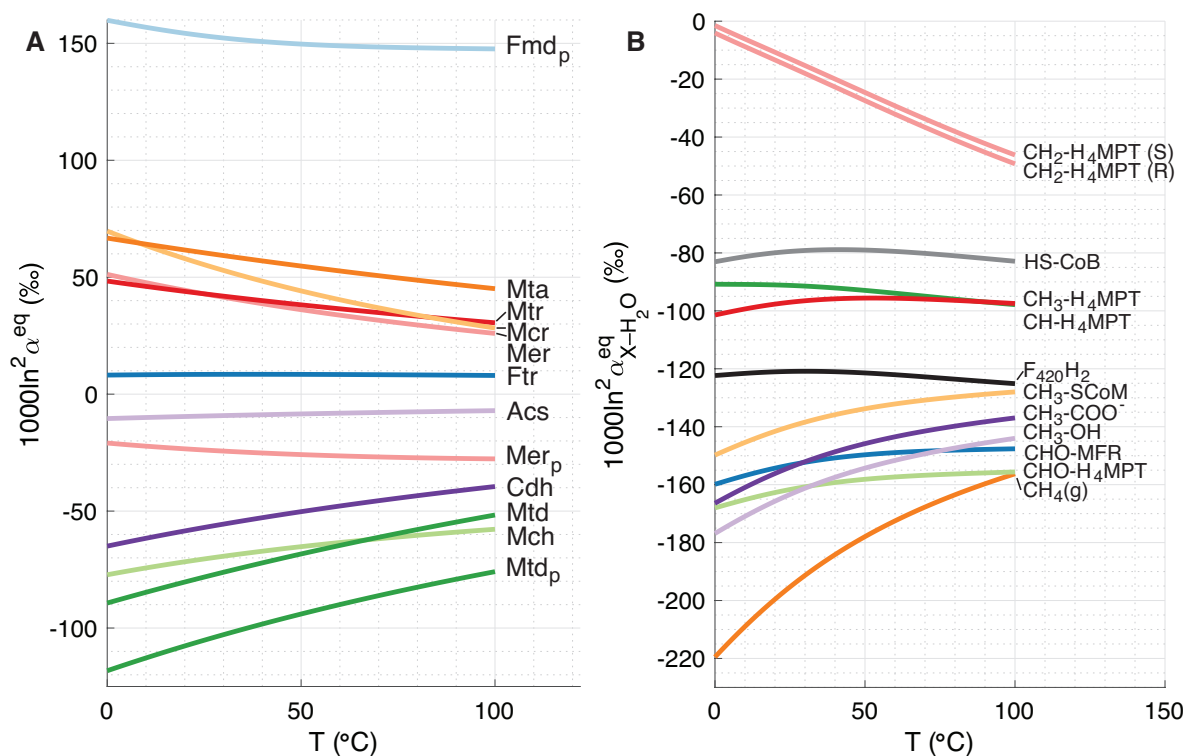


Figure 4: **Temperature dependence of the calculated equilibrium hydrogen isotope fractionation factors (EFFs) for the organic compounds involved in methanogenesis.** (A) The EFFs of the reactions catalyzed by the enzymes shown next to the corresponding lines and listed in Table 1. A subscripted ‘p’ next to the enzyme abbreviation denotes a primary EFF. (B) The hydrogen isotopic EFFs between $\text{H}_2\text{O}(l)$ and the compounds in the methanogenesis pathways ($1000\ln^2\alpha_{\text{H}_2\text{O-X}}^{\text{eq}}$, where ‘X’ denotes the intracellular compounds).

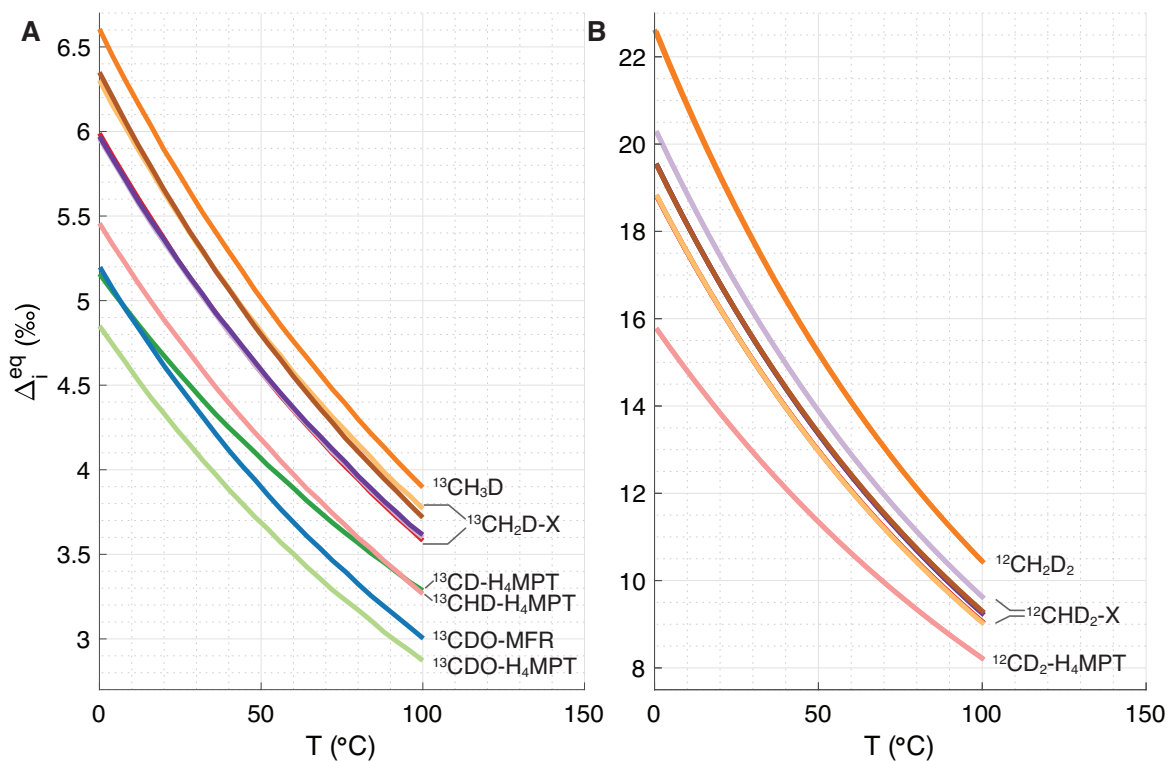


Figure 5: **Doubly-substituted (“clumped”) isotopologue compositions in methanogenesis.** The deviation of the abundance of the clumped isotopologues containing (A) a single ^{13}C -D bond and (B) two ^{12}C -D bonds from the stochastic distribution is expressed as $\Delta_i^{\text{eq}} = (R_i/R_i^*) - 1$, where R_i is the calculated ratio of the doubly-substituted isotopologue to the unsubstituted isotopologue and R_i^* is this ratio at a stochastic distribution of the rare isotopes. The clumped isotopologues of $\text{CH}_3\text{-SCoM}$, $\text{CH}_3\text{-CSCoA}$, $\text{CH}_3\text{-COO}^-$, $\text{CH}_3\text{-OH}$ and $\text{CH}_3\text{-H}_4\text{MPT}$ have similar Δ_i^{eq} values at 100 °C and are all denoted by ‘ $^{13}\text{CH}_2\text{D-X}$ ’ or ‘ $^{12}\text{CHD}_2\text{-X}$ ’. The Δ_i^{eq} values are listed in Table 7.

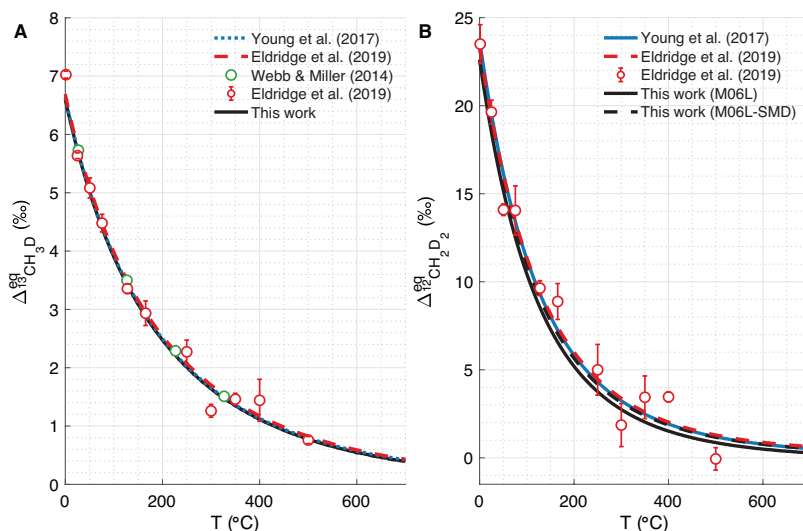


Figure 6: Comparisons of doubly-substituted isotopologue abundances calculated in this study with theoretical (lines) and experimental (circles) estimates. (A) $\Delta_{^{13}\text{CH}_3\text{D}}^{\text{eq}}$ (B) $\Delta_{^{12}\text{CH}_2\text{D}_2}^{\text{eq}}$. The error bars are 1 standard error. In panel B, the results from Webb & Miller (2014) are of Path-Integral Monte Carlo calculations.

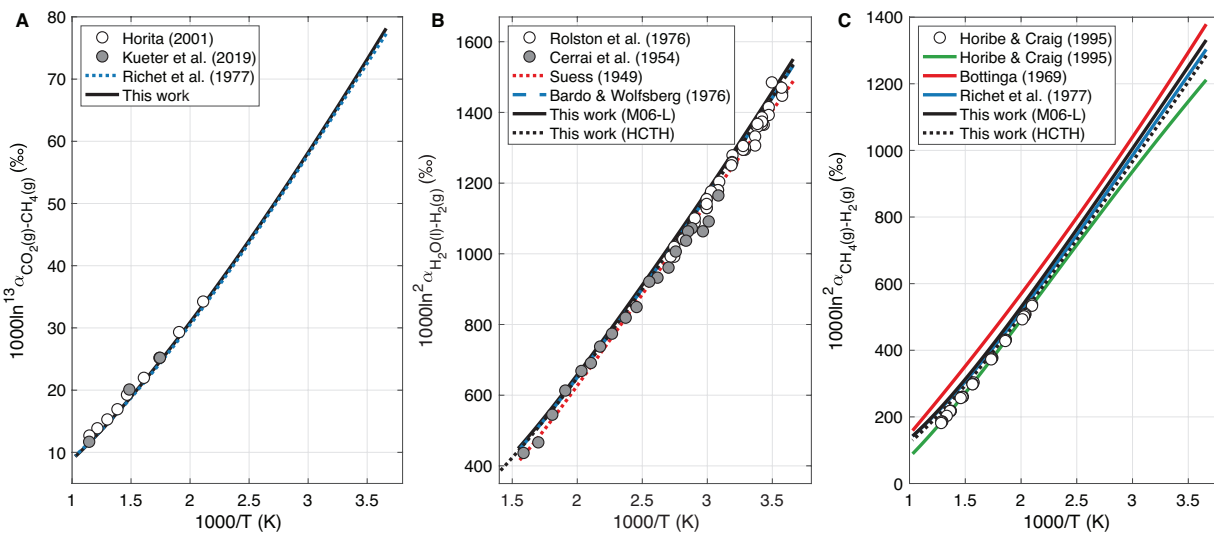


Figure 7: Comparisons of isotope fractionations calculated in this study with theoretical (lines) and experimental (circles) estimates. (A) $\text{CO}_{2(\text{g})}-\text{CH}_{4(\text{g})}$ carbon isotope fractionations. (B) $\text{H}_2\text{O}_{(\text{l})}-\text{H}_{2(\text{g})}$ hydrogen isotope fractionations. (C) $\text{CH}_{4(\text{g})}-\text{H}_{2(\text{g})}$ hydrogen isotope fractionations. The green line was derived from a linear regression of $^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$ on $10^6/T^2$.

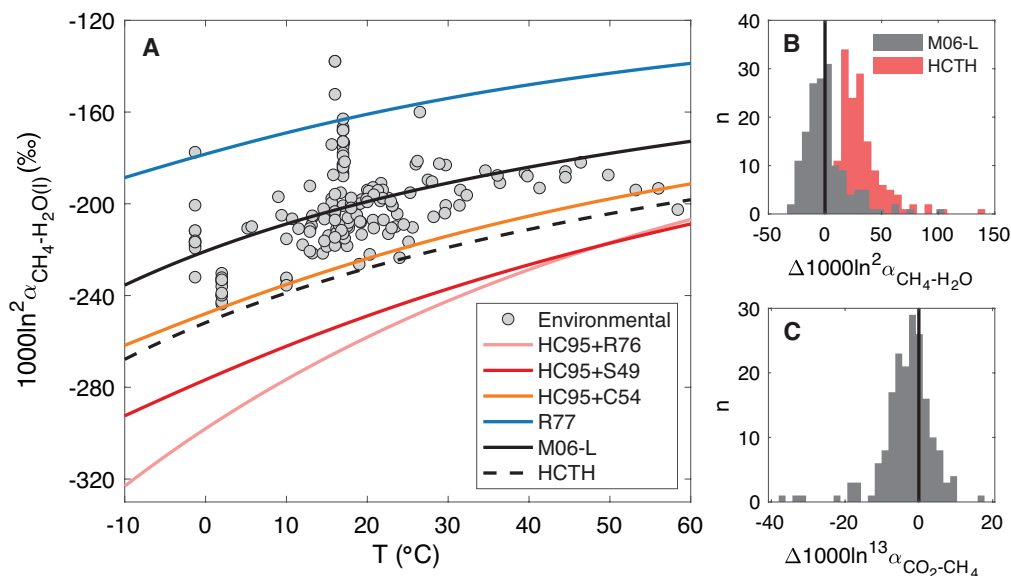


Figure 8: **Comparison of $\text{CH}_4(\text{l})\text{-H}_2\text{O}(\text{l})$ carbon and hydrogen isotope fractionations calculated in this and previous studies with environmental estimates.** (A) $1000\ln^2\alpha_{\text{CH}_4\text{-H}_2\text{O}}$ from theoretical studies and biogenic environmental samples. The lines were generated from different combinations of fits to experimental and theoretical work (Suess, 1949 (S49); Cerrai et al., 1954 (C54); Bottinga, 1969 (B69); Rolston et al., 1976 (R76); Richet et al., 1977 (R77); Horibe and Craig, 1995 (HC95) and this work using the M06-L and HCTH functionals). The $\text{H}_2\text{O}(\text{l})\text{-H}_2\text{O}(\text{g})$ hydrogen isotope fractionations were based on Horita & Wesolowski (1994), except for the results of Rolston et al. (1976), in which case this is noted in the figure legend. (B) The deviation of environmental $1000\ln^2\alpha_{\text{CH}_4\text{-H}_2\text{O}}$ from the temperature-dependent EFFs calculated in this study with the M06-L and HCTH functionals. (C) The deviation of environmental $1000\ln^{13}\alpha_{\text{CO}_2\text{-CH}_4}$ from the temperature-dependent EFFs calculated in this study with the M06-L functional. A full list of the environmental samples presented in this figure is available in Table S.3 with the corresponding references.

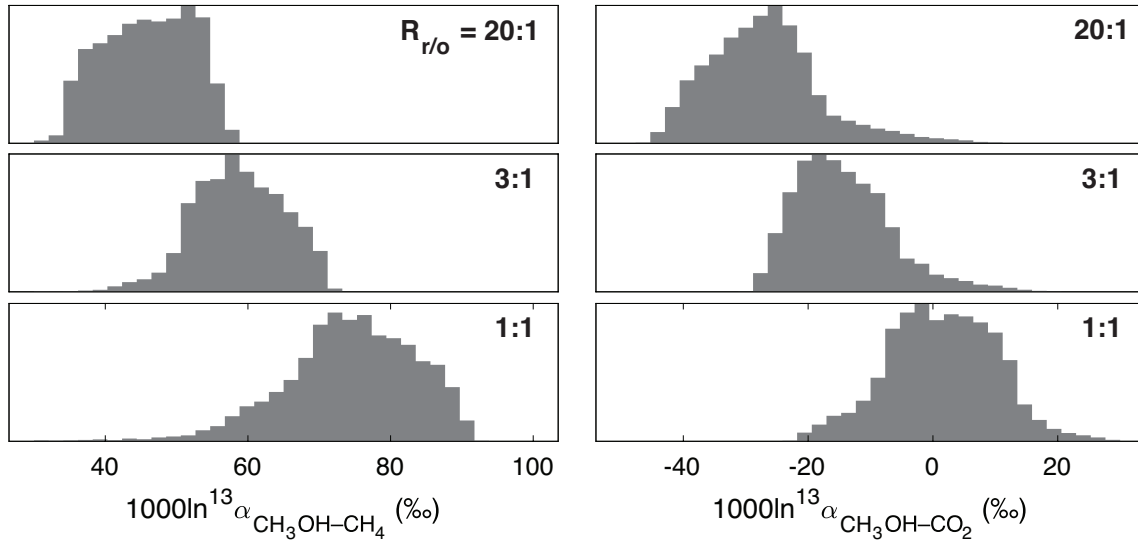


Figure 9: **Carbon isotope fractionation between methanol, $\text{CH}_4(\text{g})$ and $\text{CO}_2(\text{g})$.** *Left:* Methanol– $\text{CH}_4(\text{g})$ carbon isotope fractionation; *Right:* Methanol– $\text{CO}_2(\text{g})$ carbon isotope fractionation. Each histogram represents 10,000 simulations of methylotrophic methanogenesis with KFFs $1000\ln^{13}\alpha_{\text{methanol}\rightarrow\text{CH}_3\text{-SCoM}}^{\text{kin}}$ and $1000^{13}\alpha_{\text{CH}_3\text{-SCoM}\rightarrow\text{CO}_2}^{\text{kin}}$ in the range -30‰ to -50‰ and the reversibilities between methanol and $\text{CH}_3\text{-SCoM}$ and between $\text{CH}_3\text{-SCoM}$ and CH_4 in the range 10^{-3} to 1, each drawn randomly from uniform distributions. The reversibility between $\text{CH}_3\text{-SCoM}$ and CO_2 was held constant at 0.75, and the KFF $1000\ln^{13}\alpha_{\text{CH}_3\text{-SCoM}\rightarrow\text{CH}_4}^{\text{kin}}$ was set to -40‰ (Scheller et al., 2013). The methanol reduction:oxidation ratio, $R_{r/o}$, used for each set of simulations is indicated.

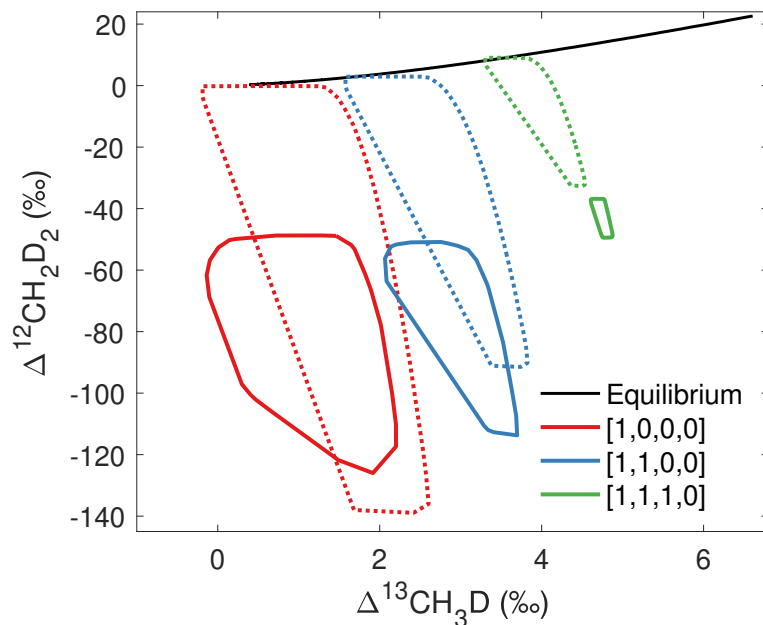


Figure 10: **Prediction of the $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ values based on three reversibility scenarios of hydrogenotrophic methanogenesis.** A comparison between results obtained with the parameters used in the study of Cao et al. (2019) (dotted lines) and the results based on the EFFs calculated in this study (solid lines). The scenarios refer to combinations of the reversibilities of the four hydrogen addition reactions in the hydrogenotrophic methanogenesis pathway, for fully reversible reactions (1) or irreversible reactions (0). The black line shows the equilibrium covariation of $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ values, calculated at the M06-L/TZVP level of theory.

7 SUPPLEMENTARY FIGURE

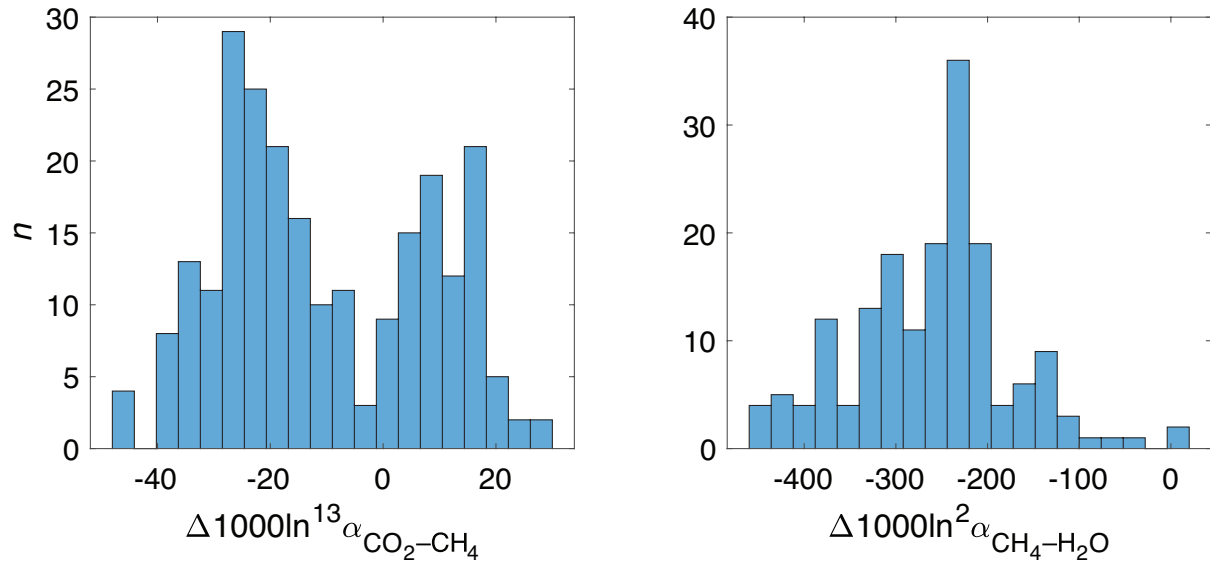


Figure S.1: **Deviations from the expected temperature-dependent EFFs in laboratory culture experiments.** *Left:* carbon isotopes ($N = 213$); *Right:* hydrogen isotopes ($N = 172$). The n on the y-axis label represents the number of samples in each bin. Laboratory data is from Valentine et al. (2004); Penning et al. (2005); Hattori et al. (2012); Okumura et al. (2016); Topçuoğlu et al. (2019). The complete list of samples is available in Table S.12.

A Isotope fractionation in linear metabolic reaction networks

A.1 General derivation

The net isotope fractionation of any linear metabolic pathway at steady state can be described by a recursive mass balance expression, which requires knowledge of the intermediate reactions' EFFs, forward KFFs and reversibilities, where the reversibility f is defined as the ratio of the reverse and forward mass fluxes (Wing & Halevy, 2014). We implement here this recursive term for carbon isotopes in the hydrogenotrophic and AOM pathways. Under steady-state conditions, the net isotope fractionation of the general reaction $r \rightleftharpoons p$ can be described by:

$$\alpha_{r-p}^{\text{net}} = (\alpha_{r-p}^{\text{eq}} - \alpha_{r \rightarrow p}^{\text{kin}}) f_{p,r} + \alpha_{r \rightarrow p}^{\text{kin}}, \quad (\text{A.1})$$

where α_{r-p}^{eq} , $\alpha_{r \rightarrow p}^{\text{kin}}$ and $\alpha_{r-p}^{\text{net}}$ are, respectively, the EFF between r and p , the KFF between r and the flux of r to p , and the net isotope fractionation between r and p . This treatment can be applied to linear pathways, such as $s \rightleftharpoons r \rightleftharpoons p$, by extending Eq. A.1:

$$\alpha_{s-p}^{\text{net}} = (\alpha_{r-p}^{\text{net}} \times \alpha_{s-r}^{\text{eq}} - \alpha_{s \rightarrow r}^{\text{kin}}) f_{r,s} + \alpha_{s \rightarrow r}^{\text{kin}} \quad (\text{A.2})$$

(full derivation in Wing and Halevy (2014)). Eq. A.2 can be further extended by recursion to any number of reactions in a linear metabolic network at steady state. We use this type of recursive expression to explore carbon isotope fractionation in the hydrogenotrophic (Section 4.4.1) and acetoclastic (Section 4.4.4) methanogenesis, and anaerobic methane oxidation (Section 4.4.5) pathways.

A.2 Equations for hydrogenotrophic methanogenesis and AOM

We used Eqs. A.3–A.9 to calculate the net carbon isotope fractionation at steady state between (i) CO_2 and CH_4 (Section 4.4.1) and (ii) CH_4 and CO_2 (Section 4.4.5). For brevity, we denote here the molecules in the pathway by the letters A-H, where for case (i) A is CO_2 and H is CH_4 , with the intracellular carbon-bearing molecules denoted by B-G, and for case

881 (ii) we use the reverse notation where CH_4 is A and CO_2 is H.

$$\alpha_{\text{G-H}}^{\text{net}} = (\alpha_{\text{G-H}}^{\text{eq}} - \alpha_{\text{G}\rightarrow\text{H}}^{\text{kin}}) f_{\text{H,G}} + \alpha_{\text{G}\rightarrow\text{H}}^{\text{kin}} \quad (\text{A.3})$$

$$\alpha_{\text{F-H}}^{\text{net}} = (\alpha_{\text{G-H}}^{\text{net}} \times \alpha_{\text{F-G}}^{\text{eq}} - \alpha_{\text{F}\rightarrow\text{G}}^{\text{kin}}) f_{\text{G,F}} + \alpha_{\text{F}\rightarrow\text{G}}^{\text{kin}} \quad (\text{A.4})$$

$$\alpha_{\text{E-H}}^{\text{net}} = (\alpha_{\text{F-H}}^{\text{net}} \times \alpha_{\text{E-F}}^{\text{eq}} - \alpha_{\text{E}\rightarrow\text{F}}^{\text{kin}}) f_{\text{F,E}} + \alpha_{\text{E}\rightarrow\text{F}}^{\text{kin}} \quad (\text{A.5})$$

$$\alpha_{\text{D-H}}^{\text{net}} = (\alpha_{\text{E-H}}^{\text{net}} \times \alpha_{\text{D-E}}^{\text{eq}} - \alpha_{\text{D}\rightarrow\text{E}}^{\text{kin}}) f_{\text{E,D}} + \alpha_{\text{D}\rightarrow\text{E}}^{\text{kin}} \quad (\text{A.6})$$

$$\alpha_{\text{C-H}}^{\text{net}} = (\alpha_{\text{D-H}}^{\text{net}} \times \alpha_{\text{C-D}}^{\text{eq}} - \alpha_{\text{C}\rightarrow\text{D}}^{\text{kin}}) f_{\text{D,C}} + \alpha_{\text{C}\rightarrow\text{D}}^{\text{kin}} \quad (\text{A.7})$$

$$\alpha_{\text{B-H}}^{\text{net}} = (\alpha_{\text{C-H}}^{\text{net}} \times \alpha_{\text{B-C}}^{\text{eq}} - \alpha_{\text{B}\rightarrow\text{C}}^{\text{kin}}) f_{\text{C,B}} + \alpha_{\text{B}\rightarrow\text{C}}^{\text{kin}} \quad (\text{A.8})$$

$$\alpha_{\text{A-H}}^{\text{net}} = (\alpha_{\text{B-H}}^{\text{net}} \times \alpha_{\text{A-B}}^{\text{eq}} - \alpha_{\text{A}\rightarrow\text{B}}^{\text{kin}}) f_{\text{B,A}} + \alpha_{\text{A}\rightarrow\text{B}}^{\text{kin}} \quad (\text{A.9})$$

882 B Isotope fractionation in nonlinear metabolic reaction 883 networks

884 The analytical expression for the calculation of net isotope fractionation presented in Ap-
885 pendix A is only applicable to reversible, linear networks. However, if some of the reactions
886 in the network have more than one source of the atom of interest, an analytical solution is
887 usually not possible, and a numerical solution is required. Consider the reaction:



888 where a , b and c are arbitrary organic residues, Y is the atom of interest, n and m are
889 the stoichiometric coefficients of Y , and ϕ is the reaction flux. For brevity, we denote aY_n ,
890 bY_m and $cY_{(n+m)}$ as r_1 , r_2 and p , respectively. The change of the isotopic composition of
891 compound p with time is:

$$\frac{d}{dt}R_p = \frac{1}{[p]} \left[\phi_{rp} (n \cdot \alpha_{r_1 \rightarrow p}^{\text{kin}} R_{r_1} + m \cdot \alpha_{r_2 \rightarrow p}^{\text{kin}} R_{r_2}) - \right. \\ \left. \phi_{pr} \cdot R_p (n \cdot \alpha_{p \rightarrow r_1}^{\text{kin}} + m \cdot \alpha_{p \rightarrow r_2}^{\text{kin}}) - R_p (m + n) (\phi_{rp} - \phi_{pr}) \right], \quad (\text{B.2})$$

892 where R_{r_1} , R_{r_2} and R_p are the ratios of the rare to abundant isotopes in pools r_1 , r_2 and p ,
893 respectively. In the specific case of a chemical and isotopic steady state, the concentration
894 and isotopic composition of p are constant, and $\frac{dR_p}{dt} = \frac{d[p]}{dt} = 0$. Rearranging Eq. B.2 yields
895 an analytical solution for R_p at steady state:

$$R_p = \frac{\phi_{rp} (n \cdot \alpha_{r_1 \rightarrow p}^{\text{kin}} R_{r_1} + m \cdot \alpha_{r_2 \rightarrow p}^{\text{kin}} R_{r_2})}{\phi_{pr} (n \cdot \alpha_{p \rightarrow r_1}^{\text{kin}} + m \cdot \alpha_{p \rightarrow r_2}^{\text{kin}}) + (m + n) (\phi_{rp} - \phi_{pr})} \quad (\text{B.3})$$

896 (Full derivation in Eq. S5 in Wing and Halevy (2014)). This approach is used here for three
897 specific cases: hydrogen isotope fractionation in hydrogenotrophic methanogenesis (Section
898 4.4.2), carbon isotope fractionation in methylotrophic methanogenesis (Section 4.4.3) and
899 clumped isotopologue compositions in hydrogenotrophic methanogenesis (Section 4.4.6).

900 B.1 Hydrogen isotope fractionation in the hydrogenotrophic methano- 901 genesis pathway

902 The last reaction in the hydrogenotrophic methanogenesis pathway, catalyzed by Mcr, has
903 a large negative ΔG_r^0 (~ -30 kJ mol $^{-1}$ at 25 °C) and is thought to be practically irreversible
904 during methanogenesis (i.e., $\phi_{\text{CH}_3\text{-SCoM} \rightarrow \text{CH}_4} \gg \phi_{\text{CH}_4 \rightarrow \text{CH}_3\text{-SCoM}}$) (Thauer, 2011). In this case,
905 the reverse reactions from methane will not affect the net isotope composition, and Eq. B.3
906 can be simplified to:

$${}^2R_{\text{CH}_4} = \frac{3}{4} \times {}^2\alpha_{\text{CH}_3\text{-SCoM} \rightarrow \text{CH}_4}^{\text{kin}} {}^2R_{\text{CH}_3\text{-SCoM}} + \frac{1}{4} \times {}^2\alpha_{\text{HS-CoB} \rightarrow \text{CH}_4}^{\text{kin}} {}^2R_{\text{HS-CoB}}. \quad (\text{B.4})$$

907 In the specific case that the reaction between H_2O and $\text{CH}_3\text{-SCoM}$, and coenzyme B reduction
 908 to HS-CoB are at chemical and isotopic equilibrium, then:

$${}^2R_{\text{CH}_3\text{-SCoM}} = {}^2R_{\text{H}_2\text{O}} / {}^2\alpha_{\text{H}_2\text{O}-\text{CH}_3\text{-SCoM}}^{\text{eq}} \quad (\text{B.5})$$

909 and

$${}^2R_{\text{HS-CoB}} = {}^2R_{\text{H}_2\text{O}} / {}^2\alpha_{\text{H}_2\text{O}-\text{HS-CoB}}^{\text{eq}}. \quad (\text{B.6})$$

910 Eq. B.4 is then:

$${}^2R_{\text{CH}_4} = \frac{3}{4} \left(\alpha_{\text{CH}_3\text{-SCoM} \rightarrow \text{CH}_4}^{\text{kin}} \cdot {}^2R_{\text{H}_2\text{O}} / {}^2\alpha_{\text{H}_2\text{O}-\text{CH}_3\text{-SCoM}}^{\text{eq}} \right) + \frac{1}{4} \left({}^2\alpha_{\text{HS-CoB} \rightarrow \text{CH}_4}^{\text{kin}} \cdot {}^2R_{\text{H}_2\text{O}} / {}^2\alpha_{\text{H}_2\text{O}-\text{HS-CoB}}^{\text{eq}} \right). \quad (\text{B.7})$$

911 The net hydrogen isotope fractionation between CH_4 and H_2O , ${}^2\alpha_{\text{CH}_4-\text{H}_2\text{O}}$, can be calculated
 912 by dividing both sides of Eq. B.7 by ${}^2R_{\text{H}_2\text{O}}$:

$${}^2\alpha_{\text{CH}_4-\text{H}_2\text{O}} = \frac{3}{4} \left({}^2\alpha_{\text{CH}_3\text{-SCoM} \rightarrow \text{CH}_4}^{\text{kin}} / {}^2\alpha_{\text{H}_2\text{O}-\text{CH}_3\text{-SCoM}}^{\text{eq}} \right) + \frac{1}{4} \left({}^2\alpha_{\text{HS-CoB} \rightarrow \text{CH}_4}^{\text{kin}} / {}^2\alpha_{\text{H}_2\text{O}-\text{HS-CoB}}^{\text{eq}} \right). \quad (\text{B.8})$$

913 **B.2 Carbon isotope fractionation in the methylotrophic methano-** 914 **genesis pathway**

915 In the methylotrophic methanogenesis pathway, methanol is converted to $\text{CH}_3\text{-SCoM}$, which
 916 is then either oxidized to CO_2 in the reverse methanogenic pathway or reduced to CH_4 by
 917 the Mcr-catalyzed reaction (Fig. 1):



918 where n and m are stoichiometric coefficients. This is a simplified view of the pathway, yet it
 919 includes the pathway's three main branches. We define $R_{r/o} \equiv n : m$, the ratio of the reduced
 920 and oxidized branches. If all methanol molecules are converted to either CO_2 or CH_4 , $R_{r/o}$
 921 is expected to be 3:1, as the source of the 2 electrons for $\text{CH}_3\text{-SCoM}$ reduction to CH_4 is
 922 from the full oxidation of $\text{CH}_3\text{-SCoM}$ to CO_2 , which yields 6 electrons. However, if some of
 923 the $\text{CH}_3\text{-SCoM}$ is instead converted to biomass, $R_{r/o}$ may vary. For brevity, we denote the
 924 metabolites here as A (CH_3OH), B ($\text{CH}_3\text{-SCoM}$), C (CH_4) and D (CO_2). The change in the
 925 isotopic composition of B (R_B) with time is:

$$\frac{d}{dt} {}^{13}R_B = \frac{1}{[\text{B}]} \left[(n + m) \cdot \phi_{\text{AB}} {}^{13}\alpha_{\text{A} \rightarrow \text{B}}^{\text{kin}} {}^{13}R_A + n \cdot \phi_{\text{CB}} {}^{13}\alpha_{\text{C} \rightarrow \text{B}}^{\text{kin}} {}^{13}R_C + m \cdot \phi_{\text{DB}} {}^{13}\alpha_{\text{D} \rightarrow \text{B}}^{\text{kin}} {}^{13}R_D - \right. \\ \left. {}^{13}R_B \left((n + m) \cdot \phi_{\text{BA}} {}^{13}\alpha_{\text{B} \rightarrow \text{A}}^{\text{kin}} + n \cdot \phi_{\text{BC}} {}^{13}\alpha_{\text{B} \rightarrow \text{C}}^{\text{kin}} + m \cdot \phi_{\text{BD}} {}^{13}\alpha_{\text{B} \rightarrow \text{D}}^{\text{kin}} \right) - \right. \\ \left. {}^{13}R_B \left((n + m) (\phi_{\text{AB}} - \phi_{\text{BA}}) + n (\phi_{\text{CB}} - \phi_{\text{BC}}) + m (\phi_{\text{DB}} - \phi_{\text{BD}}) \right) \right]. \quad (\text{B.10})$$

926 We write similar time derivatives for C and D:

$$\frac{d}{dt} {}^{13}R_C = \frac{1}{[C]} \cdot n [\phi_{BC} {}^{13}\alpha_{B \rightarrow C}^{\text{kin}} {}^{13}R_B - \phi_{CB} {}^{13}\alpha_{C \rightarrow B}^{\text{kin}} {}^{13}R_C - {}^{13}R_C (\phi_{BC} - \phi_{CB})], \quad (\text{B.11})$$

927

$$\frac{d}{dt} {}^{13}R_D = \frac{1}{[D]} \cdot m [\phi_{BD} {}^{13}\alpha_{B \rightarrow D}^{\text{kin}} {}^{13}R_B - \phi_{DB} {}^{13}\alpha_{D \rightarrow B}^{\text{kin}} {}^{13}R_D - {}^{13}R_D (\phi_{BD} - \phi_{DB})]. \quad (\text{B.12})$$

928 The metabolic network of the methyltrophic pathway as presented in Eq. B.9 is non-linear.
 929 Thus, the isotope fractionations between A, C and D are not independent of each other, and
 930 an analytical solution is nontrivial and provides little intuition. Instead, a numerical solution
 931 to this system is possible, by forward integration of Eqs. B.10–B.12 until the steady-state
 932 solution is obtained. To solve this system, we used the ode15s solver in MATLAB[®]. We
 933 assigned the reversibility of the reactions (f), the net rate (ϕ_{net}), ${}^{13}R_A$, and the forward KFFs
 934 ${}^{13}\alpha^{\text{kin}}$. We calculated the backward KFFs by the relation $\alpha_{A-B}^{\text{eq}} = \alpha_{B \rightarrow A}^{\text{kin}} / \alpha_{A \rightarrow B}^{\text{kin}}$. We assumed
 935 that the reaction from CH₃-SCoM to CO₂ is partially reversible, i.e., $\phi_{DB} / \phi_{BD} = 0.75$, to
 936 obtain the ideal fit to the observed ranges of methanol-CH₄ and methanol-CO₂ carbon
 937 isotope fractionations. The forward and reverse fluxes are related to the net rate and the f s:

$$\phi_{AB} = \frac{\phi_{net}}{1 - f_{B,A}}, \quad (\text{B.13})$$

938

$$\phi_{BA} = \frac{\phi_{net} \times f_{B,A}}{1 - f_{B,A}}. \quad (\text{B.14})$$

939 **B.3 Clumped isotopologue compositions of methane in the hy-** 940 **drogenotrophic pathway**

941 We consider a simplification of the hydrogenotrophic pathway, which includes the four steps
 942 of hydrogen addition under three scenarios of reversibility, as presented by Cao et al. (2019).
 943 Each scenario is denoted by a vector of ones (fully reversible reaction) and zeros (irreversible
 944 reaction), e.g., [1,1,1,0] represents three reversible reactions from CO₂ and H₂O to CH₃-
 945 SCoM, and an irreversible reaction from CH₃-SCoM and HS-CoB to CH₄. Notably, Cao
 946 et al. (2019) assume that the intracellular hydrogen pools (F₄₂₀H₂ and HS-CoB), which are
 947 the source of the hydrogen added to carbon to ultimately form methane, are at equilibrium
 948 with H₂O, and that the EFFs and KFFs of the different steps in the pathway are identical,
 949 allowing derivation of elegant solutions for $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ values. We explored
 950 the effect of using our calculated EFFs on the same scenarios, and used similar solutions but
 951 without the assumption of identical EFFs along the pathway. The original equations and
 952 parameters are presented in Tables 1 and 2 in Cao et al. (2019), we use similar distributions
 953 of unknown KFFs and the respective kinetic γ values. We show here the equations that we
 954 used with our calculated EFFs to find the $\Delta^{13}\text{CH}_3\text{D}$ and $\Delta^{12}\text{CH}_2\text{D}_2$ values (Fig. 10).

955 **B.3.1 Scenario [1,0,0,0]**

956 Following equations A.11a–d in Cao et al. (2019) we get:

$$\Delta^{13}\text{CH}_3\text{D} = \frac{\left(\begin{array}{l} 13,2\gamma^2\alpha^{kin} \left(1 + \Delta_{13\text{CDO-MFR}}^{\text{eq}} \right) \cdots \\ + 13,2\gamma_p^2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} \cdots \\ + 13,2\gamma_p^2\alpha_p^{kin2}\alpha_{\text{HS-CoB-CHO-MFR}}^{\text{eq}} \end{array} \right)}{\left(\begin{array}{l} 2\alpha^{kin} + 2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} \cdots \\ + 2\alpha_p^{kin2}\alpha_{\text{HS-CoB-CHO-MFR}}^{\text{eq}} \end{array} \right)} - 1, \quad (\text{B.15})$$

957 where the γ and γ_p are for the deviation of the clumped KFF from the bulk KFF, as defined
 958 by Wang et al. (2015) for secondary and primary KFFs, respectively, and ${}^2\alpha^{kin}$ and ${}^2\alpha_p^{kin}$ are
 959 secondary and primary KFFs drawn from uniform distributions, respectively.

$$\Delta^{12}\text{CH}_2\text{D}_2 = \frac{\left(\begin{array}{l} 2,2\gamma_p^2\alpha_p^{kin2}\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} \cdots \\ + 2,2\gamma_p^2\alpha_p^{kin} \left(2\alpha^{kin} + 2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} \right) 2\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} \cdots \\ + 2,2\gamma_p^2\alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{kin} \left(2\alpha^{kin} + 2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} \right) \cdots \\ + 2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} 2\alpha_{\text{HS-CoB-CHO-MFR}}^{\text{eq}} \end{array} \right)}{3/8 \left(\begin{array}{l} 2\alpha^{kin} + 2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} \cdots \\ + 2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CHO-MFR}}^{\text{eq}} \cdots \\ + 2\alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{kin} 2\alpha_{\text{HS-CoB-CHO-MFR}}^{\text{eq}} \end{array} \right)^2} - 1, \quad (\text{B.16})$$

960

961 **B.3.2 Scenario [1,1,0,0]**

962 Following equations A.15a–d in Cao et al. (2019) we get:

$$\Delta^{13}\text{CH}_3\text{D} = \frac{\left(\begin{array}{l} 13,2\gamma^2\alpha^{kin} \left(1 + \Delta_{13\text{CHD-H}_4\text{MPT}}^{\text{eq}} \right) \cdots \\ + 13,2\gamma_p^2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \cdots \\ + 13,2\gamma_p^2\alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{kin} 2\alpha_{\text{HS-CoB-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \end{array} \right)}{\left(\begin{array}{l} 2\alpha_{s2}^{kin} + 2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \cdots \\ + 2\alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{kin} 2\alpha_{\text{HS-CoB-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \end{array} \right)} - 1 \quad (\text{B.17})$$

963

$$\Delta^{12}\text{CH}_2\text{D}_2 = \frac{\left(\begin{array}{l} 2,2\gamma \left(2\alpha^{kin} \right)^2 \left(1 + \Delta_{12\text{CD}_2\text{-H}_4\text{MPT}}^{\text{eq}} \right) \cdots \\ + 2,2\gamma_p^2\alpha_p^{kin2}\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \cdots \\ + 2,2\gamma_p^2\alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{kin} \left(2\alpha^{kin2}\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \right) 2\alpha_{\text{HS-CoB-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \end{array} \right)}{3/8 \left(\begin{array}{l} 2\alpha^{kin} + 2\alpha_p^{kin2}\alpha_{\text{F}_{420}\text{H}_2\text{-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \cdots \\ + 2\alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{kin} 2\alpha_{\text{HS-CoB-CH}_2\text{-H}_4\text{MPT}}^{\text{eq}} \end{array} \right)^2} - 1 \quad (\text{B.18})$$

964

965 **B.3.3 Scenario [1,1,1,0]**

966 Following equations A.19a–d in Cao et al. (2019) we get:

$$\Delta^{13}\text{CH}_3\text{D} = \frac{\left(3^{13,2}\gamma_p^2 \alpha_{\text{CH}_3\text{-SCoM}\rightarrow\text{CH}_4}^{\text{kin}} \left(1 + \Delta_{13}^{\text{eq}} \text{CH}_2\text{D-SCoM} \right) \cdots \right)}{3^2 \alpha_{\text{CH}_3\text{-SCoM}\rightarrow\text{CH}_4}^{\text{kin}} + 2 \alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{\text{kin}} 2 \alpha_{\text{HS-CoB-CH}_3\text{-SCoM}}^{\text{eq}}} - 1 \quad (\text{B.19})$$

967

$$\Delta^{12}\text{CH}_2\text{D}_2 = \frac{\left(8^2 \alpha_{\text{CH}_3\text{-SCoM}\rightarrow\text{CH}_4}^{\text{kin}} \left(2,2\gamma_p^2 \alpha_{\text{CH}_3\text{-SCoM}\rightarrow\text{CH}_4}^{\text{kin}} \left(1 + \Delta_{12}^{\text{eq}} \text{CHD}_2\text{-SCoM} \right) \cdots \right) + 2,2\gamma_p^2 \alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{\text{kin}} 2 \alpha_{\text{HS-CoB-CH}_3\text{-SCoM}}^{\text{eq}} \right)}{3^2 \alpha_{\text{CH}_3\text{-SCoM}\rightarrow\text{CH}_4}^{\text{kin}} + 2 \alpha_{\text{HS-CoB}\rightarrow\text{CH}_4}^{\text{kin}} 2 \alpha_{\text{HS-CoB-CH}_3\text{-SCoM}}^{\text{eq}}} - 1 \quad (\text{B.20})$$

968

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