

Can We See the Energy Densities? II. Insights from Linear-Response Time-Dependent Density Functional Theory Calculations [†]

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Inspired by the analysis of Kohn-Sham energy densities by Nakai *et al*, we extended the energy density analysis to linear-response time-dependent density functional theory (LR-TDDFT) calculations. Using ethylene-tetrafluoroethylene and oxyluciferin–water complexes as examples, distinctive distribution patterns were demonstrated for the excitation energy densities of local excitations (within a molecular fragment) and charge-transfer excitations (between molecular fragments). It also provided a simple way to compute the effective energy of both hot carriers (particle and hole) from charge-transfer excitations via an integration of the excitation energy density over the donor and acceptor grid points.

1 Introduction

Wavefunction analysis has been a central component of electronic structure calculations, dating back to the dawn of modern quantum chemistry. To characterize the charge density distribution of electronic ground state, numerous population schemes were developed to extract atomic (or fragment) charges from the one-particle density matrix, the electronic density, or the total electrostatic potential.^[1-3] These include Mulliken partitioning,^[4] Löwdin partitioning,^[5,6] atoms-in-molecule partitioning,^[7,9] natural population analysis,^[10-12] electrostatic-potential-derived charges,^[13,22] Becke-weight-based partitioning,^[23] Hirshfeld partitioning,^[24-26] fragment-based Hirshfeld partitioning,^[27] iterative Hirshfeld partitioning,^[28-31] iterative Stockholder atoms partitioning,^[32-33] ex-

tended Hirshfeld partitioning,^[34] density derived electrostatic and chemical charges,^[35-39] charge models I through V,^[40-41] etc. Relatedly, Fukui functions (*i.e.* atomic population changes upon electron detachment/attachment)^[42-44] were also developed to gauge the site reactivity of organic compounds.

Most of these ground-state atomic population schemes can be readily extended to excited-state calculations to analyze the excited-state electron density, as well as the corresponding attachment, detachment, and transition densities.^[45-47] Furthermore, several metrics based on the excited-state wavefunction^[48-57] (especially the Λ value from Peach *et al*^[58]) were proposed to distinguish between different types of electronic excitations (*i.e.*, local, charge transfer, and Rydberg excitations) of molecular complexes or extended molecules. Recently, the exciton (*particle-hole* pair) concept from solid state physics perspective was also adopted by Dreuw *et al* to distinguish and characterize different excitation types and extract their relevant properties.^[59-60]

During an electron excitation, the molecular system not only undergoes a charge density distribution, which is described by the detachment (hole) and attachment (particle) densities,^[61] but also experiences a substantial increase in the total energy (*a.k.a.* the excitation energy). Conceptually, it is appealing to consider how the excitation energy is distributed within the molecule. Intuitively, we expect a map of the *excitation energy density* (*i.e.* a real-space distribution of the excitation energy) would show substantially increased energy density around the hole (because it requires energy to remove an electron from occupied orbitals) and possibly around the particle (if energy is needed to inject an electron into unoccupied orbitals). *An integration of the excitation energy density*

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around (well-separated) hole/particle will thus yield the effective energies of both the hole and particle. These effective energies could be quite valuable in the modeling of hole-particle pairs in photochemical processes, such as solar cells, light-emitting devices, plasmon-enhanced spectroscopy, and catalysis, etc.

In contrast to the much-developed charge density analysis, however, much less effort has been devoted to the grid-based energy distribution for electronic ground and excited states. As a matter of fact, the only work we are aware of in this direction is a grid-based atomic energy partitioning scheme by Nakai *et al*, who used it to decompose the total Kohn-Sham density functional theory (KS-DFT) energy into atomic and bond energy components.^{62,64} But it is rather straightforward to extend Nakai *et al*'s grid-based energy partitioning scheme to the analysis of the excitation energy distribution within the linear-response time-dependent density functional (LR-TDDFT) framework.^{65,69} Such an extension will be reported below in this article.

An interesting question here is: *is the excitation energy density uniquely defined?* Needless to say, the computed LR-TDDFT excitation energy density map of a molecular system would depend on the choices of the density functional, basis set, and numerical integration grid (for solving KS-DFT and LR-TDDFT equations and for evaluating the energy density). Given a combination of functional/basis/grid, however, only one component of the excitation energy density is found to be not uniquely defined within our formulation. It corresponds to the two-electron Hartree-Fock exchange energy (*i.e.* the electrostatic interaction between the hole-particle pair shown later in Eqs. 28 and 29), and we choose to split its contributions evenly between the hole and particle.

This article is organized as follows. In the next section, we will briefly review Nakai *et al*'s scheme for computing grid-based KS-DFT energy density, and then formulate our extension of this scheme for evaluating and partitioning LR-TDDFT excitation energy density. Results and discussions will be provided in Sections 3 and 4 for two model complexes (C₂H₄-C₂F₄ and OLH-H₂O). Concluding remarks will be presented in Section 5.

This article complements an accompanying report, where an analysis of energy densities from a real-time time-dependent density functional theory (RT-TDDFT) simulation⁷⁰ was presented.

2 Methods

In this work, all occupied Kohn-Sham orbitals (labeled as i and j), and virtual orbitals (labeled as a and b) are assumed to be all real. They are linear combinations of atom-centered Gaussian basis functions (labelled as μ , ν , λ , and σ),

$$\psi_i(\mathbf{r}) = \sum_{\mu} C_{\mu i} \phi_{\mu}(\mathbf{r}) \quad (1)$$

$$\psi_a(\mathbf{r}) = \sum_{\mu} C_{\mu a} \phi_{\mu}(\mathbf{r}) \quad (2)$$

with \mathbf{C}_o and \mathbf{C}_v collectively representing the respective molecular orbital coefficients. The ground-state one-particle density matrix is $\mathbf{P} = \mathbf{C}_o \mathbf{C}_o^{\dagger}$, namely

$$P^{\mu\nu} = \sum_i C_{\mu i} C_{\nu i} \quad (3)$$

and the corresponding electron density is

$$\rho(\mathbf{r}) = \sum_i |\psi_i(\mathbf{r})|^2 = \sum_{\mu\nu} P^{\mu\nu} \phi_{\mu}(\mathbf{r}) \phi_{\nu}(\mathbf{r}). \quad (4)$$

2.1 Grid-Based KS-DFT Ground State Energy Density

The ground-state KS-DFT energy is known to contain several components,

$$\begin{aligned} E_0 &= (E^T + E^N) + (E^J + E^K) + E^{xc} \\ &= \mathbf{P} \cdot \mathbf{h} + \frac{1}{2} \mathbf{P} \cdot \mathbf{\Pi} \cdot \mathbf{P} + \int f_{xc}(\rho(\mathbf{r})) d\mathbf{r} \end{aligned} \quad (5)$$

with the core Hamiltonian (\mathbf{h}) — kinetic (T) and nuclear attraction (N) — being

$$E^T + E^N = \sum_{\mu\nu} P^{\mu\nu} \int \phi_{\mu}(\mathbf{r}) \left[-\frac{1}{2} \nabla^2 - \sum_A \frac{Z_A}{|\mathbf{r} - \mathbf{A}|} \right] \phi_{\nu}(\mathbf{r}) d\mathbf{r} \quad (6)$$

where Z_A and \mathbf{A} are the nuclear charge and coordinates of the A -th atom, respectively. The Coulomb (J) and Hartree-Fock exchange (K) energies are,

$$E^J + E^K = \frac{1}{2} \mathbf{P} \cdot \mathbf{\Pi} \cdot \mathbf{P} = \frac{1}{2} \sum_{\mu\nu, \lambda\sigma} P^{\mu\nu} [(\mu\nu|\lambda\sigma) - \alpha_K (\mu\lambda|\nu\sigma)] P^{\lambda\sigma} \quad (7)$$

where α_K is the ratio of Hartree-Fock exchange for conventional hybrid functionals and the two-electron repulsion integrals are

$$(\mu\nu|\lambda\sigma) = \iint \phi_{\mu}(\mathbf{r}) \phi_{\nu}(\mathbf{r}) \frac{1}{|\mathbf{r} - \mathbf{r}'|} \phi_{\lambda}(\mathbf{r}') \phi_{\sigma}(\mathbf{r}') d\mathbf{r} d\mathbf{r}' \quad (8)$$

$$(\mu\lambda|\nu\sigma) = \iint \phi_{\mu}(\mathbf{r}) \phi_{\lambda}(\mathbf{r}) \frac{1}{|\mathbf{r} - \mathbf{r}'|} \phi_{\nu}(\mathbf{r}') \phi_{\sigma}(\mathbf{r}') d\mathbf{r} d\mathbf{r}' \quad (9)$$

Note that, for range-separated functionals, the Coulomb operator in Eq. 9 will be replaced with a linear combination of short-range and long-range operators.

With most quantum chemistry programs, the kinetic, nuclear attraction, Coulomb, and Hartree-Fock energy components would be calculated analytically. But, as shown by Nakai *et al*, like the exchange-correlation energy in Eq. 5, an energy density can also be defined for each of all other energy components,

$$\rho_0^E(\mathbf{r}) = \rho_0^T(\mathbf{r}) + \rho_0^N(\mathbf{r}) + \rho_0^J(\mathbf{r}) + \rho_0^K(\mathbf{r}) + f_{xc}(\rho(\mathbf{r})) \quad (10)$$

which together integrate into the total KS-DFT energy in Eq. 5

$$E_0 = \int \rho_0^E(\mathbf{r}) d\mathbf{r} \quad (11)$$

The kinetic energy density is well known to be,^{71,72}

$$\rho_0^T(\mathbf{r}) = \frac{1}{2} \sum_{\mu\nu} P^{\mu\nu} (\nabla \phi_{\mu}(\mathbf{r})) \cdot (\nabla \phi_{\nu}(\mathbf{r})), \quad (12)$$

whereas the nuclear attraction energy density is simply the product

of the electron density and the nuclear electrostatic potential

$$\rho_0^N(\mathbf{r}) = -\rho(\mathbf{r}) \sum_A \frac{Z_A}{|\mathbf{r} - \mathbf{A}|}. \quad (13)$$

Once the grid value of electrostatic potential of each pair of atomic basis functions

$$V_{\lambda\sigma}(\mathbf{r}) = \int \frac{\phi_\lambda(\mathbf{r}') \phi_\sigma(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' \quad (14)$$

is pre-computed, one can readily obtain the Coulomb (J) and Hartree-Fock exchange (K) energy densities in three steps ,

$$\rho_0^J(\mathbf{r}) = -\rho(\mathbf{r})V(\mathbf{r}) = \left[\sum_{\mu\nu} P^{\mu\nu} \phi_\mu(\mathbf{r}) \phi_\nu(\mathbf{r}) \right] \left[\sum_{\lambda\sigma} V_{\lambda\sigma}(\mathbf{r}) P^{\lambda\sigma} \right] \quad (15)$$

$$\begin{aligned} \rho_0^K(\mathbf{r}) &= -\alpha_K \sum_{\mu\nu, \lambda\sigma} \phi_\mu(\mathbf{r}) \phi_\lambda(\mathbf{r}) V_{\nu\sigma}(\mathbf{r}) P^{\mu\nu} P^{\lambda\sigma} \\ &= -\alpha_K \sum_{\nu\sigma} \left[\sum_{\mu} P^{\mu\nu} \phi_\mu(\mathbf{r}) \right] V_{\nu\sigma}(\mathbf{r}) \left[\sum_{\lambda} P^{\lambda\sigma} \phi_\lambda(\mathbf{r}) \right] \end{aligned} \quad (16)$$

where $V(\mathbf{r}) = -\sum_{\lambda\sigma} V_{\lambda\sigma}(\mathbf{r}) P^{\lambda\sigma}$ is the electrostatic potential of the total electron density. While the costs of computing $V_{\lambda\sigma}(\mathbf{r})$, $V(\mathbf{r})$, $\sum_{\mu\nu} P^{\mu\nu} \phi_\mu(\mathbf{r})$, and $\rho_0^K(\mathbf{r})$ all scale as $O(N_{\text{bas}}^2 N_{\text{grid}})$, the most expensive term is $V_{\lambda\sigma}(\mathbf{r})$ because it takes more FLOPS to evaluate one-electron integrals than to perform matrix multiplications.

2.2 Grid-Based LR-TDDFT Excitation Energy Density

Within the RT-TDDFT framework, the (unrelaxed) difference density matrix (\mathbf{P}_ω) and transition density matrix (\mathbf{R}_ω) are defined from the transition amplitudes (\mathbf{X} and \mathbf{Y} , each of dimension $N_v \times N_o$),^[73]

$$\begin{aligned} \mathbf{P}_\omega &= \mathbf{P}_\omega^{\text{attach}} - \mathbf{P}_\omega^{\text{detach}} \\ &= \mathbf{C}_v(\mathbf{X}\mathbf{X}^\dagger + \mathbf{Y}\mathbf{Y}^\dagger)\mathbf{C}_v^\dagger - \mathbf{C}_o(\mathbf{X}^\dagger\mathbf{X} + \mathbf{Y}^\dagger\mathbf{Y})\mathbf{C}_o^\dagger \end{aligned} \quad (17)$$

$$\mathbf{R}_\omega = \mathbf{C}_v\mathbf{X}\mathbf{C}_o^\dagger + \mathbf{C}_o\mathbf{Y}^\dagger\mathbf{C}_v^\dagger \quad (18)$$

of each excited state. Note that \mathbf{P}_ω is a symmetric matrix, while \mathbf{R}_ω is not. Using these matrices, a compact expression for the excitation energy is,^[74]

$$\omega = \mathbf{P}_\omega \cdot \mathbf{F} + \mathbf{R}_\omega \cdot (\mathbf{\Pi} + \mathbf{\Omega}) \cdot \mathbf{R}_\omega \quad (19)$$

where \mathbf{F} is the ground-state Fock matrix. Here, $\mathbf{\Omega}$ is the exchange-correlation portion of the Kohn-Sham response kernel

$$\Omega_{\mu\nu, \lambda\sigma} = \frac{\partial F_{\mu\nu}^{\text{xc}}}{\partial P^{\lambda\sigma}} = \int \left(\sum_{\xi, \xi'} \frac{\partial^2 f_{\text{xc}}}{\partial \xi \partial \xi'} \frac{\partial \xi}{\partial P^{\mu\nu}} \frac{\partial \xi'}{\partial P^{\lambda\sigma}} \right) d\mathbf{r} \quad (20)$$

with ξ and ξ' referring to alpha and beta electron densities (ρ_σ) and their gradient components (ρ_σ^x , ρ_σ^y , and ρ_σ^z). We shall call the $\mathbf{P}_\omega \cdot \mathbf{F}$ term in Eq. 19, which arises from orbital energy differences, the one-electron contribution to the excitation energy. The $\mathbf{R}_\omega \cdot (\mathbf{\Pi} + \mathbf{\Omega}) \cdot \mathbf{R}_\omega$ term, on the other hand, will be called two-electron contributions.

Similar to the ground-state KS-DFT energy, we can distribute

the LR-TDDFT excitation energy in Eq. 19 over a real-space grid,

$$\omega = \int \rho^\omega(\mathbf{r}) d\mathbf{r} \quad (21)$$

with the excitation energy density components being

$$\rho^\omega(\mathbf{r}) = \rho^T(\mathbf{r}) + \rho^N(\mathbf{r}) + \rho^J(\mathbf{r}) + \rho^K(\mathbf{r}) + \rho^{\text{XC}}(\mathbf{r}). \quad (22)$$

The first two components — kinetic and nuclear attraction energy densities — come only from the one-electron term ($\mathbf{P}_\omega \cdot \mathbf{F}$)

$$\rho^T(\mathbf{r}) = \frac{1}{2} \sum_{\mu, \nu, i} P_\omega^{\mu\nu} (\nabla \phi_\mu(\mathbf{r})) \cdot (\nabla \phi_\nu(\mathbf{r})) \quad (23)$$

$$\rho^N(\mathbf{r}) = -\rho_{\text{diff}}(\mathbf{r}) \sum_A \frac{Z_A}{|\mathbf{r} - \mathbf{A}|} \quad (24)$$

where the (unrelaxed) difference density is

$$\rho_{\text{diff}}(\mathbf{r}) = \sum_{\mu\nu} P_\omega^{\mu\nu} \phi_\mu(\mathbf{r}) \phi_\nu(\mathbf{r}) \quad (25)$$

The last three components (Coulomb, Hartree-Fock exchange, and exchange-correlation) of the excitation energy density in Eq. 22, on the other hand, all include both one-electron contributions (associated with difference density matrix) and two-electron contributions (associated with transition density matrix). Amongst, the Coulomb (J) and Hartree-Fock exchange (K) components can be evaluated as,

$$\rho^J(\mathbf{r}) = \sum_{\mu\nu, \lambda\sigma} \phi_\mu(\mathbf{r}) \phi_\nu(\mathbf{r}) V_{\lambda\sigma}(\mathbf{r}) \left(P_\omega^{\mu\nu} P^{\lambda\sigma} + R_\omega^{\mu\nu} R_\omega^{\lambda\sigma} \right) \quad (26)$$

$$\rho^K(\mathbf{r}) = -\alpha_K \sum_{\mu\nu, \lambda\sigma} \phi_\mu(\mathbf{r}) \phi_\lambda(\mathbf{r}) V_{\nu\sigma}(\mathbf{r}) \left(P_\omega^{\mu\nu} P^{\lambda\sigma} + R_\omega^{\mu\nu} R_\omega^{\lambda\sigma} \right) \quad (27)$$

The computation of $\rho^J(\mathbf{r})$ and $\rho^K(\mathbf{r})$ can follow a similar procedure as that of ground-state energy components shown in Eqs. 15 and 16, but it will involve more matrix multiplications. A subtle but important issue here is that the two-electron contribution to $\rho^K(\mathbf{r})$ in Eq. 27, is not uniquely defined. This can be easily understood within the MO representation, where this excitation energy density component becomes

$$\begin{aligned} \rho_2^K(\mathbf{r}) &= -\alpha_K \sum_{\mu\nu, \lambda\sigma} \phi_\mu(\mathbf{r}) \phi_\lambda(\mathbf{r}) V_{\nu\sigma}(\mathbf{r}) R_\omega^{\mu\nu} R_\omega^{\lambda\sigma} \\ &= -\alpha_K \sum_{ia, jb} [\psi_a(\mathbf{r}) \psi_b(\mathbf{r}) V_{ij}(\mathbf{r}) X_{ai} X_{bj} + \psi_a(\mathbf{r}) \psi_j(\mathbf{r}) V_{bi}(\mathbf{r}) X_{ai} Y_{bj} \\ &\quad + \psi_b(\mathbf{r}) \psi_i(\mathbf{r}) V_{aj}(\mathbf{r}) Y_{ai} X_{bj} + \psi_i(\mathbf{r}) \psi_j(\mathbf{r}) V_{ab}(\mathbf{r}) Y_{ai} Y_{bj}] \end{aligned} \quad (28)$$

and the first term (associated with $\mathbf{X} \otimes \mathbf{X}$) would dominate. For charge-transfer excitations, this density would be concentrated mainly on the electron acceptor, where virtual orbitals a and b reside. On the other hand, an equivalent way for distributing the two-electron Hartree-Fock exchange energy (that integrates to the same total exchange energy contribution to the excitation energy) is to transpose both (nonsymmetric) transition density matrices in

Eq. 27,

$$\begin{aligned}\rho_2^K(\mathbf{r}) &= -\alpha_K \sum_{\mu\nu,\lambda\sigma} \phi_\mu(\mathbf{r})\phi_\lambda(\mathbf{r})V_{\nu\sigma}(\mathbf{r})R_\omega^{\nu\mu}R_\omega^{\sigma\lambda} \\ &= -\alpha_K \sum_{ia,jb} [\psi_i(\mathbf{r})\psi_j(\mathbf{r})V_{ab}(\mathbf{r})X_{ai}X_{bj} + \psi_b(\mathbf{r})\psi_i(\mathbf{r})V_{aj}(\mathbf{r})X_{ai}Y_{aj} \\ &\quad + \psi_a(\mathbf{r})\psi_j(\mathbf{r})V_{bi}(\mathbf{r})Y_{ai}X_{ai} + \psi_a(\mathbf{r})\psi_b(\mathbf{r})V_{ij}(\mathbf{r})Y_{ai}Y_{bj}] \quad (29)\end{aligned}$$

For charge-transfer excitations, this produces an energy density mostly on the donor moiety, where occupied orbitals i and j are located. In this work, we will use the average between these two distributions (Eqs. 28 and 29). For charge-transfer excitations, this means that the two-electron Hartree-Fock exchange energy (*i.e.* the electrostatic interaction between the particle and the hole) is evenly split between the donor and acceptor moieties.

Finally, the one-electron and two-electron contributions to the exchange-correlation term in Eq. 22 are

$$\rho_1^{XC}(\mathbf{r}) = \sum_{\mu\nu} \left(\sum_{\xi} \frac{\partial f_{xc}}{\partial \xi} \frac{\partial \xi}{\partial P^{\mu\nu}} \right) P_\omega^{\mu\nu} \quad (30)$$

$$\rho_2^{XC}(\mathbf{r}) = \sum_{\mu\nu,\lambda\sigma} R_\omega^{\mu\nu} \left(\sum_{\xi,\xi'} \frac{\partial^2 f_{xc}}{\partial \xi \partial \xi'} \frac{\partial \xi}{\partial P^{\mu\nu}} \frac{\partial \xi'}{\partial P^{\lambda\sigma}} \right) R_\omega^{\lambda\sigma} \quad (31)$$

2.3 Real-Space Partitioning Schemes

Two sets of weights for real-space grid points — Becke weights²³ and those from Fragment-Based Hirshfeld (FBH) analysis²⁷ — will be employed to partition the charge and energy densities onto different fragments.

Within the Becke scheme, which is widely employed for integrating the exchange-correlation contributions to the KS-DFT energy and Fock matrix, Lebedev quadrature points are added around each atom. The weight of each grid point is defined as

$$w_n(\mathbf{r}) = \frac{P_n(\mathbf{r})}{\sum_{m \in \text{atoms}} P_m(\mathbf{r})} \quad (32)$$

with $P_m(\mathbf{r})$ being polynomial functions of the distance between the grid point from the m -th nucleus. For each molecular fragment (A), the collective weight is

$$w_A^{\text{Becke}}(\mathbf{r}) = \sum_{n \in A} w_n(\mathbf{r}). \quad (33)$$

Within the FBH analysis, one first computes the electron densities for isolated fragments, $\rho_B^{\text{isolated}}(\mathbf{r})$. The “promolecule” density for a molecular complex is defined as a sum of these fragment densities,

$$\rho^{\text{promolecule}}(\mathbf{r}) = \sum_B \rho_B^{\text{isolated}}(\mathbf{r}) \quad (34)$$

For each real-space grid point, a weight, $w_A(\mathbf{r})$, can be assigned to each fragment

$$w_A^{\text{FBH}}(\mathbf{r}) = \frac{\rho_A^{\text{isolated}}(\mathbf{r})}{\rho^{\text{promolecule}}(\mathbf{r})} \quad (35)$$

Note that FBH population was used previously to construct constrained density functional theory (CDFT) states of molecular complexes.^{27,75,76}

Using either set of atomic weights, we can partition the difference electron density in Eq. 25 and the excitation energy density in Eq. 22 onto different fragments,

$$(\Delta Q)_A = \int w_A(\mathbf{r}) \rho_{\text{diff}}(\mathbf{r}) d\mathbf{r} \quad (36)$$

$$\omega_A = \int w_A(\mathbf{r}) \rho^\omega(\mathbf{r}) d\mathbf{r} \quad (37)$$

In this work, the fragment charge in Eq. 36 was computed using the relaxed difference densities.

2.4 Characterization of Electronic Excitations

In our work, besides fragment charges, two other metrics will be used to distinguish charge-transfer excitations from local excitations. The first one is the widely-used Λ factor proposed by Peach *et al.*⁵⁸ For a given LR-TDDFT excited state, it will be computed as

$$\Lambda = \frac{\sum_{a,i} O_{ai} |X_{ai} + Y_{ai}|^2}{\sum_{a,i} |X_{ai} + Y_{ai}|^2} \quad (38)$$

where O_{ai} is the overlap of the moduli of the a -th virtual orbital and the i -th occupied orbital,

$$O_{ai} = \int |\psi_a(\mathbf{r})| |\psi_i(\mathbf{r})| d\mathbf{r}. \quad (39)$$

Alternatively, one can utilize the detachment (“hole”) and attachment (“particle”) densities, which can be computed by plugging the corresponding unrelaxed difference density matrix components in Eq. 17 into Eq. 25. In a recent work, the overlap of detachment (or attachment) densities from separate LR-TDDFT calculations was employed to compare excited states computed using different basis sets.⁷⁷ In this work, the overlap between the attachment and detachment densities of each excited state proposed first by Etienne^{50,51}

$$S_{\text{DA}} = \int [\rho^{\text{detach}}(\mathbf{r})]^{\frac{1}{2}} [\rho^{\text{attach}}(\mathbf{r})]^{\frac{1}{2}} d\mathbf{r} \quad (40)$$

will be used as an alternative metric for assessing its character.

For each excited state, both criteria will fall in the range of [0,1], with a smaller value indicating a stronger charge-transfer character.

3 Computational Details

Two model complexes were used to demonstrate the distribution of the excitation energy densities. The first was the ethylene-tetrafluoroethylene (C_2H_4 – C_2F_4) complex, which was widely used in the development of the range-separated functionals.^{78,79} Both C_2H_4 and C_2F_4 were optimized using the $\omega\text{B97X-D}$ functional⁸⁰ and 6-311++G(d,p) basis set.⁸¹ Then, these monomers were combined together (without further geometry relaxation) into three different configurations:

- Cofacial (labeled as **F**, Figure 1). Two monomers were stacked on top of each other with a 5 Å distance in between.

Table 1 Excitation character metrics (Λ and S_{DA}), FBH fragment charges (ΔQ_A), FBH fragment excitation energies (ω_A) for the lowest local excitation and charge-transfer excitations of three $C_2H_4-C_2F_4$ configurations. Obtained from LR-TDDFT calculations using the PBE0 functional and 6-31G(d) basis set.

Configuration	ES#	Λ	S_{DA}	Q_A (a.u.)		ω_A or ω (eV)		
				C_2H_4	C_2F_4	C_2H_4	C_2F_4	Total
F	2	0.623	0.631	0.000	0.000	−0.003	7.129	7.125
P1	1	0.611	0.628	−0.010	0.010	0.026	7.074	7.099
P2	1	0.623	0.631	−0.001	0.001	0.005	7.121	7.126
F	1	0.092	0.042	−0.997	0.997	0.315	6.698	7.012
P1	2	0.015	0.006	−0.990	0.990	0.426	6.819	7.244
P2	2	0.005	0.003	−0.999	0.999	0.466	6.835	7.301

- Planar 1 (labeled as **P1**, Figure 2). Two monomers laid side-by-side with a 5 Å distance between the closest carbon atoms.
- Planar 2 (labeled as **P2**, Figure 3). Two monomers laid end-to-end with a 5 Å distance between the closest carbon atoms.

The second was the oxyluciferin molecule (OLH or OxyLH₂), where 6'-oxygen is protonated, in complex with a water molecule. Its anionic form has been shown to be the light emitter in firefly bioluminescence.^[82] Three different types of configurations would also be studied:

- Hydrogen-bonded 1 and 2 (labelled as **HB1** and **HB2**, Figure 5). Water molecule formed a hydrogen bond with the 5'-oxygen or 6'-oxygen of OLH. Both complexes were optimized at ω B97X-D/6-311++G(d,p) level of theory.
- T-shape (labelled as **T**, Figure 6). Water molecule formed a T-shape complex with OLH, with its one O-H bond pointing towards the center of the benzene ring of OLH. A series of geometries were obtained via restrained geometry optimization with varying distances (1.6, 1.7, 1.8, 1.9, 2.0, and 2.1 Å) between the water hydrogen atom and the center of the OLH benzene ring.

The evaluation and partitioning of excitation energy densities were implemented within a development version of the PySCF software package.^[83] Standard and restrained geometry optimization and LR-TDDFT/TIP3P excitation energy calculations of different OLH-H₂O configurations were carried out by the Q-CHEM software package.^[84] All geometries used in this article, together with their ω B97X-D/6-311++G(d,p) energies as computed by Q-CHEM, are provided in the Electronic Supplementary Information.

4 Results

4.1 Ground-State Energy Density

Before proceeding to present our results on the excitation energy density of the two molecular complexes, it would be beneficial to analyze and understand the ground-state energy densities. This has already been carried out in the accompanying paper, where the ground-state energy densities of N₂ molecule and a small Ag₄ cluster were analyzed. Here is a summary of our key understandings of the ground-state energy densities:

- The kinetic energy density (ρ_0^T) and the Coulomb energy density (ρ_0^J) are always positive. In contrast, the nuclear attraction energy density (ρ_0^N), Hartree-Fock exchange energy density (ρ_0^K), and exchange-correlation energy density (ρ_0^{XC}) are all negative. ρ_0^K and ρ_0^{XC} are substantially smaller in the magnitude than other energy densities.
- The total ground-state energy density (ρ_0^E) is usually negative, and thus has an opposite sign as the charge density. But ρ_0^E has a positive value in a “donut” region around each nucleus, due to a slower decay of the kinetic energy density there.
- All energy density components decay rapidly away from the molecule.

4.2 Ethylene-Tetrafluoroethylene (C₂H₄-C₂F₄) Complexes

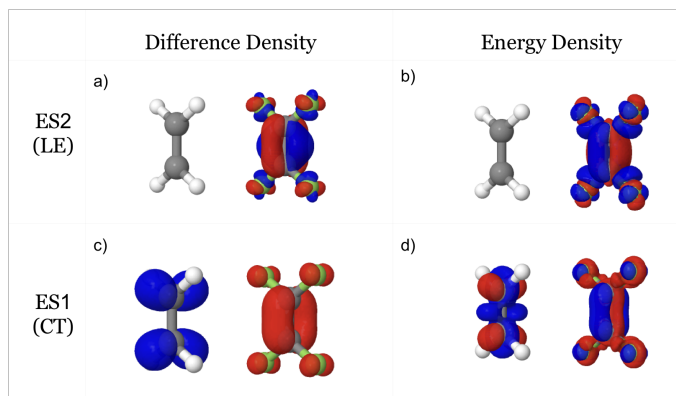


Fig. 1 Difference density and excitation energy density plots (isovalue = 0.01 au; red = negative) for the lowest (a, b) local excitation and (c, d) charge transfer excitation of the **F** (stacked) configuration of the $C_2H_4-C_2F_4$ complex from LR-TDDFT calculations with PBE0 functional and 6-31G(d) basis set.

Ethylene-tetrafluoroethylene is an interesting system. With the HOMO of the complex coming from C_2F_4 and the LUMO from C_2H_4 , one of the low-lying excited states involves a charge transfer between these orbitals from different fragments. Such a charge-transfer state can have lower energy than local excitations on either C_2F_4 or C_2H_4 fragment, especially with the use of conventional hybrid density functionals and smaller basis sets.

Table 1 collects information on the lowest two excitations for each of the three $C_2H_4-C_2F_4$ configurations, which were obtained from LR-TDDFT calculations using the PBE0 functional⁸⁵ and 6-31G(d) basis set.^{86,87} The corresponding difference densities and excitation energy densities are shown in Figures 1, 2, and 3.

The charge-transfer character of each excited state can be first assessed by examining the FBH fragment charges as defined in Eq. 36. For the cofacial configuration (F), our LR-TDDFT/PBE0/6-31G(d) calculation predicted a charge-transfer excited state (with $0.997 e^-$ within the FBH scheme shifted from C_2F_4 to C_2H_4 ; see Figure 1c for the density change) to be lower than a local excitation on C_2F_4 (with $0.000 e^-$ shifted; Figure 1a). On the other hand, for two other configurations (P1 and P2), the charge-transfer state (with 0.990 or $0.999 e^-$; Figures 2c and 3c) has a higher energy than the corresponding local excitations. Similar amounts of charge transfer between the fragments can be found in Table S10 for the Becke and ESP-derived charge schemes.

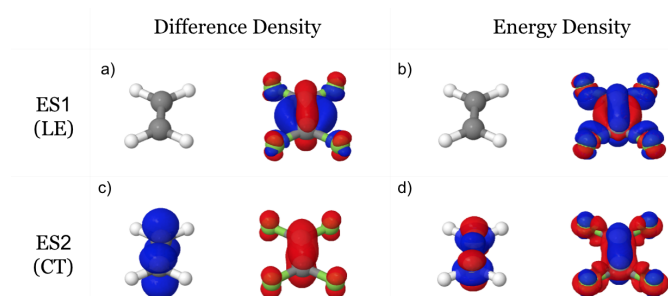


Fig. 2 Difference density and excitation energy density plots (isovalue = 0.01 au; red = negative) for the lowest (a, b) local excitation and (c, d) charge transfer excitation of the **P1** (planar side-by-side) configuration of the $C_2H_4-C_2F_4$ complex from LR-TDDFT calculations with PBE0 functional and 6-31G(d) basis set.

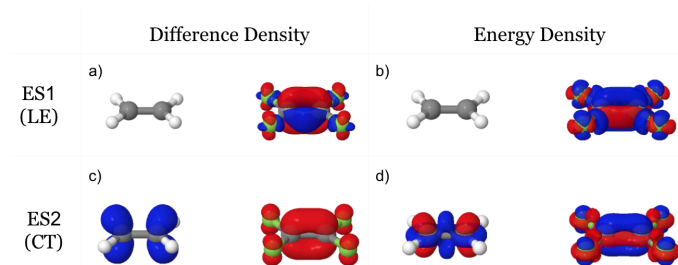


Fig. 3 Difference density and excitation energy density plots (isovalue surface of 0.01 au; red = negative) for the lowest (a, b) local excitation and (c, d) charge transfer excitation of the **P2** (planar end-to-end) configuration of the $C_2H_4-C_2F_4$ complex from LR-TDDFT calculations with PBE0 functional and 6-31G(d) basis set.

Two other metrics for characterizing excited states behaved very similarly. In Table 1, Λ and S_{DA} values were shown to be consistently smaller than 0.1 for charge-transfer states, and their values fell in the range of 0.60–0.65 for locally excited states. This confirms that the S_{DA} value can also be useful for distinguishing charge-transfer excitations from local excitations.

As expected, the excitation energy densities were shown in Figures 1, 2, and 3 to be concentrated on a molecular fragment

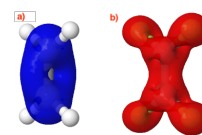


Fig. 4 Kinetic energy density (isovalue = 0.01 au) for a) C_2H_4 LUMO and b) C_2F_4 HOMO. The latter was multiplied by -1 to be consistent with its contribution to the kinetic energy density of the charge-transfer excitation.

for localized excitations, and distributed over both fragments for charge-transfer excitations. We can easily recognize two distinct contributions to each excitation energy density:

- “normal” contribution, which has the opposite sign (color) as the difference density. This is similar to our observation for the ground state energy density as summarized above in Section 4.1. For the lowest charge-transfer excitation of the cofacial configuration, for example, an electron was detached from C_2F_4 HOMO (see the red “cloud” in Figure 1c). Accordingly, one can recognize a negative electron density of a similar shape on C_2F_4 in Figure 1d.
- kinetic energy contribution, which has the same sign (color) as the different density but has a very different shape. For the cofacial configuration, the kinetic energy densities are shown in Fig 4 for C_2H_4 LUMO and C_2F_4 HOMO, which combine together to yield the kinetic energy density of the lowest charge-transfer excitation. Such a contribution is clearly responsible for the extra features within and near the molecular planes in the excitation energy density plots in, for instance, Figure 1d.

When the excitation energy densities are integrated over each fragment according to Eq. 37, the total excitation energy is divided into fragment contributions. In accordance with our expectation, the excitation energy was shown in Tables 1 and S10 to concentrate on one fragment (C_2F_4 in tested cases) for local excitations. For charge-transfer excitations, significant (>0.3 eV) and positive excitation energy values were observed on both donor and acceptor fragments. However, the value on the donor fragment (C_2F_4 in these cases) are substantially larger, reflecting that (the absolute value of) HOMO energy (*i.e.* ionization potential within Koopman’s theorem) is usually larger than the LUMO energy (*i.e.* electron affinity within Koopman’s theorem). For instance, the electron donors contributed 6.7–6.8 eV to the total excitation energies while only 0.3–0.5 eV came from electron acceptors (see Table 1). As we mentioned in the introduction, the fragment excitation energies on the donor (acceptor) fragment can be regarded as effective energies of the “hole” (“particle”) in the charge-transfer excitations.

4.3 Oxyluciferin–Water Complexes

The neutral oxyluciferin molecule (OLH) can form multiple hydrogen bond complexes with a single water molecule. As shown in Figure 5, both 5'-oxygen (on the thiazole ring) and 6'-oxygen (on the benzothiazole ring) could serve as the hydrogen bond acceptor, leading to two complexes (**HB1** and **HB2**). As indicated by the

Table 2 Binding energies, excitation character metrics (Λ and S_{DA}), FBH fragment charges, and FBH fragment excitation energies for HOMO→LUMO excitations of three neutral OLH–H₂O configurations. Obtained from LR-TDDFT calculations with the PBE0 functional and 6-31G(d) basis set.

Con	ΔE_{bind} (kcal/mol)		ES#	Λ	S_{DA}	ΔQ_A (au)		ω_A or ω (eV)		
	w/o BSSE	w/ BSSE				OLH	H ₂ O	OLH	H ₂ O	Total
HB1	−8.798	−6.599	1	0.627	0.632	0.006	−0.006	3.495	0.020	3.515
HB2	−6.115	−4.092	2	0.640	0.632	−0.006	0.006	3.638	−0.010	3.628
T1.6	7.224	7.888	1	0.594	0.607	−0.150	0.150	2.396	1.108	3.504
T1.7	4.192	7.554	1	0.602	0.616	−0.118	0.118	2.719	0.828	3.547
T1.8	1.954	4.910	1	0.602	0.636	−0.087	0.087	2.994	0.582	3.576
T1.9	0.380	2.934	2	0.615	0.631	−0.067	0.067	3.175	0.420	3.595
T2.0	−0.660	1.550	2	0.622	0.629	−0.052	0.052	3.305	0.303	3.608
T2.1	−1.361	0.502	2	0.625	0.630	−0.037	0.037	3.412	0.197	3.609

BSSE-corrected binding energies in Table 2, these hydrogen bonds could stabilize the complex by 4 to 6.5 kcal/mol.

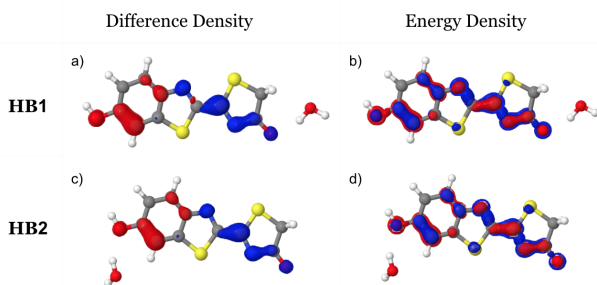


Fig. 5 Difference density and excitation energy density plots (isovalue = 0.005 au; red = negative) for the HOMO→LUMO excitations of two hydrogen-bonded OLH–H₂O complexes. Obtained from LR-TDDFT calculations with PBE0 functional and 6-31G(d) basis set.

The HOMO→LUMO vertical excitation of oxyluciferin involves a partial charge transfer from the benzothiazole ring to the thiazole ring. As shown in the difference density plots in Figure 5a and 5c, such a partial charge transfer was largely unchanged upon the binding of a water molecule in the two hydrogen bond complexes. In Table 2, the fragment charges on OLH or water in **HB1** and **HB2** were found to be only 0.006 e^- . Accordingly, the excitation energy densities in Figure 5b and 5d remained localized on OLH, with the fragment excitation energies integrated to only 0.02 eV (**HB1**) and -0.01 eV (**HB2**) on H₂O molecule in Table 2.

However, the picture can be quite different when oxyluciferin formed a T-shape complex (T) with a water molecule. As shown in the left column of Figure 6, the detachment density could more easily “spill” over to the water molecule, which corresponds to a “spillover” of OLH HOMO to the water molecule. For the HOMO→LUMO excitation of these T-shape complexes, Table 2 thus showed a net loss of 0.037 to 0.150 e^- from the water molecule. This was accompanied by a “spillover” of the excitation energy density to the water molecule in each of these T-shape complexes (see the right column of Figure 6), with the fragment excitation energy on water computed to be 0.197 to 1.108 eV.

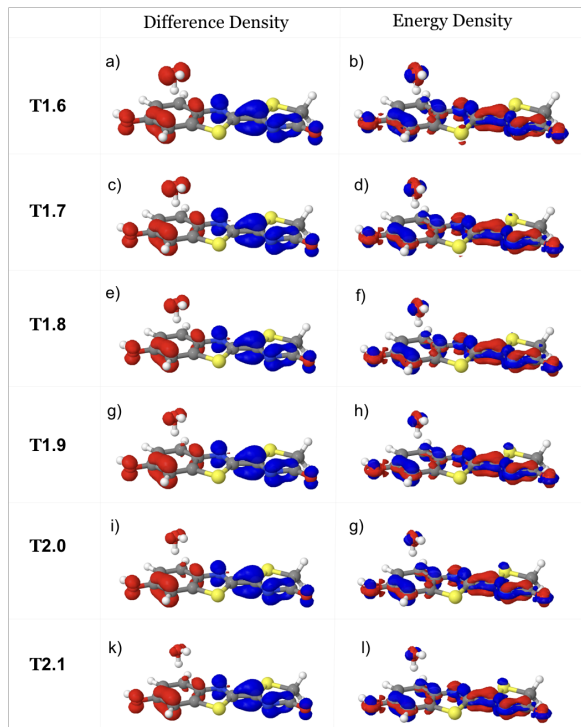


Fig. 6 Difference density and excitation energy density plots (isovalue surface of 0.005 au; red = negative) for the HOMO→LUMO excitations of six T-shape OLH–H₂O complexes (with the distance between water hydrogen and OLH benzene ring center ranging from 1.6 to 2.1 Å). Obtained from LR-TDDFT calculations with PBE0 functional and 6-31G(d) basis set.

5 Discussions

Functional and Basis Set. So far, we have focused our report on LR-TDDFT calculations using the PBE0 functional and 6-31G(d) basis set. Such a choice was made on two practical considerations — the easiness of identifying the charge-transfer excited state and a moderate computational cost. But, As shown in Tables S1–S9, our energy density analysis is also fully functioning with larger basis sets.

Our implementation of excitation energy densities is also applicable to other functionals, such as pure and range-separated

functionals, which require the use of appropriate electron repulsion operators, if any, in the calculation of exchange energy density components. Results with the PBE^[88] and ω B97X-D functionals are shown in Tables S1, S3, S4, S6, S7, and S9 for C₂H₄–C₂F₄ dimers. For local excitations, the excitation energy remain localized with these two functionals. On the other hand, in a charge-transfer excitation, the acceptor portion of the excitation energy (which can be interpreted as the effective energy of the “particle”) arises from a cancellation of the kinetic energy of the “particle” and other contributions. While it is consistently positive with the ω B97X-D functional, it can acquire a negative value with PBE and PBE0 functionals, likely due to lower (and sometimes even negative) LUMO energy values.

Computational Cost. Within our preliminary implementation, the computational cost for obtaining excitation energy density arises mainly from the evaluation of $V_{\lambda\sigma}$, which is the grid-based electrostatic potential of each function pair (*i.e.* pairs of atomic basis functions) in Eq. [14]. $V_{\lambda\sigma}$ is needed in the construction of Coulomb and exchange energy densities in Eqs. [26] and [27]. Such a calculation would become rather prohibitive for large systems and/or larger basis sets. We note that the resolution-of-the-identity (RI) approach^[89,96] was employed to approximate the ground-state Hartree-Fock exchange energy density,^[97,98] and thus anticipate a similar use of the RI approach to accelerate the evaluation of excitation energy densities.

Table 3 TDDFT (for the full system), TDDFT/TIP3P excitation energies, and the differences between them (in eV) for the HOMO \rightarrow LUMO excitations of the HB1, HB2, and T-shape configurations of neutral OLH–H₂O calculated with the PBE0 functional and 6-31G(d) basis set by Q-CHEM.

Configuration	ES#	$\omega_{\text{Full-TDDFT}}$	$\omega_{\text{TDDFT/TIP3P}}$	$\Delta\omega$
HB1	1	3.516	3.545	0.039
HB2	2	3.630	3.620	−0.010
T1.6	1	3.507	3.663	0.156
T1.7	1	3.550	3.663	0.113
T1.8	1	3.578	3.661	0.073
T1.9	2	3.597	3.656	0.059
T2.0	2	3.610	3.654	0.044
T2.1	2	3.611	3.642	0.031

Fluorophore-Solvent Charge Transfer. For the T-shape oxyluciferin-water complexes, we have noticed a “spillover” of detachment/attachment density and excitation energy density to the water molecule. This is ultimately due to a strong interaction between the fluorophore and water frontier orbitals, which can only be captured by coupling orbitals from different fragments.^[99] As shown in Table [3], this has led the LR-TDDFT/TIP3P model to systematically overestimate the vertical excitation energies of T-shape complexes.

An individual T-shape complex can be energetically unfavorable, as evident by the binding energies in Table [2]. In TDDFT/TIP3P molecular dynamics simulation of the solvated OLH (and several other fluorophores), we have nevertheless observed multiple water molecules (in the first solvation shell) forming T-shape complexes

with the fluorophore. Lacking a treatment of charge-transfer interactions between the QM and MM regions, LR-TDDFT/TIP3P can systematically overestimate the vertical excitation energy of the fluorophore (within in first solvation shell) by as much as 0.10–0.15 eV. For a more accurate description of solvatochromic effect (especially with multiple solvents), it is therefore desirable to extend orbital-dependent inter-fragment charge-transfer models (such as the EFP model)^[100] to excited state calculations.

6 Conclusions

In this article, we presented a method for distributing the LR-TDDFT excitation energy over the real space, and thus for acquiring the grid-based excitation energy density for each excited state. Due to the kinetic energy density term, the excitation energy distribution was found to be slightly more complicated than the difference electron density (between the ground and excited states).

For locally-excited states (as indicated by the attachment/detachment densities and changes in fragment charges), the excitation energy density was concentrated on a single molecular fragment, just as expected. In charge-transfer excitations, such as the ones in the C₂H₄–C₂F₄ complex, the excitation energy density would be distributed over both donor and acceptor fragments, with a higher percentage of the excitation energy allocated on the donor fragment. Fragment excitation energies from a charge-transfer excitation can be regarded as the effective energies for the “hole” and “particle”, respectively.

For excitations with a partial charge transfer between a fluorophore and water, such as T-shape OLH–water complexes, a small percentage of the excitation energy was found on the water molecules. The challenge to model such an effect with QM/MM-type methods stems from inter-fragment orbital mixing and might motivate the development of new methodologies to capture solute-solvent charge-transfer effects on electronic transitions.

Conflicts of interest

There are no conflicts to declare.

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Can We See the Energy Densities? II. Insights from Linear-Response Time-Dependent Density Functional Theory Calculations. **Electronic Supplementary Information**

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1 Partition Results

All charge and energy density calculations were carried out by PySCF. The only expectations are FBH charges from LR-TDDFT- ω B97X-D relaxed difference densities, which were obtained from Q-CHEM calculations.

Table S1: LR-TDDFT Results of C_2H_4 - C_2F_4 **F** Configuration using the PBE Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{\text{FBH,T}}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C_2H_4	C_2F_4	C_2H_4	C_2F_4	C_2H_4	C_2F_4	
6-31G(d)	1	0.058	0.018	-0.998	0.998	34.909	-69.402	-0.415	5.425	5.009
	2	0.625	0.630	0.001	-0.001	-0.037	13.541	0.002	6.788	6.790
	3	0.060	0.035	0.998	-0.998	-28.689	69.787	6.411	0.403	6.814
	4	0.017	0.021	0.998	-0.998	-28.675	83.323	6.401	1.155	7.556
	5	0.024	0.018	-0.999	0.999	25.114	-69.386	2.665	5.414	8.078
6-31+G(d)	1	0.102	0.058	-0.963	0.963	28.830	-67.046	-1.048	6.190	5.142
	2	0.394	0.377	-0.209	0.209	1.569	-55.081	0.035	5.630	5.664
	3	0.545	0.528	-0.062	0.062	0.330	-18.787	0.079	6.120	6.198
	4	0.212	0.207	0.797	-0.797	-26.583	14.795	6.811	-0.549	6.262
	5	0.347	0.312	-0.460	0.460	3.816	-55.660	0.254	6.203	6.456
6-311G(d,p)	1	0.084	0.029	-0.995	0.995	34.293	-69.793	-0.832	5.860	5.028
	2	0.092	0.056	0.993	-0.993	-28.790	70.381	6.734	-0.010	6.725
	3	0.625	0.629	0.000	0.000	-0.045	12.413	0.012	6.727	6.739
	4	0.096	0.078	-0.981	0.981	16.717	-69.313	1.136	5.871	7.006
	5	0.035	0.044	0.993	-0.993	-28.752	82.550	6.716	0.682	7.398
6-311++G(d,p)	1	0.101	0.056	-0.967	0.967	29.608	-67.862	-1.160	6.283	5.123
	2	0.360	0.335	-0.383	0.384	2.561	-58.753	-0.145	5.790	5.644
	3	0.534	0.503	-0.152	0.152	0.761	-24.058	0.055	6.153	6.207
	4	0.236	0.315	0.522	-0.522	-23.292	5.039	6.119	0.120	6.239
	5	0.254	0.327	-0.485	0.486	1.792	-55.009	0.595	5.671	6.266

Table S2: LR-TDDFT Results of C₂H₄-C₂F₄ **F** Configuration using the PBE0 Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{FBH,T}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	
6-31G(d)	1	0.092	0.042	-0.997	0.997	32.978	-66.022	0.315	6.698	7.012
	2	0.623	0.631	0.000	0.000	-0.012	15.975	-0.003	7.129	7.125
	3	0.163	0.311	0.930	-0.930	-26.069	61.986	7.274	0.952	8.226
	4	0.787	0.950	0.067	-0.067	1.570	4.361	7.691	0.715	8.406
	5	0.534	0.586	0.001	-0.001	5.829	0.029	8.498	0.010	8.508
6-31+G(d)	1	0.361	0.409	-0.134	0.134	0.816	-50.095	0.086	6.362	6.447
	2	0.437	0.575	-0.022	0.022	0.085	-4.582	0.037	6.668	6.705
	3	0.162	0.164	-0.867	0.867	21.596	-61.995	-0.438	7.284	6.845
	4	0.243	0.322	0.474	-0.474	-22.956	6.358	7.327	-0.204	7.123
	5	0.276	0.419	-0.271	0.271	4.285	-44.914	0.516	6.997	7.512
6-311G(d,p)	1	0.135	0.067	-0.992	0.992	32.029	-66.136	-0.095	7.067	6.972
	2	0.620	0.630	0.000	0.000	-0.015	14.972	-0.001	7.077	7.075
	3	0.590	0.776	0.416	-0.416	-10.663	27.599	7.671	0.388	8.059
	4	0.353	0.645	0.575	-0.575	-14.922	39.096	7.789	0.407	8.195
	5	0.550	0.631	0.002	-0.002	4.692	0.065	8.219	0.019	8.238
6-311++G(d,p)	1	0.302	0.405	-0.179	0.179	0.894	-51.070	0.047	6.432	6.479
	2	0.368	0.579	-0.025	0.025	0.084	-3.867	0.026	6.702	6.728
	3	0.171	0.158	-0.883	0.883	22.745	-62.888	-0.530	7.377	6.847
	4	0.252	0.310	0.240	-0.240	-22.340	2.446	6.969	-0.071	6.898
	5	0.287	0.210	-0.694	0.694	3.955	-60.927	-0.051	7.482	7.430

Table S3: LR-TDDFT Results of C₂H₄-C₂F₄ **F** Configuration using the ω B97X-D Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{FBH,T}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	
6-31G(d)	1	0.622	0.631	0.000	0.000	-0.007	16.853	-0.003	7.179	7.175
	2	0.862	0.956	-0.007	0.007	3.955	-0.717	7.604	0.746	8.350
	3	0.534	0.578	0.001	-0.001	5.931	0.017	8.562	0.010	8.572
	4	0.815	0.939	-0.035	0.035	1.562	-5.014	0.805	7.793	8.597
	5	0.156	0.223	-0.953	0.953	31.248	-62.876	1.122	7.637	8.758
6-31+G(d)	1	0.323	0.428	-0.099	0.099	0.583	-48.303	0.097	6.701	6.797
	2	0.385	0.597	-0.013	0.013	0.047	2.353	0.022	6.843	6.864
	3	0.267	0.396	0.176	-0.176	-19.656	1.592	7.489	0.066	7.556
	4	0.716	0.831	0.040	-0.040	-7.177	-0.056	7.398	0.252	7.650
	5	0.281	0.423	-0.228	0.228	2.725	-42.922	0.137	7.693	7.830
6-311G(d,p)	1	0.616	0.631	0.000	0.000	-0.010	16.013	-0.003	7.138	7.135
	2	0.845	0.942	-0.002	0.002	2.647	-0.302	7.808	0.257	8.064
	3	0.551	0.606	0.001	-0.001	5.034	0.035	8.289	0.018	8.308
	4	0.691	0.898	-0.158	0.158	4.633	-12.355	0.355	8.172	8.527
	5	0.393	0.414	0.005	-0.005	-11.055	0.075	8.518	0.024	8.541
6-311++G(d,p)	1	0.264	0.433	-0.107	0.107	0.531	-48.762	0.094	6.727	6.821
	2	0.410	0.600	-0.012	0.012	0.038	3.105	0.016	6.868	6.883
	3	0.239	0.327	0.101	-0.101	-21.287	0.491	7.137	0.056	7.192
	4	0.608	0.844	0.039	-0.039	-6.250	0.118	7.402	0.205	7.607
	5	0.186	0.358	0.059	-0.059	-20.640	0.390	7.770	0.080	7.850

Table S4: LR-TDDFT Results of C₂H₄-C₂F₄ **P1** Configuration using the PBE Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{FBH,T}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	
6-31G(d)	1	0.009	0.003	-0.988	0.988	34.946	-69.455	-0.322	5.538	5.215
	2	0.009	0.004	0.988	-0.988	-28.727	69.881	6.317	0.291	6.609
	3	0.619	0.620	-0.032	0.032	0.701	10.177	0.060	6.681	6.740
	4	0.070	0.069	0.965	-0.965	-28.245	81.017	6.363	0.944	7.307
	5	0.374	0.299	-0.778	0.778	19.768	-54.262	1.892	6.266	8.158
6-31+G(d)	1	0.055	0.019	-0.974	0.974	29.339	-67.360	-0.910	6.283	5.372
	2	0.407	0.388	-0.168	0.168	1.882	-53.440	0.016	5.682	5.698
	3	0.164	0.158	0.826	-0.826	-26.415	16.722	6.683	-0.651	6.032
	4	0.532	0.510	-0.118	0.118	1.326	-24.072	-0.005	6.170	6.164
	5	0.057	0.020	0.976	-0.976	-28.076	68.547	6.660	-0.409	6.251
6-311G(d,p)	1	0.013	0.004	-0.984	0.984	34.390	-69.882	-0.708	5.975	5.267
	2	0.014	0.006	0.984	-0.984	-28.878	70.652	6.611	-0.121	6.490
	3	0.580	0.563	-0.179	0.179	3.017	-6.558	0.139	6.415	6.554
	4	0.147	0.144	0.869	-0.869	-27.010	70.084	6.707	0.311	7.018
	5	0.356	0.333	-0.706	0.706	12.591	-48.878	0.810	6.478	7.288
6-311++G(d,p)	1	0.054	0.019	-0.975	0.975	30.110	-68.142	-1.020	6.372	5.352
	2	0.395	0.370	-0.253	0.253	2.291	-55.139	-0.067	5.774	5.707
	3	0.180	0.175	0.756	-0.756	-26.486	15.921	6.699	-0.658	6.041
	4	0.526	0.491	-0.170	0.170	1.413	-29.529	-0.043	6.231	6.188
	5	0.057	0.021	0.977	-0.977	-28.459	69.242	6.749	-0.500	6.250

Table S5: LR-TDDFT Results of C₂H₄-C₂F₄ **P1** Configuration using the PBE0 Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{FBH,T}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	
6-31G(d)	1	0.611	0.628	-0.010	0.010	0.194	14.812	0.026	7.074	7.099
	2	0.015	0.006	-0.990	0.990	33.110	-66.324	0.426	6.819	7.244
	3	0.015	0.018	0.990	-0.990	-28.145	66.751	7.194	0.848	8.042
	4	0.879	0.958	0.000	0.000	3.521	-0.384	7.502	0.884	8.386
	5	0.533	0.597	0.002	-0.002	5.757	0.145	8.520	-0.012	8.508
6-31+G(d)	1	0.381	0.418	-0.100	0.101	0.975	-48.722	0.057	6.420	6.476
	2	0.410	0.575	-0.040	0.040	0.409	-5.725	0.014	6.694	6.707
	3	0.207	0.259	0.597	-0.597	-23.290	10.649	7.249	-0.299	6.950
	4	0.165	0.045	-0.973	0.973	25.436	-64.515	-0.269	7.433	7.163
	5	0.295	0.393	-0.152	0.152	1.197	-43.491	0.124	7.335	7.458
6-311G(d,p)	1	0.497	0.616	-0.039	0.039	0.553	10.231	0.049	6.952	7.001
	2	0.025	0.010	-0.987	0.987	32.320	-66.576	0.048	7.191	7.239
	3	0.028	0.039	0.985	-0.985	-28.161	67.178	7.422	0.498	7.921
	4	0.250	0.397	0.308	-0.308	-16.118	17.695	7.710	0.380	8.090
	5	0.864	0.945	0.002	-0.002	2.436	-0.002	7.879	0.234	8.114
6-311++G(d,p)	1	0.359	0.417	-0.139	0.139	1.130	-48.817	0.024	6.485	6.509
	2	0.384	0.579	-0.031	0.031	0.288	-5.908	0.007	6.728	6.734
	3	0.250	0.271	0.416	-0.415	-23.203	7.259	7.068	-0.235	6.833
	4	0.245	0.047	-0.975	0.975	26.273	-65.082	-0.360	7.517	7.158
	5	0.263	0.252	0.298	-0.298	-23.019	4.821	7.460	-0.120	7.339

Table S6: LR-TDDFT Results of C₂H₄-C₂F₄ **P1** Configuration using the ω B97X-D Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{FBH,T}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	
6-31G(d)	1	0.610	0.630	-0.005	0.005	0.084	16.287	0.018	7.143	7.161
	2	0.880	0.957	0.000	0.000	3.780	-0.273	7.596	0.752	8.348
	3	0.536	0.579	-0.001	0.001	5.966	-0.059	8.591	-0.019	8.572
	4	0.861	0.942	-0.001	0.001	0.384	-2.637	0.776	7.822	8.598
	5	0.018	0.015	-0.991	0.991	32.912	-66.799	1.283	7.724	9.005
6-31+G(d)	1	0.331	0.434	-0.047	0.047	0.404	-47.652	0.063	6.766	6.829
	2	0.395	0.602	-0.031	0.031	0.279	3.502	0.034	6.849	6.883
	3	0.362	0.373	0.184	-0.184	-19.147	3.108	7.491	0.066	7.557
	4	0.595	0.838	0.010	-0.010	-6.976	0.059	7.538	0.114	7.652
	5	0.258	0.445	-0.061	0.061	0.458	-37.046	0.103	7.867	7.969
6-311G(d,p)	1	0.475	0.626	-0.014	0.014	0.187	14.135	0.032	7.068	7.100
	2	0.864	0.943	0.001	-0.001	2.655	-0.061	7.854	0.214	8.068
	3	0.555	0.607	-0.001	0.001	5.100	-0.043	8.328	-0.019	8.309
	4	0.291	0.407	0.088	-0.088	-12.039	3.448	8.253	0.281	8.535
	5	0.849	0.933	-0.001	0.001	0.079	-2.768	0.230	8.313	8.543
6-311++G(d,p)	1	0.283	0.437	-0.070	0.070	0.521	-48.076	0.056	6.791	6.847
	2	0.366	0.604	-0.022	0.022	0.180	3.638	0.017	6.883	6.900
	3	0.277	0.320	0.097	-0.097	-21.502	1.453	7.180	0.043	7.222
	4	0.624	0.850	0.009	-0.009	-5.985	0.049	7.502	0.108	7.610
	5	0.191	0.253	0.096	-0.096	-21.965	0.637	7.748	0.170	7.918

Table S7: LR-TDDFT Results of C₂H₄-C₂F₄ **P2** Configuration using the PBE Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{FBH,T}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	
6-31G(d)	1	0.003	0.001	-0.998	0.998	34.960	-69.463	-0.339	5.491	5.151
	2	0.003	0.001	0.998	-0.998	-28.735	69.879	6.336	0.336	6.673
	3	0.625	0.629	-0.002	0.002	0.034	13.254	0.008	6.782	6.789
	4	0.013	0.015	0.997	-0.997	-28.708	83.237	6.343	1.069	7.412
	5	0.532	0.574	0.000	0.000	6.378	-0.004	8.180	-0.001	8.178
6-31+G(d)	1	0.025	0.020	-0.981	0.981	29.215	-67.336	-0.935	6.261	5.326
	2	0.411	0.393	-0.099	0.099	0.941	-53.407	0.039	5.698	5.737
	3	0.093	0.088	0.907	-0.907	-27.342	16.784	6.714	-0.603	6.111
	4	0.549	0.533	-0.048	0.048	0.416	-17.770	0.056	6.155	6.211
	5	0.011	0.004	0.990	-0.990	-28.100	68.618	6.675	-0.380	6.296
6-311G(d,p)	1	0.006	0.002	-0.996	0.996	34.408	-69.898	-0.730	5.928	5.198
	2	0.007	0.003	0.995	-0.995	-28.890	70.655	6.635	-0.075	6.560
	3	0.622	0.625	-0.014	0.014	0.204	10.886	0.030	6.694	6.724
	4	0.131	0.091	-0.943	0.943	16.150	-67.607	1.082	6.045	7.126
	5	0.032	0.036	0.986	-0.986	-28.749	81.686	6.657	0.558	7.215
6-311++G(d,p)	1	0.022	0.018	-0.982	0.982	29.994	-68.128	-1.044	6.350	5.306
	2	0.394	0.367	-0.212	0.212	1.638	-55.816	-0.054	5.810	5.756
	3	0.124	0.119	0.823	-0.823	-27.249	15.489	6.728	-0.596	6.132
	4	0.211	0.194	-0.735	0.735	5.219	-63.618	-0.136	6.348	6.212
	5	0.539	0.515	-0.113	0.113	0.721	-21.591	0.047	6.169	6.216

Table S8: LR-TDDFT Results of C₂H₄-C₂F₄ **P2** Configuration using the PBE0 Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{FBH,T}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	
6-31G(d)	1	0.623	0.631	-0.001	0.001	0.013	15.848	0.005	7.121	7.126
	2	0.005	0.003	-0.999	0.999	33.086	-66.347	0.466	6.835	7.301
	3	0.005	0.013	0.998	-0.998	-28.155	66.737	7.274	0.948	8.222
	4	0.882	0.959	0.000	0.000	3.672	-0.238	7.819	0.580	8.399
	5	0.536	0.588	0.000	0.000	5.876	0.003	8.516	-0.001	8.515
6-31+G(d)	1	0.381	0.418	-0.048	0.048	0.380	-49.181	0.046	6.444	6.489
	2	0.454	0.577	-0.016	0.016	0.118	-4.107	0.034	6.681	6.715
	3	0.132	0.230	0.616	-0.616	-23.729	9.127	7.385	-0.213	7.172
	4	0.054	0.055	-0.954	0.954	24.172	-64.364	-0.264	7.468	7.204
	5	0.284	0.394	-0.203	0.203	1.813	-43.499	0.090	7.363	7.453
6-311G(d,p)	1	0.611	0.629	-0.004	0.004	0.046	14.460	0.014	7.055	7.069
	2	0.010	0.005	-0.996	0.996	32.293	-66.607	0.083	7.206	7.288
	3	0.069	0.280	0.921	-0.921	-25.878	62.110	7.543	0.561	8.105
	4	0.784	0.927	0.076	-0.076	0.192	5.080	7.949	0.175	8.124
	5	0.552	0.639	0.001	-0.001	4.703	0.050	8.244	0.003	8.247
6-311++G(d,p)	1	0.327	0.417	-0.072	0.072	0.467	-49.833	0.020	6.517	6.537
	2	0.355	0.579	-0.024	0.024	0.140	-3.860	0.032	6.702	6.733
	3	0.187	0.284	0.213	-0.213	-22.224	2.807	6.988	-0.068	6.920
	4	0.055	0.048	-0.960	0.960	25.210	-64.985	-0.353	7.555	7.202
	5	0.208	0.213	0.464	-0.464	-24.148	7.010	7.507	-0.167	7.341

Table S9: LR-TDDFT Results of C₂H₄-C₂F₄ **P2** Configuration using the ω B97X-D Functional.

Basis	ES#	Λ	S_{DA}	Q_{FBH} (au)		$\omega_{FBH,T}$ (eV)		ω_{FBH} (eV)		ω (eV)
				C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	
6-31G(d)	1	0.623	0.631	0.000	0.000	0.008	16.769	0.004	7.172	7.177
	2	0.882	0.958	0.000	0.000	3.918	-0.166	7.868	0.492	8.360
	3	0.536	0.579	0.000	0.000	5.973	-0.003	8.580	-0.002	8.579
	4	0.863	0.941	0.000	0.000	0.253	-2.706	0.506	8.092	8.597
	5	0.006	0.006	-0.999	0.999	32.786	-66.831	1.493	7.905	9.397
6-31+G(d)	1	0.351	0.434	-0.023	0.023	0.162	-47.724	0.043	6.773	6.815
	2	0.411	0.599	-0.007	0.007	0.052	2.727	0.023	6.851	6.873
	3	0.775	0.836	0.023	-0.023	-7.163	0.124	7.551	0.103	7.655
	4	0.241	0.406	0.066	-0.066	-17.975	0.784	7.606	0.057	7.663
	5	0.240	0.459	-0.101	0.101	0.736	-35.382	0.112	7.890	8.001
6-311G(d,p)	1	0.604	0.630	-0.002	0.002	0.020	15.736	0.009	7.123	7.132
	2	0.864	0.944	0.000	0.000	2.700	-0.037	7.948	0.128	8.076
	3	0.556	0.609	0.000	0.000	5.102	0.001	8.316	0.001	8.317
	4	0.385	0.412	0.018	-0.018	-11.188	0.426	8.445	0.088	8.532
	5	0.853	0.933	0.000	0.000	0.049	-2.701	0.134	8.415	8.549
6-311++G(d,p)	1	0.243	0.439	-0.029	0.029	0.168	-48.219	0.030	6.812	6.842
	2	0.306	0.600	-0.010	0.010	0.057	3.162	0.022	6.868	6.891
	3	0.211	0.319	0.042	-0.042	-21.221	0.349	7.156	0.035	7.191
	4	0.780	0.847	0.021	-0.021	-6.146	0.107	7.517	0.096	7.613
	5	0.175	0.340	0.055	-0.055	-20.918	0.417	7.720	0.098	7.818

 Table S10: ESP, FBH, and Becke fragment charges (Q_A), FBH and Becke fragment excitation energies (ω_A) for the lowest local excitations and charge-transfer excitations of three C₂H₄-C₂F₄ configurations. Obtained from LR-TDDFT calculations using the PBE0 functional and 6-31G(d) basis set.

Configuration	ES#	Q_A^{ESP} (a.u.)		Q_A^{FBH} (a.u.)		Q_A^{Becke} (a.u.)		ω_A^{FBH} (eV)		ω_A^{Becke} (eV)	
		C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄	C ₂ H ₄	C ₂ F ₄
F	2	0.006	-0.006	0.000	0.000	0.000	0.000	-0.003	7.129	-0.002	7.128
P1	1	-0.041	0.041	-0.010	0.010	-0.010	0.010	0.026	7.074	0.022	7.078
P2	1	0.019	-0.019	-0.001	0.001	-0.001	0.001	0.005	7.121	0.004	7.123
F	1	-0.967	0.967	-0.997	0.997	-0.997	0.997	0.315	6.698	0.307	6.706
P1	2	-1.016	1.016	-0.990	0.990	-0.988	0.988	0.426	6.819	0.423	6.821
P2	2	-0.964	0.964	-0.999	0.999	-0.997	0.997	0.466	6.835	0.463	6.839

2 Geometry of C₂H₄–C₂F₄ Complexes

Energy values (in Hartree) and nuclear coordinates (in Å) of C₂H₄–C₂F₄ configurations, whose monomer geometries were optimized on the ω B97X-D/6-311++G(d,p) level of theory.

```
F
12
-554.0963807
C      0.6628906040    0.0000000000   -2.5000000000
C     -0.6628906040    0.0000000000   -2.5000000000
H      1.2317033864    0.9241285878   -2.5000000000
H      1.2317033864   -0.9241285878   -2.5000000000
H     -1.2317033864    0.9241285878   -2.5000000000
H     -1.2317033864   -0.9241285878   -2.5000000000
C      0.6595916614    0.0000000000    2.5000000000
C     -0.6595916614    0.0000000000    2.5000000000
F      1.3822221343    1.0961774622    2.5000000000
F      1.3822221343   -1.0961774622    2.5000000000
F     -1.3822221343   -1.0961774622    2.5000000000
F     -1.3822221343    1.0961774622    2.5000000000
```

```
P1
12
-554.0965940
C      0.6628906040   -2.5000000000    0.0000000000
C     -0.6628906040   -2.5000000000    0.0000000000
H      1.2317033864   -1.5758714122    0.0000000000
H      1.2317033864   -3.4241285878    0.0000000000
H     -1.2317033864   -1.5758714122    0.0000000000
H     -1.2317033864   -3.4241285878    0.0000000000
C      0.6595916614    2.5000000000    0.0000000000
C     -0.6595916614    2.5000000000    0.0000000000
F      1.3822221343    3.5961774622    0.0000000000
F      1.3822221343    1.4038225378    0.0000000000
F     -1.3822221343    1.4038225378    0.0000000000
F     -1.3822221343    3.5961774622    0.0000000000
```

```
P2
12
-554.0959918
C     -2.5000000000    0.0000000000    0.0000000000
C     -3.8257812080    0.0000000000    0.0000000000
H     -1.9311872176    0.9241285878    0.0000000000
H     -1.9311872176   -0.9241285878    0.0000000000
H     -4.3945939904    0.9241285878    0.0000000000
H     -4.3945939904   -0.9241285878    0.0000000000
C      3.8191833228    0.0000000000    0.0000000000
C      2.5000000000    0.0000000000    0.0000000000
F      4.5418137957    1.0961774622    0.0000000000
F      4.5418137957   -1.0961774622    0.0000000000
F      1.7773695271   -1.0961774622    0.0000000000
F      1.7773695271    1.0961774622    0.0000000000
```

3 Geometry of OLH–water Complexes

Energy values (in Hartree) and optimized nuclear coordinates (in Å) of OLH–water configurations using the ω B97X-D/6-311++G(d,p) level of theory.

HB1			
25			
-1517.3893302			
O	4.2538611198	-1.7102968078	-0.1350976023
C	3.3964102437	-0.8640460222	-0.0859406977
N	2.0273555376	-1.1458831479	-0.0973289914
C	1.3242793726	-0.0708136003	-0.0278193880
S	2.1176375128	1.4902628698	0.0622830011
C	3.7077245615	0.6328554136	-0.0052917195
H	4.3138184598	0.8368822411	0.8777987212
H	4.2834701088	0.9340393659	-0.8810678458
C	-0.1353073011	-0.1142940247	-0.0213642704
S	-0.9789467739	-1.6479280033	-0.1202116923
N	-0.8653056269	0.9466227640	0.0560134334
C	-3.7741242270	-1.2532458443	-0.0762464236
C	-2.4713989033	-0.7633500956	-0.0506952797
C	-2.1987357592	0.6160598787	0.0430297164
C	-3.2599006526	1.5252024173	0.1151242163
C	-4.5510605475	1.0484584333	0.0915766709
C	-4.8070093427	-0.3337940158	-0.0042851212
O	-6.0716069925	-0.8218348565	-0.0301146719
H	-3.9986916083	-2.3094071051	-0.1498797088
H	-3.0518198573	2.5854334539	0.1897401919
H	-5.3849462344	1.7411819787	0.1483214212
H	-6.7047270793	-0.1045243627	0.0268935355
O	6.6343604358	-0.2168495670	0.1563320983
H	6.0017953469	-0.9397810477	0.0343875855
H	7.4890590282	-0.6323942618	0.2664158559
HB2			
25			
-1517.3851365			
O	5.0259513484	-2.0014583322	-0.0316786647
C	4.2870055691	-1.0599050082	-0.0195902268
N	2.8819536360	-1.1520773836	-0.0226945452
C	2.3299593991	0.0045091464	-0.0092913001
S	3.3252712664	1.4573053635	0.0102155570
C	4.7872245795	0.3941181819	0.0016537620
H	5.3923123267	0.5531723007	0.8943126994
H	5.4005646549	0.5775573914	-0.8805935767
C	0.8766259455	0.1614966296	-0.0095077730
S	-0.1660211427	-1.2461002185	-0.0233549430
N	0.2997054642	1.3153765189	0.0013697439
C	-2.8810978010	-0.4791167950	-0.0178181022
C	-1.5241528495	-0.1649122829	-0.0148740276
C	-1.0672891776	1.1677582022	-0.0013652846
C	-1.9937927795	2.2153360921	0.0095735641
C	-3.3381914072	1.9163637961	0.0038500803
C	-3.7720016050	0.5786566290	-0.0106176172
O	-5.1051569251	0.2750575801	-0.0211521256
H	-3.2505920093	-1.4982578426	-0.0204390721

H	-1.6431137918	3.2398060457	0.0209210291
H	-4.0705213241	2.7177214825	0.0090674630
H	-5.6308461690	1.0720591820	0.0620210063
O	-5.3641244758	-2.6073825078	0.1204771076
H	-5.5810960020	-1.6704576957	0.0619820363
H	-5.9193651539	-3.0449055372	-0.5245561629

T1.6

25

-1517.3649052

O	-4.7930287203	1.5941094205	0.1280499006
C	-3.9435865972	0.7517553082	0.0922975267
N	-2.5601893057	1.0176468787	0.0884265343
C	-1.8707695535	-0.0622449643	0.0490702525
S	-2.6766812938	-1.6253285409	0.0057999983
C	-4.2597126006	-0.7518015777	0.0466498860
H	-4.8347924661	-1.0267494424	0.9309521335
H	-4.8500930330	-0.9697932719	-0.8433737380
C	-0.4091348319	-0.0346182506	0.0421194685
S	0.4458955352	1.4974835522	0.0859023645
N	0.3117963693	-1.1019367688	0.0037510161
C	3.2400505115	1.0788022798	0.1056610113
C	1.9303205691	0.5999987520	0.0505104515
C	1.6470148267	-0.7821615018	0.0093919767
C	2.7030881473	-1.7026849679	0.0265958224
C	3.9993285342	-1.2368589283	0.0790654603
C	4.2691419939	0.1478199993	0.1184032553
O	5.5302595850	0.6256924374	0.2038209922
H	3.4719340383	2.1337511749	0.1712485626
H	2.4864778886	-2.7629689814	0.0354238488
H	4.8231418407	-1.9400358178	0.1341814217
H	6.1520619473	-0.0953473168	0.3166390784
H	2.9196211740	-0.3555486229	1.6841345732
O	2.9124016296	-0.4777833107	2.6509028988
H	2.5461490113	0.3323871612	3.0054092039

T1.7

25

-1517.3702160

O	-4.7955588337	1.5942681066	0.1207736146
C	-3.9458103010	0.7521828067	0.0863554274
N	-2.5624496420	1.0185782990	0.0841115317
C	-1.8726395865	-0.0610205586	0.0451429217
S	-2.6779774173	-1.6244548722	0.0013729286
C	-4.2613459832	-0.7514966895	0.0409266175
H	-4.8366808273	-1.0263481110	0.9251138257
H	-4.8513161715	-0.9700489235	-0.8492154203
C	-0.4109046876	-0.0332429320	0.0384745670
S	0.4445454891	1.4984717655	0.0825523376
N	0.3095831484	-1.1008504576	0.0005495449
C	3.2383471771	1.0788304120	0.0953702795
C	1.9289818219	0.6001947097	0.0475609229
C	1.6453788987	-0.7812954558	0.0065322078
C	2.7004751955	-1.7019662586	0.0171444854
C	3.9967404977	-1.2364029162	0.0633689901
C	4.2667675921	0.1477671107	0.1008820777
O	5.5293404089	0.6254821159	0.1710477277
H	3.4710188436	2.1340491245	0.1541219872
H	2.4836859210	-2.7623211380	0.0206186998

H	4.8214125529	-1.9394843362	0.1076784087
H	6.1524277850	-0.0958209687	0.2745542877
H	2.9359488118	-0.3568752410	1.7696232561
O	2.9281144718	-0.4808407006	2.7320471916
H	2.5526100347	0.3262298088	3.0843254814

T1.8

25

-1517.3742191

O	-4.7968532131	1.5949258404	0.1184197734
C	-3.9470461237	0.7529597990	0.0831815456
N	-2.5636671113	1.0195929632	0.0795659686
C	-1.8737668599	-0.0599096642	0.0406064958
S	-2.6789034001	-1.6234927394	-0.0018750736
C	-4.2623927878	-0.7507682652	0.0379376727
H	-4.8376114015	-1.0256645487	0.9221717339
H	-4.8523929855	-0.9694168588	-0.8521716536
C	-0.4119345297	-0.0321278506	0.0329180485
S	0.4438482500	1.4994007964	0.0753794164
N	0.3082052793	-1.0999611371	-0.0037577130
C	3.2375880945	1.0788138977	0.0827550972
C	1.9284288743	0.6005242826	0.0412740847
C	1.6444866690	-0.7806061013	0.0017438672
C	2.6988852950	-1.7014426106	0.0059827358
C	3.9953652089	-1.2362025678	0.0464164310
C	4.2654634735	0.1476094486	0.0834800627
O	5.5289781579	0.6253587424	0.1410915681
H	3.4710305073	2.1342166627	0.1353732787
H	2.4817554629	-2.7618207042	0.0044147170
H	4.8206490362	-1.9393279535	0.0790099207
H	6.1526408892	-0.0953523035	0.2452023944
H	2.9476613567	-0.3688964003	1.8538059641
O	2.9455946340	-0.4779137081	2.8149313048
H	2.5446824240	0.3230856804	3.1531762590

T1.9

25

-1517.3771603

O	-4.7968675731	1.5969244894	0.1115908846
C	-3.9471539640	0.7547940529	0.0781467068
N	-2.5637400985	1.0212339032	0.0752939694
C	-1.8739343005	-0.0583532008	0.0375620770
S	-2.6793094404	-1.6219163055	-0.0037176884
C	-4.2626778889	-0.7489462961	0.0348870850
H	-4.8378797157	-1.0225625729	0.9195481137
H	-4.8528097419	-0.9688068439	-0.8548252038
C	-0.4120996874	-0.0308128581	0.0297892076
S	0.4442160741	1.5004275090	0.0706651510
N	0.3077156535	-1.0989174518	-0.0062854634
C	3.2375640202	1.0794057968	0.0697182360
C	1.9287570292	0.6008588306	0.0367250656
C	1.6443264470	-0.7799189729	-0.0019549414
C	2.6984471837	-1.7007093353	-0.0034989065
C	3.9950118825	-1.2352781115	0.0297273436
C	4.2652175704	0.1483418823	0.0640001228
O	5.5292886489	0.6262094931	0.1093128494
H	3.4712834828	2.1350799783	0.1156573172
H	2.4817406969	-2.7612351056	-0.0080874762
H	4.8208550826	-1.9382705915	0.0528557460

H	6.1544745760	-0.0945954917	0.2029486309
H	2.9562608170	-0.3850780958	1.9391950678
O	2.9622636145	-0.4750309404	2.8998746214
H	2.5197448310	0.3107409384	3.2219053837

T2.0

25

-1517.3792127

O	-4.7958109488	1.5994521710	0.1159949457
C	-3.9465898952	0.7570321045	0.0791366150
N	-2.5629704137	1.0229013275	0.0749881151
C	-1.8737414434	-0.0569362822	0.0351588288
S	-2.6798016947	-1.6200724728	-0.0078915815
C	-4.2627924343	-0.7464710380	0.0324964653
H	-4.8385167305	-1.0218936253	0.9162198349
H	-4.8525568633	-0.9639512233	-0.8580696431
C	-0.4118070575	-0.0298396414	0.0262855317
S	0.4448260510	1.5012244491	0.0657021497
N	0.3076339244	-1.0982582224	-0.0092123827
C	3.2377369931	1.0797384525	0.0576616036
C	1.9293966431	0.6011483514	0.0316933418
C	1.6445903777	-0.7793892411	-0.0056562399
C	2.6981447968	-1.7002252800	-0.0117990616
C	3.9951807319	-1.2347245886	0.0163437312
C	4.2653256116	0.1487603764	0.0478748764
O	5.5297676302	0.6272060702	0.0820648661
H	3.4718930773	2.1355163930	0.0991483349
H	2.4813210081	-2.7608007411	-0.0182635215
H	4.8211632324	-1.9378926706	0.0328705594
H	6.1566315597	-0.0934416407	0.1650418543
H	3.0064570805	-0.4208423347	2.0248812018
O	2.9744591403	-0.4574765578	2.9869204814
H	2.4507548233	0.3028205642	3.2414429934

T2.1

25

-1517.3806181

O	-4.7915291530	1.6011037138	0.1067271921
C	-3.9418644182	0.7589026106	0.0751581744
N	-2.5584517092	1.0255223246	0.0661440469
C	-1.8685971699	-0.0541110863	0.0322003096
S	-2.6738980271	-1.6180615542	0.0028485902
C	-4.2573105527	-0.7451053664	0.0416304741
H	-4.8295770056	-1.0137300490	0.9297158820
H	-4.8503052712	-0.9702619077	-0.8448462642
C	-0.4067291796	-0.0262920921	0.0189812075
S	0.4494724423	1.5051619002	0.0471696316
N	0.3130165947	-1.0947567947	-0.0117611159
C	3.2424447544	1.0846369658	0.0313473585
C	1.9346962538	0.6053076721	0.0142902655
C	1.6501774768	-0.7754728907	-0.0140928344
C	2.7043520012	-1.6960374644	-0.0201721358
C	4.0009205712	-1.2295162560	0.0002595819
C	4.2701671461	0.1541616333	0.0227516099
O	5.5347033476	0.6331720970	0.0444434234
H	3.4760659813	2.1408633995	0.0627745411
H	2.4880780579	-2.7568144607	-0.0235426314
H	4.8276433441	-1.9320195355	0.0112802593
H	6.1624419123	-0.0866320158	0.1278205766

H	2.9461494127	-0.4527285337	2.1043103744
O	2.9703410905	-0.4625130114	3.0658010651
H	2.3982872997	0.2588054017	3.3297943176