Performance of Microporous Carbon Electrodes for Supercapacitors: Comparing Graphene with Disordered Materials

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Abstract

Over the past decades, the specific surface area and the pore size distribution have been identified as the main structural features that govern the performance of carbon-based supercapacitors. As a consequence, graphene nanostructures have been identified as strong candidates for maximizing their capacitance. However, this hypothesis could not be thoroughly tested so far due to the difficulty of synthesizing perfect materials with high pore accessibility and a sufficiently large density. Here we perform molecular simulations of a series of perforated graphene electrodes with single pore sizes ranging from 7 to 10 Å in contact with an adsorbed
ionic liquid, and compare the capacitances (using various metrics) to the one obtained with a typical disordered nanoporous carbon. The latter displays better performances, an observation that we explain by analyzing the structure of the liquid inside the pores. It appears that although the smaller pores are responsible for the largest surface charges, larger ones are also necessary to store the counter-ions and avoid the formation of detrimental opposite charges on the carbon. These results rationalize the need for disordered or activated carbon materials to design efficient supercapacitors.

Carbon-based supercapacitors are electrochemical devices that store electricity through the adsorption of ions from an electrolyte at the surface of porous electrodes. For decades, the state-of-the-art materials for the latter were mesoporous, *i.e.* with pore sizes ranging from 2 to 50 nm.\(^1\) In this family of materials, the capacitance, which quantifies the charge stored in the electrode as a function of applied voltage, generally correlates with the accessible surface area (ASA): the larger the surface, the larger the capacitance. Thus the relative performances of carbon materials were usually compared by normalizing the capacitance by the ASA. This allowed for example to address the effect of various activation techniques after synthesis.

The use of microporous carbons (with pore sizes distributed below 2 nm)\(^2,3\) has deeply impacted this field of research.\(^4\) It was then shown that the capacitance per unit surface area could be greatly enhanced while keeping the ASA relatively constant, suggesting that other physico-chemical features play an important role. The matching between the pore size and the ionic dimensions was quickly identified as a key aspect,\(^5\) and although this picture has now been refined through the use of various theoretical,\(^6,7\) simulation\(^8,9\) and *in situ* experimental techniques,\(^10\) it is now widely accepted that the pore size distribution (PSD) of the carbon materials plays a role of utmost importance.\(^11\)

However, despite these advances, it is still very difficult to predict the performance of a carbon material solely based on its ASA and/or its PSD. In fact, even the experimental determination of these quantities should be subject to caution in micropores. As a consequence, it remains necessary to perform lengthy electrochemical testings. This is particularly true for comparing carbons
Carbide-derived carbon Nanoporous graphene

Figure 1: Representative snapshots of the inner structure of the two nanoporous carbon electrodes simulated in this study. In the graphene case, the interlayer spacing is systematically varied between 7 and 10 Å.

with very different textures. It would therefore be highly desirable to develop accurate simulation methods that allow to determine the capacitance and to link it to the microscopic charging mechanisms. Here we illustrate this by simulating two types of nanoporous carbons with very different features using molecular dynamics. As shown on representative snapshots on Figure 1, the first system consists in a carbide-derived carbon (CDC) with a highly disordered structure. It was obtained by Palmer et al.\textsuperscript{12} using quenched molecular dynamics and was shown to match with an experimental structure of a CDC synthesized at 1,200°C (it will be labelled CDC-1200 in the following). We compare it to a series of highly-ordered nanoporous perforated graphene (PG) electrodes consisting of 6 graphene planes separated by an interlayer distance which was systematically varied between 7 and 10 Å. Holes were included inside the structure to allow the access of the ions. Graphene was chosen because it has the largest ASA possible for a carbon material, and was therefore investigated as a promising electrode material for supercapacitors.\textsuperscript{13–16} The electrolyte is a pure ionic liquid held at 400 K, the 1-butyl-3-methylimidazolium hexafluorophosphate, which is modelled using a coarse-grained description\textsuperscript{17} validated in the context of electrochemical cells in our previous works.\textsuperscript{18,19} Full supercapacitors are simulated by setting up symmetric cells in
which the electrolyte is put in contact with two similar electrodes. The latter are polarized through the application of a constant potential difference between them. Such simulations were shown to provide capacitances in remarkable agreement with the experimental data for CDC electrodes, not only with ionic liquids, but also with organic electrolytes or aqueous solutions.

![Figure 2: The ASA is not a well defined quantity for comparing the performances of materials with different pore size distributions and surface topologies. Surfacic capacitance of the various nanoporous carbon materials are shown as a function of the size of the probe used to calculate the ASA. The value for graphite is also provided for comparison.](image)

The (non-normalized) single electrode capacitance of the simulated supercapacitor is given by

\[ C = \frac{2\langle Q_+ \rangle}{\Delta \Psi} \]  

(1)

where \( \langle Q_+ \rangle \) is the average charge of the positive electrode over the full simulation and the factor 2 arises by assuming that the potential drop across the double-layer is the same for both electrodes (hence, \( \Delta \Psi/2 \)). However, this capacitance cannot be compared directly between systems since the CDC and the nanoporous graphenes have different ASA, mass and volume. In a first step, we try to normalize it by calculating the ASA. In principle, this should more easily be done in simulations than in experiments since we have access to the exact molecular structure. We use the software Zeo++, in which the only required parameter is a probe size. The ASA was systematically
determined for sizes ranging between 0.5 and 3.5 Å, which encompass the estimated values for the
probes used in adsorption experiments (such as argon) and for the ions of our electrolyte. Figure 2
clearly demonstrates that whatever the probe, the CDC always outperforms the PGs. If we limit
the comparison to the argon and PF$_6^-$ radii, the CDC surfacic capacitance is larger by factors of
2.2 and 3.1 than the one of the best performing PG (with 7 Å interlayer distance). This result is
somewhat unexpected since the latter geometry is supposed to give the best access to the surface
while ensuring that the ionic dimensions match with the pore size. However, if we also compare
with the case of graphite, for which only one side of the carbon plane is accessible to ions, we
immediately see that the capacitance per unit surface area is also higher than the ones of perforated
graphenes.

Figure 3: Single-electrode capacitances normalized by the electrode mass (panel a) or volume
(panel b).

Before analyzing the origin of these differences in performance at the microscopic scale, it is
useful to do additional comparisons with less probe-dependent normalizations, by computing the
specific and volumetric capacitances (normalization by the mass and the volume of the electrode,
respectively). As shown on Figure 3, in both cases the CDC-based supercapacitor remains the
most performant, even though the difference is much less pronounced than when using the ASA
for the normalization. The specific capacitance is 30 % larger (130 F g$^{-1}$ in CDC-1200 compared
to 100 F g$^{-1}$ in the nanoporous graphene with pore sizes ranging between 7 and 10 Å). As for the
volumetric capacitance (panel b), the high density of the 7 Å PG results in a capacitance similar to
that of CDC (99 F cm\(^{-3}\) compared to 112 F cm\(^{-3}\)).

In order to estimate the effect of the local structure on the capacitance, we compute the distribution of capacitance per carbon atom for a positively charged electrode, defined as \(q_i/\Delta\Psi\), where \(q_i\) is the local charge carried by a carbon atom, in Figure 4a). Firstly, we observe that the distribution is much more skewed for the CDC than for all the nanoporous graphene electrodes, in agreement with our previous work.\(^{18}\) However the 7 Å wide nanoporous graphene shows a broad distribution, with a relatively large number of highly charged carbon atoms. The reason for its lower performance is therefore to be found in the negative side of the distribution. Contrarily to the CDC, which almost has no negatively charged carbon, the 7 Å distribution exhibits the largest numbers among all the studied electrodes. This is due to the peculiar geometry of the nanoporous graphenes. Since there is only one pore size, anions and cations necessarily lie in the middle of the pore. As shown in our recent study focusing on the structure of the liquid, a monolayer of ions is formed for separations ranging between 7 and 9 Å, but in the 10 Å this monolayer is split in two, leading to two subpeaks with smaller intensities.\(^{24}\) Therefore the cations that still remain inside the pores are very close to the carbon surface and are therefore at the origin of the observed large negative charges in the 7 Å nanoporous graphene. In the CDC electrode, the structure is very different: There are several pore sizes within the material (ranging from 7 Å to 10 Å); this

Figure 4: a) Distributions of capacitance per atom are given for all the positively charged electrodes. b) Ion density profiles normal to the positive electrode surface for CDC-1200 and some of the PG materials (normalized by the total density of the pore).
allows strong reorganizations of the liquid structure. As a consequence, cations tend to move away from the surface and to reside in the middle of the largest pore, so that they do not induce negative charges on the carbon atoms.

This analysis is further corroborated by computing the ionic densities inside the pores, as a function of the distance to the pore wall. As shown in Figure 4b for the positively charged electrode, where they are normalized by the total pore density for each species, the distribution of anions is qualitatively similar in the CDC-1200 and the 7 Å PG. On the contrary, while in the graphene the cations share the same layer as the anions (leading to a distribution centered at the same distance to the electrode as for the anions), in the CDC-1200 the cation distribution is much broader, with some surface-cation distances reaching similar values as in the 10 Å nanoporous graphene.

In conclusion, molecular dynamics simulations allow to directly compare the performance of a variety of electrode structure at the same level of description and without the various sources of discrepancies that may be found in experiments (presence of surface groups in the carbons, discrepancies linked to the difficult characterization of nanoporous structures). In this work, by comparing a disordered nanoporous carbon with regular structures made of perforated graphene layers with various interlayer spacings, all of them put in contact with the same ionic liquid, we were able to show the importance of allowing co-ions (i.e. ions of the same sign as the electrode) to adopt positions far from the surface in order to maximize the capacitance. This result reinforces the idea that hierarchical nanoporous structures are (potential) good candidates for supercapacitor applications,\textsuperscript{25,26} not only to allow a faster diffusion of the ions but also to increase the capacitance. On the contrary, too narrow pore size distributions should probably be avoided. Note that these conclusions may not hold in the presence of ionophobic pores, for which the structure of the adsorbed liquid is very different.\textsuperscript{27–29}

Although these findings may be generalized to the case of organic electrolytes for supercapacitors (since they generally charge with similar mechanisms as ionic liquids\textsuperscript{20}), further investigation should be performed in the case of aqueous solutions. The latter, which are used for blue en-
ergy / desalination applications,\textsuperscript{30} involve inorganic ions that are difficult to desolvate, even in nanopores.\textsuperscript{21} This may strongly impact on the structure of the liquid inside perforated graphene electrodes.

**Methods**

The simulations were carried out within an \textit{NVE} ensemble at an average temperature of 400 K, which was chosen due to the high viscosity of the 1-butyl-3-methylimidazolium hexafluorophosphate ionic liquid at room temperature. Indeed, it has been previously shown that the capacitance, shows little changes with increasing the temperature from 298 K to 400 K.\textsuperscript{31,32} The liquid, composed of 4194 or 600 ions pairs (for the PG and CDC simulations, respectively), is represented by means of a coarse-grained model developed by Roy and Maroncelli,\textsuperscript{17} in which the cations and anions are respectively characterized by 3 and 1 interaction sites. The potential parameters used for the carbon atoms of the electrodes were chosen following Cole and Klein.\textsuperscript{33} The Lennard-Jones parameters for dissimilar atoms were computed using the Lorentz-Berthelot mixing rules. PG electrodes are composed of 21245 carbon atoms distributed into six fixed graphene layers. The five inner layers are randomly perforated with round 10 Å-radius holes (2 per layer) in order to allow the entrance of the liquid into the porous electrodes with fast charging and discharging rates.\textsuperscript{34} Four distances between consecutive graphene layers (7, 8, 9 and 10 Å) were simulated. For the CDC-1200, the structure obtained by Palmer \textit{et al.} using quenched molecular dynamics\textsuperscript{12} was used. Periodic boundary conditions are applied along two directions, and electrostatic interactions are calculated employing a two-dimensional Ewald summation.\textsuperscript{35} The simulations were carried out by holding the electrodes at constant applied potential between the electrodes according to the model of Siepmann and Sprik.\textsuperscript{36}

The systems were first equilibrated at constant charge during 500 ps, where the charge of the electrodes was fixed at 0. Then we performed a second equilibration of 500 ps, in which the charges of the carbon atoms were set to $+0.01e$ and $-0.01e$ in the left and the right electrodes, respectively.
We then carried out production runs (with a time step of 2 fs) for around 1.3 ns using the constant applied potential method. Since this applied potential cannot be chosen by calculating the Poisson potential across the cell for the constant charge runs,\(^\text{37}\) we performed several short simulations with different starting potentials and we chose the one for which the total charge on the electrodes showed to be nearly constant: This yielded values of $\Delta \Psi = 1$ V for the CDC electrode, 1.8 V for the PGs with pore sizes ranging from 7 to 9 Å and 2.7 V for the PG with 10 Å spacing between the planes. All the comparisons are thus performed for almost similar electrode charges, which is more meaningful since the ionic charge excess is then identical.

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**References**


