Microstructure determines water and salt permeation in commercial ion exchange membranes

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Abstract

Ion exchange membrane (IEM) performance in electrochemical processes such as fuel cells, redox flow batteries, or reverse electrodialysis (RED) is typically quantified through membrane selectivity and conductivity, which together determine the energy efficiency. However, water and co-ion transport (i.e., osmosis and salt diffusion / fuel crossover) also impact energy efficiency by allowing uncontrolled mixing of the electrolyte solutions to occur. For example, in RED with hypersaline water sources, uncontrolled mixing consumes 20-50% of the available mixing energy. Thus, in addition to high selectivity and high conductivity, it is desirable for IEMs to have low permeability to water and salt in order to minimize energy losses. Unfortunately, there is very little quantitative water and salt permeability information data available for commercial IEMs, making it difficult to select the best membrane for a particular application. Accordingly, we measured the water and salt transport properties of 20 commercial IEMs and analyzed the relationships between permeability, diffusion and partitioning according to the solution-diffusion model. We found that water and salt permeance vary over several orders of magnitude among commercial IEMs, making some membranes better-suited than others to electrochemical processes that involve high salt concentrations and/or concentration gradients. Water and salt diffusion coefficients were found to be the principal factors contributing to the differences in permeance among commercial IEMs. We also observed that water and salt permeability were highly correlated to one another for all IEMs studied, regardless of polymer type or reinforcement. This finding suggests that transport of mobile salt in IEMs is governed by the microstructure of the membrane, and provides clear evidence that mobile salt does not interact strongly with polymer chains in highly-swollen IEMs.

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1.0 Introduction

Ion exchange membranes (IEMs) are versatile materials used in a variety of electrochemical processes for water and waste treatment, energy production, energy storage, and industrial separation.^{1–3} IEM performance in electrochemical systems is typically quantified through membrane permselectivity and resistance, which together determine the energy efficiency and/or power output of a given process.^{4–6} Permselectivity measures the degree to which IEMs selectively allow ions of opposite charge (counter-ions) to permeate, while excluding ions of like charge (co-ions).⁷ In a cation exchange membrane (CEM), for example, cations are the counterions and anions are the co-ions.

Permselectivity and resistance concern the transport of counter-ions. However, water and co-ions also permeate through IEMs (see Figure 1). $8-15$ Water permeates the membrane by two mechanisms: osmosis and electro-osmosis. Osmosis is simply the diffusion of water, while electro-osmosis refers to the transport of water molecules in the hydration shells of counter-ions permeating the IEM as a result of migration in an electric field. Co-ions permeate IEMs accompanied by counter-ions as "mobile salt."^{10,16} In dense polymers in which water permeation by convection is negligible, co-ion transport can be viewed as salt diffusion through the membrane.^{10,17}

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Figure 1. Mass transport phenomena occurring inside electrodialysis (ED) (left) and reverse electrodialysis (RED) (right) stacks.

Because neither osmosis nor salt diffusion responds to electric fields, both have a detrimental effect on the energy or separation efficiency of electrochemical processes such as electrodialysis (ED) and reverse electrodialysis (RED) .^{12,18–21} Osmosis and salt diffusion both lower the salt concentration in the concentrated feed, which in ED compromises separation, and in RED causes uncontrolled mixing (i.e., mixing that does not produce electricity, Figure 1). The magnitude of the effects of water and salt transport on efficiency depends on both the process (ED, RED, energy storage, etc.) and the process conditions (e.g., salt concentrations). For example, in RED with seawater and river water, the combined effects of salt diffusion and osmosis reduce power output by approximately 10%-25%.^{11,12,18} Another study found that uncontrolled mixing reduced the current efficiency of RED from 65% to only 20%.¹⁹ With larger concentration gradients (e.g., hypersaline water sources or industrial brines), uncontrolled mixing reduces current efficiency by 20-50%.¹⁸ In ED desalination, osmosis reduced current efficiency by approximately 10% compared to ideally-selective membranes, ¹⁹ and salt diffusion was estimated to increase the required energy consumption by 2-3 times.²⁰ In energy storage applications, osmosis reduces the

round-trip energy efficiency by as much as 50%, while salt diffusion has a similar or smaller impact, depending on the membrane used.^{14,15,22,23} The effect of osmosis on energy efficiency increases dramatically with higher salt concentrations, limiting the concentrations that can be used and consequently restricting the energy density of these systems.²³

Thus, in addition to high permselectivity and low resistance, it is desirable for IEMs to have low permeability to water and salt in order to minimize energy losses. Unfortunately, very little quantitative data exists for the water and salt permeance of commercial IEMs, making it difficult to select the best IEMs for a particular application. Furthermore, it is currently unknown how water and salt permeance are related to other membrane properties. Such knowledge is necessary for the development of advanced IEMs.

Accordingly, the objectives of this study were to: 1) quantify the water and salt transport characteristics of commercially-available IEMs; 2) evaluate whether water and salt transport are controlled by the thickness or the intrinsic transport properties (i.e., partitioning and/or diffusion) of the membranes; and 3) examine relationships between these transport characteristics and membrane polymer type. We measured the water and salt permeability of 20 IEMs using a twocompartment cell and characterized other properties using well-known techniques. Using the solution-diffusion model framework, we report partition and diffusion coefficients for both water and salt for each membrane, and relate the permeability, partition, and diffusion coefficients to polymer backbone type. Our results show that membrane microstructure is the primary factor governing water and salt transport in IEMs.

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2.0 Theoretical background

2.1 Solution-diffusion model

The solution-diffusion model is the most widely-accepted framework for describing the transport of small molecules, such as water and salt, through dense polymer membranes.^{8,10,17} In this model, molecules are assumed to permeate the membrane by partitioning from the bulk solution into the membrane polymer at the upstream interface, diffusing through the membrane, and then partitioning into the bulk solution at the downstream interface. As such, solvent and solute permeate independently of one another (i.e., convection and frictional coupling of fluxes are neglected). While there is not a vast body of literature confirming whether the solution-diffusion model is rigorously applicable to IEMs, its validity is well established for desalination polymers,¹⁰ and IEMs have pore sizes in the same size range as reverse osmosis (RO) and nanofiltration (NF) membranes (0.4-2 nm for RO/NF membranes vs. 0.4-1.5 nm for IEMs).^{2,13,24–} 26 Furthermore, several researchers have applied the solution-diffusion model to describe salt transport in IEMs with good results. Therefore, we adopted the solution-diffusion model to analyze water and salt transport data throughout this paper.

The permeability $P(m^2 \text{.} \text{s}^{-1})$ represents the steady-state flux of a molecule through the membrane, normalized by membrane thickness and the driving force. ⁸ Permeability is the product of a kinetic parameter – the molecular diffusion coefficient $D(m^2.s^{-1})$ –and a thermodynamic parameter—the molecular partition coefficient K (dimensionless). Thus,

$$
P = DK \tag{1}
$$

The diffusion coefficient is a measure of how quickly the substance transports through the membrane, while the partition coefficient is defined as the concentration of the substance in the membrane divided by its concentration in bulk solution. Throughout this manuscript, we will use subscripts w and s to denote transport properties for water and salt, respectively.

2.2 Donnan-Manning theory

Kamcev et al. recently showed that Manning's counter-ion condensation theory can be used in conjunction with Donnan theory to predict salt partition coefficients (K_s) in IEMs with good accuracy.^{9,27,28} The crucial parameter in Manning theory is the Manning parameter, ξ , which is defined as

$$
\xi = \frac{\lambda_b}{b} \tag{2}
$$

where b (m) is the distance between fixed charge sites along the polymer chain and λ_b (m) is the Bjerrum length of the solution inside the membrane. If ξ and the fixed charge concentration of an IEM are known, Donnan-Manning theory can be used to calculate the mobile salt concentration inside the membrane as a function of bulk salt concentration.²⁷ Conversely, ξ can be determined from experimental data if the concentration of fixed charges and mobile salt in an IEM are known. Given the very recent emergence of Donnan-Manning theory as a useful tool for predicting IEM behavior, ξ has only been reported for three commercial IEMs to date.²⁷

3.0 Experimental

3.1 Ion exchange membranes

We measured the properties of 20 homogeneous commercial IEMs with a diverse range of characteristics representative of a majority of the IEMs commonly studied in literature. Table 1 summarizes the structural, physical, and chemical characteristics of the IEMs studied. All membranes were stored as directed by the respective manufacturers. Prior to measurements, membrane coupons were immersed in sodium chloride solutions at room temperature for a

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minimum of 24 h. The concentration of the equilibration solution was matched to that of the measurement solution, and the solution was changed at least three times to ensure complete conversion of the functional groups to either $Na⁺$ or Cl⁻ form. We prepared all solutions from reagent grade sodium chloride (Alfa Aesar, 99+% purity). All measurements reported in this work represent the mean and standard error of at least three independent measurements of replicate membrane coupons.

3.2 Membrane thickness

We measured membrane thickness with a micrometer (L.S. Starrett Co., Athol, MA, model 3732XFL-1) immediately following tests of osmosis and diffusion (see Section 3.6). After removing the membrane coupon from the test cell, we blotted it dry with a laboratory wipe, and measured its thickness. It was important to measure the thickness in this way because the membrane may swell differently when exposed to a concentration gradient different from that between pure water and 4 M NaCl solution.

Table 1. Structural, chemical, and physical properties of ion exchange membranes used in this work. Reported values represent the average and propagated standard error of at least three replicates.

^a MAm = methacrylamide, pAro = polyaromatic, $St/DVB = styrene - divinylbenzene copolymer$, $sPEEK = sulfonated$ poly(etheretherketone), PFSA = perfluorinated sulfonic acid, PE = poly(ethylene), PP = poly(propylene), PVC = poly(vinylchloride). Structural details not available in literature were obtained by personal communication with the respective manufacturers. Structural and reinforcement details for the Fujfilm membranes are assumed based on information in patent literature.^{29,30}

^b Wet thickness measured after experiments in contact with 4 M NaCl (concentrated side) and pure water (dilute side) (see Section 3.2).

^c Ion exchange capacity (see Section 3.4).

^d Swelling degree of the membrane in the NaCl form in equilibrium with 4 M NaCl (see Section 3.3).

^e Fixed charge density per unit of water sorbed by the membrane (see Section 3.4).

^f Calculated from measured co-ion partition coefficient in 0.5 M NaCl (see Section 3.5 and Table S1).

3.3 Water Content

The swelling degree of IEMs was measured gravimetrically.⁴ Membrane coupons were equilibrated in the desired concentration of salt solution as described in Section 3.1, then blotted dry with a laboratory wipe^{31,32} and weighed immediately on an analytical balance. Membranes were subsequently dried in an incubator at 65 \degree C for 48 h³³ and then weighed again. Swelling degree (*SD*, $g H_2O$ per g dry polymer) was calculated as⁴

$$
SD = \frac{m_{wet} - m_{dry}}{m_{dry}} \tag{3}
$$

where m_{wet} (g) and m_{dry} (g) are the wet and dry masses, respectively. Membrane coupons were not used for any further analysis after drying.^{31,32}

We used the swelling degree to calculate the volume fraction of water in the membrane, ϕ_w , and the water partition coefficient, K_w , as¹⁰

$$
\phi_w = \frac{SD}{SD + \frac{\rho_w}{\rho_p}}\tag{4}
$$

and

$$
K_w = \frac{\phi_w M_w}{c_w^s V_w} \tag{5}
$$

where ρ_p (g.mL⁻¹) is the dry polymer density, for which we used a value of 1.15 g.mL⁻¹ based on a weighted average of the dry densities of the base polymers for the IEMs used in this work $34-38$ (see Table 1). M_w (18.015 g.mol⁻¹) is the molar mass of water, and C_w^s (g.L⁻¹) is the mass concentration of water in the bulk solution. Note that when C_w^s is approximately equal to the density of pure water, which is true within \sim 1% for salt concentrations lower than 0.5 M, then $K_w \approx \phi_w$. Although the two parameters are effectively equal in much of the desalination

literature,^{10,39} we will make a distinction between them due to the high salt concentration used in this work (4 M, $C_w^s = 915.5 \text{ g.L}^{-1}$). Throughout the text, we use the terms "water sorption," "water uptake," or "swelling" to refer generally to water absorption by IEMs as indicated by ϕ_w , SD, or K_w .

3.4 Membrane charge

We quantified membrane charge through ion exchange capacity (IEC, meq charge per g dry polymer) and fixed charge concentration (mol charge per L of water absorbed by the membrane). IEC was determined according to well-established titration methods. For CEMs, we soaked membrane coupons in 1 M HCl for at least 12 h^4 to convert charged sites to H⁺ form, replacing the solution at least twice $40,41$ to ensure complete ion exchange. Membranes were then removed from the solution, rinsed thoroughly with DI water, and immersed in 2 M NaCl for at least 3 h, again changing the solution at least twice.⁴ We collected all of the discarded NaCl solution and analyzed it for H^+ by titration with 0.1 M NaOH.³³ For anion exchange membranes (AEMs), we soaked the membrane coupons in 2 M NaCl for at least 12 h, changing the solution at least twice, to convert all charged sites to Cl form. Then, we quickly removed the membranes and rinsed with DI water that had been degassed under nitrogen. The degassing was necessary to prevent dissolved $CO₂$ from exchanging with Cl⁻ ions and biasing the measurement.⁴⁰ Membranes were then placed in 2 M NaNO₃ solution for at least 6 h,³³ during which the solution was changed at least twice. The exchanged solutions were collected and analyzed for Cl⁻ ion by titration with 0.1 M AgNO₃.^{4,33} Both AEMs and CEMs were subsequently dried in an incubator at 65 °C for 48 h.³³ Ion exchange capacity was calculated as⁴

$$
IEC = \frac{V_{titrant}C_{titrant}}{m_{dry}}
$$
 (6)

where $V_{titrant}$ (L) and $C_{titrant}$ (M) are the volume and concentration of titrant used,

respectively, and m_{dry} (g) is the dry weight of the membrane coupon.

The concentration of fixed charges inside the IEM, C_{fix} , in units of equivalents of charge per L of water absorbed by the membrane, is given by

$$
C_{fix} = \frac{IEC}{SD} \rho_w \tag{7}
$$

3.5 Co-ion sorption and Manning parameter

Kamcev et al.²⁷ showed that salt sorption data obtained at a single salt concentration can be used to calibrate the Manning parameter ξ and predict salt sorption at any other salt concentration. Accordingly, we used procedures similar to those of Kamcev et al.^{27,28} to determine mobile salt sorption and ξ in 0.5 M NaCl, then calculated the concentration of mobile salt in each membrane in 4 M NaCl. Briefly, we equilibrated membrane coupons in 0.5 M NaCl as described in Section 3.1. We then removed each coupon from solution, blotted the surface dry with a laboratory wipe, weighed it, and placed it in a plastic vial containing 30 mL of pure water for at least 48 h. Mobile salt in the membrane desorbed into the water during this period. Kamcev et al. showed that a single desorption step (e.g., without changing the water) was sufficient to effectively desorb all mobile salt in the membrane.⁴² After desorption, we analyzed the co-ion concentration (Na⁺ for AEMs, Cl⁻ for CEMs) using inductively-coupled mass spectrometry for Na⁺ (see Supporting Information for method details) and an ion-selective electrode (Fisher Scientific, Fair Lawn, NJ, model 13-620-100) for Cl⁻. The membrane coupons were removed from the vials, dried in an incubator at 65 \degree C for 48 h,³³ and weighed. The co-ion concentration in the desorption solution and the membrane weights were used to obtain the co-ion concentration in the membrane $(\bar{\mathcal{C}}_s)$, mol per unit volume of water sorbed) as

$$
\bar{\mathcal{C}}_S = \frac{c_c V_w \rho_w}{m_{wet} - m_{dry}} \tag{8}
$$

where C_c (M) is the co-ion concentration in the desorption solution, V_w (30 mL) is the volume of the desorption solution, ρ_w (0.998 g.mL⁻¹) is the density of water, and m_{wet} and m_{dry} (g) are the wet and dry masses of the membrane coupon, respectively. The measured co-ion concentrations in 0.5 M NaCl, the measured Manning parameters, and the calculated co-ion concentrations in 4 M NaCl are given in Table S1.

Next, K_s was calculated as

$$
K_s = \frac{\bar{c}_s \phi_w}{c_s} \tag{9}
$$

where \bar{C}_s (see Section 3.5) and C_s are the (mobile) salt concentrations inside the IEM and in bulk solution, respectively. Throughout the text, membrane-phase salt concentrations are reported in units of mol salt per L of water absorbed by the membrane, as required by Manning theory.^{9,27,28} ϕ_w in Equation (9) serves as a conversion factor to convert the numerator into units of mol salt per L of swollen polymer, which is the appropriate unit of measure to use when calculating K_s .

3.6 Simultaneous measurement of osmosis and diffusion through IEMs

Figure 2. Schematic of two-compartment cell used for permeability measurements. Compartment volume = 16 mL, exposed membrane area = 7.55 cm^2 , stirring rate = 300 rpm. Burets with 0.05 mL graduations were connected to each compartment through small openings (diameter <1 mm) and approximately 15 cm of tubing. At the beginning of each experiment, the fluid levels in the two burets were equalized to prevent any hydrostatic pressure difference between the compartments.

We measured water and salt permeability simultaneously using the two-compartment cell illustrated in Figure 2. One side of the cell contained 4 M NaCl solution, the other contained pure water. We chose 4 M NaCl for the concentrated solution to maximize the rate of osmosis and facilitate water transport measurements (as suggested by $Tanaka³³$), and also because non-ideal transport of water and salt are of greatest concern in IEM processes involving high concentrations.¹⁸ Membrane coupons were stabilized in the cell for 1-4 h prior to measurements in order to allow for osmosis and diffusion to reach a pseudo-steady state. The solutions were changed at least once during the stabilization period, and the compartments were refilled with

fresh solutions immediately prior to the measurement. Once measurements began, the salt solutions in both compartments were stirred at 300 rpm by means of magnetic stir bars.

During measurement of salt and water permeability, water flowed into the high-concentration compartment as a result of osmosis, while salt diffused into the pure water compartment. Each cell compartment was sealed and connected to a buret with 0.05 mL markings, allowing the volume change in the compartment to be measured with high precision. We measured changes in the volumes of the compartments and in the salt concentration in the dilute compartment with time for at least 60 min, or until the volume change was at least 0.25 mL (corresponding to 5 markings on the buret). To obtain precise volume measurements, we watched the meniscus in each buret and waited until it exactly crossed each marking, then recorded both the volume and the elapsed time, rather than recording volume at pre-determined time intervals. Water flux was obtained from the rate of volume change and used to calculate water permeance and permeability (see Section 3.7).

A conductivity probe (eDAQ Pty Ltd, Sydney, Australia, model ET915) was placed in the pure water compartment to quantify the change in conductivity with time. A calibration curve was used to obtain salt concentration from conductivity measurements, and the time series of salt concentration data was used to calculate the salt permeance and permeability (see Section 3.8).

3.7 Calculation of water permeance and permeability

Because we measured osmosis (water flux) and diffusion simultaneously, it was necessary to account for the diluting effect of osmosis on the salt concentration gradient. In other words, over time, water flux from the pure water compartment diluted the salt concentration in the other

compartment, lowering the driving force for diffusion and osmosis. We accounted for this effect by solving an appropriate mass balance (see Supporting Information).

First, water permeance $A(L.m^{-2}.hr^{-1}.bar^{-1})$ was calculated from the steady-state volumetric water flux n_w (L.m⁻².hr⁻¹) as¹⁰

$$
A = \frac{n_w}{\Delta P - \Delta \pi} \tag{10}
$$

where ΔP and $\Delta \pi$ (bar) are the net differences in hydrostatic and osmotic pressure, respectively, across the membrane. In our experiments, both burets were filled to the same initial height, so $\Delta P = 0$, while $\Delta \pi = 243.4$ bar (calculated using the Gibbs equation and the Pitzer model^{43–45} for activity coefficients).

Next, we calculated D_w from water permeance as ^{10,39}

$$
D_w = A \frac{RT}{v_w L} (1 - \phi_w)^2 (1 - 2\chi \phi_w) \quad , \tag{11}
$$

where R (8.314 J.mol⁻¹.K⁻¹) is the ideal gas constant, T (K) is the temperature, L (m) is the swollen membrane thickness (Section 3.2), V_w (0.0182 L.mol⁻¹) is the molar volume of water, ϕ_w (dimensionless) is the volume fraction of water in the membrane (Section 3.3), and χ (dimensionless) is the Flory-Huggins interaction parameter, determined by fitting water sorption data in 4 M NaCl to the Flory-Huggins model (Equation S15). In highly swollen polymers such as many of the IEMs we studied, convective frame-of-reference and thermodynamic effects must be accounted for when converting water permeance into water permeability.^{10,39} Equation (11) reflects both corrections (see Supporting Information for detailed discussion).

Water permeability, P_w , was obtained from the water diffusion coefficient D_w and the water partition coefficient K_w according to

$$
P_w = D_w K_w \tag{12}
$$

3.8 Calculation of salt permeance and permeability

Similarly to water, we analyzed salt diffusion data to obtain salt permeability, diffusion coefficient, and partition coefficients $(P_s, D_s, \text{ and } K_s,$ respectively) according to

$$
P_s = D_s K_s \tag{13}
$$

 P_s was calculated directly from the observed salt concentration vs. time data using a mass balance that accounted for the effects of both osmosis and diffusion on the salt concentration in the dilute compartment of the cell (see Supporting Information).

Having obtained K_s (Section 3.5), we then calculated the salt diffusion coefficient D_s as

$$
D_s = \frac{P_s}{K_s} \tag{14}
$$

Finally, the salt permeance $B(L.m^{-2}.hr^{-1})$ was obtained from the measured salt permeability and thickness as

$$
B = \frac{P_S}{L} \tag{15}
$$

4.0 Results and Discussion

4.1 Membrane permeance

4.1.1 Water permeance

We first consider the water permeance of 20 commercial IEMs. Water permeance varied over about 1 order of magnitude among the IEMs tested, from 0.001 - 0.011 L.m⁻².hr⁻¹.bar⁻¹ (Figure 3a and 3b, solid bars, Table S2), consistent with the range of values reported in literature (0.005- 0.009 L.m⁻².hr⁻¹.bar⁻¹).^{13,23,46} It is noteworthy that the water permeance of CEMs was generally higher than that of the AEMs.

Figure 3. Water permeance (solid bars, linear scale) and salt permeance (empty bars, log scale) of commercial (a) AEMs and (b) CEMs measured in a diffusion cell containing 4 M NaCl and pure water. In all panels, red bars denote AEMs and blue bars denote CEMs. Error bars represent the propagated standard error of at least three replicates.

4.1.2 Salt permeance

The salt permeance of the IEMs varied by \sim 2.5 orders of magnitude, from 0.002-0.5 L.m⁻².hr⁻¹ (Figure 3a and 3b, empty bars, Table S2). This range of values is consistent with data reported by Porada et al.²¹ for lab-prepared IEMs based on FAS and FKE polymer solutions (0.003-0.025) $L.m^{-2}.hr^{-1}$). Similarly to the results for water permeance, CEMs generally had higher salt

permeance than AEMs, but the contrast between CEMs and AEMs was greater than that seen for water permeance.

4.2 Contribution of water and salt permeability to permeance

Having observed variations of several orders of magnitude in both the water and salt permeance of IEMs, we next sought to understand whether those variations were caused by differences in material properties (i.e., permeability) or geometry (i.e., thickness). Thus, we will now discuss measured water and salt permeability, membrane thickness, and their relationship with permeance.

4.2.1 Water permeability

Water permeance is related to water permeability P_w according to^{10,39}

$$
A = \frac{P_w}{L} \frac{V_w}{RT} \tag{16}
$$

According to Equation 16, variations in P_w and L together comprise all of the variation in A by definition. Thus, by examining the magnitudes of the respective variations in P_w and L, we can gain insight into which of the two variables makes a greater contribution to variations in permeance. Note that Equation 16 is approximate in the case of highly swollen polymers^{10,39} such as some of our IEMs. We present it here for the purpose of discussion, as we obtain the same conclusion when using a more rigorous equation (see Supporting Information).

Figure 4a presents a plot of water permeance vs. thickness for all IEMs studied. The thicknesses of the membranes varied by approximately 1 order of magnitude, from 20-232 µm (Table 1). Thickness values clustered into roughly two groups along the *x*-axis: a "thin" group (20-32 µm) and a "thick" group (96-136 μ m, Figure 4a and Table 1). Inspection of Figure 4a shows that

within each thickness group, A varied by nearly an order of magnitude. Thus, there were substantial differences in water permeance among IEMs with approximately the same thickness, indicating that variations in water permeance were driven primarily by differences in permeability. Furthermore, a plot of $\log A$ vs. $\log P_w$ (Figure 4c) shows that higher permeance was closely associated with higher permeability within each thickness group. As with permeance, the permeability within each thickness group varied over nearly an order of magnitude from $\sim 2 \times 10^{-11} - 2 \times 10^{-10}$ m².s⁻¹ (Figures 4c and S2), reinforcing the conclusion that variations in permeance were driven by variations in permeability rather than in thickness.

4.2.2 Salt permeability

As was the case with water, the salt permeability and thickness determine salt permeance by definition (see Equation 15). Figure 4b presents salt permeance vs. thickness and shows that the permeance within each of the thickness groups varied by roughly 2 orders of magnitude. Thus, we can conclude that differences in salt permeance were primarily attributable to differences in salt permeability rather than differences in thickness. The salt permeability varied over \sim 3 orders of magnitude across all membranes, from 10^{-11} to 10^{-14} m².s⁻¹ (Figure 4d). Similarly to water, higher salt permeance was clearly associated with higher permeability within each thickness group (Figures 4d and S2).

In summary, we found that the substantial (1-3 order of magnitude) differences in water and salt permeance among IEMs were primarily attributable to differences in the respective permeabilities of the membranes, rather than differences in their thickness.

Figure 4. Water and salt permeance of 20 commercial IEMs measured in 4 M NaCl and pure water vs. membrane thickness $L(a,b)$ and permeability $P(c, d)$. Lines in panels c and d are drawn to guide the eye. Red symbols denote AEMs, blue symbols denote CEMs, and the shape of the symbol indicates the membrane polymer type (see legend in inset of panel (d)). Error bars represent the propagated standard error of at least three replicates. Refer to Table 1 for definitions of the membrane polymer abbreviations.

4.3 Contribution of partitioning and diffusivity to permeability

Since we observed substantial variations in permeability among IEMs, and those variations were the primary factor affecting membrane permeance, we will now examine the partition and diffusion coefficients of the IEMs, which together determine the permeability (see Equation 1).

4.3.1 Water partition and diffusion coefficients

We first consider the partition and diffusion coefficients of water in the IEMs (Figures 5a and 5c, Tables S3 and S4). Water partition coefficient K_w varied from 0.1 to 0.35, while the water diffusion coefficient D_w varied by about 1 order of magnitude, from $10^{-10} - 10^{-9}$ m².s⁻¹. The obtained values of D_w were consistent with average D_w values for six commercial IEM pairs reported by Veerman et al.¹¹ (5.8x10⁻¹¹ - 7.9x10⁻⁹ m².s⁻¹). K_w is not usually reported for IEMs, but the corresponding swelling degrees (0.09-0.37, Table 1) are in the same range as those reported by Guler et al.⁴ for twelve commercial IEMs (0.08-0.56). Ji et al.⁴⁷ reported $K_w = 0.06$ -0.51 in a series of lab-synthesized CEMs, which is also similar to the range we obtained. The fact that D_w varied over a substantially larger range than K_w (~10x vs. ~3x) indicates that variations in D_w were more important than variations in K_w in explaining variations in P_w . Furthermore, although neither D_w nor K_w clustered into groups as thickness did, we observed that for any given value of K_w , D_w varied by up to one order of magnitude (Figure S3). In contrast, for any given value of D_w , K_w varied over a substantially smaller range.

 D_w and K_w were not correlated to each other (R²<0.02, p=0.41, Figure S3). This lack of correlation indicates that water partitioning (water sorption) is not strongly coupled to the rate of water transport in IEMs. This finding suggests that water molecules hydrating the fixed charge sites within the polymer are relatively immobile. That is, a highly-charged IEM may absorb a great deal of water (high K_w), but only "free" water molecules within the structure contribute to diffusion (thus high K_w does not necessarily lead to high D_w).

Figure 5. Water and salt transport properties of 20 commercial ion exchange membranes measured in a diffusion cell containing 4 M NaCl and pure water. (a) Water permeability vs. water diffusion coefficient. (b) Salt permeability vs. salt diffusion coefficient. (c) Water permeability vs. water partition coefficient. (d) Salt permeability vs. salt partition coefficient. Red symbols denote AEMs, blue symbols denote CEMs, and the shape of the symbol indicates the membrane polymer type (see legend in inset of panel (b)). Error bars represent the propagated standard error of at least three replicates. Refer to Table 1 for definitions of the membrane polymer abbreviations.

4.3.2 Salt partition and diffusion coefficients

Salt partition coefficients K_s ranged from 0.05-0.24 (Figure 5b, Table S3 and S4), while salt diffusion coefficients D_s varied from about 10^{-10} to 10^{-13} m².s⁻¹ (Figure 5b, Table S3 and S4). The

obtained values of K_s were similar to the range reported by Kamcev et al.⁹ for three commercial IEMs in 1 M sodium chloride (0.08-0.14), and to values for several lab-synthesized CEMs in 0.5 or 1 M sodium chloride reported in other studies^{47,48} (0.2-0.25). D_s values also compared well with previous reports in the literature $(1.8x10^{-14}$ to $1x10^{-10}$ m².s⁻¹).^{11,49–51} The larger variation in D_s compared to D_w (3 orders of magnitude vs. 1 order of magnitude, respectively) was consistent with previous reports as well: Veerman et al.¹¹ reported that D_s ranged from $1.8 \times 10^{-14} - 3.2 \times 10^{-11}$ $\text{m}^2 \cdot \text{s}^{-1}$, while D_w ranged from 5.8x10⁻¹¹ - 7.9x10⁻⁹ $\text{m}^2 \cdot \text{s}^{-1}$ for a set of commercial IEM pairs.

As was the case with water, D_s varied over a substantially larger range than K_s . For any given value of K_s , D_s varied by at least one order of magnitude (Figure S3). The much larger variation in D_s compared to K_s (1,000x vs. 5x) indicates that diffusion was primarily responsible for the observed variations in P_s among IEMs. Both $\log D_s$ and K_s correlated strongly with $\log P_s$ (p<0.01, Figures 5b and 5d), but similarly to water, the regression coefficient for diffusion coefficient was greater than that for partition coefficient (\mathbb{R}^2 =0.96 vs. 0.56, respectively), reinforcing the conclusion that variations in D_s drive variations in P_s .

 D_s and K_s were weakly correlated to one another (R²=0.36, p<0.01, Figure S3), indicating that partitioning and diffusion of mobile salt in IEMs are coupled to some extent. This is in contrast to the finding for water that diffusion and partitioning were not correlated (Figure S3).

In summary, for both water and salt, permeability was correlated to diffusion and partition coefficients. However in both cases, P and D varied over several orders of magnitude, while K varied over a much smaller range, indicating that differences in diffusion coefficient were the primary cause of variations in permeability. D_w and K_w were not correlated, while D_s and K_s were weakly correlated.

4.4 Membrane polymer

Having examined the water and salt transport properties of commercial IEMs in aggregate, we will now consider differences in transport properties among different membrane polymers. It is evident from Figures 4c and 4d that membranes in the "thick" group generally had higher permeability than those in the "thin" group (although the ranges overlap). This finding is logical considering these IEMs are engineered for commercial applications: manufacturers may have sought to control permeance by increasing the thickness of the materials with higher permeability. However, it also reflects differences in behavior among different polymers (different symbol shapes in Figures 4-7). The "thin" group consisted only of pAro and sPEEKbased IEMs (squares and upward-facing triangles), while the "thick" group included the St/DVB-, PFSA-, and MaM based IEMs (circles, diamond, and downward-facing triangles). Thus, the apparent trend of increasing permeability with increasing thickness may simply reflect the differences in permeability between these two classes of materials.

Comparing these two membrane groups in more detail shows that in general, the pAro- and sPEEK-based IEMs had lower permeabilities than the other IEMs (Figures 4c and 4d). The average P_w and P_s of the "thin" IEMs was 37% and just 6%, respectively, of the corresponding values for the "thick" IEMs. We observed a similar trend for partitioning, in which the "thin" IEMs on average had lower K_w and K_s (approximately 50% of the value for "thick" IEMs, Figures 5c and 5d). By contrast, there was little apparent difference in D_w among the groups (Figure 5a). For D_s , five of the six IEMs in the "thin" group had D_s values approximately one order of magnitude lower than the other IEMs, with the exception of three monovalent-selective AEMs from the "thick" group (three red circles at the lower left of Figure 4d or 5b). As a result, the average D_s for the "thin" group was only 13% of the average value for the other membranes.

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Consistent with the finding in Section 4.3 that differences in diffusion coefficient are the primary cause of variations in permeability, the lower D_s of the "thin" group of membranes explains why the "thin" IEMs have a substantially lower salt permeability than the others. The substantially lower D_s values of the monovalent-selective AEMs within the "thick" group can be explained by the presence of heavily-crosslinked coatings on these membranes that impart additional hindrance to ion transport.^{52,53} The fact the AEMs with coatings made from a completely different material had similar D_s values to the IEMs in the "thin" group suggests that steric effects may explain differences in performance between the groups.

Overall, the pAro- and sPEEK-based IEMs had somewhat lower P , D , and K values than the other IEMs, but the ranges for most parameters overlapped between the groups. Thus not surprisingly, differences in membrane polymer structure influence water and salt transport. However, the overlap between groups and the significant range of variation in most transport properties among IEMs made of the same polymer indicate that other factors play a larger role in modulating water and salt transport.

4.5 Relationships between water and salt transport

To further explore the factors that govern transport properties, we next consider relationships between water and salt transport. Figure 6 shows that $\log P_w$ and $\log P_s$ were strongly correlated for all IEMs studied (R^2 =0.90, p<0.01). Remarkably, all IEMs fell on the same trend line, irrespective of polymer backbone, reinforcing, or charge (positively-charged AEM or negativelycharged CEM). Both AEMs and CEMs span the entire range of P_w and P_s , and most individual membrane polymers span a significant range as well. Yet for all membranes, higher water permeability was associated with higher salt permeability. This striking result provides evidence that in highly-swollen polymers like IEMs, unassociated cations and anions (i.e., mobile salt) do

not have significant interactions with the polymer chains due to the large amount of free volume available for permeation.⁵⁴ If such interactions were significant, we would expect different membrane polymers to have different relative rates of water and salt transport, since charged ions and neutral water would interact differently with each polymer.

The slope of the regression line in Figure $6(2.57\pm0.43)$ indicates that a unit change in water permeability is accompanied by a proportionally larger change in salt permeability. The larger change in P_s for a given change in P_w is consistent with free volume theory, which states that the diffusion rate of a larger penetrant relative to a smaller one (i.e., salt relative to water) increases as the free volume element size increases.^{10,39,55} Therefore, salt permeability should be more sensitive than water permeability to changes in free volume (i.e., membrane microstructure).

Figure 6. Water and salt permeability of 20 commercial ion exchange membranes measured in a diffusion cell containing 4 M sodium chloride solution and pure water. Red symbols denote AEMs, blue symbols denote CEMs, and the shape of the symbol indicates the membrane polymer type (see legend). Error bars represent the propagated standard error of at least three replicates. Refer to Table 1 for definitions of the membrane polymer abbreviations.

We observed relationships between water and salt diffusion coefficients that generally paralleled those observed with permeability. $\log D_w$ and $\log D_s$ correlated moderately well (R²=0.65, p<0.01, Figure 7a), and the slope of the regression line (2.31) indicates that a unit change in water diffusivity is accompanied by a proportionally larger change in salt diffusivity. The correlation between water and salt diffusivity suggests that similar physical mechanisms (likely steric hindrance) underlie both water and salt diffusion through IEMs, while the proportionally higher change in D_s compared to D_w is consistent with free volume theory as discussed above. The apparent importance of steric hindrance to the permeability and diffusion rates of water and salt indicates that water and salt transport in IEMs is controlled primarily by membrane microstructure (e.g., pore size and connectivity) and reinforces the conclusion that chemical interactions with the polymer chain are limited in IEMs. In other words, the differences in P , D , and K that we observed among different materials can be attributed to differences in microstructure.

Similarly to permeabilities and diffusion coefficients, partition coefficients for water and salt also correlated very strongly (R^2 =0.95, p<0.01, Figure 7b), which can be rationalized with reference to fixed charge concentration. Membranes with lower water uptake (low K_w and correspondingly low SD, Table 1) tend to have higher fixed charge concentrations (see Equation 7). Their high charge promotes strong Donnan exclusion of co-ions, reducing the quantity of mobile salt in the membrane and lowering K_s . Therefore, membranes with low K_w tend to have low K_s , and vice-versa.

Figure 7. Water and salt (a) diffusion coefficients and (b) partition coefficients of 20 commercial ion exchange membranes measured in a diffusion cell containing 4M sodium chloride solution and pure water. Red symbols denote AEMs, blue symbols denote CEMs, and the shape of the symbol indicates the general polymer making up the membrane (see legend in inset of panel (b)). Error bars represent the propagated standard error of at least three replicates. Refer to Table 1 for definitions of the membrane and polymer abbreviations.

5.0 Conclusions

In this work, we measured the water and salt transport properties of 20 commercial ion exchange

membranes (IEMs) and investigated relationships between water and salt transport properties

and membrane polymer type. The following points summarize our main findings:

- Water and salt permeance varied over a wide range (1-3 orders of magnitude), even among membranes with similar thickness, suggesting that differences in permeability drive differences in permeance among commercial IEMs.
- Variations in diffusion coefficients among IEMs were the primary factors determining variations in permeability among membranes.

• Permeability, diffusion, and partition coefficients for water were highly correlated to those for salt. Strikingly, all IEMs fell on the same trendline, regardless of membrane polymer, charge (AEM or CEM), or reinforcement. This result indicates that water and salt transport are determined primarily by the microstructure of the membrane rather than by the polymer chemistry or charge, and provides clear evidence that ions do not interact strongly with polymer chains in highly-swollen IEMs.

The above findings offer insights that inform advanced IEM development. As stated in the Introduction, it is desirable to develop IEMs that minimize salt diffusion and water transport in order to maximize the energy efficiency of electrochemical processes. We have shown that the membrane microstructure appears to be the primary factor controlling rates of water and salt transport in IEMs, rather than chemical interactions with the polymer chain. Recognition of this fact by the membrane research community may open new polymer chemistries and processing methods for consideration that have not previously been studied as ion exchange materials. To facilitate the design of new membrane polymers, future studies should investigate which physico-chemical properties best describe the variations in transport behavior we observed among materials.

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