# Holistic Prediction of pK<sub>a</sub> in Diverse Solvents Based on Machine Learning Approach

Qi Yang, Yao Li, Jin-Dong Yang, Yidi Liu, Long Zhang\*, Sanzhong Luo,\* Jin-Pei Cheng

Center of Basic Molecular Science, Department of Chemistry, Tsinghua University, Beijing, China, 100084



E-mail: luosz@tsinghua.edu.cn, zhanglong@tsinghua.edu.cn

**ABSTRACT**: The acid dissociation constant  $pK_a$  dictates a molecule's ionic status, and is a critical physicochemical property in rationalizing acid-base chemistry in solution and in many biological contexts. Although numerous theoretic approaches have been developed for predicating aqueous  $pK_a$ , fast and accurate prediction of non-aqueous  $pK_a$ s has remained a major challenge. On the basis of *i*BonD experimental  $pK_a$  database curated across 39 solvents, a holistic  $pK_a$  prediction model was established by using machine learning approach. Structural and physical organic parameters combined descriptors (SPOC) were introduced to represent the electronic and structural features of molecules. With SPOC and ionic status labelling (ISL), the holistic models trained with neural network or XGBoost algorithm showed the best prediction performance with MAE value as low as 0.87  $pK_a$  unit. The holistic model showed better performance than all the tested single-solvent models (SSMs), verifying the transfer learning features. The capability of prediction in diverse solvents allows for a comprehensive mapping of all the possible  $pK_a$  correlations between different solvents. The *i*BonD holistic model was validated by prediction of aqueous  $pK_a$  and micro- $pK_a$  of pharmaceutical molecules and  $pK_a$ s of organocatalysts in DMSO and MeCN with high accuracy. An

on-line prediction platform (http://pka.luoszgroup.com) was constructed based on the current model.

KEYWORDS:  $pK_a$  prediction, machine learning, iBond, XGBoost, neural network, organocatalyst

#### **INTRODUCTION**

The acid dissociation constant,  $pK_a$ , dictates the extent to which a proton dissociates from a molecule. As a fundamental physicochemical parameter defining heterolytic X-H bond (X = C or other heteroatoms) cleavage free energies,  $pK_a$  is also the primary constant for the derivation of other bond energies such as BDE, BDFE,  $pK_a$  (HA<sup>-</sup>), hydride affinity, which provides largely the quantitative basis for the rational evolution of chemistry.<sup>1</sup> Hence, accurate measurement and prediction of  $pK_a$  have been actively pursued in chemical and medical science and continue to be research focus echoing the increasing demand on rational design and development.<sup>1c-1e</sup> Historically,  $pK_a$  was first measured under aqueous media and large quantity of data along this line has been accumulated ever since largely driven by its fundamental importance in assessing the ionic status of biomolecules and pharmaceutical molecules.<sup>2</sup> As heterolytic constant,  $pK_a$  is highly sensitive to solvents. Non-aqueous  $pK_{as}$ , critical for rationalization of acid/base catalysis, energy materials and ADMET of drug molecules in solution, are profoundly different from their aqueous counterparts, as a result of the varied solvation behaviors between a molecule and its derived ions. However, data on non-aqueous  $pK_{as}$  are rather scarce. Analysis of the most extensive public  $pK_a$  database<sup>3</sup> revealed less than 30% non-aqueous experimental pKas distributing across more than 40 non-aqueous solvents (Figure 1). Many efforts have been devoted to rescale or transfer the aqueous  $pK_a$  to its organic solvent counterparts,<sup>4</sup> however, the successes along this line were unfortunately very limited and only applicable to those closely analogue compounds.

In the pursuit of highly accurate  $pK_a$  prediction, quantum mechanical (QM) computation have been extensively explored and could now reach prediction accuracy of MAE <1  $pK_a$  unit in organic solvents,<sup>5</sup>

however, the QM method is time and resource exhausting process particularly for large molecules with more than 50 atoms. On the basis of traditional QSAR (quantitative structure activity/property relationship) strategy,<sup>6</sup> machine learning (ML) algorithms such as random forest, extreme gradient boosting (XGBoost), support vector machine (SVR), neural network (NN), etc. have recently been explored in the predication of  $pK_a$  using either public or industrial data as training sets.<sup>7</sup> The state-of-the-art ML models such as Bayer's "S+pK<sub>a</sub>" (incorporated in the commercial ADMET Predictor software<sup>8</sup>) could reach a mean average error (MAE) below 1 pK<sub>a</sub> unit.<sup>9</sup> The Bayer's model was developed using the so-called Artificial Neural Network Ensembles (ANNEs) on 10 pre-classified libraries of compounds. However, all these ML models are only applicable for aqueous pK<sub>a</sub>s and ML models for non-aqueous pK<sub>a</sub> prediction with reasonable accuracy remain virtually underdeveloped. Very recently, Grzybowski and coworkers developed a prediction model for pK<sub>a</sub> in DMSO with MAE 2.1 pK<sub>a</sub> units by using graph convolutional neural networks (GCNNs), the model was trained with a small data set (817 pK<sub>a</sub>s) composed with half experimental data and half DFT calculated ones and is limited to only C-H acidity prediction in DMSO.<sup>10</sup>

In the past decade, we have engaged in collecting and curating accurate bond energies. In 2016, we established a user-friendly internet-based databank of  $pK_a$  and BDE data: *i*BonD,<sup>3</sup> which is freely available at http://ibond.nankai.edu.cn. The *i*BonD covers more than 30000 experimental  $pK_a$  data for about 20000 compounds in 46 different solvents. With these data in hand, we have developed a holistic model for predicating both aqueous and nonaqueous  $pK_a$  using machine learning algorithm without pre-classification of compounds. The *i*BonD model could provide an accurate prediction over 39 solvents with MAE 0.87  $pK_a$  unit. The model could be successfully applied in the prediction of microstate  $pK_a$ s of pharmaceutical compounds in water and also in the scaling of organocatalysts in DMSO and acetonitrile. We'll present the details on construction and applications of this model in this full article. The model is also incorporated into

a Web version freely available at <u>http://pka.luoszgroup.com</u>, which we hope will become a useful tool for rationalization of acid-based equilibration and reactions in solution.

#### **RESULTS AND DISCUSSION**

#### 1. The dataset

Our holistic model was constructed based on experimental data collected in *i*BonD database. Over the years, the data in *i*BonD has underwent rigorous quality and consistency check: duplicates were removed, errors in structures were corrected and doubtful values were either double-checked with original sources or verified by independent experimental measures. In this study, the  $pK_a$  dataset in *i*BonD was further cleaned and curated according to the following principles: 1) According to the solvent leveling effect,<sup>11</sup>  $pK_a$  data out of each solvent's  $pK_a$  window are excluded from the dataset, and so as for those data were mainly obtained by extrapolation of the experimental data, hence containing large errors; 2) since experimental data extracted from different resources may vary as recorded in *i*BonD, for each molecule with multiple recorded entries, an average  $pK_a$  was used as the output if the variation is less than 2.0  $pK_a$  unit; otherwise the molecule was removed from the training set; and 3) outliers were picked for further scrutiny during the process of model training and in this way we have identified more than 100 errors, mostly arisen from erroneous drawings of structures or typos in  $pK_a$  values. For cases that no clear-cut rationalization on the large  $pK_a$  deviation could be made, the molecules were excluded from the training dataset. The extensive and rigorous vetting process ensures high quality and credibility of the experimental data in *i*BonD to be used for model training.



Figure 1. The  $pK_a$  distribution in different solvents. The blue bar denotes the spanning  $pK_a$  range in each solvent and the amount of molecules are shown in the blue bar.

Eventually, we reached a curated dataset containing 15338 chemical compounds with a total of 19397 p $K_a$  values in 39 solvents. The most applied solvents with more than 400 p $K_a$  data include water (61.7%), DMSO (9.3 %), EtOH/H<sub>2</sub>O (1:1) (8.2 %), CH<sub>3</sub>OH (3.6 %), CH<sub>3</sub>CN (5.2 %) and DMF (2.2 %) and the aqueous p $K_a$  data are dominant (Figure 1). There are 487 compounds with p $K_a$  values available in both of the top 2 solvents H<sub>2</sub>O and DMSO, 187 compounds in H<sub>2</sub>O, DMSO and MeOH, and meanly 3 compounds (acetic acid, protonated pyridine and 4-chloro-3-nitrobenzoic acid) with data available in all the top 6 solvents, indicating the severe scarcity of non-aqueous p $K_a$ s.



Figure 2. Category distribution of the database.

Structurally, the curated *i*BonD dataset consists of mainly N-H (47%), O-H (44%) and C-H (7%) p $K_a$ s and also S-H, P-H and minor other constants (2% in total) (**Figure 2**). The sub-categories of N-H acidity include the p $K_a$ s of protonated amines (68%), sulfonamides (12%), amines (11%) and amides (9%). As for the O-H acidity, the carboxylic acids are dominant (52%) together with 38% for alcohols and phenols as well as minor protonated O-H (6%). For C-H p $K_a$ s, the most experimentally determined ones are for C(sp<sup>3</sup>)-H (99.3%) with minor C(sp<sup>2</sup>)-H (0.4%) and C(sp)-H (0.3%).



Figure 3. Definition of  $pK_a$  subtype on the basis of ionic status.

In *i*BonD, each experimental  $pK_a$  value was assigned to the major responsible ionization site when possible, hence the resulted library of compounds in the curated *i*BonD  $pK_a$  dataset is composed of >50% neutral molecules (ca. 11105 p $K_a$  values), >1/3 protonated molecules (ca. 7104 p $K_a$  values), and a small portion of negatively charged molecules (1224 p $K_a$  values). The latter two types of ionic molecules were annotated as p $K_{aH}$  and p $K_{aN}$ , respectively (Figure 3). Particularly, p $K_{aH}$ , an indication of basicity of a molecule, refers to the dissociation constant of its conjugate acid. A primary concern is the appropriate identification of the site of protonation/deprotonation in regard to the p $K_a$  value. For charged molecules, additional challenge arises when the molecule contains multiple ionization (or titratable) sites. In these cases, the recorded experimental data are macroscopic p $K_a$  values, *i.e.* the acid dissociation constant of a given molecule regardless of individual titratable site (Scheme 1). The acidity of each of the titratable group is known as microscopic p $K_a$ , and the experimentally determined macroscopic p $K_a$  is the net results of equilibration of each microstate according to equation 1 (Scheme 1). For these multi-ionizable charged molecules (both positively and negatively charged ones), we restrict our structural designation to the dominant microstate, of which the microscopic p $K_a$  can serve as a good approximation of the macroscopic constant. We have designated more than 2000 such multi-ionizable compounds in the curated *i*BonD dataset. In a few cases that dominant microstates cannot be unambiguously assigned, the molecules were excluded from the dataset.

In addition, the average Tanimoto similarity was also tested based on comparisons of Morgan  $Fingerprints^{12}$  with radii = 2 of all possible pairs of molecules, only 0.18 was found for the entire set, verifying its structural diversity.



Scheme 1. The relationship between macro- and micro- $pK_a$ 

## 2. Strategies and methods

A workflow for model training is depicted in Figure 4. Firstly, the suitable molecular descriptors were collected to represent the features of the molecules. The acidity of a given compound was mainly determined by its structure and consequently physicochemical properties. Therefore, we introduced in this study Structure and PhysicoChemical (denote also Physical Organic Chemistry) properties combined descriptors (**SPOC**). The **SPOC** was generated by taking into consideration of their general applicability as well as the computation cost. Readily available molecular fingerprints such as MACCS<sup>13</sup>, Estate<sup>X</sup> and Morgan fingerprints<sup>X</sup>, and physicochemical descriptors extracted from the RDKit were screened to account for the electronic and fragment features of molecules. By doing so, the selection-bias can be largely minimized and the expected **SPOC** for each molecule can be generated in milliseconds. The molecules were also annotated regarding their ionic status with respective to neutral ( $pK_a$ ), positively charged ( $pK_{aH}$ ) or negatively charged ( $pK_{aN}$ ) (named as ionic status labeling (**ISL**)) (Figure 3).

A holistic model (HM) was trained over the entire curated iBonD dataset in all the 39 solvents. The HM

would address the issues associated with the scarcity of data in organic solvents in model training. For comparison, single solvent models (SSM) for the top six most used solvents (H<sub>2</sub>O, DMSO, EtOH/H<sub>2</sub>O(1:1), acetonitrile, MeOH and DMF) were also constructed using the individual  $pK_a$  sub-dataset in each of the six solvents. The following model training was performed with a range of algorithms such as Tree Regression, Random Forest, Gaussian Process, Gradient Boosting, Support Vector Machine (SVM), K-nearest Neighbors (KNN), Ada Boost, Bagging Tree and Extra Tree. The Neural Network (NN) was also examined considering its powerful ability in identifying non-linear patterns. In addition, the XGBoost algorithm, which is known for its high efficiency and accuracy, was also tested. Once the optimal algorithms were identified, data curation was first conducted in the preliminary rounds of model training. The final HM model was reached on the curated dataset.



Figure 4. Work flow for the construction of  $iBonD pK_a$  model.

## 3. Model Training

Selections of Descriptors: Selecting suitable descriptors is very critical for the  $pK_a$  prediction task. in this study, we tried to use several molecular fingerprints (MF) such as Morgan fingerprints with 2 or 3 radii, estate and MACC to account for the structural information. In addition, the molecular physicochemical descriptors were generated using RDkit to account for the physical organic chemical (POC) information. The XGBoost algorithm was used to evaluate their prediction performance in a holist model. It is found that the sole use of

either MF or POC descriptor led to RMSE = 1.91 and 1.82, respectively, with the latter performed slightly better (**Figure 5** and SI). Among all the other molecular fingerprints screened, MACC fingerprints showed the best performance. Delightfully, the combination of MACC with POC, the **SPOC**, could improve the prediction with RMSE = 1.70,  $R^2 = 0.92$ . Inclusion of the ionic status label (**ISL**) in this **SPOC** descriptor could further improve the results to RMSE = 1.50,  $R^2 = 0.94$ . The following model construction were performed with **SPOC-ISL** descriptors.



Figure 5. The selection of descriptors based on holistic model training with XGBoost.

Screening of algorithms. To find the most suitable ML algorithm for the  $pK_a$  prediction task of HM, a 5fold cross validation (CV) was performed based on the whole dataset. The average results of the five runs were used as the CV statistic. Among different algorithms examined (**Figure 6A**), full collected neutral network (NN) with three hidden layers was found to give the best results with RMSE = 1.41, MAE = 0.87 and R<sup>2</sup> = 0.95 (**Figure 6C**). To avoid overfitting, the early stopping was used to halt the training of neural network. The XGBoost algorithm also gave comparable results with RMSE = 1.50, MAE = 0.88 and R<sup>2</sup> = 0.94 (**Figure 6B**). Other boosting methods such as Gradient boosting and Ada boost showed slightly poorer performance, The Gaussian process was also a good choice, with RMSE = 1.59, MAE = 0.92 and R<sup>2</sup> = 0.93. Based on these results, the following model training and validation were performed with NN and XGBoost algorithm.



**Figure 6.** The 5-fold cross-validation of **HM** with different ML methods (**A**): 1-Tree regression; 2-Random Forest; 3- Gaussian Process; 4-Gradient Boosting; 5-SVM; 6-KNN; 7-Ada Boost; 8-Bagging Tree; 9-Extra Tree; 10-NN; 11-XGBoost; the performance of XGBoost (**B**) and Neutral Network (**C**) model.

**Comparison of SSM and HM.** As experimental  $pK_a$  values in organic solvent are only sparsely available, the training of SMM in these solvents would suffer from lacking of data with high risk of overfitting. For the holistic model in 39 solvents, it is expected that the hidden relationship between  $pK_a$  values in different solvents could be gleaned during the model training. To verify this hypothesis, we reorganized the  $pK_a$  data in the most widely used six solvents by randomly splitting into 80:20 ratio of training and testing subsets, and the individual training and testing subsets were then separately combined to train a holistic model **HM**-

**6S** (Figure 7, A). As clearly illustrated in Figure 7B, HM-6S performed better than all the six SMMs with the same testing set. HM-6S, with MAE = 0.89, was comparable with the holistic model for 39 solvents. These results indicated that the HM was more robust than the SSM, and some structural and physiochemical features among molecules in different solvents were indeed learned during the model training process.

It is worthy to note that MAE of **SMM** models varies dramatically, and exceptional large MAE was observed in DMSO and acetonitrile. This can be rationalized by considering the varied range of  $pK_a$  values between different solvents due to the solvent-leveling effect. For example, the recorded  $pK_a$  ranges of DMSO and acetonitrile in *i*BonD are -6.08~35.1 and -3.7~33.3, respectively. In comparison, those for EtOH/H<sub>2</sub>O (1:1) and MeOH were much narrow as -0.54~14.7 and -0.67~22.74, respectively. Indeed, the lowest MAE was observed in EtOH/H<sub>2</sub>O with the narrowest  $pK_a$  distributions.



Figure 7. The construction of SSM and HM-6S model (A) and their comparison (B).

The  $pK_a$  correlation between different solvents. As experimental  $pK_a$  values are dominant in aqueous media and to a much less extent also DMSO, the direct scaling and transfer of these data to other solvents have been extensively explored according to the free energy relationship  $pK_a$  (solvent 1) = a\*  $pK_a$  (solvent 2) + b.<sup>14</sup> However, good linear correlations have only been observed in structurally related analogue compounds.<sup>15</sup> The current holistic model **HM** allows us to correlate  $pK_a$ s between different solvents over a

broad range of molecular structures. Hence,  $pK_{as}$  in top six solvents for the entire *i*BonD compounds (15338) compounds) were predicted and analyzed for the intrinsic free-energy relationship between any pair among the six solvents (Table S6, SI). The obtained correlation was also compared with the experimental one if sufficient experimental  $pK_{as}$  are available., A survey of the correlation data revealed the following general trends (Figure 8, see also Table S6 in SI): 1) Good linear correlations (with  $R^2 > 0.9$ ) were generally not observed. Protic solvent pairs such as H<sub>2</sub>O/EtOH-H<sub>2</sub>O (1:1) and MeOH/EtOH-H<sub>2</sub>O (1:1) showed good correlations due to their similar solvation behaviors. This similarity has been used to estimate the  $pK_a$  value in pure water via Yasuda-Shedlovsky extrapolation.<sup>16</sup> As for the aprotic polar DMSO-DMF pair, their properties are extremely similar and the correlation with experimental data also give a perfect linear relationship ( $R^2$ =0.98, Figure S11 in SI); 2) like-solvents correlate better than the like-unlike pairs do. Among the six examined solvents (protic: H<sub>2</sub>O, EtOH/H<sub>2</sub>O and MeOH; aprotic: DMSO, MeCN and DMF), DMSO- $H_2O$  combination shows a rather poor correlation with  $R^2 = 0.66$ . In comparison, the  $R^2$  of DMSO-MeCN is 0.74. The H<sub>2</sub>O-DMSO-MeCN 3D-plot shows much scattered distribution than that of H<sub>2</sub>O-MeOH-EtOH/H<sub>2</sub>O plot (Figure 8, A vs B). Similar pattern was also observed between DMSO-MeCN-EtOH/H<sub>2</sub>O and DMSO-DMF-MeCN (Figure 8, C vs D); 3) Generally, the predicated correlations are in good consistence with the experimentally determined ones with slightly better R<sup>2</sup>. Large deviation was observed for the DMSO-EtOH/H<sub>2</sub>O, MeCN-DMF and MeOH-DMF solvent pairs (Table S6, entries 8, 13 and 15). These exceptions were mainly caused by the few experimental data found in the dataset and its irregular distribution (See Figure S9, 14 and 16, SI). In all, these observations clearly showed that the inherent link and different solvation behaviors have been learned during the training of the holistic model.



**Figure 8.** The 3D-scatter plot of p*K*<sub>a</sub> data in different solvents, **A**: MeCN-H<sub>2</sub>O-DMSO; **B**: MeOH-H<sub>2</sub>O-EtOH/H<sub>2</sub>O (1:1); **C**: EtOH/H<sub>2</sub>O-DMSO; **D**: EtOH/H<sub>2</sub>O-DMSO-DMF (Grey: Scatter plot in 3D-space; Red: Projection on XY-plane; Green: Projection on XZ-plane; Blue: Projection on YZ-plane).

## 4. Verification and application of the model

The obtained holistic model (**HM**) was further tested in out-of-sample predications and three representative applications are shown herein.

**Macro and micro-p** $K_a$  prediction of pharmaceutical molecules in H<sub>2</sub>O. In the year of 2017, a blind p $K_a$  prediction challenge named SAMPL6 has been established by the Drug Design Data Resource Community,<sup>17</sup>

which consists of predicting microscopic and macroscopic  $pK_a$  of 24 drug-like small molecules (17 drugfragment-like and 7 drug-like). The submitted prediction strategies included quantum-chemistry based calculation,<sup>18</sup> EC-RISM theory,<sup>19</sup> QM/MM approach,<sup>20</sup> ab initio quantum mechanical prediction<sup>21</sup> as well as machine learning.<sup>22</sup> The machine learning methods were built with the general Gaussian process with unfortunately only moderate accuracy. Based on the HM-XGBoost model, we obtained a prediction with MAE = 0.80 and RMSE = 1.07 (Figure 9 and Figure S17A). The prediction with holistic NN model also gave comparable results (See SI, Figure S17B), with slightly higher MAE and RMSE. In contrast, the prediction with the **SSM-H<sub>2</sub>O** model gave a higher MAE of 0.92, further confirming the robustness of the **HM** model. Significant overestimate for SM14 ( $\Delta pK_a = 2.45$ ) and SM24 ( $\Delta pK_a = 1.58$ ) were observed, it was deduced that the large deviations come from the doubly protonated status for which the examples in the training data are extremely rare in *i*BonD. Large deviations were also observed for SM03 (+2.0), SM05 (+1.99) and SM18a





Figure 9. The prediction of SAMPL6 puzzles with the HM-XGboost model

Most biologically active molecules contain multiple protonation/deprotonation sites, their site-specific micro-p $K_a$ s are critical in the rationalization of their pharmaceutical profiles. To verify the capability of our holistic model in predicting micro-p $K_a$ s, 17 pharmaceutical molecules with multi-dissociation sites, which were not included in the original data set, were selected as external validation set.<sup>23</sup> As shown in **Figure** 10, the results with HM-XGboost are extremely good with the average MAE = 0.44. In these cases, the micro-p $K_a$  of all dissociable sites were predicted independently and the macro-p $K_a$  were calculated according to equation 1 (Scheme 1). The micro-p $K_a$  provides a definitive assignment of the protonation sites as well as the determination of the equilibrium distributions. For example, for Thenalidine, Aprindine and Methaphenilene, protonation would mainly occur on the tertiary amine moieties with few on the aromatic nitrogen (< 0.05%) under physiologic pH. While for Metoclopramide, though protonation onto primary amine is still dominant, protonation on aromatic nitrogen is unneglectable and constitutes about 35%.



Figure 10. The  $pK_a$  prediction of pharmaceutical molecules with HM-XGboost, micro- $pK_a$ s were shown in blue.

Prediction and scaling of organocatalysts acidity in DMSO. Hydrogen-bonding (HB) moieties,

ubiquitous structural units in chiral organocatalysts, are critical in tuning both activity and stereoselectivity via hydrogen-bonding interaction or acid catalysis to a broad sense. Acidity, represented by  $pK_{as}$ , is one of the key physicochemical parameters that define HB catalytic properties. We and others have experimentally determined the  $pK_{as}$  for a series of organocatalysts including thiourea, squaramide, BINOL, prolinamides and 6'-hydrogen bonding cinchona alkaloids (6'-HBCA) in DMSO.<sup>24</sup> In total, an external set involving 84 organocatalysts' pKas, not included in the training set, were tested with HM-XGBoost. As shown in Figure 11, the prediction of thioureas and prolinamides gave extremely accurate results, with MAE = 0.16 and 0.23respectively. The prediction of squaramides also give good results, with MAE = 0.64. These predictions even surpassed the results obtained with DFT calculations.<sup>25</sup> In contrast, the prediction of Binol-type hydrogen bond catalysts showed relatively poor accuracy and most of the  $pK_a$  value were overestimated. It should be noted that the internal H-bonding between the two phenol groups may significantly enhance the acidity of the molecule, however, the HM model likely failed to identify this feature due to lack of examples in the training set. As for the 6'-HBCA, the prediction is slightly worse than mean accuracy, possibly caused by the partially zwitterionic form for these molecules. The overall MAE for the five types of organocatalysts was 1.01.



**Figure 11.** The  $pK_a$  prediction of organocatalysts.

**Prediction and scaling of aminocatalysts basicity in MeCN.** The nucleophilicity of aminocatalysts is a key parameter that defines their catalysis in enamine or iminium-based transformations. The  $pK_{aH}$  of aminocatalyst is frequently employed as a rough estimation of its nucleophilicity. Recently, Mayr and coworkers have experimentally determined the  $pK_{aH}$  of a series of commonly used secondary aminocatalysts, including those privileged ones. <sup>26</sup> The acidity of these protonated molecules ranges from 10.54 to 24.02. These data were used as out-of-sample test for our model. To our delight, the **HM** performed quite well (**Figure** 12) and the overall MAE was found to be 1.57. Considering that only 1017  $pK_a$  records in MeCN can be found in the original datasets, the slightly large MAE was reasonable and acceptable. The imidazolinones and silyl substituted pyrrolidines showed large deviations, possibly caused by the lack of examples in training set. It should be noted that most of the predicted values in these cases were underestimated, indicating the influence of the appended substituents to the pyrrolidinyl core was overestimated.



Figure 12. The  $pK_{aH}$  prediction of aminocatalysts in MeCN

#### CONCLUSION

In summary, we have developed a holistic  $pK_a$  prediction model (**HM**) based on the *i*BonD experimental  $pK_a$  dataset. Structural and physicochemical combined descriptors (**SPOC**) were introduced to represent

molecular features and the optimal model was identified with Neural Network and XGboost algorithm, showing accuracy of MAE = 0.87 and 0.88 p $K_a$  unit, respectively. The *i*BonD **HM** model provides so far the best accuracy in prediction non-aqueous p $K_a$ s and is equally applied for aqueous and micro- p $K_a$  prediction. The superior performance of **HM** over **SSM** verified the transfer learning from one solvent to another. The capability in predicting p $K_a$ s in diverse solvents allows for a comprehensive mapping of the p $K_a$  relationships between different solvents. Finally, the robustness of this HM was validated in out-of-sample predictions of aqueous p $K_a$ s of pharmaceuticals, p $K_a$ s and p $K_{aH}$  of organocatalysts in organic solvents (DMSO and MeCN) with good accuracy. We also provide a website interface for this p $K_a$  prediction model (http://pka.luoszgroup.com), which we hope will become a useful tool for the scientific community in rationalizing acid-base chemistry.

## **AUTHOR INFORMATION**

Corresponding Author

Luosz@tsinghua.edu.cn

zhanglong@tsinghua.edu.cn

Notes

Any additional relevant notes should be placed here.

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