The Role of Sodium Sulfate Supporting Electrolyte in Ammonium Transport and Reduction at Interface Between Platinum Cathode and Solution

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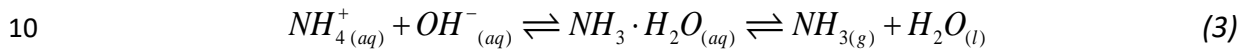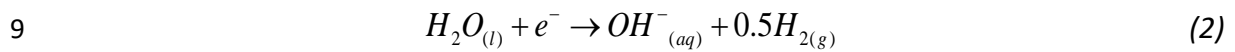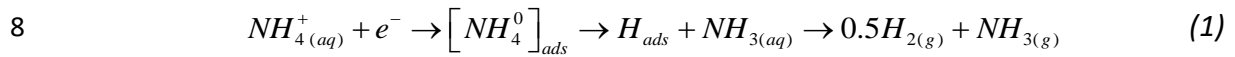[*]*Corresponding author: dophegood@gmail.com; phone: +86-88521315*

Abstract

Ammonium is a potential hydrogen fuel and can be recovered from high ammonium wastewater via electrodeionization (EDI) process. Since NH_4^+ is a weak acid ion, sodium sulfate (Na_2SO_4) is used as a supporting electrolyte to improve electrolyte's conductivity. This manuscript investigated the NH_4^+ behaviors in high Na_2SO_4 solution through electrochemical analysis methods and molecular dynamics (MD) simulations. Ionic strength increased, leading to a decreased ionic activity, and thus negatively influenced NH_4^+ transportation with the increasing concentration of Na_2SO_4 solution. Na^+ competitively occupied the place of electric double layer (EDL) and impeded NH_4^+ to get closer to the electrode surface. Besides, water molecules played a critical role in determining the net charge density and the potential drop. The experimental tests and theoretical simulation demonstrated that NH_4^+ reduction ($NH_{4\,(aq)}^+ + e^- \rightarrow 0.5 H_{2(g)} + NH_{3(g)}$) in the cathode was strengthened in the low concentration range (0-0.25 M Na_2SO_4) but inhibited in the concentration range of 0.5-1.5 mol L^{-1}.

Keywords   Supporting electrolyte concentration, Ammonium transport and reduction, Electric double layer, Molecular dynamic simulation

1   Introduction

The concentrated ammonium existing in wastewater and landfill leachate can be recovered as ammonia and hydrogen gas via electrodeionization (EDI) [1]. NH_3 generation has two paths: (1) NH_4^+ is reduced to proton and NH_3 via a one-electron transfer process in the EDI cathode (Eq. 1) [2]; (2) Water splits into OH^- that reacts with NH_4^+ to generate NH_3 (Eq.2 and Eq.3) [3]. NH_4^+ reduction is more likely to occur other than water splitting when EDI is process operated at the low applied voltage (<1.23 V).

$$NH_{4\,(aq)}^+ + e^- \rightarrow \left[NH_4^0 \right]_{ads} \rightarrow H_{ads} + NH_{3(aq)} \rightarrow 0.5H_{2(g)} + NH_{3(g)} \tag{1}$$

$$H_2O_{(l)} + e^- \rightarrow OH^-_{(aq)} + 0.5H_{2(g)} \tag{2}$$

$$NH_{4\,(aq)}^+ + OH^-_{(aq)} \rightleftharpoons NH_3 \cdot H_2O_{(aq)} \rightleftharpoons NH_{3(g)} + H_2O_{(l)} \tag{3}$$

During NH_4^+ reduction, slow mass transfer determines the generation of NH_3 gas since NH_4^+ is a weak acid ion. To solve this issue, a strong electrolyte such as sodium sulfate is usually added as the supporting electrolyte to enhance electrolyte's conductivity [2, 4-9]. However, the added co-ion often provokes a competition with the target ion. As reported by Casadellà et al. who studied the cation completion of K^+, Na^+ and NH_4^+ in urine through polymer inclusion membranes, the order of selective recovery ($K^+ > Na^+ > NH_4^+$) and two-fold flux in Na^+ (4.5×10^{-3} mmol cm^{-2} h^{-1}) over NH_4^+ (1.5×10^{-3} mmol cm^{-2} h^{-1}) was observed [10]. Liu et al. conducted a study on the competitive transport of Na^+ and NH_4^+ in bioelectrochemical systems and concluded that Na^+ in anolyte facilitated the transport of NH_4^+ due to the Donnan equilibrium at cation exchange membrane-anolyte/catholyte interfaces [9]. Rosasco et al. investigated cation competition in the electrical double layer

3

22 (EDL) at a well-defined Pt (111) electrode surface and found the strength order of cation

23 retention, $Na^+ > NH_4^+$, which might be related to the hydrated radius of Na^+ (3.58 Å) over

24 that of NH_4^+ (3.31 Å) weakening electrochemical activities, e.g., charge density, dielectric

25 constant, and rate capability [11-15]. Besides, some researchers reported that the

26 accumulated Na^+ attracted to water molecules and built a compacted Na^+-H_2O layer,

27 which deterred the electrochemical reaction kinetics [16, 17]. Others depicted that Na^+

28 competitively reduced the effective current efficiency of NH_4^+ and produced electrode

29 overpotential at a fixed electric current [18-21]. Therefore, the influences of Na^+ on the

30 behaviors of mass transportation in the EDL cannot be ignored when Na_2SO_4 is used as

31 the supporting electrolyte.

32 Mass transportation in the EDL is investigated through theoretical simulation other than

33 experimental tests due to the measuring difficulties of the transport coefficient and mass

34 quantification. The classical theories of the mass distribution in the EDL includes Fick's

35 diffusion laws, Nernst-Planck, and Nernst-Einstein equation. The latest theoretical

36 simulations such as molecular dynamics (MD) simulations built on EDL theories are

37 increasingly popular because simulations from the molecular level can deliver insightful

38 information about the interactions at the electrode interface. For instance, Soroosh and

39 Hai conducted MD simulations of flexible-boundary Quantum Mechanics/Molecular

40 Mechanics to reveal ion solvation and found that NH_4^+ had a more significant discrepancy

41 in the extent of charge transfer (by about 0.3 e[-]) and more extensive distribution than Na^+

42 (0.1 e-) [12]. Soetardji et al. used the Langmuir model to study NH_4^+ removal from

43 wastewater via sodium hydroxide modified zeolite mordenite and found that the

44   competition from Na^+ decreased the removal efficiency of NH_4^+ through the different

45   reaction mechanisms [21]. To date, however, NH_4^+ transport at the interface of Pt-

46   solution under the different gradients of Na^+ concentration has not yet been well studied.

47   The objective of this study is to understand the mechanism of supporting electrolyte

48   concentration affecting NH_4^+ behavior and provide the opportunity to elucidate the

49   related molecular-level mechanism. Therefore, we employed electrochemical tests

50   combined with MD simulations to examine the effects of Na_2SO_4 concentration on NH_4^+

51   migration, reduction, and electric properties of the cathodic EDL.

52   **2   Experimental tests and theoretical calculation**

53   2.1   Experimental tests

54   *Equipment setup.* Figure 1 shows the configuration of a sandwich-type EDI stack. The

55   working volume is 40.0 cm^3: 60.0 mm × 60.0 mm × 11.0 mm, in which the 11.0 mm

56   included a 10.0 mm distance between the anode and the cathode and 1.0 mm thick

57   silicone gaskets. The electrodes were titanium plates coated in a 0.02 mm thick layer of

58   platinum, with a 16.0 cm^2 effective area. The original electrolyte was 0.25 M ammonium

59   sulfate, which was then mixed with 0–1.5 M sodium sulfate supporting electrolyte at a

60   25.0 °C operating temperature. The conductivity was measured with a conductivity meter

61   (Shanghai Leici-Chuangyi Instrument and Meter Co., Ltd).

62   *Cyclic voltammetry scanning.* The tests of current density versus applied voltage were

63   carried out using the EDI stack as described above. The scanning electrolyte was the

64   mixtures of fixed ammonium sulfate (0.25 M) and changed the concentration of sodium

65   sulfate (0.125-1.5 M).   The reference electrode was Ag/AgCl-217 (INESA Scientific

66   InstrumentCo.ˏ Ltd) that has a double-salt bridge. The current was recorded and

67   analyzed by the electrochemical working station (CorrWare®, Scribner Associates Inc.,

68   U.S.A.), as shown in Figure 1.

69   2.2   Computational methods

70   *Electrode/electrolyte interface modeling.* The simulation system was a three-dimensional

71   supercell with periodic boundary conditions, constructed in the Materials Studio software.

72   It was composed of Pt sheets (50 Å × 50 Å) as electrodes and the electrolyte aligned in

73   parallel with an interlayer distance of 140 Å, shown in Figure SI-1(a). To simulate the Pt

74   electrode/electrolyte interface, water molecules and NH_4^+ with different concentrations

75   of Na^+ and SO_4^{2-} were added to the space between anode and cathode. Both anode and

76   cathode were Pt (100) surface consisting of 338 atoms, 7 layers for each pole. The

77   numbers of the atoms of the Pt-solution system are summarized in Table SI-1 and Table

78   SI-2.

79   *Equilibrium relaxation and data collection.* MD simulations were performed using the

80   Atomic/Molecular Massively Parallel Simulator package (LAMMPS) at a temperature of

81   300 K and a pressure of 1 atm [3, 22]. The interatomic interactions were simulated using

82   Lennard-Jones (LJ) potential as described in Eq. 4:

83
$$E = 4\xi_{LJ}\left[\left(\frac{d_{LJ}}{r}\right)^{12} - \left(\frac{d_{LJ}}{r}\right)^{6}\right]$$
(4)

84 Where ξ_{LJ} and d_{LJ} are the respective parameters of energy and length, as summarized in

85 Table SI-2. The electrostatic interaction between charged atoms was calculated using

86 Coulomb's law (Eq. 5) with the Coulombic interactions computed using the particle-

87 particle particle-mesh (PPPM) algorithm [23].

88
$$E = \frac{Cq_1q_2}{\varepsilon r}$$
(5)

89 where C is an energy-conversion constant, q_1 and q_2 are the charges carried by two atoms,

90 ε is the dielectric constant. Bonds and angles among atoms are held rigid using the SHAKE

91 algorithm [24]. Water molecules are simulated using the rigid SPC/E water model and the

92 Pt atoms are held fixed [25]. The NVT ensemble simulations were carried out at 300 K

93 with Langevin thermostats for 1.0 ns with a 0.5 fs time step size. NPT ensemble

94 simulations at 1 atm and 300 K were then carried out.

95 After the systems reaching the thermal equilibrium state, we collected data (i.e., mass

96 density, number density, mean square displacement (MSD), radial distribution function

97 (RDF), etc.) during an NVE ensemble for 0.5 ns, as displayed in Figure SI-1(b) and Figure

98 SI-1(c). A voltage of 3.0 V was applied to the solution by applying the corresponding

99 electrostatic forces $F = qE$ on each charged atom. For post-processing the results, the

100 channel was split into a set of bins (1.0 Å in width) along the direction (x) perpendicular

101 to the Pt surface. The mass density $\rho(x)$ was then used to analyze the EDL structures.

102   2.3   Data analysis

103   *Charge density*. Charge density is an important property for analyzing EDL. According to

104   the axial number density of atoms, the total charge density profile, $\sigma_{q(x)}$, is contributed by

105   ions and water, as expressed in Eq. 6.

106

$$\sigma_{q(x)} = \sum_{i \ni surf} \sigma_i(x)q_i + \sigma_O(x)q_O + \sigma_H(x)q_H \qquad (6)$$

107   where σ_i, σ_O, and σ_H are the number densities of ions, water–oxygen, and water–hydrogen,

108   respectively. q_i, q_O, and q_H are the charges carried by them, respectively.

109   *Electric field and potential profiles.* Electric field strength and potential oscillate with

110   variations in charge density. The electric field ($E_{q(x)}$) component normal to the Pt surface

111   was calculated by integrating the net charge density as described by Eq. 7.

112

$$E_{q(x)} = -\left(1/\epsilon_0\right)\int_{-\infty}^{x} \sigma_q(x')(x-x')dx' \qquad (7)$$

113   The potential was computed by integrating the Poisson equation in one dimension, as

114   described in Eq. 8.

115

$$\frac{\partial^2 V(x)}{\partial x^2} = -\frac{\sigma(x)}{A_{Pt}\varepsilon_0} \qquad (8)$$

116   where $\sigma(x)$, A_{Pt}, and ε_0 are the net charge density, the size of the Pt sheet and the vacuum

117   dielectric constant, respectively. Eq. 8 was numerically integrated to obtain *V(x)*, as shown

118   in Eq. 9 using *x=L/2* (the middle of the channel) as a reference that was regarded as zero

119   charge density (Eq. 9).

120
$$V(x) = \int \int_{L/2}^{x} \frac{\sigma(x)}{A_G \varepsilon_0} dx^2 \qquad (9)$$

121 *Mean square displacement (MSD).* MSD is expressed by R^2 that is a measure of the length

122 of the path of a molecule traveled. It is directly related to the diffusion coefficient of this

123 molecule through Einstein's equation [26]. As a result, MSD can be used to gain insight

124 into transport phenomena [27]. MSD in MD simulation can be calculated as:

125
$$R^2 \equiv \left\langle \left(x - x_0 \right)^2 \right\rangle = \frac{1}{N} \sum_{n=1}^{N} \left(x_n(t) - x_n(0) \right)^2 \qquad (10)$$

126 where N is the number of particles to be averaged, $x_n(0) = x_0$ is the reference position of

127 each particle, and $x_n(t)$ is the position of each particle at time, t. By tracking the molecular

128 positions, the MSD of the particles was calculated to quantify ion and water transport in

129 the EDL.

130 *Diffusion coefficient.* The diffusion coefficient is the rate of mass transport, as described

131 by the slope (r) of the *MSD* versus t curves (Eq. 11) from Einstein's equation.

132
$$D = \lim_{t \to \infty} \frac{1}{6t} \left\langle \left[r(t) - r(0) \right]^2 \right\rangle \qquad (11)$$

133 where r and t are atomic compound position and time, respectively.

134 *Radial distribution function (RDF).* RDF is defined as Eq. 12.

135
$$g(r) = \rho(r) / \rho \qquad (12)$$

136 where $\rho(r)$ is the local number density of atoms at a given radius; ρ is the average mass

137 of the whole solution.

3   Results and discussion

3.1   Ion transport in interfacial solution via experimental tests

3.1.1 Solution properties

The influence of Na_2SO_4 concentration on ion strength and activity coefficient [28, 29] of

NH_4^+ ($z_i=1$, $a_i^0=0.3$ and $b_i=0.2$) was plotted (Figure 2(a)). The ion strength is strengthened

from 1.0 M at 0.125 M Na_2SO_4 to 5.5 M at 1.5 M Na_2SO_4. However, the activity coefficient

of NH_4^+ goes down from 0.3 to 0.05, signifying that the increased concentration of

supporting electrolyte negatively affected the activity of NH_4^+. The concentration also

influenced pH value and conductivity. As shown in Figure 2(b), pH value experiences a

sharp increase as the concentration of Na_2SO_4 solution below 0.5 M but a smooth increase

to 9.99 at 1.5 M, indicating that increasing the concentration of Na_2SO_4 solution does not

bring an apparent effect on pH value in the concentrated range.

3.1.2 Ion migration

The changed characteristics caused by ion strength and activity impacts ion transport in

the interfacial solution. Ion migration can be described through viscosity and mobility.

Viscosity calculated based on Jones-Dole`s equation [30-32] experiences a slow

growth from 80 mPas below 0.25 M, and a sharp climb to 330 mPas at 1.5 M. The visible

increase in dynamic viscosity reflects that increasing concentration lowers the liquidity of

bi-electrolyte so that produces a high resistance to ion migration (Figure SI-2). The

variations of ion mobility and number calculated according to $\mu=ez/6\pi\eta r$ [33] were

158   summarized in Table 1. NH_4^+ has an increase in mobility from 1.01 m^2 V^{-1} s^{-1} to 1.49 m^2 V^{-1}

159   ^{1} s^{-1} at 0.125 M, but a drop to 1.27 m^2 V^{-1} s^{-1} at 1.5 M. Na^+ and SO_4^{2-} have drops to 1.63

160   m^2 V^{-1} s^{-1} and 0.81 m^2 V^{-1} s^{-1}, respectively. Concerning transport number, both NH_4^+ and

161   SO_4^{2-} decreases from 0.17 and 0.5 at 0.125 M to 0.08 and 0.28 at 1.5 M, respectively.

162   However, Na^+ increases to 0.64 at 1.5 M. The results of ion transport reveal that the large

163   hindrance may lead to the lack of NH_4^+ as an electron carrier at the cathode interface,

164   which has been elaborated by Pal [16].

165   3.2   Ion transport in electric double layer via MD simulation

166   3.2.1 Ion diffusion coefficient

167   Due to the limitation of experimental detection, the diffusion coefficient was elaborated

168   using MD simulation. The migrations of NH_4^+ and Na^+ in the EDL were quantified via the

169   MSD values of N and Na atoms. The average MSD slope of the N atoms grows from 2.1874

170    $\times 10^3$ at 0 M to 3.1687 $\times 10^3$ at 0.25 M but drops to 1.457 $\times 10^3$ at 1.5 M in 0–1.5 M Na_2SO_4

171   and as a function of time of 0.5 ns (Table SI-3). The corresponding diffusion coefficient of

172   NH_4^+ increases from 2.1874 $\times 10^{-9}$ m^2 s^{-1} at 0 M to 5.2812 $\times 10^{-9}$ m^2 s^{-1} at 0.25 M but falls

173   to 2.4319 $\times 10^{-9}$ m^2 s^{-1} at 1.5 M as displayed in Figure 3(a) and Figure 3(b). The largest

174   diffusion coefficients are obtained at 0.25 M. For the over-concentrated Na_2SO_4

175   electrolyte (> 0.5 M), the diffusion coefficient of Na^+ is smaller than that of NH_4^+, meaning

176   that the concentrated Na^+ does not only impede NH_4^+ migration but also influence it self-

177   transport. For the dilution, the trend of the diffusion coefficient can be explained by the

178   Nernst-Einstein equation that establishes the relationship between the molar limiting

179   conductivity ($\Lambda_{m,i}^0$) and the diffusion coefficient D_i [34].

$$D_i = \frac{RT}{z_i^2 F^2} \Lambda_{m,i}^0 \qquad (13)$$

180

181   where z_i, T, F, and R are charge number of ion i, absolute temperature, Faraday's constant,

182   and the ideal gas constant, respectively. The diffusion coefficients linearly rely on the

183   molar limiting conductivity ($\Lambda_{m,i}^0$). However, this formula becomes more complicated for

184   the concentrated solution. The diffusion coefficient is also related to the trajectories of

185   the particle [35]. Namely, the decreases of diffusion coefficients may be caused by the

186   charge neutralization in OHP [36, 37]. Apart from Na^+ and NH_4^+, water molecular should

187   not be ignored since the H-H bond effect on the electronic structure is essential for

188   understanding the physical and chemical properties of the EDL [38, 39]. From the calculated

189   results of average MSD slope of water molecules using Einstein's equation, its diffusion

190   coefficient of D_{water}, 7.5×10^{-9} m^2 s^{-1} indicates that water molecules have the largest

191   migration coefficient (Figure SI-3). This trend is because the self-diffusion and interdiffusion

192   coefficients decrease with an increase of salt concentration and water molecules in pure water

193   diffuse faster than in concentrated electrolyte. Our simulation results are in good

194   agreement with the study conducted by Kong et al. and Lyubartsev and Laaksonen [40,

195   41]. Therefore, the order of diffusion constants of NH_4^+, Na^+ and water is $D_{water} > D_{Na+} >$

196   D_{NH4+} in the diluted concentration, and $D_{water} > D_{NH4+} > D_{Na+}$ in the concentrated Na_2SO_4

197   solution.

198   3.2.2 Ion concentration distribution

199   The concentration distribution was described with mass density calculated via the mass

200   coordinate. Figure 4 shows the distributions of the mass density of NH_4^+ and Na^+ along

201   the x-axis near the cathodic surface. Specifically, NH_4^+ density increases to the most

202   significant peak (0.016 g cm^{-3}), which is a compacted charge layer called the inner

203   Helmholtz plane (IHP) in the region nearest to the Pt surface [42, 43]. As the distance

204   extending to the bulk solution, NH_4^+ density displays the second peak (0.007 g cm^{-3}, on

205   average) that is considered the outer Helmholtz plane (OHP). When the distance extends

206   further away from the Pt surface, NH_4^+ density stabilizes at 0.0045 g cm^{-3} in Figure 4(b),

207   which is regarded as the diffusion layer (DL) [44]. The distribution profile of Na^+ has similar

208   peaks to that of NH_4^+ along the x-axis (Figure 4(d)), whereas the peak of Na^+ closest to the

209   Pt surface increases from 0 g cm^{-3} at 0 M to 0.018 g cm^{-3} at 1.5 M with the bulk Na_2SO_4

210   electrolyte concentrate. The comparison of the concentration distribution of NH_4^+ and

211   Na^+ in Figures 4(c) and 4(d) shows that the NH_4^+ density reduces from 0.016 g cm^{-3} to

212   0.003 g cm^{-3}, which is significantly lower than that of Na^+ at the corresponding

213   concentration. The difference in the concentration distributions of NH_4^+ and Na^+ may

214   depend on the diffusion coefficient since the diffusion coefficient of NH_4^+ is smaller than

215   that of Na^+. Additionally, the concentration profiles of NH_4^+ and Na^+ indicate that the

216   lowered peak of NH_4^+ is caused by the competitive increase of Na^+ concentration,

217   especially in the over-concentrated Na_2SO_4 electrolyte (>0.5 M). The phenomena above

218   are related to the transient repulsion of ammonium ($[NH_4^{0\cdot}]_{ads}$) and Na-H_2O hydration

219   "atmosphere" [45].

220   3.2.3 Ion charge density and EDL thickness

221   Ion transportation and accumulation forms an EDL around the electrodes. Figure 5(a) and

222   5(b) illustrates the charge density profiles and the potential drop of NH_4^+ and Na^+ in the

223   range of 0–1.5 M. There are two remarkable peaks (0.0009 e $Å^{-3}$ and 0.0004 e $Å^{-3}$)

224   referring to the IHP and OHP of the NH_4^+ charge density curve, in which the value of NH_4^+

225   potential changes from -0.0225 V to 0 V (Figure 5(c) and 5(d)). Integrating NH_4^+ charge in

226   the x-axis, the charge density and potential drop of NH_4^+ film decline from 0.0041 e $Å^{-3}$

227   and -0.0226 V at 0 M to 0.0006 e $Å^{-3}$ and -0.0151 V at 1.5 M, respectively, as summarized

228   in Table 2. Na^+ charge density increases and the potential escalating. However, the film

229   of Na^+ peaks disappear as Na_2SO_4 becomes over-concentrated.

230   All atoms with different charge always interact with each other in the aqueous condition.

231   Due to the negative charge carried by O in the H_2O molecule, the total charge density and

232   potential drop shift from 0.0011 e $Å^{-3}$ and 0.0095 V to -0.0228 e $Å^{-3}$ and -0.0449 V,

233   respectively, (Figure SI-5 and Table 2). The variation of net charge density indicates the

234   importance of water molecule. As studied by Guo et al., water molecule at the interface

235   between the solution and electrodes forming hydrogen bonding changed the local

236   electronic structure of EDL [38]. The results gained by Velasco-Velez et al. elucidates that

237   the inert electrode surface can induce water molecules when the electrode is negatively

238   charged and therefore attracting the more positive H atoms [46].

239   Based on the total charge density and potential drop, the thicknesses of the NH_4^+ layer

240   and Na^+ layer as the function of Na_2SO_4 concentration are calculated and summarized in

241   Table 3. The total thickness of NH_4^+ EDL experiences a slight increase from 19.0 Å at 0 M

242   to 21.0 Å at 1.5 M but an apparent decrease to 16.0 Å at 1.5 M. In the Na_2SO_4, the IHP

243   declines to 4.0 Å from 6.0 Å; the OHP increases to 8.5 Å at 0.25 M but decreases to 6.5 Å

244   at 0.25 M; and DL varies from 5.5 to 7.0 Å. The comparison of IHP, OHP, and DL discloses

245   that Na_2SO_4 concentration has a greater influence on the Helmholtz layer (IHP and OHP)

246   than DL. The total thickness of Na^+ increases from 0 Å at 0 M to 23.5 Å at 1.5 M. The HP

247   is thicker than the DL. These variations are mainly attributed to the excess accumulation

248   of ions from the diffusion layer and the insufficient supply of ions in the bulk solution [15,

249   47, 48]. Taking the thickness overlap of NH_4^+ and Na^+ into consideration, the total EDL

250   thickness increases from 19.5 Å at 0 M to 23.5 Å at 1.5 M. According to the Debye–Hückel

251   equation, the charge density of Na^+ adsorption causes an increase of the Na^+ layer [49].

252   Therefore, the thick Na^+ layer blocks the rate of electron transfer of NH_4^+ reduction so

253   that the lack of an electron acceptor results in the decrease of the current density peak
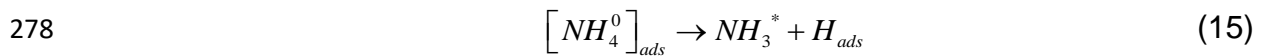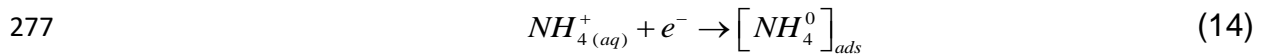
254   of NH_4^+ reduction.

255   3.3   Ammonium reduction

256   The differences of electric properties in charge density, potential drop, capacitance, and

257   thickness can reflect the kinetics of ion oxidation/reduction. To exam NH_4^+ reduction at

258   the cathode interface of EDI, current-voltage and generated gas were measured. The

259   current-voltage curves were obtained at a 10.0 mV s^{-1} scanning rate under 0–1.5 M

260   Na_2SO_4 as supporting electrolyte (Figure 6). A single peak in the range of 0-0.8 V applied

261   voltage was observed on each curve. For forward scanning, the current density increases

262   to 0.005 mA cm^{-2} with Na_2SO_4 concentration increasing to 0.5 M from 0 M. However, the

263   forward current density does not continuously increase although the concentration of

264   Na_2SO_4 increases to 1.5 M. For backward scanning, the peak current decreases from -

265   0.023 mA cm^{-2} to -0.005 mA cm^{-2}, moving to the positive y-axis as the bulk Na_2SO_4

266   electrolyte concentrating at 0.23 V (Figure 6(a)). The results are constant with that of the

267   experimental tests.

268   The generated gas was analyzed through gas chromatography and quantified through the

269   mass of nitrogen element. The plot shows that the mass in the liquid (anodic and cathodic)

270   is dominant, ammonia nitrogen takes second place and nitrogen gas is tiny (Figure 6(b)).

271   The changes of anodic-N and cathodic-N are because of migration. NH_3 and N_2 gas are

272   from NH_4^+ reduction (Eq.1) and base neutralization (Eq.2 and Eq.3).

273   NH_4^+ reduction experiences the absorption of intermediates, $[NH_4^0]_{ads}$ and H_{ads}. $[NH_4^0]_{ads}$,

274   adsorbed Rydberg radicals and repulsed NH_4^+ solvent molecules approaching for

275   additional binding so that the accumulation of $[NH_4^0]_{ads}$ in the EDL leads to the NH_4^+

276   concentration reducing [50-54].

277
$$NH_{4\,(aq)}^{+} + e^{-} \rightarrow \left[NH_4^0 \right]_{ads} \tag{14}$$

278
$$\left[NH_4^0 \right]_{ads} \rightarrow NH_3^* + H_{ads} \tag{15}$$

279
$$NH_3^* \rightarrow NH_2^* + H_{ads} \tag{16}$$

280
$$\vdots$$

281
$$2N^* \rightarrow N_2 + 2^* \tag{17}$$

282   where * is an active site.

283 The first step is dominant, and the flowing steps process slowly so that the mass of

284 nitrogen gas is little. As integrating the experimental and theoretical results, we find

285 that the increase of the concentration of Na_2SO_4 electrolyte changes the current density

286 of ammonium reduction (from -0.023 mA cm^{-2} to -0.005 mA cm^{-2} at 0.23 V).

4   Conclusion

288 This paper discussed the effects of Na_2SO_4 supporting electrolyte from 0 M to 1.5 M on

289 NH_4^+ reduction in the cathode surface of EDI using electrochemical analysis and MD

290 simulations. The results demonstrate that increasing the concentration of Na_2SO_4

291 supporting electrolyte enhances the conductivity and total current but reduces ion

292 activity. The migration rates of NH_4^+ and Na^+ increase in the dilute range (0-0.25 M) but a

293 decrease in the concentrated range (>0.5 M). The fierce competitive adsorption of Na^+

294 forming a thick layer blocks NH_4^+ migration and electron transportation in the EDL. NH_4^+

295 reduction is weakened with the increase of Na_2SO_4 supporting electrolyte. Interestingly,

296 water molecules play a critical role in determining the net charge density and potential

297 drop. Therefore, the mechanisms presented in this manuscript disclose the function of

298 the co-ion concentration and the results can allow the manipulation of EDI capacity

299 optimization.

5   Acknowledgements

6   References

[1] L. Xu, F. Dong, H. Zhuang, W. He, M. Ni, S.P. Feng, P.H. Lee, Energy upcycle in anaerobic treatment: Ammonium, methane, and carbon dioxide reformation through a hybrid electrodeionization–solid oxide fuel cell system, Energy Conversion and Management 140 (2017) 157-166.

[2] O. Berkh, Y. Shacham-Diamand, E. Gileadi, Reduction of ammonium ion on Pt electrodes, Journal of The Electrochemical Society 155(10) (2008) F223-F229.

[3] D.J. Little, M.R. Smith III, T.W. Hamann, Electrolysis of liquid ammonia for hydrogen generation, Energy & Environmental Science 8(9) (2015) 2775-2781.

[4] E. Simons, E. Cairns, D. Surd, The performance of direct ammonia fuel cells, Journal of The Electrochemical Society 116(5) (1969) 556-561.

[5] L. Xu, F. Dong, H. Zhuang, W. He, M. Ni, S.-P. Feng, P.-H. Lee, Energy upcycle in anaerobic treatment: Ammonium, methane, and carbon dioxide reformation through a hybrid electrodeionization–solid oxide fuel cell system, Energy Conversion and Management 140 (2017) 157-166.

[6] L. Alvarado, A. Chen, Electrodeionization: principles, strategies and applications, Electrochimica Acta 132 (2014) 583-597.

[7] S.-H. Moon, S.-H. Yun, Process integration of electrodialysis for a cleaner environment, Current Opinion in Chemical Engineering 4 (2014) 25-31.

[8] I. Wenten, K. Khoiruddin, P. Aryanti, A. Hakim, Scale-up Strategies for Membrane-Based Desalination Processes: A Review, Journal of Membrane Science and Research 2(2) (2016) 42-58.

[9] M.P. Mousavi, B.E. Wilson, S. Kashefolgheta, E.L. Anderson, S. He, P. Bu¨hlmann, A. Stein, Ionic Liquids as Electrolytes for Electrochemical Double-Layer Capacitors: Structures that Optimize Specific Energy, ACS Applied Materials & Interfaces 8(5) (2016) 3396-3406.

[10] J. Goodenough, H. Abruna, M. Buchanan, Basic Research Needs for Electrical Energy Storage. Report of the Basic Energy Sciences Workshop on Electrical Energy Storage, April 2-4, 2007, DOESC (USDOE Office of Science (SC)), 2007.

[11] E.J. Olson, P. Bühlmann, Unbiased Assessment of Electrochemical Windows: Minimizing Mass Transfer Effects on the Evaluation of Anodic and Cathodic Limits, Journal of The Electrochemical Society 160(2) (2013) A320-A323.

[12] A. Casadellà, O. Schaetzle, K. Nijmeijer, K. Loos, Polymer inclusion membranes (PIM) for the recovery of potassium in the presence of competitive cations, Polymers 8(3) (2016) 76.

[13] Y. Liu, M. Qin, S. Luo, Z. He, R. Qiao, Understanding ammonium transport in bioelectrochemical systems towards its recovery, Scientific Reports 6 (2016).

[14] S.D. Rosasco, J.L. Stickney, G.N. Salaita, D.G. Frank, J.Y. Katekaru, B.C. Schardt, M.P. Soriaga, D.A. Stern, A.T. Hubbard, Cation competition in the electrical double-layer at a well-defined electrode surface Li+, Na+, K+, Cs+, H+, Mg2+, Ca2+, Ba2+, La3+, tetramethylammonium, choline and acetylcholine cations at Pt (111) surfaces containing an ordered layer of cyanide, Journal of Electroanalytical Chemistry And Interfacial Electrochemistry 188(1-2) (1985) 95-104.

[15] C. Cagle, G. Feng, R. Qiao, J. Huang, B.G. Sumpter, V. Meunier, Structure and charging kinetics of electrical double layers at large electrode voltages, Microfluidics and Nanofluidics 8(5) (2010) 703-708.

[16] G. Jiang, C. Cheng, D. Li, J.Z. Liu, Molecular dynamics simulations of the electric double layer capacitance of graphene electrodes in mono-valent aqueous electrolytes, Nano Research 9(1) (2016) 174-186.

349 [17] A. Yoshida, K. Imoto, Electric double layer capacitor and method for producing the same,
350 Google Patents, 1992.
351 [18] S. Yoon, J.H. Jang, H.K. Bok, S.M. Oh, Complex capacitance analysis on rate capability of electric-
352 double layer capacitor (EDLC) electrodes of different thickness, Electrochimica Acta 50(11) (2005)
353 2255-2262.
354 [19] M. Vossen, F. Forstmann, Integral equation theory for the electrode-electrolyte interface with
355 the central force water model. Results for an aqueous solution of sodium chloride, Molecular Physics
356 86(6) (1995) 1493-1516.
357 [20] Z. Ma, M. Wang, X. Gao, C. Gao, Charge and separation characteristics of nanofiltration
358 membrane embracing dissociated functional groups, Frontiers of Environmental Science &
359 Engineering 8(5) (2014) 650-658.
360 [21] S. Alexey, M. Jr, A. D, Competition among Li+, Na+, K+, and Rb+ monovalent ions for DNA in
361 molecular dynamics simulations using the additive CHARMM36 and Drude polarizable force fields,
362 The Journal of Physical Chemistry B 119(12) (2015) 4428-4440.
363 [22] P. Soroosh, L. Hai, Molecular dynamics simulations of ion solvation by flexible-boundary
364 QM/MM: On-the-fly partial charge transfer between QM and MM subsystems, Journal of
365 Computational Physics 35(24) (2014) 1778-1788.
366 [23] J.P. Soetardji, J.C. Claudia, Y.-H. Ju, J.A. Hriljac, T.-Y. Chen, F.E. Soetaredjo, S.P. Santoso, A.
367 Kurniawan, S. Ismadji, Ammonia removal from water using sodium hydroxide modified zeolite
368 mordenite, Rsc Advances 5(102) (2015) 83689-83699.
369 [24] L. Joly, C. Ybert, E. Trizac, L. Bocquet, Hydrodynamics within the electric double layer on slipping
370 surfaces, Physical Review Letters 93(25) (2004) 257805.
371 [25] J.W. Lee, J.A. Templeton, K.K. Mandadapu, J.A. Zimmerman, Comparison of molecular and
372 primitive solvent models for electrical double layers in nanochannels, Journal of Chemical Theory
373 and Computation 9(7) (2013) 3051-3061.
374 [26] S. Plimpton, Fast parallel algorithms for short-range molecular dynamics, Journal of
375 Computational Physics 117(1) (1995) 1-19.
376 [27] J.-P. Ryckaert, G. Ciccotti, H.J. Berendsen, Numerical integration of the cartesian equations of
377 motion of a system with constraints: molecular dynamics of n-alkanes, Journal of Computational
378 Physics 23(3) (1977) 327-341.
379 [28] D.A. Skoog, D.M. West, F.J. Holler, S. Crouch, Fundamentals of analytical chemistry, Nelson
380 Education2013.
381 [29] J. Kielland, Individual activity coefficients of ions in aqueous solutions, Journal of the American
382 Chemical Society 59(9) (1937) 1675-1678.
383 [30] A. Alp, A. Nain, N. Kumar, M. Ibrahim, Density and viscosity of magnesium sulphate in
384 formamide+ ethylene glycol mixed solvents, Journal of Chemical Sciences 114(5) (2002) 495-500.
385 [31] A. Korosi, B. Fabuss, VISCOSITIES OF BINARY AQUEOUS SOLUTIONS OF NACL KCL NA2SO4
386 AND MGSO4 AT CONCENTRATIONS AND TEMPERATURES OF INTEREST IN DESALINATION
387 PROCESSES, Journal of chemical and engineering data 13(4) (1968) 548-&.
388 [32] A. Bald, Z. Kinart, R. Tomaš, Viscosity Coefficients of KCl, NaCl, NaI, KNO 3, LiNO 3, NaBPh 4 and
389 Bu 4 NI in Water-Dimethyl Sulfoxide Binary Mixtures With a Low Organic Solvent Content, Croatica
390 Chemica Acta 89(3) (2016) 345-353.
391 [33] S. Trasatti, Atkins' Physical Chemistry, P. Atkins, J. De Paula, Oxford University Press, Oxford, UK
392 (2006), ISBN: 0198700725, Pergamon, 2007.
393 [34] D. Frenkel, B. Smit, Understanding molecular simulation: from algorithms to applications,
394 Academic press2001.

395 [35] D.C. Rapaport, D.C.R. Rapaport, The art of molecular dynamics simulation, Cambridge university
396 press2004.
397 [36] S.W. Feldberg, On the dilemma of the use of the electroneutrality constraint in electrochemical
398 calculations, Electrochemistry Communications 2(7) (2000) 453-456.
399 [37] E.M. Ney, Electrical Double Layer Potential Distribution in Nanoporous Electrodes from
400 Molecular Modeling and Classical Electrodynamics Analysis, (2016).
401 [38] J.-H. Guo, Y. Luo, A. Augustsson, J.-E. Rubensson, C. Såthe, H. Ågren, H. Siegbahn, J. Nordgren,
402 X-ray emission spectroscopy of hydrogen bonding and electronic structure of liquid water, Physical
403 review letters 89(13) (2002) 137402.
404 [39] P.L. Silvestrelli, M. Parrinello, Structural, electronic, and bonding properties of liquid water from
405 first principles, The Journal of chemical physics 111(8) (1999) 3572-3580.
406 [40] J. Kong, Z. Bo, H. Yang, J. Yang, X. Shuai, J. Yan, K. Cen, Temperature dependence of ion
407 diffusion coefficients in nacl electrolyte confined within graphene nanochannels, Physical Chemistry
408 Chemical Physics 19(11) (2017) 7678-7688.
409 [41] A.P. Lyubartsev, A. Laaksonen, Concentration effects in aqueous NaCl solutions. A molecular
410 dynamics simulation, The Journal of Physical Chemistry 100(40) (1996) 16410-16418.
411 [42] S. Krishnamurthy, P. Bhattacharya, P. Phelan, R. Prasher, Enhanced mass transport in nanofluids,
412 Nano Letters 6(3) (2006) 419-423.
413 [43] B.N. Pal, B.M. Dhar, K.C. See, H.E. Katz, Solution-deposited sodium beta-alumina gate dielectrics
414 for low-voltage and transparent field-effect transistors, Nature Materials 8(11) (2009) 898.
415 [44] M. Belonenko, N. Lebedev, S. Sudorgin, Electrical conductivity and diffusion coefficient of
416 electrons in a graphene bilayer, Technical Physics 57(7) (2012) 1025-1029.
417 [45] H. Lim, W. Lu, X. Chen, Y. Qiao, Effects of ion concentration on thermally-chargeable double-
418 layer supercapacitors, Nanotechnology 24(46) (2013) 465401.
419 [46] J.-J. Velasco-Velez, C.H. Wu, T.A. Pascal, L.F. Wan, J. Guo, D. Prendergast, M. Salmeron, The
420 structure of interfacial water on gold electrodes studied by x-ray absorption spectroscopy, Science
421 346(6211) (2014) 831-834.
422 [47] E.M. Evleth, E. Kassab, Role of Rydberg radicals in electrochemistry, Pure and Applied Chemistry
423 60(2) (1988) 209-214.
424 [48] K. Laidler, J. Meiser, B. Sanctuary, Physical Chemistry 2003, Houghton Mifflin: Boston, MA.
425 [49] N. Kallay, T. Preočanin, D. Kovačević, J. Lützenkirchen, E. Chibowski, Electrostatic potentials at
426 solid/liquid interfaces, Croatica chemica acta 83(3) (2010) 357-370.
427 [50] M. Morita, T. Kaigaishi, N. Yoshimoto, M. Egashira, T. Aida, Effects of the electrolyte composition
428 on the electric double-layer capacitance at carbon electrodes, Electrochemical and Solid-state
429 Letters 9(8) (2006) A386-A389.
430 [51] K. Kordesch, J. Gsellmann, M. Cifrain, S. Voss, V. Hacker, R.R. Aronson, C. Fabjan, T. Hejze, J.
431 Daniel-Ivad, Intermittent use of a low-cost alkaline fuel cell-hybrid system for electric vehicles, J.
432 Power Sources 80(1) (1999) 190-197.
433 [52] N. Dekker, G. Rietveld, Highly efficient conversion of ammonia in electricity by solid oxide fuel
434 cells, J. Compos. Tech. Res. 3(4) (2006) 499-502.
435 [53] A. Fuerte, R. Valenzuela, M. Escudero, L. Daza, Ammonia as efficient fuel for SOFC, J. Power
436 Sources 192(1) (2009) 170-174.
437 [54] M. Boudart, G. Djéga-Mariadassou, Kinetics of heterogeneous catalytic reactions, Princeton
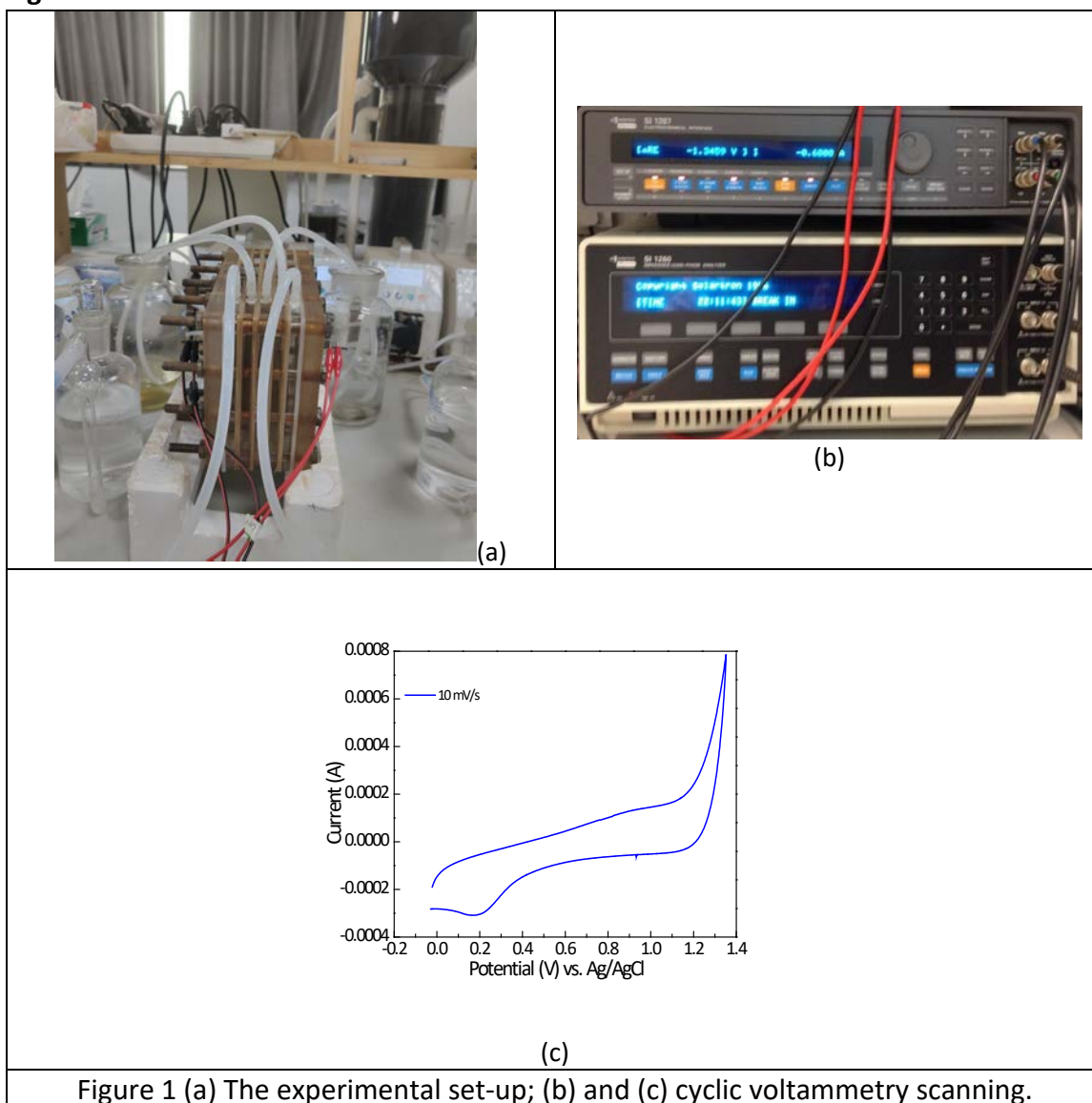438 University Press2014.

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Figures
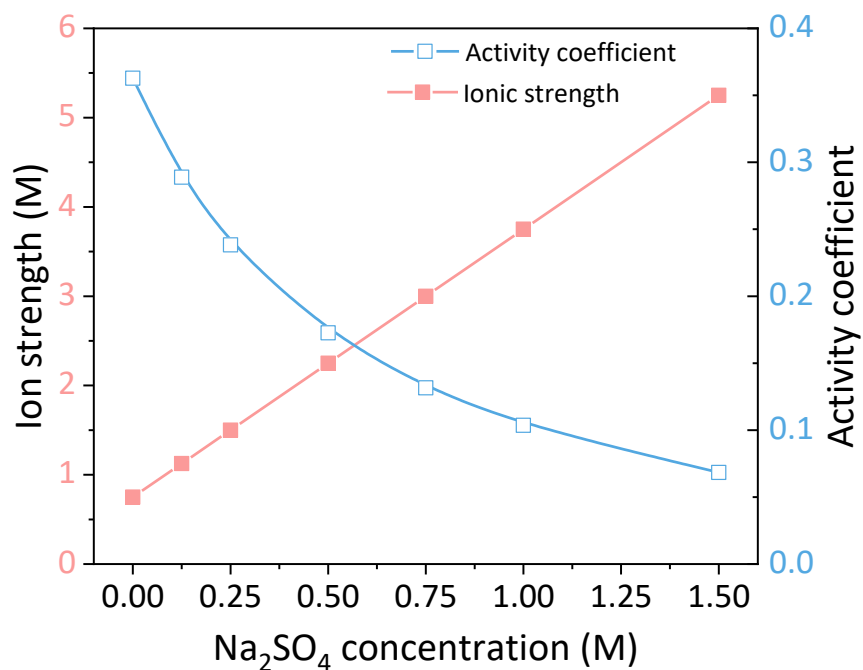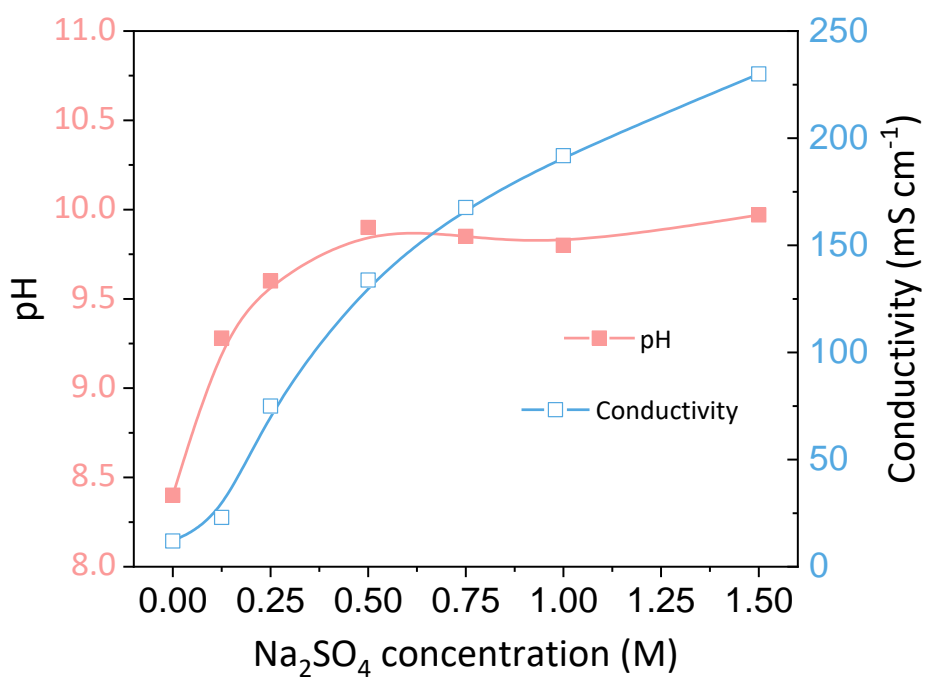

(a)

(b)

(c)

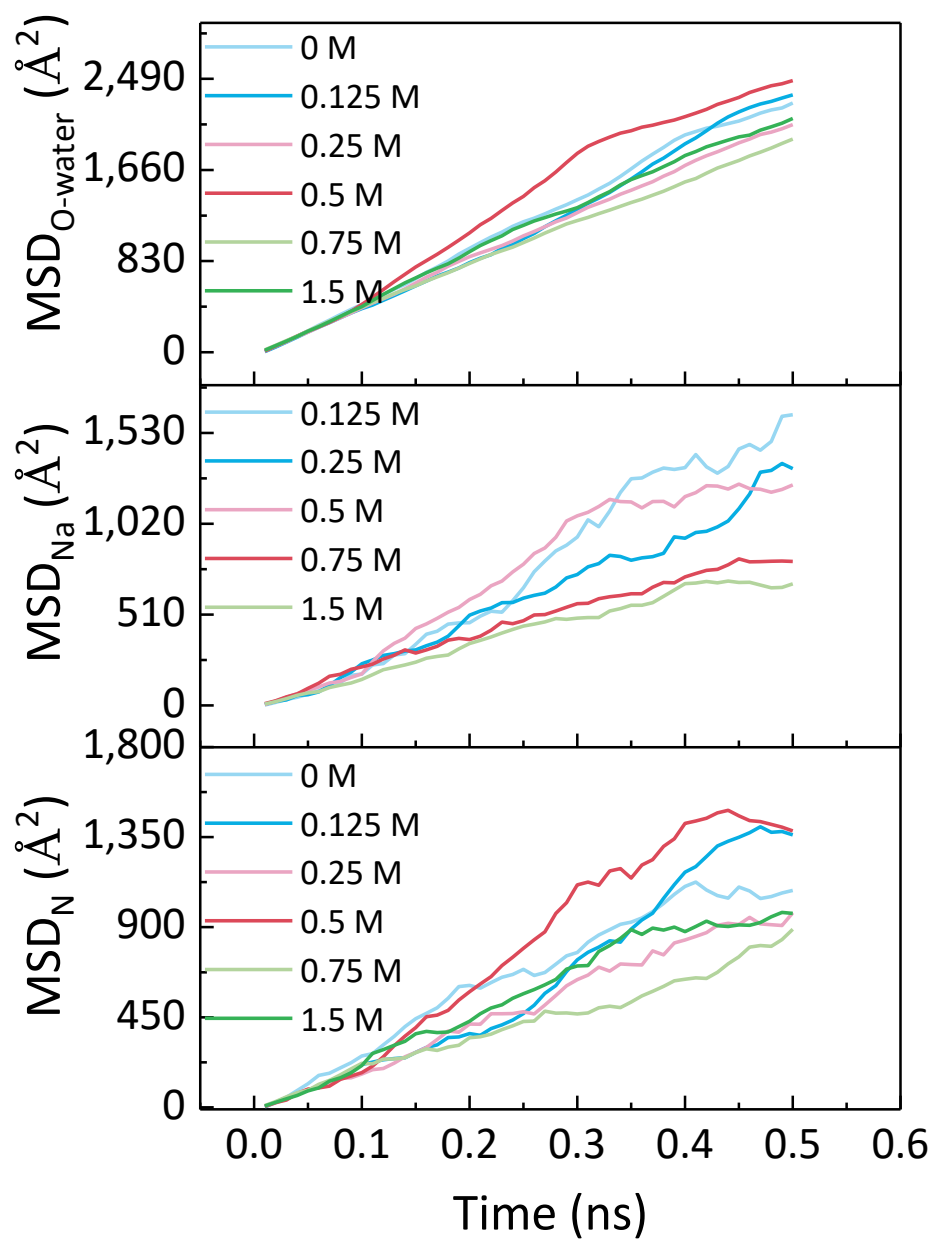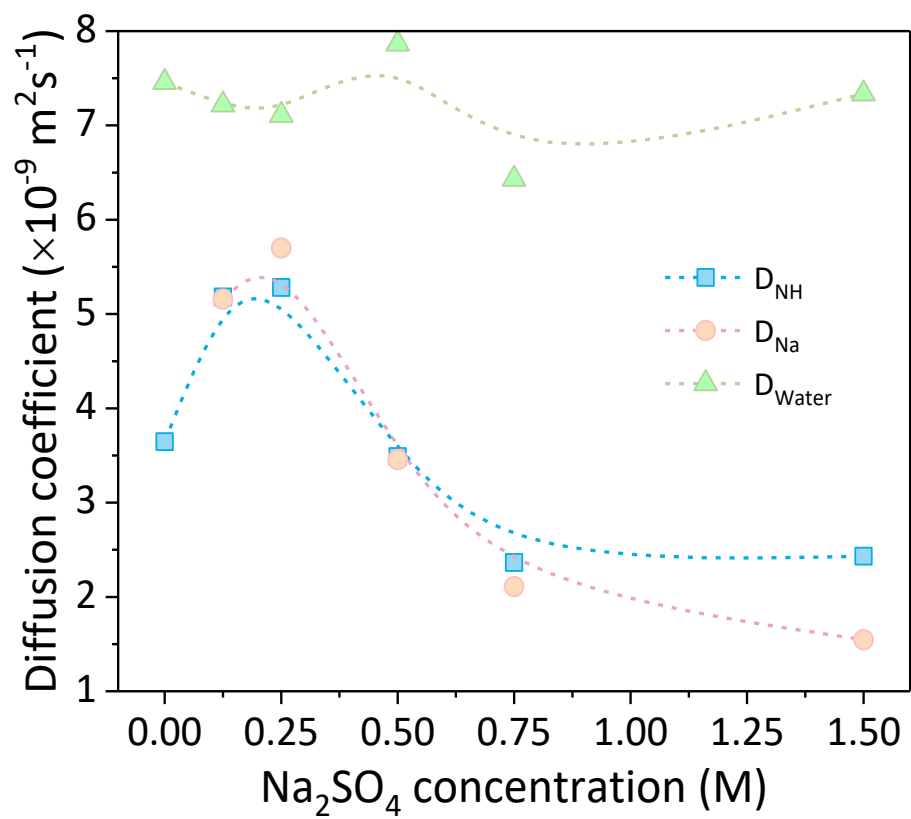Figure 1 (a) The experimental set-up; (b) and (c) cyclic voltammetry scanning.

(a)

(b)

Figure 2 Characteristics of solution at 0-1.5 M Na_2SO_4 electrolyte. (a)Ion strength and activity coefficient of NH_4^+; (b) pH and conductivity
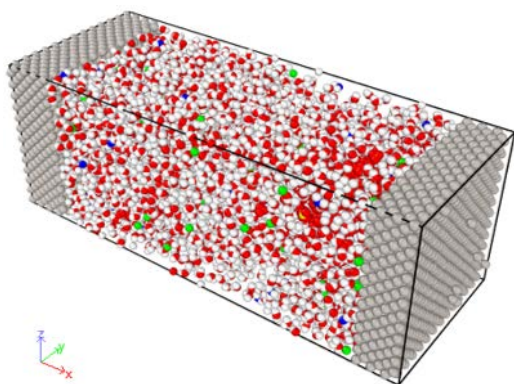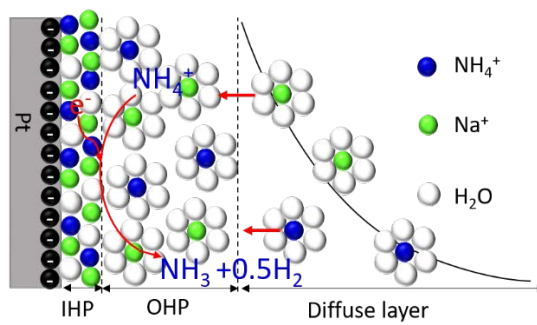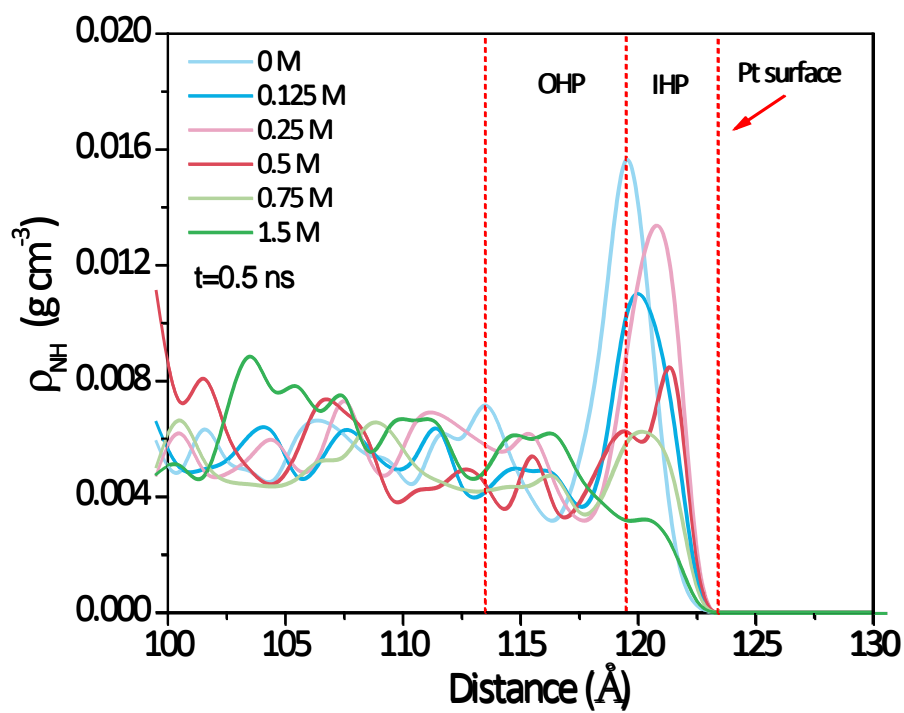
(a)

(b)

Figure 3 (a) MSD values of N, Na and O-water in 0.5 ns; (b) diffusion rates of NH_4^+, Na^+ and H_2O molecules as a function of Na2SO4 concentration.
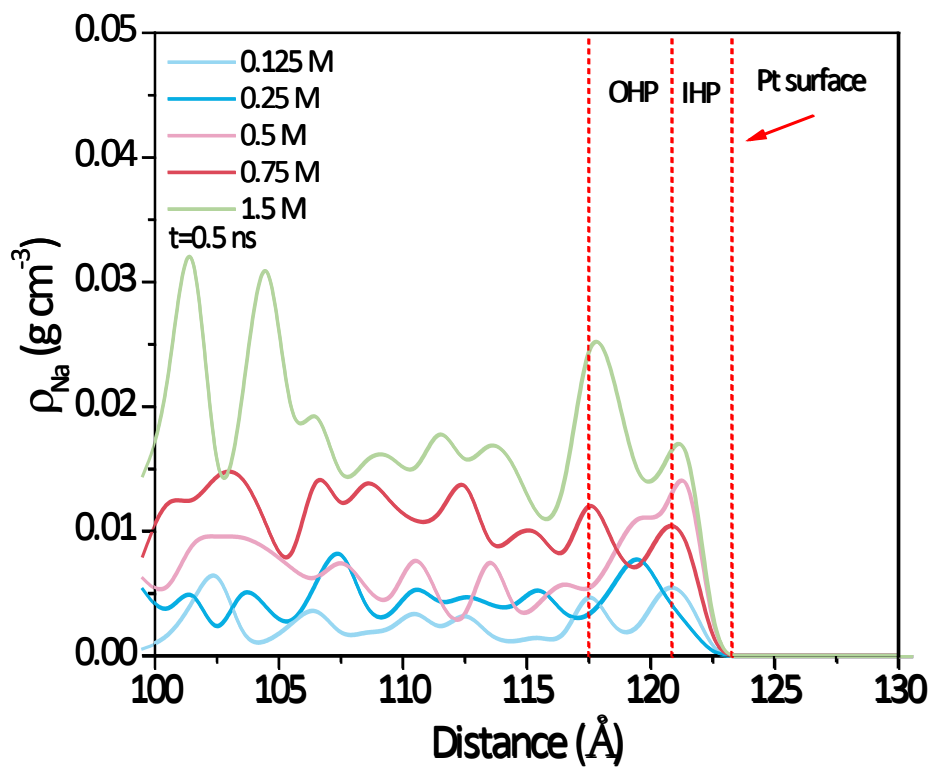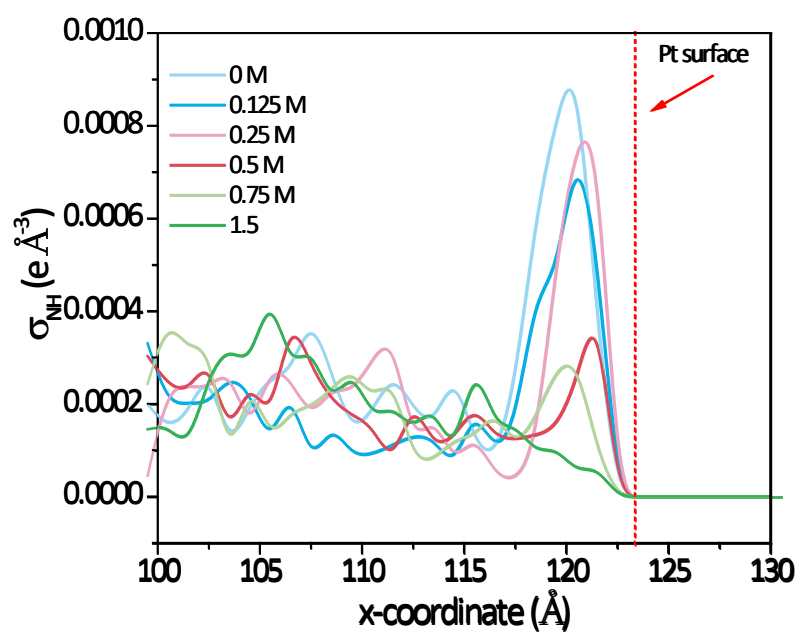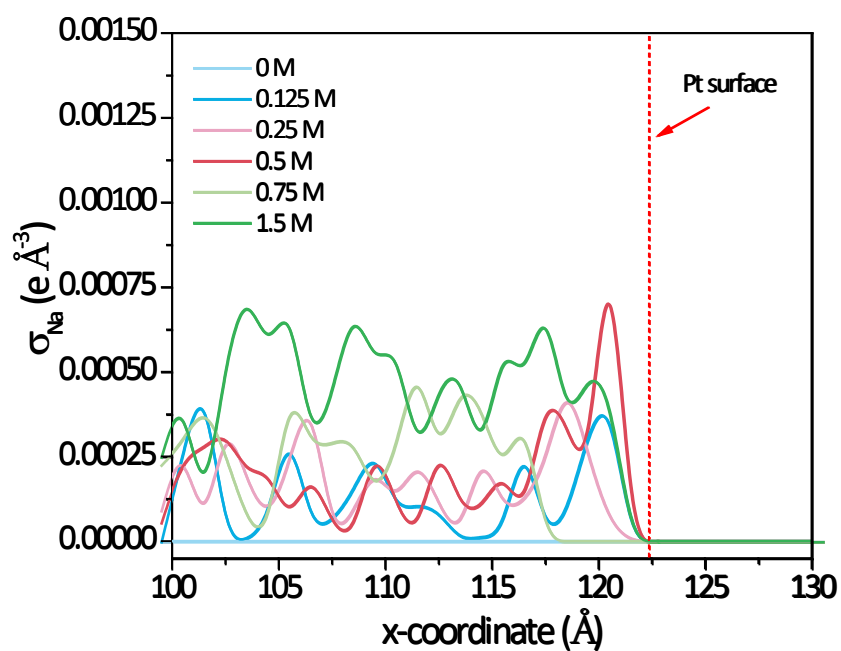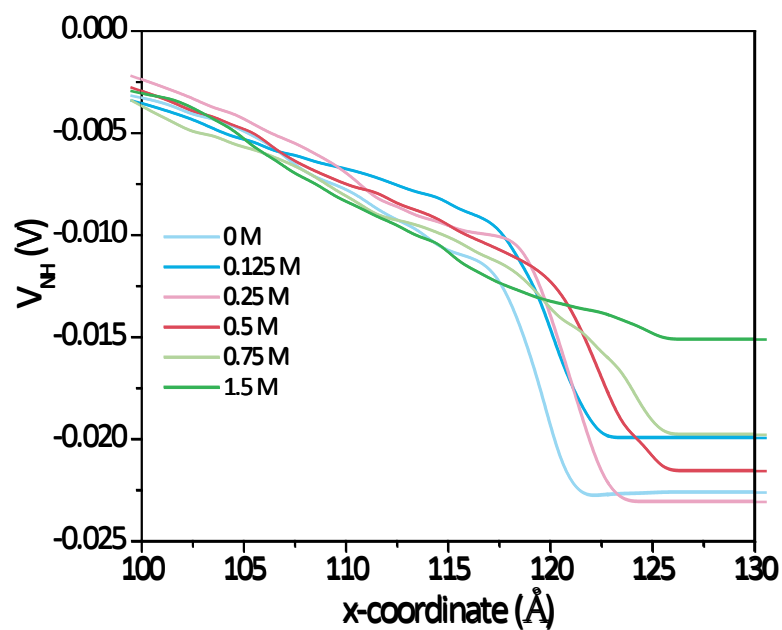
(a)

(b)

(c)

(d)

Figure 4 (a) Single channel model of electrodeionization; (b) NH_4^+ EDL film; (c) and (d) concentration profiles of NH_4^+ and Na^+ as a function of Na_2SO_4 concentration (0–1.5 M).
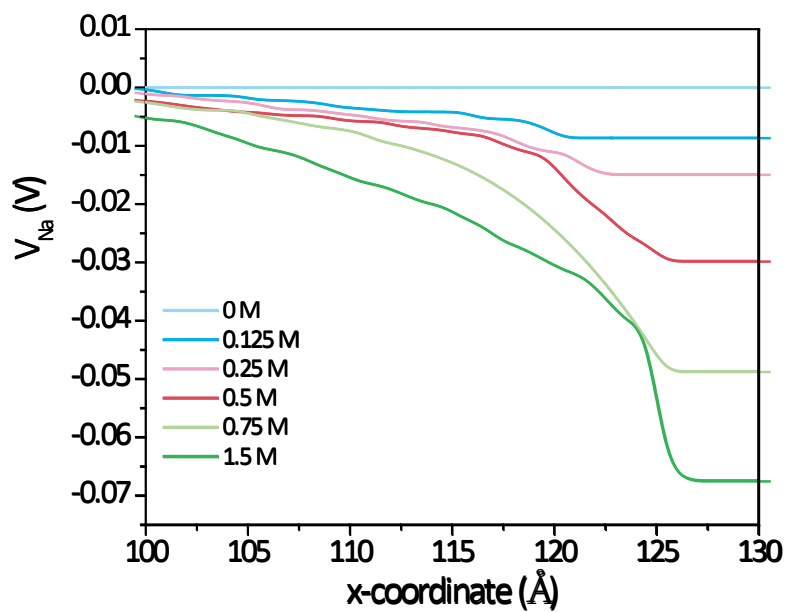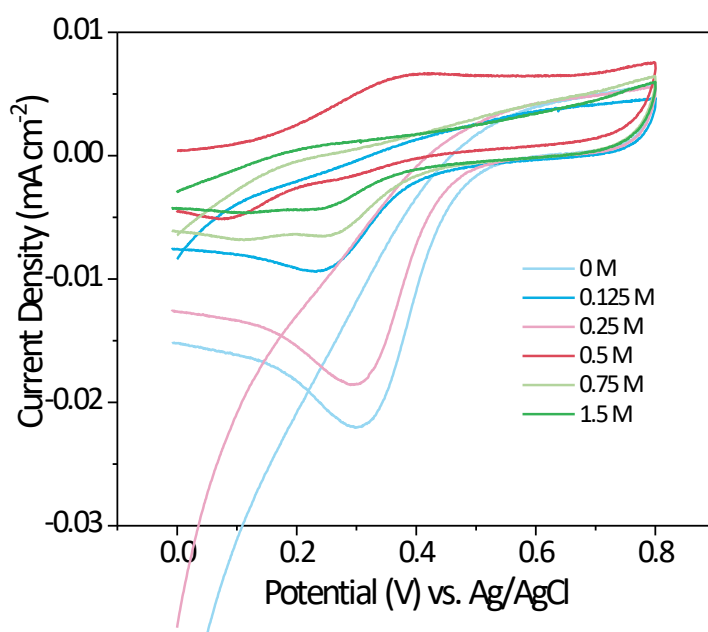
(a)

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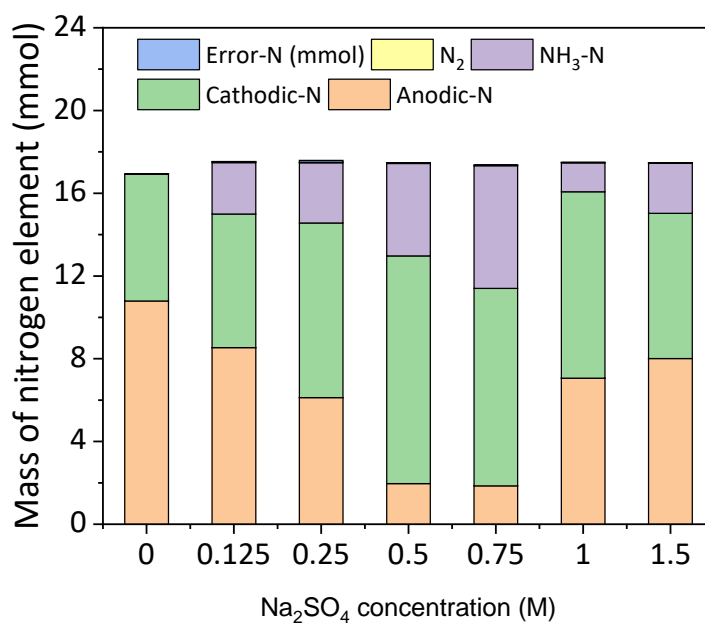
(d)

Figure 5 (a) and (b) Charge density distributions; (c) and (d) potential drops of NH_4^+ and Na^+ along the x-axis under 0–1.5 M Na_2SO_4.

Figure 5 (a) and (b) Charge density distributions; (c) and (d) potential drops of NH_4^+ and Na^+ along the x-axis under 0–1.5 M Na_2SO_4.

(a)

(b)

Figure 6 (a) Current-Voltage curves at 0–1.5 M Na$_2$SO$_4$; (b) Nitrogen constituents.

Tables

Table 1   Mobility and transport numbers of NH_4^+, Na^+ and SO_4^{2-} at 0–1.5 M Na_2SO_4

Na₂SO₄ concentration mol L⁻¹	Mobility $\times10^{-8}$ m² V⁻¹ s⁻¹			Transport number		
	NH_4^+	Na^+	SO_4^{2-}	NH_4^+	Na^+	SO_4^{2-}
0	1.01	-	3.29	0.67	-	0.33
0.125	1.49	4.06	2.03	0.17	0.33	0.50
0.25	1.33	3.40	1.70	0.17	0.42	0.41
0.50	1.29	2.78	1.39	0.11	0.63	0.26
0.75	1.34	2.45	1.22	0.11	0.63	0.26
1.00	1.37	1.87	0.93	0.08	0.65	0.27
1.50	1.27	1.63	0.81	0.08	0.64	0.28

Table 2   Electric properties of NH_4^+ film and EDL capacitance via MD

Na_2SO_4 concentration mol L^{-1}	Charge density e Å^{-3}				Potential drop V				EDL capacitance ×10^{-19} F Å^{-3}
	NH_4^+	Na^+	H_2O	Total	NH_4^+	Na^+	H_2O	Total	
0	0.0041	0.0000	-0.0030	0.0011	-0.0226	0.0	0.0321	0.0095	0.1795
0.125	0.0030	0.0013	-0.0083	-0.0040	-0.0220	-0.0086	0.0252	-0.0054	1.1920
0.25	0.0026	0.0015	-0.0125	-0.0083	-0.0230	-0.0149	0.0231	-0.0149	0.8939
0.5	0.0016	0.0024	-0.0235	-0.0194	-0.0215	-0.0298	0.0262	-0.0251	1.2363
0.75	0.0013	0.0010	-0.0312	-0.0290	-0.0198	-0.0487	0.0276	-0.0409	1.1321
1.5	0.0006	0.0031	-0.0265	-0.0228	-0.0151	-0.0645	0.0347	-0.0449	0.8117

Table 3   EDL structures and thicknesses (NH_4^+ and Na^+) via MD

Na_2SO_4 concentration mol L^{-1}	NH_4^+ layer			Na^+ layer Å			Total thickness
	IHP	OHP	DL	IHP	OHP	DL	
0	6.0	7.5	5.5	--	--	--	19.0
0.125	5.5	8.0	6.0	4.5	4.0	7.5	19.5
0.25	5.5	8.5	7.0	6.0	6.0	6.5	21.0
0.5	5.0	7.0	5.0	8.5	8.5	7.0	24.0
0.75	5.0	6.5	6.0	8.0	7.0	6.0	21.0
1.5	4.0	6.5	5.5	7.5	8.5	7.5	23.5