

Revisiting van der Waals radii: from comprehensive structural analysis to knowledge-based classification of interatomic contacts

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This paper is dedicated to W.D.S. Motherwell who showed the power of structural chemistry to the first author.

Abstract: Weak noncovalent interactions are responsible for structure and properties of almost all supramolecular systems, such as nucleic acids, enzymes, and pharmaceutical crystals. However, the analysis of their significance and structural role is not straightforward and commonly requires model studies. Herein we describe an efficient and universal approach for the analysis of noncovalent interactions and determination of vdW radii using the Line-of-Sight (LoS) concept. The LoS allows to unambiguously identify and classify the “direct” interatomic contacts in complex molecular systems. This approach not only provides an improved theoretical base to molecular “sizes” but also enables the quantitative analysis of specificity, anisotropy and steric effects of intermolecular interactions.

Introduction

Van der Waals (vdW) radii (R_{vdW}) are one of the cornerstones of contemporary chemistry. The visual perception and basic analysis of chemical structures and architectures are rooted in the concept of vdW radii providing the basic definition of the atomic “sizes”. Even though this concept has a little physical grounding, it is easily interpretable and therefore is widely used in the theoretical chemistry, particularly in design of force fields (in the Lennard-Jones parameter form),^[1] dispersion corrections,^[2] and COSMO-RS-type solvate models.^[3] These models are directly or indirectly operate by the intermolecular interatomic distances, which are regarded as corresponding to the minimum energy of atom-atom interactions and are usually defined as a function of the sum of vdW radii. However, it has been noted^[4,5] that the sum of R_{vdW} for available vdW sets including the most widely used one tabulated by Bondi^[6] consistently underestimate the position of the energy minimum by as much as 0.3–0.4 Å. An illustrative example is the C₂Cl₆ crystal with the shortest $r(\text{Cl}\cdots\text{Cl}) = 3.65$ Å that exceeds significantly the $2R_{vdW}^{\text{Bondi}}(\text{Cl}) = 3.50$ Å. The latter can only be achieved at a very high pressure of ca. 1.2 GPa.^[7] Moreover, about 2.0 % (>4 000) of unique organic molecular

crystals in the Cambridge Structural Database (CSD)^[8] do not contain intermolecular contacts shorter than sum of R_{vdW}^{Bondi} (see the first section of SI for the details). The question arises: why are all bonds in these crystals longer than the distance, which is usually considered as the most probable, in other words closest to the energy minimum of the respective interatomic potential?

This inconsistency is rooted to the indirect nature of the approaches used to obtain the vdW parameters from experimental structural datasets. Conventionally, R_{vdW} are derived from the position of the vdW peak in the distributions of contact distances between nonbonded atoms (Figure 1a-b).^[6,9,10] Such distributions represent a superposition of a gaussian curve due to the vdW peak, and a rapidly growing function due to the randomly distributed contacts (Figure 1a). Because the position of the vdW peak maximum (D_{max}) is often hidden within the dataset for other contacts (Figure 1b), the sum of vdW radii is normally taken as the half-height of the vdW peak distance, D_{half} instead of the D_{max} (Figure 1a). However, D_{max} has more clear physical meaning: it is the distance corresponding to the energy minimum of the considered interaction.^[4] On the contrary, D_{half} -based vdW radii are qualitative, as interpretation of their sum is not straightforward. Although alternative knowledge-based^[11] and *ab initio* computational^[12] approaches to derive R_{vdW} have been proposed, their universality and applicability are still rather limited.

In this work, we introduce a new method to define the D_{max} and, accordingly, to compute D_{max} -based vdW radii (R_{max}) for almost any intermolecular interaction directly from diverse structural datasets. The key idea is to eliminate the background from randomly distributed contacts using the Line-of-Sight^[13] concept. It considers the atoms are interacting only when they “see” each other (Figure 1d) because no other atom in the structure intrudes between them or, in other words, shields them from one other. This concept allows one to redetermine vdW parameters from the bulk structural data and provide an opportunity to find atom-type specific D_{max} -based vdW radii for elements in different chemical environments with clear physical meaning. It should be noted, that intermolecular interactions cannot be efficiently reduced to atom-atom interactions^[14] and analyzed in great details using energy decomposition schemes.^[15] Even though, our approach is in fact a statistical way to approximate the potential energy surfaces, which is independent of the interpretation of the results in terms of atom-atom interactions. We argue that R_{max} can be used to improve accuracy of computational approaches directly or indirectly involving consideration of the size of molecules. It will be useful for the analysis of intermolecular interactions in combination with quantum chemistry methods.

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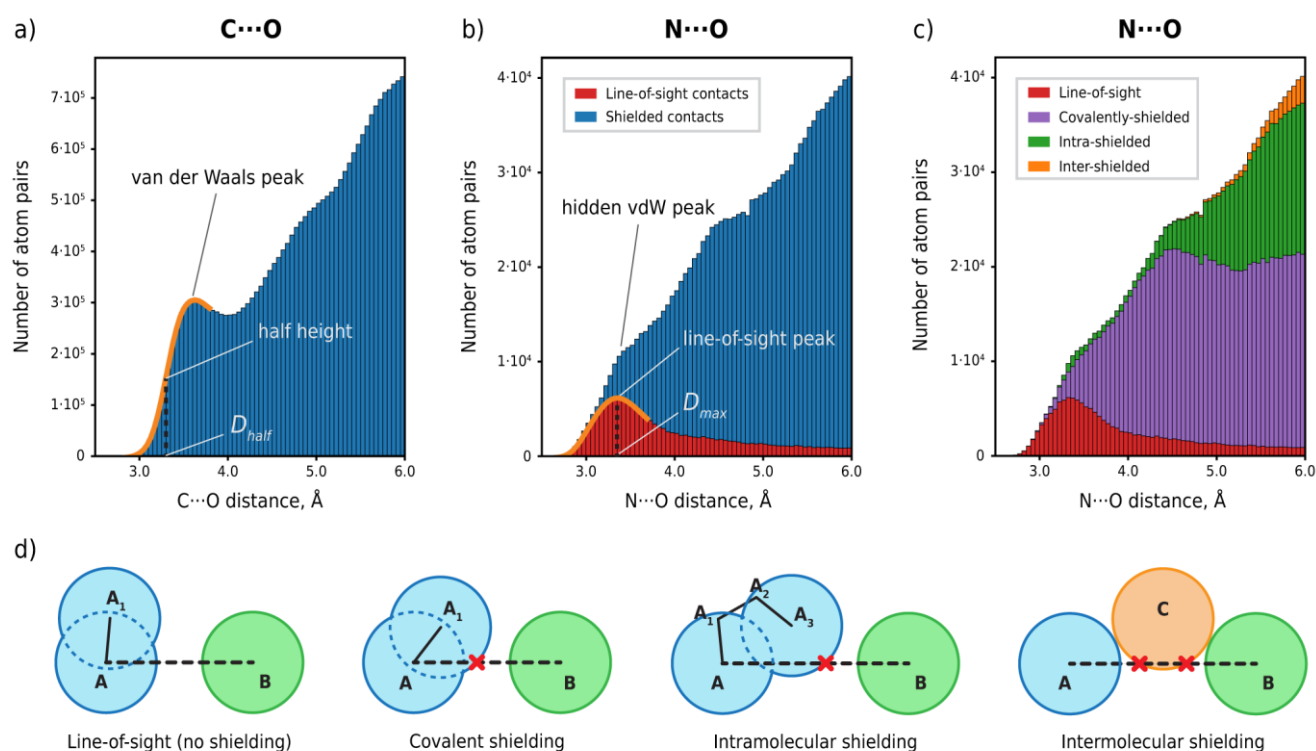


Figure 1. Distance distributions for all intermolecular C...O (a) and N...O (b,c) intermolecular contacts from molecular crystals in CSD. The contacts between atom pairs are classified (c) as the line-of-sight and various shielded contacts. The respective contributions to the overall contact distance distributions of $r(\text{N}\cdots\text{O})$ are presented in parts (b,c).

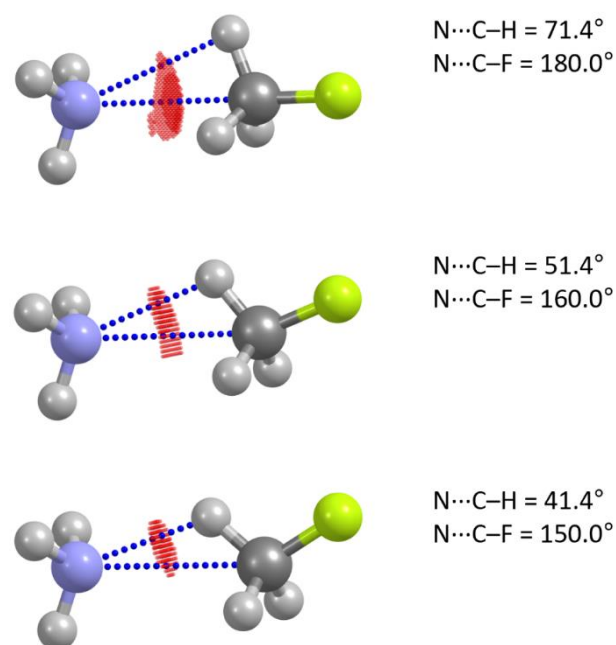


Figure 2. Dependence of NCI surface (isosurface value is set to 0.5) in $\text{H}_3\text{N}\cdots\text{H}_3\text{CF}$ system on $\text{N}\cdots\text{C}-\text{F}$ angle and $\text{N}\cdots(\text{H})\text{C}$ shielding.

Results and Discussion

We propose to implement the Line-of-Sight^[13] concept (LoS) to eliminate the background from randomly distributed contacts, which is equivalent to classification of contacts into corresponding and noncorresponding to interatomic interactions. Thus, we start with understanding the physical meaning of this procedure. LoS concept considers the atoms as interacting only when they “see” each other (Figure 1d) because no other atom in the structure intrudes between them or, in other words, shields them from one other (for the exact definition see the SI). We identify three main types of contact shielding, namely, the covalent, intra- and intermolecular shielding depending on the type of shielding atom (Figure 1d), with the only the covalent shielding having the characteristic distances comparable to that of the D_{max} . A representative example of the contributions of the LoS and shielded contacts for the complete dataset of N...O contacts is illustrated in Figure 1c.

To further validate and illustrate this concept, we carried out a detailed conformational and bonding analysis on a model $\text{H}_3\text{N}\cdots\text{CH}_3\text{F}$ system (Figure 2) by means of density functional theory (DFT) calculations (B3LYP/6-311++G(d,p)). The *ab initio* electron density based noncovalent interaction surface (NCIS) method^[16] was employed to detect and quantify the intermolecular interactions. Basic geometric considerations within the LoS model imply the $\text{N}\cdots\text{C}$ interaction for a configuration with $\angle\text{N}\cdots\text{C}-\text{F}$ of 180° and $\angle\text{N}\cdots\text{C}-\text{H}$ of $\sim 70^\circ$. The decrease of $\angle\text{N}\cdots\text{C}-\text{F}$ would

result in the gradual shielding of the N...C contact by the H atoms and ultimately vanishing the N...C interaction at $\angle \text{N}\cdots\text{C}-\text{F} \sim 155\text{--}160^\circ$ and $\angle \text{N}\cdots\text{C}-\text{H} \sim 45\text{--}50^\circ$, depending on the assumed R_{vdW} . The NCIS analysis supports these predictions (Figure 2). The NCIS has a pronounced maximum between the N and C atoms in linear $\text{H}_3\text{N}\cdots\text{CH}_3\text{F}$. Upon bending the geometry, the NCIS redistributes towards the N...H area evidencing strengthening of the respective N...H contact with a concomitant weakening of the initial N...C interaction (Figure 2). These data show that the shielding does not fully eliminate the original two-atom contact but rather decreases its contribution to the overall intermolecular interaction. On contrary, the LoS contacts are dominated by their respective diatomic contributions that makes them perfectly suitable for the statistical analysis of the intermolecular contacts.

The LoS concept was next used to determine the vdW radii for the main group elements from the structural data in the Cambridge Structural Database (CSD).^[8] We processed 224 001 unique CSD entries, from which more than 40 000 000 intermolecular LoS contacts were obtained and analyzed. An iterative procedure was employed, in which at the 0th iteration, the LoS was defined with Bondi's R_{vdW} .^[6] The LoS contact distance distributions were used to determine D_{max} values for all possible A...B atom pair contacts, while the D_{max} values were used to compute the vdW radii, R_{vdW} , for all elements in the dataset by means of least-squares minimization of the function:

$$f = \sum_{\text{A}\cdots\text{B}} w(\text{A}\cdots\text{B}) \cdot [D_{\text{max}}(\text{A}\cdots\text{B}) - R_{\text{vdW}}(\text{A}) - R_{\text{vdW}}(\text{B})]^2 \quad (1)$$

where the outer summation is carried out over all selected A...B contacts, and $w(\text{A}\cdots\text{B})$ is a weight defined as the root square of number of LoS contacts shorter than D_{max} . Because the contact shielding depends on vdW radii, the R_{vdW} values obtained at the first step were used to recalculate the contact shielding parameters and determine the D_{max} values for all atom pairs. This procedure was repeated iteratively until a convergence of 0.001 Å was reached for all R_{vdW} .

This procedure has revealed that for some contacts D_{max} significantly deviate from the sum of the atomic type specific R_{vdW} (Table S1). We identify several scenarios leading to such deviations: (1) the interacting atoms are not in a state typical for common organic compounds or (2) are sterically hindered, (3) the contact corresponds to the obviously specific interaction (e.g. hydrogen or halogen bond), and (4) its D_{max} values does not strongly depend on the contact geometry. We did not use these contacts to determine R_{vdW} as our final goal was to obtain R_{vdW} corresponding to weak nonspecific interactions that were not affected by secondary effects. For example, tetra-coordinated B, P and As atoms were not considered due to steric hindrance, and $\text{N}_{\text{sp}}/\text{N}_{\text{sp}2}/\text{S}_{\text{sp}2}$ due to significant dependence of D_{max} on the contact geometry. The contacts used for R_{vdW} determination are marked with '+' sign in the second column of Table S1. The R_{vdW} values determined using this procedure (R_{max}) are listed in Table 1 and compared with the respective values from the most popular vdW radii sets (R_{half}).

The results in Table 1 reveals that the LoS model yields vdW radii consistently exceeding the values obtained by other approaches by as much as 0.10–0.20 Å resulting in the increase of the sum of R_{vdW} by 0.2–0.4 Å. This is attributed to the transition

of the analysis from the rather arbitrary D_{half} parameters to a more specific and rigorously defined D_{max} values. We argue that R_{max} are more physically sound as they directly reflect the most probable contact distance, whereas R_{half} appear to correspond to strongly shortened interactions, which are usually denoted as "specific" in the chemical literature. Of all elements analyzed here, only for boron the R_{max} determined by our approach is close to R_{half} by Alvarez.^[10] This numerical match is most likely associated with the overestimation of Alvarez's R_{vdW} due to the selection of sterically hindered tetravalent B for plotting B...O distance distribution in Ref. [10].

Table 1. Van der Waals radii of elements typical for organic compounds.

Atom	Van der Waals radii, Å				Atom or contact type ^[b]
	<i>R</i> _{half}			<i>R</i> _{max}	
	Bondi	Rowland & Taylor	Alvarez		
H	—	—	—	1.21	C—H⋯X, X ≠ H
	1.20	—	1.20	1.29	C—H⋯H—C
B	—	—	1.91	1.90	Z ₃ B
C	1.70	1.75	1.77	1.87	C _{sp2}
	—	—	—	1.91	C _{sp3} , (C— <u>Me</u>)
N	1.55	1.61	1.66	1.76	N _{sp3} ([R/H] ₃ N)
O	1.52	1.56	1.50	1.74	O _{sp3} (ROH/R ₂ O) ^[c]
	—	—	—	1.65	O _{sp2} (C=O) ^[d]
F	1.47	1.44	1.46	1.55	C—F
P	1.80	—	1.90	2.09 ^[a]	Z ₃ P
S	1.80	1.79	1.89	1.95	R ₂ S
Cl	1.75	1.74	1.82	1.91	C—Cl
As	1.85	—	1.88	2.07 ^[a]	Z ₃ As
Se	1.90	—	1.82	2.04	Z ₂ Se
Br	1.85	1.85	1.86	2.00	C—Br
I	1.98	2.00	2.04	2.17	C—I

[a] Values in italic correspond to the cases where insufficient data was available for the accurate determination of R_{vdW} . [b] Atom types used for determination of van der Waals radii in this work. If there are several radii for one element, the first row lists "default" R_{vdW} for the current element that can be compared the values from other vdW radii sets. R and Z in formulae stands for C-bonded and any monovalent substituents, respectively. [c] Water molecules were excluded as D_{max} of the respective interactions were systematically different from those for ROH/R₂O. [d] Carboxylates and charged atoms were excluded from the datasets as the D_{max} of the corresponding interactions were systematically different from those for uncharged atoms, which is apparently due to the increased electrostatic contribution.

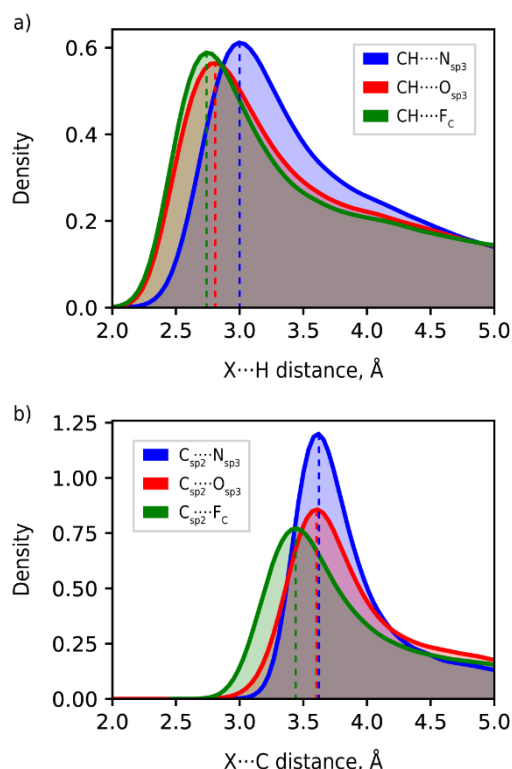


Figure 3. Distance distribution of C-H...X line-of-sight contacts for X = N, O, F. Gaussian kernel density estimation^[19] is used instead of histograms for the purpose of clarity.

Furthermore, our data analysis allows to identify the contact-angle dependencies in vdW radii. A representative example is the interhalogen interactions C-Hal₁...Hal₂-C, Hal = Cl, Br, I (X-bonds, XBs), which are usually classified as types I and II.^[17] Type I XBs are characterized by $\angle\text{C-Hal}_1\cdots\text{Hal}_2 \approx \angle\text{C-Hal}_2\cdots\text{Hal}_1$ and are usually nonspecific and weak, whereas type II XBs are characterized by $\angle\text{C9-Hal}_1\cdots\text{Hal}_2 \approx 90^\circ$ and $\angle\text{C-Hal}_1\cdots\text{Hal}_2 \approx 180^\circ$ and are usually strong and shorter than type I XBs due to the σ -hole interaction.^[18] Therefore, our approach can specifically be used to discriminate the respective noncovalent interactions and obtain different $R_{\text{max}}(\text{Hal})$ values for 90° and 180° C-Hal...X angles (see for examples Figures S2-27-29,49-51,64-66,73-75). It should also be noted, that different R_{max} values were obtained for H atoms from H...H and H...X, X≠H contacts (1.21 Å and 1.29 Å, respectively). This finding should be considered when analyzing interactions between aliphatic tails.

It should be noted, that R_{max} are in fact a condensed representation of the analyzed contacts and therefore can be instrumental for the more detailed analysis of noncovalent interactions and statistical definition of qualitative structural features of chemical systems. For example, specific interactions and sterically hindered contacts can be automatically identified by D_{max} substantially deviating from the sum of the respective vdW radii. Let us consider two representative examples of CH...O and C...O contacts, for which the D_{max} are, respectively, shorter or longer than the sum of R_{max} .

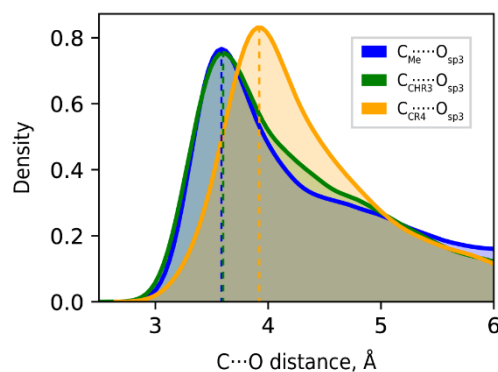


Figure 4. Distance distribution of C...O_{sp3} line-of-sight contacts for different carbon types. Gaussian kernel density estimations used instead of histograms for the purpose of clarity.

CH...O contacts show D_{max} values shorter by 0.14 Å than the sum of R_{max} . This deviation is much larger than that (<0.02 Å) detected for the related CH...N and CH...F interactions (Table S1). The CH...O contacts are shorter by 0.18 Å than CH...N and very similar to CH...F (Figure 3a), although an opposite trend can be seen in the C_{sp2}...O/N/F contacts (Figure 3b). Such deviation of D_{max} from the sum of R_{max} imply that CH...O contacts are highly specific and their structure forming role is more significant than that of the other CH...X contacts, including CH...F, despite the similar electrostatic nature of these contact types.^[20]

The sterically hindered C_{CR4}...O contacts formed by quaternary carbon exceed by 0.30 Å the corresponding R_{max} sum, which, in turn, cohere well with the D_{max} values for the C...O contacts formed by primary (C_{Me}) and tertiary (C_{HR3}) carbon atoms (Figure 4). Such a shift of the C_{CR4}...O vdW peak is in line with the expected significant steric repulsions between the neighbors of the interacting carbon atom and the oxygen atom. This means that one should distinguish vdW radii of atoms in different environments. The atoms confined in tetrahedral or octahedral environments (e.g. Si, Bi, most of d, f-elements, and other elements considered by Alvarez in Ref. [10]) would show an increased effective size due to the unaccounted steric effects. The corresponding D_{max} values will merely indicate the position of the first maximum of radial distribution function and make little sense in terms of noncovalent interactions. Only the atoms in an "open" environment such as trigonal, square planar or square pyramidal configurations can be used to determine R_{vdW} from contact distance distributions without shielding effects to be crucial.

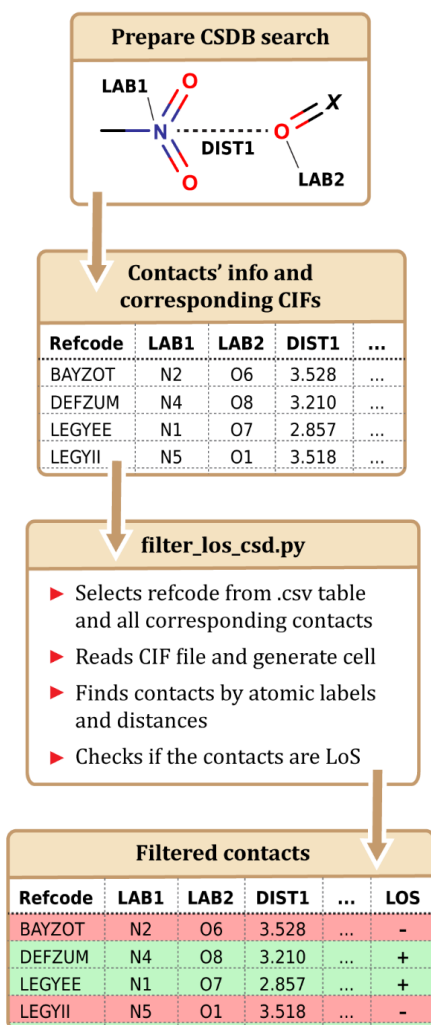


Figure 5. Description of developed workflow for non-LoS contacts filtration.

These examples illustrate that despite all advantages, the element-defined R_{max} radii still fail to generally define the “energy minimum position” of intermolecular interactions. The preferred and more accurate approach is to directly utilize D_{max} values determined for the given atom pair contact rather than the sum of vdW radii. In this way, the structural analysis will automatically account for the specificity of the analyzed interactions, their anisotropy, and the impact of steric effects. We have developed an algorithm and implemented it in a script (deposited at the GitHub^[21]) that allows searching the CSD for intermolecular contacts with certain geometry (ConQuest output) with their subsequent classification as line-of-sight or shielded contacts (Figure 5). The produced datasets can readily be used for the determination of the D_{max} using any standard table processing or data analysis software. Such D_{max} values obtained for specific contacts with a certain geometry can be used to create high-throughput geometry-based descriptors of intermolecular interactions, applicable e.g. to high-throughput screening of heterogeneous catalysts.^[22]

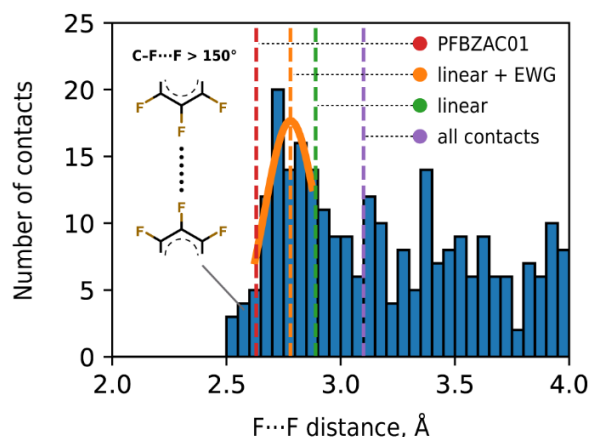


Figure 6. Distance distribution for linear ($C-F\cdots F > 150^\circ$) intermolecular $F\cdots F$ contacts between two electron-withdrawing fragments. From left to right: red dashed line denotes the shortest $F\cdots F$ intermolecular distance in PFBZAC01; orange line stands for D_{max} of linear $F\cdots F$ contacts between two aromatic fragments; green and purple lines stand for D_{max} of linear and all $F\cdots F$ contacts, respectively.

Although the described approach is statistical, it can be used for the analysis of specific systems. In this case, one needs to compare the length of an intermolecular contact with D_{max} of the distribution of the corresponding contacts. Detailization of atom environment of interacting atoms and geometry of an interaction eliminates the bias caused by differences in nature of atoms and anisotropy of the interaction. As a result, one can analyze the potential energy surface of the specific condensed system using experimental structural data. The same outcome can be achieved by analyzing potential energy surface by means of quantum chemical modelling, however, its application to condensed systems is qualitative and not straightforward.^[23] As representative example of the approach we provide the analysis of the short $F\cdots F$ contact in crystalline pentafluorobenzoic acid (PFBA, CSD refcode PFBZAC01).^[24] It is 2.63 Å long, and both $C-F\cdots F$ are equal to 155° . This is much shorter than the sum of the element-specific R_{max} (3.10 Å) suggesting that such a contact should be forced and potentially repulsive in nature. However, this conclusion does not hold when atom-type specific radii are utilized for the analysis. The interatomic contact cannot anymore be regarded as an ultrashort one when considering D_{max} for linear $F\cdots F$ contacts (2.90 Å), or, even more specifically, the aromatic C_3F_3 fragments (2.78 Å). (Figure 6). Unfortunately, further refinement of the fluorine-containing fragments is currently not possible due to the small amount of available structural data. However, given that the fluorine environment in PFBA is more electronegative than in more common C_6F_5 groups, we can assume that the most probable $r(F\cdots F)$ in PFBA is even smaller than 2.78 Å. This implies that such “ultrashort” contact are the intrinsic characteristics of the molecule itself and the role of the packing features for their occurrence is only minor if any.

Conclusion

In summary, a new approach for automated analysis and classification of noncovalent interactions has been developed. The key feature of the reported methodology is the filtration of the direct interatomic contacts from the other background structural features based on the LoS concept. The validity of this approach has been confirmed by density functional theory calculations. The LoS concept was used to recompute R_{vdW} for light elements, which turned out to be substantially larger than those currently accepted by the chemistry community. Our analysis reveals that the underestimations of the “atomic sizes” noted earlier for most tabulated vdW radii (R_{half}) is solely related to the deficiencies of the datasets used for their determination. The R_{max} introduced here are free from statistical bias and are based on clear physical grounds. We anticipate the high practical utility of R_{max} , and particularly, their atom type-specific variations for improving of molecular sizes in different chemical methods and approaches, and for the analysis of intermolecular interactions on a wide variety of systems including the experimental structural databases and the results of theoretical calculations on molecular and condensed systems relevant to various fields of chemistry and material sciences. The current LoS approach implemented now in the relevant software enables the quantitative analysis of specificity, anisotropy and steric effects of intermolecular interactions while benchmarking databases as well as studying specific systems.

Computational Methods

Version 5.39 with 4 updates (up to August 2018) of CSD^[6] was used for selection of organic crystals containing H(D), B, C, N, O, F, Si, P, S, Cl, As, Se, Br and I atoms. Disordered, erroneous, polymeric, pressurized, powder structures and experiments with R-factor > 0.075 were removed from consideration. 224 001 selected crystals were used for search of unique intermolecular contacts A...B with distance D(A...B) up to 7.0 Å. C–H, N–H and O–H bond lengths were normalized to CCDC/ConQuest defaults: C–H: 1.089 Å, N–H: 1.015 Å, O–H: 0.993 Å. Acetylenic C_{sp}–H bond lengths were normalized to 1.06 Å (neutron diffraction: ACETYL05, RALDEN01, XEHLEB, ZULDEP01), and S–H bond lengths were normalized to 1.34 Å (microwave data: H₂S,^[25] neutron diffraction: NALCYS02). For each contact the following information were collected: (1) contact geometry, (2) chemical nature of contact atoms, (3) shielding atom, and (4) contact shielding value. A total of c.a. 640 000 000 contacts were found, more than 40 000 000 of which was LoS depending on used vdW radii (41 346 551 for the final version from **Table 1**). These data were used further to build and analyze the distribution of distances of various contacts and is available for download.^[26]

Obtained line-of-sight A...B contacts were used to plot histograms of contact distance distributions for all possible A, B atom type pairs (Table S1). Primary analysis of these distributions combined with chemical common sense allowed to select atom types and, therefore, contacts used for the van der Waals radii determination. The main requirements were: (1) the contact corresponds to non-specific interaction; (2) influence of steric effects on A...B distance can be excluded; (3) line-of-sight contacts distribution contains a line-of-sight peak that is similar to the Gaussian function; (4) addition of the contact to the list of contacts used for van der Waals radii determination does not change any radius significantly (>0.05 Å). This selection is subjective to a certain degree, however, it's well suited for our final goal which was to obtain R_{vdW} corresponding to weak nonspecific interactions that are not affected by any effects. Selected

contact types were used for R_{max} determination and are marked with ‘+’ sign in the second column of Table S1. Using the data of Table S1 together with the data on intermolecular contacts^[26] allows one to reproduce this work, or to choose another set of contact types to determine another version of R_{max} .

Quantum chemical computations were performed with the Gaussian16^[27] in the B3LYP/6-311++G(d,p) approximation, and the subsequent NCIS analysis was performed with the Multiwfn package.^[28] Geometry of the H₃N...CH₃F complex was obtained by merging optimized NH₃ and CH₃F molecules into the staggered C_{3v} structure with D(N...C) = 3.0 Å. The N...C–F angle was changed so that the H₃N...CH₃F complex retains the N...(H)C–F symmetry plane. NCI surface (0.5 isosurface value) dependence on N...C–F angle remains unchanged with D(N...C) increasing.

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Keywords: Van der Waals radii • molecular crystals • CSD analysis • intermolecular contacts • intermolecular interactions

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