Carbon species solvated in molten carbonate electrolyser cell from first-principles simulations

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Abstract

We study the solvation of molecules and ions that are key in the context of Molten Carbonate Electrolyser Cells using first-principles simulations. Focusing on the electroreduction of CO_2 to CO in a molten carbonate medium, we investigate the solvation of both the reactant CO_2 and the product CO in the eutectic LiKCO₃ (containing 62 % Li₂CO₃, 38 % K₂CO₃). CO₂ is found to spontaneously react with the carbonate ions to form the transient pyrocarbonate species, $C_2O_5^{2-}$. To investigate the similar reaction that could occur with CO and CO_3^{2-} to form an oxalate, we simulated that species and found it to be stable in the melt, supporting this hypothesis. We further present the solvation of O^{2-} , finding that it shows preferential formation of a complex with four lithium cations in a tetrahedral arrangement. Estimates of the diffusion coefficients of these species are then reported, showing that CO has the faster diffusion of all the molecules and ions studied.

Keywords: Molten carbonate, first-principles simulation, solvation properties

1. Introduction

Molten carbonates are nowadays used in many applications. For instance, molten carbonate fuel cells (MCFC) can produce electricity in the MW range with long term stability[1]. Moreover, because MCFC consume CO_2 at the cathode side and release CO_2 at the anode side, they have been proposed to combine this electricity production capability with the capture and the concentration of CO_2 out of exhaust gas from steel mills [2, 3]. Alternatively, the high solubility

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of CO_2 in molten carbonates is a possible path to perform carbon capture and utilization (CCU) by electroreduction of CO_2 in molten carbonate electrolyser cells (MCEC)[4, 5]. The reduction of CO_2 in MCEC into amorphous carbon has been well documented and the conversion of CO_2 to CO or even CH_4 has also been evidenced recently [6, 7], thus adding another opportunity for carbon capture and utilisation using carbonate melts.

Optimizing the conditions for an efficient electroreduction of CO_2 in MCEC, for example by tuning the melt temperature or the composition, calls for a better understanding of the microscopic processes involved. In particular, there is need to better understand the speciation of the carbon species and their solvation properties in the melt. Cyclic voltametry[7] has shown that the mechanism of electroreduction of CO_2 in CO is complex and involves the formation of several other species during the reaction. However, the exact nature of these species remains unclear and cyclic voltametry provides only limited microscopic information about these species.

Several recent studies have highlighted the power of computational approaches for the understanding of these complex systems, and a number of of molecular dynamics simulation of molten carbonates have been reported [8, 9, 10, 11, 12, 13, 14]. Molecular dynamics simulations can provide a picture of molecular mechanisms and can accurately predict physico-chemical properties, especially in high temperature and high pressure conditions where experiments are hard to perform.

Molecular dynamics simulations exist in two different flavours: first-principles molecular dynamics (FPMD) and force field based molecular dynamics (FFMD). In the latter, energy and nuclear forces are calculated at each time step via a force field function. This method is very efficient numerically and can be used to perform molecular dynamics simulation in large systems, but it requires the design and parametrization of a specific force field describing the interactions between the molecular components of the system. On the other hand, FPMD provides an alternative route by computing on the fly the forces acting on the atoms using an explicit description of the electrons via quantum chemistry methods (e.q. DFT). [15] FPMD simulations are thus free of force field parametrization and have the further advantage of being able to directly describe chemical phenomena (e.g. bond breaking and forming); however they have a much higher computational cost than classical methods. In the context of modelling molten carbonate, FPMD simulations showed in particular that the solvation of CO_2 within $CaCO_3$ at geological conditions (T=1773 K and GPa pressure) leads to the formation of a transient species, the pyrocarbonate anion $C_2O_5^{2-}$. [9] This reactivity of CO_2 with the carbonate ions has consequences both on the solubility of CO_2 and on its transport properties; it could not have been observed in a force field-based simulation. FPMD simulations can also be used in combination with FFMD simulations by building new force fields based on the data obtained during the FPMD simulation, and then rely on the efficiency of FFMD to study large systems. This strategy has been successfully applied to the description of alkaline-earth molten carbonates and molten carbonates of lithium, sodium and potassium[10, 13, 14], for instance in order to predict the equation of state

of liquid $CaCO_3$, its viscosity and its conductivity[8] in good agreement with available experiments[16]. However, these first-principles based FFMD do not allow to study the reactivity and the formation/disproportionation of the transient pyrocarbonate anion in $CaCO_3$, underlining the necessity to use FPMD to model the solvation of potentially reactive species such as CO_2 or CO in molten carbonates.

We present here a FPMD study of the solvation of species involved during the CO₂ reduction process in the eutectic (62 % :38 %) LiKCO₃. Among the different melts presently under investigation to operate in a MCEC, we decided to look specifically at the solvation properties in the eutectic (62 % 38 %) LiKCO₃ (simply denoted LiKCO₃ in the following). This binary mixture has a lower eutectic temperature (T = 761 K) than its other alkali-carbonates counterparts (T = 771 K for 42.7 % 57.3 % LiKCO₃, T = 774 K for 52 % 48 % LiNaCO₃ and T = 983 K for 56 % 44 % NaKCO₃). The first species are CO₂ itself and the corresponding pyrocabonate ion $C_2O_5^{2-}$. Next, we study the end product of the reaction, *i.e.* CO. It has been proposed in cyclic voltametry experiments that CO can also react with CO_3^{2-} to form the oxalate anion according to[7]

$$CO + CO_3^{2-} \leftrightarrow C_2 O_4^{2-}.$$
 (1)

The oxidation number of carbon in oxalate is +III, which can then be seen as an intermediate species that can disproportionate into CO and $\text{CO}_3^{2^-}$. Finally, a crucial parameter in the efficiency of MCFC and MCEC is the oxoacidity of the melt, which can be tuned through the cation composition. Oxoacidity is characterized by the dissociation constant $K_{\rm D}$ of $\text{CO}_3^{2^-}$:

$$\operatorname{CO}_3^{2-} \leftrightarrow \operatorname{CO}_2 + \operatorname{O}^{2-}.$$
 (2)

We therefore studied in detail the solvation of O^{2-} in the eutectic LiKCO₃.

The paper is organized as follows. In section 2 we present the FPMD setup used in this study. Then we present results in section 3, first discussing the reactivity of CO_2 with CO_3^{2-} in section 3.1, then solvation structures in section 3.2 and finally dynamics in section 3.3. We then conclude in section 4.

2. Methods

We studied four different systems, each one consisting of a single molecule or anion (CO₂, C₂O₄²⁻, CO or O²⁻) solvated in the eutectic (62 % 38 %) LiKCO₃ at T = 1000 K and P = 1 atm, *i.e.* close to the operating conditions of MCFC/MCEC. In these conditions, the experimental density of molten carbonate is $\rho = 1.88$ g.cm⁻³ [17] and we thus placed one solvated species (CO₂, C₂O₄²⁻, CO or O²⁻), 158 lithium atoms (159 for the system that contains O²⁻) , 96 potassium atoms (97 in the case of O²⁻) and 127 CO₃²⁻ (126 in the case of C₂O₄²⁻) in a cubic box of size a = 22.23 Å. Periodic boudary condition are applied in all directions. The initial positions of the atoms were obtained from a classical molecular dynamics simulation of pure LiKCO₃ (with a force field developped previously in our lab [10]), from which one CO_3^{2-} anion (two CO_3^{2-} anions in the case of $C_2O_4^{2-}$) is removed and replaced by the solvated species (CO₂, $C_2O_4^{2-}$, CO or O²⁻).

The molecular dynamics (MD) simulations were run in the NVT ensemble, using a velocity-Verlet integrator (with a timestep $\Delta t = 0.5$ fs) and a canonical sampling/velocity rescaling (CSVR) thermostat [18] (with $\tau_{\text{CSVR}} = 1$ ps). The length of trajectories for CO₂, C₂O₄²⁻, CO, O²⁻ is 89 ps, 60 ps, 41 ps and 43 ps, respectively. Positions of all atoms are stored at every time step for analysis.

As we aim to study the reactivity and stability of the different solvated molecules in the molten carbonate, we opted for first-principles molecular dynamics where energies and forces are calculated at each time step at a DFT level. We used the software CP2K that employs a hybrid Gaussian planewave method (GPW). [19, 20, 21] To reduce the number of explicit electrons, core electrons were replaced by Goedecker-Teter-Hutter (GTH) norm-conserving pseudo-potentials. [22, 23, 24] The remaining valence electrons were projected into a double-zeta valence plus polarisation (DZVP) basis set optimized for molecules for each atom type (C, O, Li and K). [25] A cutoff of 700 Ry was used for the electronic density. We chose the BLYP functional to determine the exchange-correlation interactions [26, 27] and the DFT-D3 scheme with a cut-off of 40 Å for the dispersive interactions. [28]

We complemented these simulations with four gas phase simulations of the species CO_2 , $C_2O_5^{2-}$, $C_2O_4^{2-}$ and CO at T = 1000 K. Each of these gas phase simulations consisted of one molecule in a cubic box of size a = 22.23 Å with periodic boundary conditions, and was run for 20 ps. All parameters for the gas phase simulations (integrator, thermostat, DFT calculations, basis set and pseudopotentials) are the same as for the liquid-phase simulations.

3. Results

3.1. Reactivity

We first investigate the stability and the potential reactivity of CO_2 , $C_2O_5^{2-}$, $C_2O_4^{2-}$, CO, and O^{2-} when they are present in the molten carbonate medium. Different reactions involving these molecules have been suggested in the literature based on indirect experimental evidence (*e.g.* the presence of peaks in cylic voltammetry experiments [7]), in particular the following reactions with the carbonate anion:

$$CO_2 + CO_3^{2-} \to C_2O_5^{2-}$$
, (3)

$$\mathrm{CO} + \mathrm{CO}_3^{2-} \to \mathrm{C}_2\mathrm{O}_4^{2-} , \qquad (4)$$

$$CO_3^{2-} \to O^{2-} + CO_2$$
. (5)

We thus wanted to determine wether such reactions occur in our firstprinciples MD simulations, but molecules are not intrinsically defined in this kind of simulations. Among different possible criteria to define the molecules from first-principles MD trajectories (*i.e.* the position of all atoms at a given time), we decided to rely on a simple hysteresis geometrical criterion: a pair of atoms (C-O or C-C) are connected at time t if their interatomic distance is below 1.7 Å or if they were connected at the previous timestep $t - \Delta t$ and their interatomic distance is still below 1.9 Å. These criteria mean that a bond can form only when the interatomic distance is below 1.7 Å and can break only when the interatomic distance becomes larger than 1.9 Å. The 1.7 Å/1.9 Å values were chosen because the radial distribution function of the C-O pair in the bulk $LiKCO_3$ is close to zero between those distances. [10] The hysteris approach allows a smoother behaviour than using only a single criterion and were inspired by the criteria used to define hydrogen bonds in water. [29] Based on these criteria, we built at each time step a $N_{\text{atoms}} \times N_{\text{atoms}}$ connectivity matrix $\mathbb{C}(t)$, with $\mathbb{C}_{ij}(t) = 1$ if atoms i and j are connected at time t and $\mathbb{C}_{ij}(t) = 0$ otherwise. We then determined the connected components of connectivity matrix $\mathbb{C}(t)$, each of these connected components is a molecule present at time t.

By applying this molecule-search analysis to the four MD trajectories, we found that: (i) the CO₂ molecule reacts with a carbonate to form a pyrocarbonate anion $C_2O_5^{2-}$ (a detailed analysis of this reaction will be given in the next paragraph), (ii) the carbon monoxide CO does not react with carbonate anions to form an oxalate during the 41 ps simulation, while the oxalate $C_2O_4^{2-}$ does not dissociate into CO and CO_3^{2-} during the 60 ps of simulation, and (iii) similarly, none of the 507 CO_3^{2-} dissociates into O^{2-} and CO_2 among the 233 ps accumulated from the four simulations, while the anion O^{2-} remains stable for 41 ps of simulation. The stability of these different solvated species will allow us to present their intra- and intermolecular structure and their dynamical properties in section 3.2 and 3.3, respectively.

The formation of $C_2O_5^{2-}$ was already observed in CaCO₃ at geological condition (high pressure and high temperature T = 1773 K), [9] but the present work shows that such a reactivity exists also in the milder conditions of an operating MCFC or MCEC (atmospheric pressure, intermediate temperature T = 1000 K). Fig. 1(a) illustrates the presence of $C_2O_5^{2-}$ in the eutectic LiKCO₃. The kinetics of the formation/dissociation equilibrium of the pyrocarbonate anion affect the diffusion and the electrochemical properties of CO₂ solvated in this molten carbonate and the process of MCFC and MCEC. From the MD trajectory, we quantified the stability of $C_2O_5^{2-}$ and Fig. 1(b) shows the cumulative lifetime distribution of both CO_2 and $C_2O_5^{2-}$. The lifetime of the transient $C_2O_5^{2-}$ is at maximum half an order of magnitude shorter than that of CO_2 (2.5 ps vs 12 ps). To extract the characteristic lifetime, both distributions were fitted with an exponential function and we obtained $\tau_{\rm CO_2} = 2.3$ ps and $\tau_{C_2 O_{\epsilon}^{2-}} = 0.6$ ps. These lifetimes are of the same order of magnitude as the one calculated in the geological CaCO₃ (0.88 ps for CO₂ and 0.38 ps for $C_2O_5^{2-}$), but the slower kinetics are consistent with the lower temperature. On average, the pyrocarbonate is present about $f_{C_2O_{\pi}^{2-}} = 19$ % of the time, which means that, even as a transient species, it impacts quantitatively the thermodynamics of the solvated CO_2 (e.g. its solubility and its redox potential). From the fraction of time of presence of the pyrocarbonate $f_{C_2O_5^{2-}}$, we estimated the free enthalpy of its formation (eq. 3), $\Delta G = RT \ln(1 - f_{C_2O_5^{2-}}) / f_{C_2O_5^{2-}} = 12 \text{ kJ.mol}^{-1}$. The fraction of time of presence and the free enthalpy of formation are similar as in CaCO₃ at 1773 K: 0.24 % and 16.8 kJ.mol⁻¹, respectively. We also estimated the enthalpy of formation by considering the difference of average potential energy in presence of pyrocarbonate and in presence of CO_2 , $\Delta H = \langle U \rangle_{C_2O_5^{2^-}} - \langle \widetilde{U} \rangle_{CO_2} = 45 \text{ kJ.mol}^{-1}, \text{ where the bracket } \langle \cdot \rangle_I \text{ indicates an } V = 0.02,$ average over configurations where the species I is present. The reaction (3) is thus endothermic, meaning the fraction of pyrocarbonate will increase at higher temperature. The entropy of formation, $\Delta S = (\Delta H - \Delta G)/T = 33 \text{ J.mol}^{-1}$, is positive, which indicates the formation of pyrocarbonate is entropically favoured. This latter observation seems counterintuitive as the reaction 3 reduced the number of molecules from 2 to 1, *i.e.* a decrease in the translational entropy. In section 3.2.1 and 3.2.2, we will analyse the solvation of CO_2 and $C_2O_5^{2-}$ and show that the solvation structure of the latter is more disordered, which may explain the positive entropy of formation.

3.2. Intramolecular and Intermolecular Structure

We now explore the interactions between the solvated species and the molten carbonate, in particular to understand their differences in stability and reactivity. We consider the intramolecular structure (distances, angles and dihedral angles) as well as the intermolecular solvation structures.

3.2.1. Carbon dioxide

We first focus on the properties of CO_2 , the key molecule in the redox processes occurring within MCFC and MCEC. From the first-principles MD simulations of CO_2 solvated in LiKCO₃ and CO_2 in the gas phase, we extracted the geometrical properties that characterized the CO_2 molecule: the CO distance and the \overrightarrow{OCO} angle. Table 1 gathers the average value and the standard deviation obtained in both phases at T = 1000 K. The average CO distance and standard deviation are identical in LiKCO₃ and in gas phase (1.18 Å and 0.03 Å, respectively). If the average and standard deviation of the \overrightarrow{OCO} angle are also similar for CO_2 solvated in LiKCO₃ and in the gas phase, the full distribution (shown in Fig. 2(b)) are markedly different between the two phases.

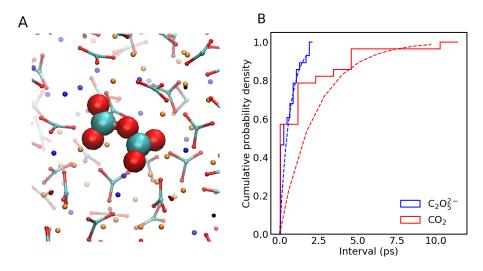


Figure 1: Formation/dissociation of pyrocarbonate $C_2O_5^{2-}$. (a) Snapshot of $C_2O_5^{2-}$ formed in the eutectic LiKCO₃. Carbonate molecules in the solvent are represented by cyan/red sticks, O atoms by red spheres, K atoms in blue and Li atoms in orange. (b) Cumulative lifetime distribution of CO_2 and of $C_2O_5^{2-}$ and exponential fit of these distributions (dashed lines).

properties (distance and angle) extracted from the MD simulations.						
Molecule	Geometrical	in LiKCO ₃		in gas phase		
	properties	Mean	Standard	Mean	Standard	
			deviation		deviation	
CO_2	$d_{\rm CO}$ (Å)	1.18	0.03	1.18	0.03	
	$\widehat{\text{OCO}}$ (°)	167.0	7.9	170.3	5.8	
$C_2O_5^{2-}$	$d_{\rm CO}$ (Å)	1.26	0.05	1.27	0.04	
	$d_{\rm CC}$ (Å)	2.56	0.13	2.65	0.11	
	$d_{\rm CO^*}$ (Å)	1.49	0.11	1.51	0.09	
	$\widehat{\text{OCO}}$ (°)	130.1	6.6	129.8	4.7	
	$\widehat{\mathrm{OCO}^*}$ (°)	114.5	6.3	114.7	5.7	
	$\widehat{\mathrm{CO}^*\mathrm{C}}$ (°)	119.2	8.7	123.4	6.8	
$C_2O_4^{2-}$	$d_{\rm CO}$ (Å)	1.28	0.05	1.29	0.04	
	$d_{\rm CC}$ (Å)	1.57	0.08	1.65	0.09	
	\widehat{OCO} (°)	125.4	5.1	125.3	5.1	
	\widehat{OCC} (°)	116.8	6.0	117.1	5.9	
CO	$d_{\rm CO}$ (Å)	1.16	0.06	1.15	0.02	

Table 1: Geometry of the different molecules in the eutectic LiKCO₃ and in the gas phase at T = 1000 K. Mean and standard deviation are obtained from the distribution of the geometrical properties (distance and angle) extracted from the MD simulations.

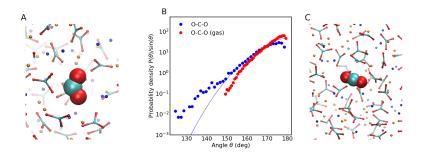


Figure 2: Intramolecular properties of CO₂ molecule. (a,c) Snapshots of CO₂ solvated in LiKCO₃ illustrating (a) a bended configuration ($\widehat{OCO} = 124.4^{\circ}$) and (c) a linear configuration ($\widehat{OCO} = 179.9^{\circ}$). (b) Distribution of O-C-O angle of the CO₂ molecule solvated in the eutectic LiKCO₃ at 1000 K and in the gas phase. For the solvated molecule, angles are measured during the time intervals of existence of CO₂. The distribution is normalized by dividing by sin θ . Gaussian fits of the form exp ($A(\theta - 180)^2 + B$) are shown as blue and red solid lines for the solvated molecule and gas phase cases. Values of the fitted parameters: A = -0.0045, B = 3.33 (solvated molecule) and A = -0.0067, B = 3.81 (gas phase).

The distribution of CO_2 solvated in LiKCO₃ is broader than for a gas phase CO_2 molecule, with a long-tail ($OCO < 140^\circ$) that displays an exponentiallike decay, while the full distribution in the gas phase coincides almost with a Gaussian curve. Fig. 2(a) illustrates a bended configuration of CO₂ solvated in LiKCO₃ while Fig. 2(c) shows a perfectly linear configuration of CO₂. If we had previously noticed a broader distribution of OCO in the case of a CO_2 molecule solvated in $CaCO_3$ at T = 1773 K compared to the gas phase distribution at the same temperature, the OCO distribution in CaCO₃ coincides however with a Gaussian curve, even at small angles ($OCO < 140^{\circ}$). In both LiKCO₃ and $CaCO_3$, these large OCO distributions indicate that the CO_2 molecules can bend up to 120°, facilitating the formation of the pyrocarbonate. The larger distribution in $LiKCO_3$ implies the CO_2 bending is more likely in this molten carbonate rather than in $CaCO_3$, but the difference of temperature between the two systems (1000 K in LiKCO₃ and 1773 K in $CaCO_3$) prevents us from discussing further the (small) difference of lifetime of CO_2 (2.3 ps in LiKCO₃) and 0.88 ps in $CaCO_3$).

To understand better the formation of the pyrocarbonate, we explored the solvation structure around CO_2 and its specific interactions with the different ions of the melt. Fig. 3 displays the radial distribution function (RDF) between (a) the carbon atom (C_{CO_2}) and (b) the oxygen atoms (O_{CO_2}) and all the solvent atoms (K, Li and C and O atoms of the carbonate, denoted respectively C_{carb} and O_{carb}). The potassium cations show the strongest affinity with the CO_2 molecule, with a clear intermolecular structure characterized by two peaks, at 4 Å and 6.5 Å for C_{CO_2} and 3.5 Å and 7 Å for O_{CO_2} . The situation is notably different for the lithium cations, for which we observed no peaks in the RDF with C_{CO_2} or O_{CO_2} , meaning that no specific interaction exists between

 $\rm CO_2$ and lithium. This absence of interaction may be explained by the competition with the strong lithium-carbonate interactions. The latter is revealed in the RDFs for C_{carb}-Li and O_{carb}-Li pairs shown in the Fig. 4 of Ref. [10]. The O_{carb}-Li RDF displays in particular a very strong peak at 2.5 Å. The neutral CO₂ molecule cannot interact strongly enough with Li⁺ to counteract the $\rm CO_3^{2^-}-Li^+$ interaction and Li does not form a solvation structure around CO₂.

The RDFs give only access to isotropic information and therefore neglect the particular orientation of the CO₂ with respect to the carbonate, potassium and lithium ions. To better highlight the three-dimensional solvation structure of CO₂, we built two-dimensional histograms of the probability of the presence of the solvent atoms (C_{carb}, O_{carb}, Li and K) around CO₂ in a cylindrical $\rho - \zeta$ coordinate system, where ζ is the projection of an atom position along the O_{CO2}-O_{CO2} axis and ρ the distance from the O_{CO2}-O_{CO2} axis. The origin of the the cylindrical coordinate system is chosen to be the mid-point of the O_{CO2}-O_{CO2} vector, *i.e.* close to the average position of C_{CO2}. Fig. 4(a-d) shows these two-dimensional histograms for C_{carb}, O_{carb}, Li and K atoms, respectively.

Fig. 4(a-b) reveals a preferential orientation of CO_3^{2-} with respect to CO_2 . The highest probability of presence is observed in the region $3 < \rho < 4$ Å and $-1 < \zeta < 1$ Å for C_{carb} and in the region 2.5 $< \rho < 3.5$ Å and $-0.5 < \zeta <$ 0.5 Å for O_{carb} . The solvation of the CO_2 molecule by the carbonate anion is thus characterized by a T-shaped structure formed by the CO_2 molecule and one CO bond of the carbonate. Such a preferential orientation was previously observed for CO_2 solvated in the molten $CaCO_3$ and participates to the formation of the pyrocarbonate. The solvation structure of K^+ around CO_2 is also anisotropic, as shown in Fig. 4(d). The presence of K^+ is the highest within two regions, which are symmetrical with respect to the $\zeta = 0$ axis, which have the shape of an arc of circle with center C_{CO_2} and a radius of 4 Å (that corresponds to the first peak in the RDF between K and C_{CO_2}) and which extend between the angles 46° and 65° with respect to the $\zeta = 0$ axis (maximum around 56°). The potassium cation positions preferentially between the carbon and the oxygen atoms and close to the CO_2 molecule. The two-dimensional histogram has thus permitted to analyse in details the first peak of the $K-C_{CO_2}$ RDF. Such a double-arc structure in-between C and O atoms was also observed in the case of the probability of presence of Ca atoms around CO₂ in CaCO₃, which indicates that K^+ and Ca^{2+} play similar role in the solvation of CO_2 . On the other hand, the lithium solvation structure (displayed in Fig. 4(c)) does not show any preferred positions for lithium around CO_2 , which confirms the previous analysis of the $\text{Li-C}_{\text{CO}_2}$ RDF and corroborates the absence of specific Li-CO₂ interaction, probably due to the strong $Li^+-CO_3^{2-}$ interaction. The observation of the different solvation structures formed by Li and K around CO_2 is a major step to understand the role of the molten carbonate composition in the solubility or diffusivity of CO_2 .

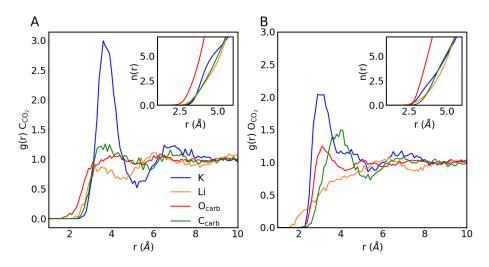


Figure 3: Radial distribution function (RDF) around the (a) oxygen atom of CO₂ molecule O_{CO_2} and (b) carbon atom of CO₂ molecule C_{CO_2} . Intermolecular distances are measured during the time of existence of CO₂ as a molecular species. Insets: coordination number n(r) obtained from the integration of the radial distribution functions. The same color code applies for figures (a) and (b).

3.2.2. Pyrocarbonate anion, $C_2 O_5^{2-}$

We will now consider the structure and the solvation of the unusual pyrocarbonate ation formed by reaction between the solvated CO_2 molecule and a carbonate CO_3^{2-} of the solvent. We first calculated the average and standard deviation of the intramolecular distances, both for a pyrocarbonate solvated within the molten carbonate and in the gas phase. The central oxygen atom of $C_2O_5^{2-}$ will be labelled O^{*} while the four external oxygens and the two carbons will be labelled O and C. Table 1 gathers these distances, that follow on average the trend $\langle d_{\rm CO} \rangle < \langle d_{\rm CO^*} \rangle < \langle d_{\rm CC} \rangle$ and whose standard deviations due to thermal fluctuations are relatively low (between 4 % and 7 %). The distances $d_{\rm CO}$ and $d_{\rm CO^*}$ are almost identical between the solvated pyrocarbonate and the gas phase pyrocarbonate (with difference in average value or standard deviation < 0.02 Å), while $\langle d_{\rm CO} \rangle$ is slightly longer in gas phase, with an increase of 0.09 Å compared to the solvated anion. The average intramolecular distances of the pyrocarbonate in $LiKCO_3$ are also similar to the one in $CaCO_3$, whose average value are 1.26 Å, 1.43 Å and 2.53 Å for $d_{\rm CO}$, $d_{\rm CO^*}$ and $d_{\rm CC}$, respectively. Table 1 also displays the average and standard deviation of the three intramolecular angles of the pyrocarbonate. Like for the distances, the thermal fluctuations are of the order of 5 % to 7 %, the average values are equivalent between the solvated and the gas phase molecule (with the maximum difference for CO^*C at 4.2°). They are also very close between pyrocarbonate ion solvated in LiKCO₃ and ion solvated in CaCO₃ (with the maximum difference for $\overline{CO^*C}$ at 4.0°). Finally, we conclude the analysis of the geometry of $C_2O_5^{2-}$ by looking

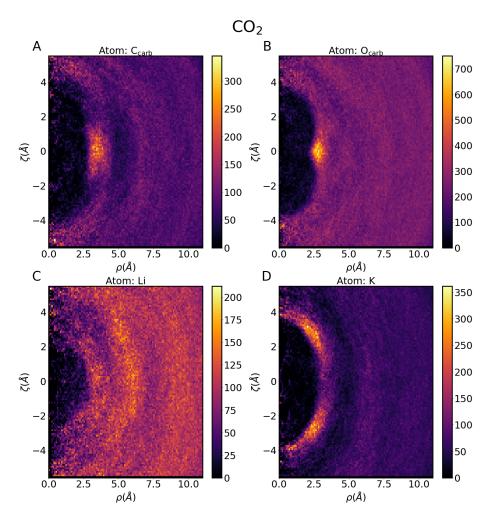


Figure 4: Solvation structure around the CO₂ molecule. Two dimensional colour charts representing the probability of the presence of the following atoms around CO₂: C_{carb} atom (a); O_{carb} atom (b): Li atom (c) and K atom (d). CO₂ is oriented with its O_{CO2}-O_{CO2} axis along the $\hat{\zeta}$ direction, where $\zeta = 0$ is the mid-point of the O-O distance. ζ is thus the projection of an atom position along the O_{CO2}-O_{CO2} axis, and ρ its distance from the O_{CO2}-O_{CO2} axis.

at the dihedral angle OCO^{*}C. Fig. 5 displays the distributions of OCO^{*}C for the solvated and gas phase pyrocarbonate. Both distributions peak around 0° and 180° which indicates the pyrocarbonate forms preferentially a planar structure. The probability to observe other angles is however far from negligible: the smallest probability is found for dihedral angles of \pm 90° and is only half of the highest probability (planar structure). C₂O₅²⁻ is therefore flexible and it alternates planar and twisted structures.

To understand the formation and relative stability of this transient species, we analyse here its solvation structure. We start with the RDF (shown in Fig. 6(a-c)), between the three types atoms of $C_2O_5^{2-}$ (C_{pyro} , O_{pyro} and O_{pyro}^* , respectively) and the four solvent atoms (C_{carb}, O_{carb}, Li and K). The RDFs reveal a different structure of solvation compared to the $\rm CO_2$ molecule: the closest peak (*i.e.* intramolecular distance) occur now with Li for all atoms in pyrocarbonate, with distances of 3 Å and 2 Å for C_{pyro} and O_{pyro} respectively. But except for these peaks, the lithium solvation does not present a medium-range structure (RDF close to 1 after 5 Å). The RDFs K-C_{pyro} and K-O_{pyro} are characterized by a double-peak structure, more pronounced for C_{pyro}, a behaviour similar to the one observed around CO_2 . The RDFs between the carbonate atoms and C_{pyro} and O_{pyro} displays almost no solvation-induced structuration, with a small peak (RDF close to 1.3) between C_{carb} and C_{pyro} and O_{pyro} at 4 Å and 6 Å respectively, while no peaks occur for C_{carb} . We conclude the discussion of the RDFs by noting that O^*_{pyro} is embedded with the pyrocarbonate molecule and less reachable: its RDFs with solvent atoms (see Fig. 6(c)) does not present any marked solvation structure (except a broad peak for potassium).

As explained in the case of CO_2 , the RDFs only provide isotropic information and we therefore calculated the two-dimensional cylindrical-based histograms to characterize the solvation structure and elucidate the peaks observed in the RDFs with respect to Li and K. Fig. 6(d-e) displays the cylindrical-coordinate density of probability of presence of solvent atoms surrounding the pyrocarbonate. ζ is now the projection along the C_{pyro}-C_{pyro} axis, ρ the distance with this axis and the origin is the midpoint between C_{pyro} atoms. To account for the disymmetry that might be induced by the formation of pyorcarbonate from the reaction between CO_2 and CO_3^{2-} , we always placed the C from the former CO_2 in the region $\zeta < 0$. Fig. 6(c) shows that the lithium atoms surround almost homogeneously the pyrocarbonate, with a slightly higher density of probability in the plane perpendicular to the pyrocarbonate (*i.e.* in the region $\zeta = 0$, $\rho = 3$ Å), which means the peak in RDF between lithium and pyrocarbonate does not split into different preferential positions. The same analysis holds for the probability of presence of K^+ (shown in Fig. 6(d) which also surround homogeneously the pyrocarbonate but with a higher probability of presence both in the perpendicular plane but also in the C_{pyro} - C_{pyro} axis ($\rho = 0$ Å, $\zeta = \pm 4$ Å). We note that such homogeneous surrounding was also observed for the presence of calcium atoms around the pyrocarbonate formed in $CaCO_3$, which again underlines the similar role played by K^+ and Ca^{2+} in the solvation of CO_2 and

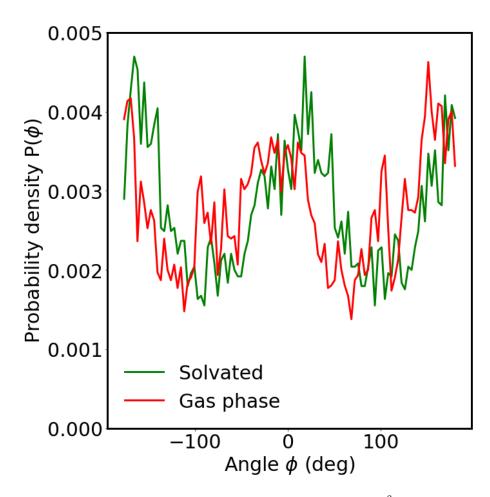


Figure 5: Distribution of O-C-O^{*}-C dihedral angle of pyrocarbonate $C_2O_5^{2-}$ solvated in the eutectic LiKCO₃ at 1000 K and in the gas phase. For the solvated molecule, the dihedral angle is measured during the time intervals of existence of $C_2O_5^{2-}$.

 $C_2O_5^{2-}$.

The cylindrical-coordinate density of probability reveals the key difference of the solvation structure around CO_2 and around $C_2O_5^{2-}$: (i) Li⁺ rarely approach close to CO_2 while it solvates $C_2O_5^{2-}$ homogeneously at 3 Å, and (ii) K⁺ solvates CO_2 anisotropically while it surrounds $C_2O_5^{2-}$ homogeneously. The difference of solvation of Li⁺ may be related to the difference of charges of these molecules $(q_{CO_2} = 0, q_{pyro} = -2), C_2O_5^{2-}$ can compete with CO_3^{2-} to interact with the lithium cation, leading to that stronger solvation than between CO_2 and Li. The potassium plays a role in the solvation of both CO_2 and $C_2O_5^{2-}$, but it displays a more disorder structure around $C_2O_5^{2-}$. This result may contribute to the positive sign of the entropy of formation discussed in section 3.1. When the pyrocarbonate anion is formed, the anisotropic solvation structure of K⁺ around CO_2 disappears, leading to a increase of entropy.

3.2.3. Oxalate anion, $C_2 O_4^{2-}$

Besides CO₂ and pyrocarbonate, the oxalate anion $C_2O_4^{2-}$ may also play a role in the electrochemical properties of MCFC and MCEC. The formation of this species can occur via the reaction between CO and CO_3^{2-} (eq. 4), though we did not directly observe this reaction in the system containing a CO molecule or the inverse reaction in the system containing $C_2O_4^{2-}$ (see the discussion on stability in section 3.1). From the 60 ps MD trajectory containing the stable $C_2O_4^{2-}$ solvated in LiKCO₃, we extracted the intramolecular and solvation structure, in particular to understand its relative stability in comparison with the pyrocarbonate.

The oxalate intramolecular geometry is characterized by two distances ($d_{\rm CC}$ and $d_{\rm CO}$), two angles (OCC and OCO) whose average values and standard deviations in both molten carbonate and gas phase are presented in Table 1. The shortest distance is $d_{\rm CO}$, with an average value (1.28 Å) close to that of pyrocarbonate (1.26 Å) but 8 % longer than in CO_2 (1.18 Å). Similarly to what we observed for CO_2 and the pyrocarbonate anion, the thermal fluctuations for the distances and the angles are small (about 5 %) and solvated oxalate and gas phase oxalate ions have almost identical structure (only the CC distance is 5 %higher in gas phase). Finally, Fig. 7(a) shows the distribution of the dihedral angle OCCO for both the solvated molecule and the gas phase. The maxima of distribution are situated at $\pm 100^{\circ}$, indicating the oxalate is preferentially twisted (as illustrated in Fig. 7(b)). Similarly to what was observed for pyrocarbonate, the distribution of dihedral angles is widely spread, the minimum is found at 0° , with a probability only half of the maximal value. Like the pyrocarbonate ion, the oxalate anion is flexible and alternates twisted and planar structures when solvated in molten carbonate.

The solvation structure of the oxalate is characterized by the RDF (Fig.8(ab)) and the cylindrical density of probability (Fig. 8(c-d)). The analysis of

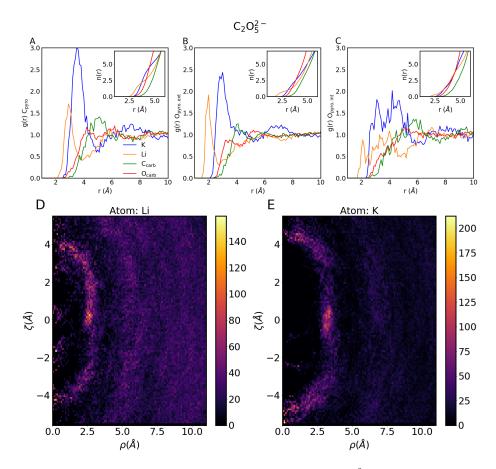


Figure 6: Solvation structure around the pyrocarbonate anion $C_2O_5^{2-}$. Upper panel: radial distribution function (RDF) for (a) carbon atom (b) external oxygen atoms and (c) internal oxygen atom of $C_2O_5^{2-}$. Insets: coordination number n(r) obtained from the integration of the radial distribution functions. The same color code applies for figures (a), (b) and (c). Lower panel: two dimensional colour charts representing the probability of the presence of the following atoms around $C_2O_5^{2-}$: Li atom (d) and K atom (e). $C_2O_5^{2-}$ is oriented with its $C_{pyro}-C_{pyro}$ axis along the $\hat{\zeta}$ direction, where $\zeta = 0$ is the mid-point of the $C_{pyro}-C_{pyro}$ distance. ζ is thus the projection of an atom position along the $C_{pyro}-C_{pyro}$ axis, and ρ its distance from the $C_{pyro}-C_{pyro}$ axis. The C of the former CO₂ molecule is always placed in the negative ζ portion of the plots.

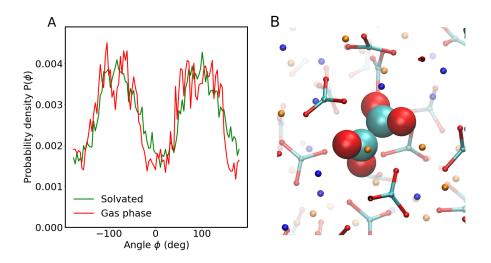


Figure 7: (a) Distribution of O-C-C-O dihedral angle of oxalate $C_2O_4^{2-}$ solvated in the eutectic LiKCO3 at 1000K and in gas phase. (b) Snapshot of $C_2O_4^{2-}$ in the eutectic LiKCO3. Carbonate molecules in the solvent are represented by cyan/red sticks, O atoms by red spheres, K atoms in blue and Li atoms in orange.

RDFs between the atoms of the oxalate (O_{oxa} and C_{oxa}) and the solvent atoms reveal some similarity with the solvation structure of pyrocarbonate, both being anionic species: (i) the RDFs with lithium peak closer than the RDFs with potassium, with a larger Li- O_{oxa} RDF peak than K- C_{oxa} , while Li- C_{oxa} RDF peak is smaller than K- C_{oxa} RDF peak; (ii) the RDF K- C_{oxa} exhibits a two-peak structure; (iii) the RDFs with C_{carb} and O_{carb} display only a very slight structuration, though the RDF C_{carb} - C_{oxa} presents two distinct peaks at 5 Å and 9 Å.

Likewise, the cylindrical densities of probability of presence of Li and K (Fig. 8(c-d)) show some resemblance with the one of pyrocarbonate. Here the cylindrical coordinates are defined with respect to the C_{oxa} - C_{oxa} axis, with ζ the projection onto this axis, ρ the distance to that axis and the origin the midpoint of the C_{oxa} - C_{oxa} bond. Li and K atoms surround homogeneously the oxalate, with a higher density for lithium along the C_{oxa} - C_{oxa} and for potassium in the plane perpendicular to the C_{oxa} - C_{oxa} axis ($\zeta = 0$ Å) and along the C_{oxa} - C_{oxa} axis. This solvation structure, close to that of $C_2O_5^{2-}$, indicates the existence of different solvation patterns between charged species (pyrocarbonate, oxalate) and neutral species (CO₂). We will confirm this opposition by looking now into the solvated CO molecules and the oxygen anion O^{2-} .

3.2.4. Carbon monoxide

The production of carbon monoxide CO is one of the main objectives of molten carbonate electrolyser cells (MCEC) and we therefore present here the solvation properties of CO in the eutectic LiKCO₃. In particular, the stabil-

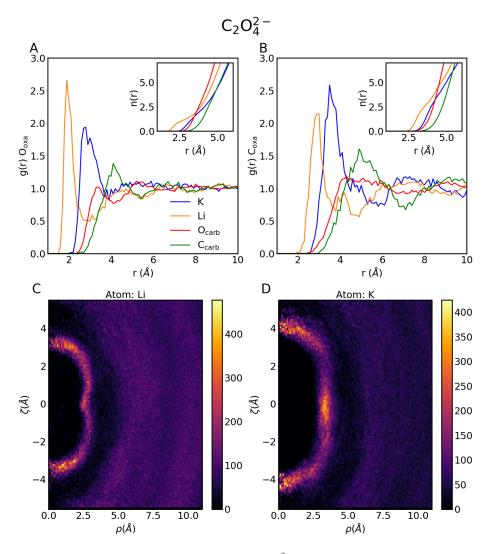


Figure 8: Solvation structure around the oxalate $C_2O_4^{2-}$ anion. Upper panel: radial distribution function (RDF) for (a) carbon atom of $C_2O_4^{2-}$ and (b) oxygen atom of $C_2O_4^{2-}$. Insets: coordination number n(r) obtained from the integration of the radial distribution functions. The same color code applies for figures (a) and (b). Lower panel: two dimensional colour charts representing the probability of the presence of the following atoms around $C_2O_4^{2-}$: Li atom (c) and K atom (d). $C_2O_4^{2-}$ is oriented with its C_{oxa} - C_{oxa} axis along the $\hat{\zeta}$ direction, where $\zeta = 0$ is the mid-point of the C_{oxa} - C_{oxa} distance. ζ is thus the projection of an atom position along the C_{oxa} - C_{oxa} axis, and ρ its distance from the C_{oxa} - C_{oxa} axis.

ity of CO discussed in section 3.1 will be analysed by comparing the solvation structures of CO and CO_2 . The dynamical properties, and in particular the diffusion, will be discussed in section 3.3.

From the 41 ps first-principles MD simulation, we measure the average C-O distance and standard deviation in both the molten carbonate and gas phase. The average CO distance is similar in molten carbonate and in gas phase and is the smallest C-O intramolecular distance among the different solvated molecules we investigated (it is 0.02, 0.10 and 0.12 Å smaller than C-O distance in CO_2 , pyrocarbonate and oxalate, respectively), as expected due to its triple-bond nature. The thermal fluctuations are of the order of 5 % in the molten carbonate and 3 % in the gas phase.

More interestingly, the solvation around CO is notable for its absence of marked structure. Fig. 9(a-b) shows the RDFs between the two atoms of CO (panel (a) for O_{CO} and panel (b) for C_{CO}) and the different solvent atoms. These RDFs present some similarity with the ones around CO_2 . First, the highest peak is between potassium and C_{CO} and panel O_{CO} at 3.5 Å and 4 Å, respectively, with a second smaller peak observed between C_{CO} and K at 6.5 Å. The first C_{CO} -K RDF peak reaches however a value of 2 for CO and 3 for CO₂, that indicates a weaker interaction in the case of CO. Secondly, the RDFs with Li reveal an absence of preferential CO-Li distance, similar to that was already noticed for CO_2 . Finally, the RDFs with the carbonate atoms show a slight solvation structure around O_{CO} : the RDF O_{carb} - O_{CO} peaks at 3.5 Å (with a value of 1.4), while the RDF O_{CO} - C_{carb} peaks at 4 Å (with a value of 1.5). As no peaks are observed for C_{CO} in Fig. 9(b), this shows that the carbonate anion surrounds preferentially the oxygen atom of CO, with one oxygen of CO_3^{2-} pointing toward O_{CO} . This specific interaction is explained by the positive charge carried by the O atom of CO (while C carries the opposite negative charge).

This particular dipole of CO also impacts the cylindrical-coordinate density of probability for Li and K displayed in Fig. 9(c(d). Here the ζ coordinate is the projection onto the C_{CO}-O_{CO} axis, ρ is the distance to that axis, and the origin of the referential is the midpoint of the C_{CO}-O_{CO} vector. The oxygen O_{CO} is placed in the $\zeta < 0$ portion of the plots. As seen in the RDF, the probability of presence of Li is more diffuse than the one of K, but both Li and K show their highest probability of presence in the vicinity of C_{CO}, along the C_{CO}-O_{CO} axis ($\rho = 0$ Å, $\zeta = 3$ Å), *i.e.* the cations of the molten carbonate position preferentially close to the negatively charged C_{CO}.

Overall, CO presents a similar solvation pattern to CO_2 with a strong solvation with K⁺ and an (almost) absence of solvation with Li⁺. The main differences are (i) the preferential position of Li⁺ close to C_{CO}, which is explained by the negatively charged carbon that can (slightly) compete with the Li⁺-CO₃²⁻ interaction, (ii) the absence of anisotropic potassium solvation structure around CO and (iii) the absence of preferential solvation of carbonate around CO.

3.2.5. Oxygen anion

We conclude our analysis of solvated species in the molten carbonate LiKCO₃ with the oxygen anion O^{2-} . O^{2-} may be involved in the electrochemical processes at the interface between molten carbonate and electrodes in MCFC or MCEC. Moreover, in that liquid melt, it also plays the important role of being the strongest oxo-base, an analogue of HO^- in water. The solvation structure of this mono-atomic species is simply characterized by the RDFs with the different solvent atoms, shown in Fig. 10(a). The Li^+-O^{2-} RDF displays the most notable feature, with a high peak at 2 Å (RDF reaches here a value of 17) followed by a minimum (RDF close to 0) at 3 Å. This peak induces a plateau is the coordination number n(r) between 2 and 3 Å at n(r) = 4, which means that O^{2-} forms a relatively stable solvation shell with four lithium atoms, as illustrated in Fig. 10(b). By looking at the MD ab-initio trajectory, we estimate that the exchange of Li⁺ (entrance in or exit of the solvation shell) occurs in the timescale of few picoseconds, meaning that OLi_4^{2+} is a transient species of electrochemical relevance, rather than the isolated O^{2-} anion. Besides the O^{2-} - Li^+ RDF peak, each RDF between O^{2-} and the other solvent atoms displays successively a much smaller peak (RDF is around 2) at 3, 3.5 and 4 Å for K, O_{carb} and C_{carb} , respectively.

3.3. Diffusion and Rotation

We now conclude the analysis of these solvated species in $LiKCO_3$ by investigating two dynamical properties: the translational diffusion in the liquid and the reorientation of these molecules.

The diffusion of these species within the molten carbonate medium —to and from the electrodes— is an essential step in the electrochemical processes of MCFC/MCEC, but the values of diffusion coefficient are often difficult to obtain experimentally. In MD simulations, the diffusion coefficient of a given molecule is obtained by taking the slope of the mean-square displacement (MSD) at long time, $D_I = \lim_{\tau\to\infty} \frac{1}{6} \frac{\mathrm{dMSD}_I(\tau)}{\mathrm{d}\tau}$, with $\mathrm{MSD}_I(\tau) = \langle |\mathbf{R}_I(\tau) - \mathbf{R}_I(0)|^2 \rangle$ and where $\mathbf{R}_I(t)$ is the center-of-mass of molecule I at time t and the bracket represents an average over time. We applied this MSD definition for $C_2O_4^{2-}$, CO, O^{2-} as well as the solvent molecules, but we must take a special care in the case of the reactive CO₂. We adapt the definition of the MSD to integrate the transient nature of CO₂ and the variable index of its constituent atoms,

$$\mathrm{MSD}_{\mathrm{CO}_{2}}(\tau) = \frac{\sum_{t=1}^{N_{\mathrm{steps}}} |\mathbf{R}(t+\tau) - \mathbf{R}(t)|^{2} \chi_{t} \chi_{t+\tau}}{\sum_{t=1}^{N_{\mathrm{steps}}} \chi_{t} \chi_{t+\tau}}$$
(6)

where the characteristic function $\chi_t = 1$ if CO₂ is present at time t and $\chi_t = 0$ otherwise. Fig. 11(a) shows the MSDs vs time for the four solvated species and the linear functions fitted on the MSDs to extract the diffusion coefficients. The latter are summarized in Table 2 together with the diffusion coefficient for the

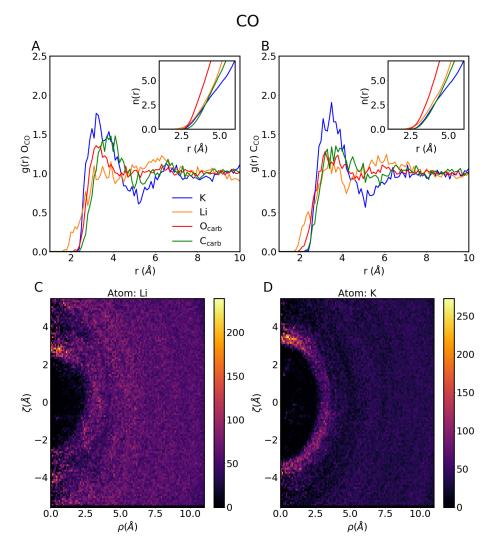


Figure 9: Solvation structure around the carbon monoxide CO. Upper panel: radial distribution function (RDF) for (a) carbon atom of CO and (b) oxygen atom of CO. Insets: coordination number n(r) obtained from the integration of the radial distribution functions. The same color code applies for figures (a) and (b). Lower panel: two dimensional colour charts representing the probability of the presence of the following atoms around CO: Li atom (c) and K atom (d). CO is oriented with its O_{CO} - C_{CO} axis along the $\hat{\zeta}$ direction, where $\zeta = 0$ is the mid-point of the O_{CO} - C_{CO} distance and O_{CO} is always placed in the negative ζ portion of the plots.

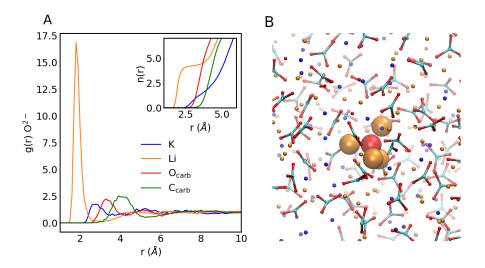


Figure 10: (a) Radial distribution function (RDF) for oxygen anion O^{2-} . Insets: coordination number n(r) obtained from the integration of the radial distribution functions. (b) Snapshot of O^{2-} in the eutectic LiKCO₃ surrounded by four Li⁺ cations. Carbonate molecules in the solvent are represented by cyan/red sticks, O atoms by red spheres, K atoms in blue and Li atoms in orange.

three ionic species that composed the solvent. The diffusion coefficient range from 0.5 to $4 \cdot 10^{-5}$ cm².s⁻¹, where the highest diffusion coefficient is found for CO. We explain this feature of CO by noting that CO is a neutral molecule, with a small electrostatic dipole ($p_{\rm CO} = 0.11$ D), a relatively small size and a near spherical shape. These features indicates that CO interacts only weakly with the surrounding molten carbonate and behaves probably similarly to a noble gas that can diffuse quickly in the liquid. The second highest diffusion coefficient is that of the CO_2 species. The MSD for CO_2 (eq. 6) takes into account its reactivity and the displacement induced by the successive formation and dissociation of pyrocarbonate. If CO_2 shares some similarity with CO (a neutral molecule with a small dipole moment), its interaction with the solvent is stronger, in particular with the carbonate anion CO_3^{2-} that forms a preferential "T-shaped" structure as discussed in section 3.2.1. The smallest diffusion coefficient is that of the oxygen anion O^{2-} (0.54·10⁻⁵ cm².s⁻¹). As described in section 3.2.5, this divalent anion strongly attracts four lithium ions to form a relatively stable OLi_4^{2+} complex that could explain its slow diffusivity due its larger size and bulkier nature. We also note that the diffusion coefficient of the solvent molecules are three times smaller than the one measured experimentally at 1100 K [30] $(3.52 \cdot 10^{-5} \text{ cm}^2 \text{ for } \text{CO}_3^{2-} \text{ and } 3.81 \cdot 10^{-5} \text{ cm}^2 \text{ for } \text{K}^+)$, but they correspond to the calculated diffusion coefficient from MD simulations in the 1100 K to 1200 K temperature range [31, 32, 10, 33] (0.55- $1.9 \cdot 10^{-5}$ cm², 2.55- $5.38 \cdot 10^{-5}$ cm² and $1.55 \cdot 4.99 \cdot 10^{-5}$ cm² for CO₃²⁻, Li⁺ and K⁺ respectively).

Table 2: Dynamical properties of the molecules solvated in the eutectic LiKCO₃. The diffusion coefficient is obtained from a linear fitting of the mean-square displacement, and the reorientation time from an exponential fitting of the time-correlation reorientation function (eq. 8).

(04.0).		
Molecule	Diffusion coefficient $(10^{-5} \text{cm}^2.\text{s}^{-1})$	Reorientation time (ps)
CO ₂	1.4	1.4
$C_2O_5^{2-}$		2.6
$\begin{array}{c} C_2 O_5^{2-} \\ C_2 O_4^{2-} \end{array}$	1.0	3.4
$\begin{array}{c} \text{CO} \\ \text{O}^{2-} \end{array}$	3.9	0.1
O^{2-}	0.54	—
CO_3^{2-}	0.69	1.3
$\begin{bmatrix} \mathrm{CO}_3^{2-} \\ \mathrm{Li}^+ \\ \mathrm{K}^+ \end{bmatrix}$	2.4	
K ⁺	1.4	—

We then analysed our simulations to obtain information on the reorientation of these species in the molten carbonate, a property that could be more easily measured experimentally and may bring information on their diffusion mechanism. We quantified the reorientation process in our MD simulations using the second-order reorientation time-correlation function,

$$C_2(t) = \langle P_2 \left[\mathbf{u}(t) \cdot \mathbf{u}(0) \right] \rangle \tag{7}$$

$$= \left\langle \frac{1}{2} \left(3 |\mathbf{u}(t) \cdot \mathbf{u}(0)|^2 - 1 \right) \right\rangle \tag{8}$$

where P_2 is the second-order Legendre polynomial and **u** is a normalized vector characterizing the orientation of the molecule (we choose the vector between O atoms for CO₂, between C atoms for $C_2O_5^{2-}$ and $C_2O_4^{2-}$ and between C and O atoms for CO). Fig. 11(b) shows the reorientation time-correlations $C_2(t)$ for the different solvated molecules, as well as an exponential-fitted decay (of the form $A \exp(-t/\tau_{\rm reor})$) of $C_2(t)$. The reorientation times obtained from the fit, $\tau_{\rm reor}$, are gathered in table 2 for the different solvated molecules and for the solvent anion CO_3^{2-} . Except for the particular case of CO molecule ($\tau_{\rm reor} = 0.1$ ps), the reorientation times range between 1.3 ps and 3.4 ps with the following order: $CO_3^{2-} < CO_2 < C_2O_4^{2-} < C_2O_5^{2-}$. The short reorientation time of the CO molecule indicates that it can freely rotate in the molten carbonate and confirms the observation made for the translational diffusion that CO only weakly interacts with the molten carbonate. In contract, the oxalate and pyrocarbonate anions are charged and relatively large molecules whose reorientation is about 30 times slower than CO.

4. Conclusion

We have investigated in this work the solvation properties of key molecules in the operation of MCFC/MCEC in the eutectic (62 % 38 %) LiKCO₃ using first-principles molecular dynamics. Similar to what happens in molten CaCO₃, we find that the solubilized CO₂ molecule spontaneously reacts with CO₃²⁻ to

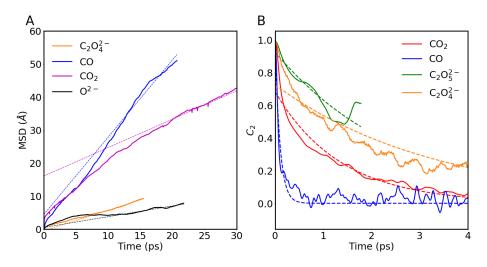


Figure 11: Dynamical properties of the solvated species. (a) Mean-square displacement (MSD) along time. The MSD are fitted to a linear function (dashed lines) to calculate the diffusion coefficient, see Table 2. The MSD for CO₂ molecule is calculated between times where the CO₂ molecule is present. (b) Reorientation time-correlation functions $C_2(t)$ (eq. 8). The $C_2(t)$ function are fitted to an exponential decay function to determine the reorientation time, see Table 2.

form the transient pyrocarbonate species $C_2O_5^{2-}$. The lifetime of the pyrocarbonate anion is however significantly longer in the eutectic LiKCO₃ than in CaCO₃, possibly because of the lower temperature. In contrast to $CO_2/C_2O_5^{2-}$, both CO and the oxalate anion, $C_2O_4^{2-}$, are found to be stable in the eutectic LiKCO₃. This confirms the oxalate anion as a putative intermediate in the reduction of CO₂. Its disproportionation reaction (or inversely its formation) is probably activated as it needs not only the breaking of the C-C bond but also the breaking and formation of a C-O bond. Such activated process are unlikely to be observed during the simulation times accessible to our first-principles simulations, and further studies are needed to describe the formation mechanism and thermodynamics of oxalate. Free energy methods could be employed in combination with first-principles molecular dynamics in order to measure these thermodynamics properties.

The study of the solvation structures highlights the different behaviour of K^+ and Li^+ in the molten carbonate medium. Because of its smaller size, Li^+ binds more strongly to charged species $(C_2O_5^{2-}, C_2O_4^{2-}, O^{2-} \text{ and } CO_3^{2-})$. O^{2-} forms in particular a complex with four Li^+ in tetrahedral configuration. K^+ is found preferentially around neutral molecules (CO₂ and CO). These contrasting behaviour regarding solvation between Li^+ and K^+ — and their effects on solubility and transport properties — may contribute to the choice of an optimal molten carbonate composition to operate an MCEC process.

Finally, we have estimated the diffusion coefficients of these solvated species, which are important parameters for the interpretation of experimental data and the modelling of MCEC operation. Of all the species studied, CO diffuses significantly faster consistently with its small size and poor interaction with the melt. In the future, we plan to compute other experimental observables allowing for a direct comparison with in situ experiments, such as Raman spectra or NMR chemical shifts. [34]

5. Acknowledgement

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